

$$1.) a) \begin{cases} 20000x + 30000y + 10000z = 5'200'000 \\ 10000x + 17000y + 6000z = 3'000'000 \\ 2000x + 3000y + 2000z = 760'000 \end{cases}$$

$$\begin{array}{ccc|c} 20000 & 30000 & 10000 & 5'200'000 \\ 10000 & 17000 & 6000 & 3'000'000 \\ 2000 & 3000 & 2000 & 760'000 \end{array} \quad | : 20000$$

$$\begin{array}{ccc|c} 1 & 3/2 & 1/2 & 260 \\ 10000 & 17000 & 6000 & 3'000'000 \\ 2000 & 3000 & 2000 & 760'000 \end{array} \quad \begin{array}{l} \\ \text{II} - 10000 \cdot \text{I} \\ \end{array}$$

$$\begin{array}{ccc|c} 1 & 3/2 & 1/2 & 260 \\ 0 & 2000 & 1000 & 400000 \\ 2000 & 3000 & 2000 & 760'000 \end{array} \quad \begin{array}{l} \\ \\ \text{III} - 2000 \cdot \text{I} \end{array}$$

$$\begin{array}{ccc|c} 1 & 3/2 & 1/2 & 260 \\ 0 & 2000 & 1000 & 400000 \\ 0 & 0 & 1000 & 240000 \end{array} \quad \begin{array}{l} \\ : 2000 \\ : 1000 \end{array}$$

$$\begin{array}{ccc|c} 1 & 3/2 & 1/2 & 260 \\ 0 & 1 & 1/2 & 200 \\ 0 & 0 & 1 & 240 \end{array} \quad \begin{array}{l} \text{I} - \frac{3}{2} \cdot \text{II} \\ \\ \end{array}$$

$$\begin{array}{ccc|c} 1 & 0 & -1/4 & -40 \\ 0 & 1 & 1/2 & 200 \\ 0 & 0 & 1 & 240 \end{array} \quad \begin{array}{l} \text{I} - -1/4 \cdot \text{III} \\ \text{II} - 1/2 \cdot \text{III} \\ \end{array}$$

$$\begin{array}{ccc|c} 1 & 0 & 0 & 20 \\ 0 & 1 & 0 & 80 \\ 0 & 0 & 1 & 240 \end{array} \quad \begin{array}{l} x = 20 \\ y = 80 \\ z = 240 \end{array}$$

$$b) A = \begin{pmatrix} 20000 & 30000 & 10000 \\ 10000 & 17000 & 6000 \\ 2000 & 3000 & 2000 \end{pmatrix}$$

$$L = \begin{pmatrix} 1 & 0 & 0 \\ 0,5 & 1 & 0 \\ 0,1 & 0 & 1 \end{pmatrix}$$

$$R = \begin{pmatrix} 20000 & 30000 & 10000 \\ 0 & ? & ? \\ 0 & ? & ? \end{pmatrix}$$

$$A' = \begin{pmatrix} 20000 & 30000 & 10000 \\ 0 & 2000 & 1000 \\ 0 & 2700 & 1800 \end{pmatrix}$$

$$L = \begin{pmatrix} 1 & 0 & 0 \\ 0,5 & 1 & 0 \\ 0,1 & 1,35 & 1 \end{pmatrix} \quad R = \begin{pmatrix} 20000 & 30000 & 10000 \\ 0 & 2000 & 1000 \\ 0 & ? & ? \end{pmatrix}$$

$$A'' = \begin{pmatrix} 20000 & 30000 & 10000 \\ 0 & 2000 & 1000 \\ 0 & 0 & 270 \end{pmatrix}$$

$$R = \begin{pmatrix} 20000 & 30000 & 10000 \\ 0 & 2000 & 1000 \\ 0 & 0 & 270 \end{pmatrix} \quad L = \begin{pmatrix} 1 & 0 & 0 \\ 0,5 & 1 & 0 \\ 0,1 & 1,35 & 1 \end{pmatrix}$$

$$c) \begin{cases} 20000x_1 + 30000x_2 + 10000x_3 = 5'720'000 \\ 10000x_1 + 17000x_2 + 6000x_3 = 3'300'000 \\ 2000x_1 + 3000x_2 + 2000x_3 = 836'000 \end{cases}$$

$$L_y = b$$

$$y_1 = 5720000$$

$$0,5y_1 + y_2 = 3'300'000$$

$$0,1y_1 + 1,5y_2 + y_3 = 836000$$

$$y_2 = 0,5 \cdot 5'720'000 + y_2 = 3'300'000$$

$$y_2 = 440'000$$

$$y_3 \quad 0,1 \cdot 5'720'000 + 1,35 \cdot 440'000 + y_3 = 836'000$$

$$y_3 = -330'000$$

$$R_x = y$$

$$20'000x_1 + 30'000x_2 + 10'000x_3 = 5'720'000$$

$$2000x_2 + 1000x_3 = 440'000$$

$$270x_3 = -330'000$$

$$x_3 = 270x_3 - 330'000$$

$$x_3 = -1222,22$$

$$x_2 = 2000x_2 + 1000 \cdot (-1222,22) = 440'000$$

$$x_2 = 831,11$$

$$x_1 = 20000x_1 + 30000 \cdot 831,11 - 10000 \cdot 1222,22 = 5'720'000$$

$$x_1 = -345,54$$