

Overcast 4 samples 4 Yes, 0 No

$$\text{Entropy}(\text{overcast}) = -\left(\frac{4}{4}\right) \cdot \log_2\left(\frac{4}{4}\right) - \left(\frac{0}{4}\right) \cdot \log_2\left(\frac{0}{4}\right) = 0.$$

No info gain since it's all yes.

Rainy 5 samples 3 Yes, 2 No

$$\begin{aligned}\text{Entropy}(\text{rainy}) &= -\left(\frac{3}{5}\right) \log_2\left(\frac{3}{5}\right) - \left(\frac{2}{5}\right) \log_2\left(\frac{2}{5}\right) \\ &= 0.442 + 0.529 = 0.971\end{aligned}$$

Temperature mild 3 cool 2
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 Yes 2 No 1 Yes 1 No 1

$$\begin{aligned}\text{Gain}(\text{rainy, temp}) &= 0.971 - \left[\frac{3}{5} \left(-\frac{2}{3} \log_2\left(\frac{2}{3}\right) - \frac{1}{3} \log_2\left(\frac{1}{3}\right) \right) \right] - \\ &\quad \left[\frac{2}{5} \left(-\frac{1}{2} \log_2\left(\frac{1}{2}\right) - \frac{1}{2} \log_2\left(\frac{1}{2}\right) \right) \right] \\ &= 0.971 - 0.951 = 0.02\end{aligned}$$

Humidity High 2 Normal 3
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 Yes 1 No 1 Yes 2 No 1