

$$I = \int_{t_1}^{t_2} (L(q, \dot{q}) + F) dt$$

$$I = \int_{t_1}^{t_2} L(Q, \dot{Q}) dt$$

$$I = \int_{t_1}^{t_2} (p\dot{q} - H(q, p) + F) dt$$

$$I = \int_{t_1}^{t_2} (P\dot{Q} - H(q, p)) dt$$

$$\delta I = 0$$

$$\begin{cases} \dot{q} = \frac{\partial H}{\partial p} \\ \dot{p} = -\frac{\partial H}{\partial q} \end{cases}$$

$$\begin{vmatrix} \frac{\partial Q}{\partial q} & \frac{\partial Q}{\partial p} \\ \frac{\partial P}{\partial q} & \frac{\partial P}{\partial p} \end{vmatrix} = 1$$



$$\begin{cases} \dot{Q} = \frac{\partial H}{\partial P} \\ \dot{P} = -\frac{\partial H}{\partial Q} \end{cases}$$

$$\delta I = 0$$