

Problem 3

a) void f1 (int n)
{

int i=2;

while (i<n) {

/* something that takes $O(1)$ time */

i = i * i;

}

}

Plug in n value of 25

$n = 25$ $i = 2 \rightarrow i = 4 \rightarrow i = 16 \rightarrow i > n$ so stop while loop

$i = i * i$ so ~~repeats~~ i is being squared so

$O(\log n)$

b) void f2 (int n)
{

for (int i=1; i<=n; i++) {

if (i % (int) sqrt(n) == 0) {

for (int k=0; k<pow(i,3); k++) {

/* $O(1)$ time thing */

}

}

}

First for loop runs n times

if statement constant time $O(1)$

2nd for loop has $\text{pow}(i,3)$ \rightarrow runs n^3 times

$n \cdot (1+n^3) =$

$O(n^4)$


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c) for (int i=1; i<=n; i++) {
    for (int k=1; k<=n; k++) {
        if (A[k] == i) {
            for (int m=1; m<=n; m=m+m) {
                // O(1) time thing
                // array contents not changed
            }
        }
    }
}

```

First for loop and second for loop run n times
 If statement constant time
 2nd for loop $n/2 = 1/2 * n = n$

$m = m + m$

$1 \rightarrow 1+1=2 \rightarrow 2+2=4 \rightarrow 4+4=8 \rightarrow 8+8=16 \rightarrow 16+16=32$

$\hookrightarrow O(\log n)$

d) First for loop for (int i=0; i<n; i++) runs n times

int newSize = 3 * size / 2

size = newSize \rightarrow size = $1.5 * \text{size}$
 \uparrow
 $1.5 \log n$

$O(n^2)$