

CT – Chip Trees

SLT – Small Log Trees (<=80 ft³)

LLT – Large Log Trees (>80 ft³)

SL – Small Trees (<=80 ft³)

ALT – All Log Trees

Removals, trees/acre

$$Removals_{ST} = Removals_{CT} + Removals_{SLT} \quad (1)$$

$$Removals_{ALT} = Removals_{SLT} + Removals_{LLT} \quad (2)$$

$$Removals = Removals_{CT} + Removals_{SLT} + Removals_{LLT} \quad (3)$$

Volume Per Acre, ft³/acre

$$VolPerAcre_{CT} = Removals_{CT} \times TreeVol_{CT} \quad (4)$$

$$VolPerAcre_{SLT} = Removals_{SLT} \times TreeVol_{SLT} \quad (5)$$

$$VolPerAcre_{LLT} = Removals_{LLT} \times TreeVol_{LLT} \quad (6)$$

$$VolPerAcre_{ST} = VolPerAcre_{CT} \times TreeVol_{SLT} \quad (7)$$

$$VolPerAcre_{ALT} = VolPerAcre_{SLT} \times TreeVol_{LLT} \quad (8)$$

$$VolPerAcre = VolPerAcre_{CT} + VolPerAcre_{SLT} \times TreeVol_{LLT} \quad (9)$$

Tree Volume, ft³/tree

$$TreeVol_{ST} = \frac{VolPerAcre_{ST}}{Removals_{ST}} \quad (10)$$

$$TreeVol_{ALT} = \frac{VolPerAcre_{ALT}}{Removals_{ALT}} \quad (11)$$

$$TreeVol_{ST} = \frac{VolPerAcre}{Removals} \quad (12)$$

Other Assumptions

$$MaxManualTreeVol, ft^3 = 150 \quad (13)$$

$$MaxMechTreeVol, ft^3 = 80 \quad (14)$$

$$MoistureContentFraction, wet basis = 0.50 \quad (15)$$

$$LogLength, ft = 32 \quad (16)$$

$$LoadWeight, green tons (logs) = 25 \quad (17)$$

$$LoadWeight, green tons (chips) = 25 \quad (18)$$

$$CTLTrailSpacing, ft = 50 \quad (19)$$

$$HardwoodCostPremium, fraction = 0.20 \quad (20)$$

$$ResidueRecoveryFraction \text{ for WT systems} = 0.80 \quad (21)$$

$$ResidueRecoveryFraction \text{ for } CTL = 0.50 \quad (22)$$

Calculated Intermediates

DBH

DBH – Diameter at Breast Height, in

$$DBHCT = \sqrt{\frac{TreeVolCT + 3.675}{0.216}} \quad (23)$$

$$DBHSLT = \sqrt{\frac{TreeVolSL + 3.675}{0.216}} \quad (24)$$

$$DBHLLT = \sqrt{\frac{TreeVolLLT + 3.675}{0.216}} \quad (25)$$

$$DBHST = \sqrt{\frac{RemovalsCT \times DBHCT^2 + RemovalsSLT \times DBHSLT^2}{RemovalsST}} \quad (26)$$

$$DBHALT = \sqrt{\frac{RemovalsSLT \times DBHSLT^2 + RemovalsLLT \times DBHLLT^2}{RemovalsALT}} \quad (27)$$

$$DBH = \sqrt{\frac{RemovalsCT \times DBHCT^2 + RemovalsALT \times DBHALT^2}{Removals}} \quad (28)$$

Tree Height

$$HeightCT = -20 + 24 \times \sqrt{DBHCT} \quad (29)$$

$$HeightSLT = -20 + 24 \times \sqrt{DBHSLT} \quad (30)$$

$$HeightLLT = -20 + 24 \times \sqrt{DBHLLT} \quad (31)$$

$$HeightST = \frac{RemovalsCT \times HeightCT + RemovalsSLT \times HeightSLT}{RemovalsST} \quad (32)$$

$$HeightALT = \frac{RemovalsSLT \times HeightSLT + RemovalsLLT \times HeightLLT}{RemovalsALT} \quad (33)$$

$$Height = \frac{RemovalsCT \times HeightCT + RemovalsALT \times HeightALT}{Removals} \quad (34)$$

Wood Density

If the wood density for chip trees, small log trees or large log trees is not specified by users, then it is 50 lb/ft³ by default.

$$WoodDensityST = \frac{WoodDensityCT \times VolPerAcreCT + WoodDensitySLT \times VolPerAcreSLT}{VolPerAcreST} \quad (35)$$

$$\begin{aligned} & \text{WoodDensityALT} \\ &= \frac{\text{WoodDensitySLT} \times \text{VolPerAcreSLT} + \text{WoodDensityLLT} \times \text{VolPerAcreLLT}}{\text{VolPerAcreALT}} \end{aligned} \quad (36)$$

$$\begin{aligned} & \text{WoodDensity} \\ &= \frac{\text{WoodDensityCT} \times \text{VolPerAcreCT} + \text{WoodDensityALT} \times \text{VolPerAcreALT}}{\text{VolPerAcre}} \end{aligned} \quad (37)$$

Hardwood Fraction

If the hardwood fraction for chip trees, small log trees or large log trees is not specified by users, then it is 0 by default.

$$\begin{aligned} & \text{HdwdFractionST} \\ &= \frac{\text{HdwdFractionCT} \times \text{VolPerAcreCT} + \text{HdwdFractionSLT} \times \text{VolPerAcreSLT}}{\text{VolPerAcreST}} \end{aligned} \quad (38)$$

$$\begin{aligned} & \text{HdwdFractionALT} \\ &= \frac{\text{HdwdFractionSLT} \times \text{VolPerAcreSLT} + \text{HdwdFractionLLT} \times \text{VolPerAcreLLT}}{\text{VolPerAcreALT}} \end{aligned} \quad (39)$$

$$\begin{aligned} & \text{HdwdFraction} \\ &= \frac{\text{HdwdFractionCT} \times \text{VolPerAcreCT} + \text{HdwdFractionALT} \times \text{VolPerAcreALT}}{\text{VolPerAcre}} \end{aligned} \quad (40)$$

Butt Diameter

$$\text{ButtDiamSLT} = \text{DBHSLT} + 3 \quad (41)$$

$$\text{ButtDiamST} = \text{DBHST} + 3 \quad (42)$$

Logs Per Tree

Logs per chip tree was assumed as 1.

$$\text{LogsPerTreeCT} = 1 \quad (43)$$

$$\text{LogsPerTreeSLT} = -0.43 + 0.678 \times \sqrt{\text{DBHSLT}} \quad (44)$$

$$\text{LogsPerTreeLLT} = -0.43 + 0.678 \times \sqrt{\text{DBHLLT}} \quad (45)$$

$$\begin{aligned} & \text{LogsPerTreeST} \\ &= \frac{\text{LogsPerTreeCT} \times \text{RemovalsCT} + \text{LogsPerTreeSLT} \times \text{RemovalsSLT}}{\text{RemovalsST}} \end{aligned} \quad (46)$$

$$\begin{aligned} & \text{LogsPerTreeALT} \\ &= \frac{\text{LogsPerTreeSLT} \times \text{RemovalsSLT} + \text{LogsPerTreeLLT} \times \text{RemovalsLLT}}{\text{RemovalsALT}} \end{aligned} \quad (47)$$

$$\begin{aligned} & \text{LogsPerTree} \\ &= \frac{\text{LogsPerTreeCT} \times \text{RemovalsCT} + \text{LogsPerTreeALT} \times \text{RemovalsALT}}{\text{Removals}} \end{aligned} \quad (48)$$

Log Volume

$$\text{LogVolST} = \frac{\text{TreeVolST}}{\text{LogsPerTreeST}} \quad (49)$$

$$\text{LogVolALT} = \frac{\text{TreeVolALT}}{\text{LogsPerTreeALT}} \quad (50)$$

$$LogVol = \frac{TreeVol}{LogsPerTree} \quad (51)$$

CTL Logs Per Tree

The minimum for CTLLogsPerTree is 1.

$$CTLLogsPerTreeCT = 2 \times (-0.43 + 0.678 \times \sqrt{DBHCT}) \quad (52)$$

$$CTLLogsPerTree = 2 \times (-0.43 + 0.678 \times \sqrt{DBHST}) \quad (53)$$

CTL Log Volume

$$CTLLogVolCT = \frac{TreeVolCT}{CTLLogPerTreeCT} \quad (54)$$

$$CTLLogVol = \frac{TreeVolST}{CTLLogsPerTree} \quad (55)$$

BFperCF

$$BFperCF = 5 \quad (56)$$

Bole Weight

$$BoleWtCT = \frac{WoodDensityCT \times VolPerAcreCT}{2000} \quad (57)$$

$$BoleWtSLT = \frac{WoodDensitySLT \times VolPerAcreSLT}{2000} \quad (58)$$

$$BoleWtLLT = \frac{WoodDensityLLT \times VolPerAcreLLT}{2000} \quad (59)$$

$$BoleWtST = BoleWtCT + BoleWtSLT \quad (60)$$

$$BoleWtALT = BoleWtSLT + BoleWtLLT \quad (61)$$

$$BoleWt = BoleWtCT + BoleWtALT \quad (62)$$

Residue Weight

RF – Residue Fraction

$$ResidueCT = UserSpecRFCT \times BoleWtCT \quad (63)$$

$$ResidueSLT = UserSpecRFSLT \times BoleWtSLT \quad (64)$$

$$ResidueLLT = UserSpecRFLLT \times BoleWtLLT \quad (65)$$

$$ResidueST = ResidueCT \times ResidueSLT \quad (66)$$

$$ResidueALT = ResidueSLT \times ResidueLLT \quad (67)$$

$$Residue = ResidueCT \times ResidueALT \quad (68)$$

Manual Machine Size

The maximum of ManualMachineSize is 1.

$$ManualMachineSizeALT = \frac{TreeVolALT}{MaxManualTreeVol} \quad (69)$$

$$ManualMachineSize = \frac{TreeVol}{MaxManualTreeVol} \quad (70)$$

Mechanized Machine Size

The maximum of MechMachineSize is 1.

$$MechMachineSize = \frac{TreeVolST}{MaxMechTreeVol} \quad (71)$$

Chipper Size

The maximum of ChipperSize is 1.

$$ChipperSize = \frac{TreeVolCT}{MaxMechTreeVol} \quad (72)$$

NonSelfLevelCabDummy

$$NonSelfLevelCabDummy_{slope < 15} = 1 \quad (73)$$

$$NonSelfLevelCabDummy_{15 < slope < 35} = 1.75 - 0.05 \times Slope \quad (74)$$

$$NonSelfLevelCabDummy_{slope > 35} = 0 \quad (75)$$

CSlopeFB&Harv (Mellgren 90)

$$CSlopeFB_{Harv} = 0.00015 \times Slope^2 + 0.00359 \times NonSelfLevelCabDummy \times Slope \quad (76)$$

CRemovalsFB&Harv (Mellgren 90)

$$CRemovalsFB_{Harv} = 0.66 - 0.001193 \times RemovalsST \times 2.47 + 5.357 \times 10^{-7} \times (RemovalsST \times 2.47)^2 \quad (77)$$

CSlopeSkidForwLoadSize (Mellgren 90)

$$CSlopeForwLoadSize = 1 - 0.000127 \times Slope^2 \quad (78)$$

Chardwood

$$CHardwoodCT = 1 + HdwdCostPremium \times HdwdFractionCT \quad (79)$$

$$CHardwoodSLT = 1 + HdwdCostPremium \times HdwdFractionSLT \quad (80)$$

$$CHardwoodLLT = 1 + HdwdCostPremium \times HdwdFractionLLT \quad (81)$$

$$CHardwoodST = 1 + HdwdCostPremium \times HdwdFractionST \quad (82)$$

$$CHardwoodALT = 1 + HdwdCostPremium \times HdwdFractionALT \quad (83)$$

$$CHardwood = 1 + HdwdCostPremium \times HdwdFraction \quad (84)$$

System Product Summary

Amounts Recovered Per Acre

ResidueRecoveredPrimary – WT residue recovered as part of primary product, GT/ac

ResidueRecoveredOptional – Optional residue recovered, GT/ac

$$BoleVolCCF = \frac{VolPerAcre}{100} \quad (85)$$

$$ResidueRecoveredPrimary = ResidueRecovFracWT \times ResidueCT \quad (86)$$

$$PrimaryProduct = BoleWt + ResidueRecoveredPrimary \quad (87)$$

$$ResidueRecoveredOptional = ResidueRecovFracWT \times (ResidueSLT + ResidueLLT) \quad (88)$$

$$TotalPrimaryAndOptional = PrimaryProduct + ResidueRecoveredOptional \quad (89)$$

Amounts Unrecovered and Left within the Stand Per Acre

GroundFuel – Activity fuels (residues) on the ground, GT/ac

$$GroundFuel = ResidueLLT + ResidueST \times (1 - ResidueRecovFracWT) \quad (90)$$

ResidueLLT not times 1-ResidueRecovFracWT?

Amounts Unrecovered and Left at the Landing

PiledFuel – Piled activity fuels (residues), GT/ac

$$PiledFuel = ResidueSLT \times ResidueRecovFracWT \quad (91)$$

No CT and LLT residue Piled? Assume all ResidueLLT left within the stand?

TotalResidues

$$TotalResidues = ResidueRecoveredPrimary + ResidueRecoveredOptional + ResidueUncutTrees + GroundFuel + PiledFuel \quad (92)$$

System Cost Elements

For Primary Products (boles & WT residues), \$/CCF of material treated by the activity

Fell&Bunch: trees <=80 cf	12.70
Manual Fell, Limb, Buck: all trees	
Manual Fell, Limb, Buck: all log trees	
Manual Fell, Limb, Buck: trees >80cf	12.78
Manual Fell: trees <=80 cf	
Manual Fell: chip trees	
Harvest: trees <=80 cf	
Skid Bunched: all trees	35.42
Skid Unbunched: all trees	
Forward: trees <=80 cf	
Yard Unbunched: all trees	
Yard CTL: trees <=80 cf	
Process: log trees <=80 cf	8.18
Load: log trees	7.78
Load CTL: log trees <=80 cf	
Chip: chip whole trees	7.76
Chip: chip tree boles	
Chip CTL: chip tree boles	
Primary Product Move-In Costs, \$/CCI	79.06

For Optional Residues, \$/GT of additional residue recovered

$$\begin{aligned} \text{Chip Loose Residues: from log trees} &\leq 80 \text{ cf} \\ &= \text{CostChipLooseRes} \times \text{CollectionOption} \times \text{InLimits1} \end{aligned} \quad (93)$$

$$\begin{aligned} \text{Residue MoveIn Costs, } \frac{\$}{\text{GT}} \\ &= 0 \times \text{CalcMoveIn} \times \text{CalcResidues} \times \text{InLimits1} \end{aligned} \quad (94)$$

What is the point of residue move-in costs?

For All Products, \$/ac

$$\begin{aligned} \text{ChipLooseResiduesFromLogTreesLess80cf} \\ &= \text{CostChipLooseRes} \times \text{CalcResidues} \\ &\quad \times \text{ResidueRecoveredOptional} \times \text{InLimits1} \end{aligned} \quad (95)$$

$$\begin{aligned} \text{FellAndBunchTreesLess80cf} \\ &= \frac{\text{CostFellBunch} \times \text{VolPerAcreST} \times \text{InLimits1}}{100} \end{aligned} \quad (96)$$

$$\begin{aligned} \text{ManualFellLimbBuckTreesLarger80cf} \\ &= \text{CostManFLBLT} \times \text{VolPerAcreLLT}/100 \times \text{InLimits1} \end{aligned} \quad (97)$$

$$\text{SkidBunchedAllTrees} = \text{CostSkidBun} \times \text{VolPerAcre}/100 \times \text{InLimits1} \quad (98)$$

$$\begin{aligned} \text{ProcessLogTreesLess80cf} \\ &= \text{CostProcess} \times \text{VolPerAcreSLT}/100 \times \text{InLimits1} \end{aligned} \quad (99)$$

$$\text{LoadLogTrees} = \text{CostLoad} \times \text{VolPerAcreALT}/100 \times \text{InLimits1} \quad (100)$$

$$\text{ChipWholeTrees} = \text{CostChipWT} \times \text{VolPerAcreCT}/100 \times \text{InLimits1} \quad (101)$$

$$\begin{aligned} \text{Stump2TruckPrimaryProductWithoutMovein (Mech WT)} \\ &= \text{FellAndBunchTreesLess80cf} \\ &\quad + \text{ManualFellLimbBuckTreesLarger80cf} \\ &\quad + \text{SkidBunchedAllTrees} + \text{ProcessLogTreesLess80cf} \\ &\quad + \text{LoadLogTrees} + \text{ChipWholeTrees} \end{aligned} \quad (102)$$

$$\begin{aligned} \text{Movein4PrimaryProduct} \\ &= \text{MoveInCosts! G39} \times \text{CalcMoveIn} \times \text{BoleVolCCF} \\ &\quad \times \text{InLimits1} \end{aligned} \quad (103)$$

$$\begin{aligned} \text{OntoTruck4ResiduesWoMovein (Mech WT)} \\ &= \text{ChipLooseResiduesFromLogTreesLess80cf} \end{aligned} \quad (104)$$

Movein4Residues

$$= 0 \times \text{CalcMoveIn} \times \text{CalcResidues} \quad (105)$$

$$\times \text{ResidueRecoveredOptional} \times \text{InLimits1}$$

System Cost Summaries

$$\begin{aligned} \text{TotalPerAcre} = & \text{Stump2Truck4PrimaryProductWithoutMovein} \\ & + \text{Movein4PrimaryProduct} \quad (106) \\ & + \text{OntoTruck4ResiduesWoMovein} + \text{Movein4Residues} \end{aligned}$$

$$\text{TotalPerBoleCCF} = \frac{\text{TotalPerAcre}}{\text{BoleVolCCF}} \quad (107)$$

$$\text{TotalPerGT} = \frac{\text{TotalPerAcre}}{\text{TotalPrimaryProductsAndOptionalResidues}} \quad (108)$$

Limits

$$\text{MaximumLLTperAcre} = \text{none} \quad (109)$$

$$\text{MaxLLTasPercentALT} = \text{none} \quad (110)$$

$$\text{ExceededMaxLLT} = 0 \quad (111)$$

$$\text{AvgTreeSizeLimit4Chipping} = 80 \quad (112)$$

$$\text{AvgTreeSizeLimit4Processing} = 80 \quad (113)$$

$$\text{AvgTreeSizeLimit4ManualFellLimbBuck} = 250 \quad (114)$$

$$\text{AvgTreeSizeLimit4loading} = 250 \quad (115)$$

$$\text{AvgTreeSize4GrappleSkiddingOfBunchedTrees} = 250 \quad (116)$$

$$\begin{aligned} \text{ExceededMaxTreeVol} = & \text{IF}(\text{OR}(\text{TreeVolCT} \\ & > \text{AvgTreeSizeLimit4Chipping}, \text{TreeVolSLT} \\ & > \text{AvgTreeSizeLimit4Processing}, \text{TreeVolLLT} \\ & > \text{AvgTreeSizeLimit4ManualFellLimbBuck}, \text{TreeVolALT} \\ & > \text{AvgTreeSizeLimit4loading}, \text{TreeVol} \\ & > \text{AvgTreeSize4GrappleSkidding}), 1, 0) \end{aligned} \quad (117)$$

$$\text{SkiddingLimit}(\text{Slope}, \%) = 40 \quad (118)$$

$$\text{ExceededMaxSkidSlope} = \text{IF}(\text{Slope} > \text{SkiddingLimit}, 1, 0) \quad (119)$$

$$\text{YardingDistLimit} = 0 \quad (120)$$

$$\text{ExceededMaxYardingDist} = 0 \quad (121)$$

$$\begin{aligned} \text{InLimits1} = & \text{IF}(\text{OR}(\text{ExceededMaxLLT} = 1, \text{ExceededMaxTreeVol} \\ & = 1, \text{ExceededMaxSkidSlope} \\ & = 1, \text{ExceededMaxYardingDist} = 1), \text{NA}(), 1) \end{aligned} \quad (122)$$