

SOLUTION FILE

1. Formulate 8 Queen's Problem as a CSP.

Let X be set of variables, D be set of domains and set of constraints.

$X = [Q_1, Q_2, Q_3, Q_4, Q_5, Q_6, Q_7, Q_8]$

$D = \{1, 2, 3, 4, 5, 6, 7, 8\}$

$C_1 = \langle \text{For all } i \neq j = (1, 2, 3, 4, 5, 6, 7, 8), (Q_i, Q_j), i \neq j \rangle (\text{Not in the same column})$

$C_2 = \langle \text{For all } i \neq j = (1, 2, 3, 4, 5, 6, 7, 8), Q_i \neq Q_j \rangle (\text{Not in the same row})$

$C_3 = \langle \text{For all } i \neq j = (1, 2, 3, 4, 5, 6, 7, 8), |Q_i - Q_j| \neq |i - j| \rangle (\text{Not in the same diagonal})$

2. Formulate an empty Sudoku problem as a CSP

Let X be set of variables, D be set of domains and set of constraints.

$X = 81 \text{ variables}$

- A1, A2, A3, ..., I7, I8, I9
- Letters index row, top to bottom
- Digits index column, left to right

$D = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$

$C_1 = \langle (A_i \neq A_j, B_i \neq B_j, C_i \neq C_j, D_i \neq D_j, E_i \neq E_j, F_i \neq F_j, G_i \neq G_j, H_i \neq H_j, I_i \neq I_j), (i \neq j) \rangle (\text{numbers in a row are not same})$

$C_2 = \langle (A_i \neq B_i \neq C_i \neq D_i \neq E_i \neq F_i \neq G_i \neq H_i \neq I_i), (i = [1, 2, 3, 4, 5, 6, 7, 8, 9]) \rangle (\text{numbers in a column are not same})$

$C_3 = \text{for each } 3 \times 3 \text{ block, } \langle K_i \neq K_j \text{ and } L_i \neq L_j, \text{ and } K_i \neq L_i, (i \neq j) \rangle$

	1	2	3	4	5	6	7	8	9
A		6		1		4		5	
B			8	3		5	6		
C	2								1
D	8			4		7			6
E			6				3		
F	7			9		1			4
G	5								2
H			7	2		6	9		
I		4		5		8		7	

3. Solve the crypt arithmetic problems given in the slides and formulate the crypt arithmetic problem TWO+TWO=FOUR as CSP.

<ul style="list-style-type: none"> SEND + MORE <u>MONEY</u> 		S	9	
		E	5	
		N	6	
		D	7	
		M	1	
		O	0	
		R	8	
		Y	2	

<ul style="list-style-type: none"> TWO + TWO <u>FOUR</u> 	<p>Set of Variables, $X=F,T,O,W,U,R$</p> <p>Set of Domains, $D=\{0,1,2,3,4,5,6,7,8,9\}$</p> <p>Set of Constraints:</p> <p>$C_1=\langle F \neq 0, T \neq 0 \rangle,$</p> <p>$C_2=\langle F \neq T, F \neq O, F \neq W, F \neq U, F \neq R, T \neq O, T \neq W, T \neq U, T \neq R, O \neq W, O \neq U, O \neq R, W \neq U, W \neq R, U \neq R \rangle,$</p> <p>$C_3=\langle O+O=R, W+W=U, T+T=FO \rangle$</p>
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