

Fixed Packet Solver

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Chapter 1

Directory Structure

This project has the following files:

- `formatter.cpp`: Converts raw data into required format.
 - Input : Raw data (List of edges)
 - Output : Formatted data (Input for NaivePLW)
 - Status : Complete
- `NaivePLW.cpp` : Implementation of the algorithm given by our paper.
 - Input : Hitting index; unweighted, undirected Graph; Edge weight function, \mathbf{b} of $L \times x = \mathbf{b}$, ϵ : error param
 - Output : Column vector \mathbf{x}
 - Status : Working on Phase-2

1.1 Input format for PLW-SOLVE

The Input for PLW-SOLVE is formatted as:

```
<G> // G is the undirected, weighted graph corresponding to L
<b> // b is the column vector in  $Lx = b$ 
<epsilon> // epsilon is the error parameter for the algorithm's termination
```

or as:

```
0 // Denotes Debug/Analysis mode
<G> // G is the undirected, weighted graph corresponding to L
<b> // b is the column vector in  $Lx = b$ 
<epsilon> // epsilon is the error parameter for the algorithm's termination
<x> // x is the final solution to  $Lx = b$ , computed through standard solvers
```

Note the below protocol for the exact formats.

1.2 Data Format for PLW-SOLVE Entities

1.2.1 HashMaps

1.2.1.1 Hitting Table Index

```
<number of nodes>
<start node> <end node> <indexed node> <occurences> // 1st Entry
<start node> <end node> <indexed node> <occurences> // 2nd Entry
...
...
...
<start node> <end node> <indexed node> <occurences> // <number of nodes> ^ 3 th Entry
```

1.2.2 Graphs

1.2.2.1 Unweighted & Undirected

```

<number of nodes>
<number of edges>
<node_1> <node_2> //edge number 1
<node_1> <node_2> //edge number 2
...
...
...
<node_1> <node_2> //edge number <number of edges>

```

1.2.2.2 Weighted & Undirected

```

<number of nodes>
<number of edges>
<node_1> <node_2> <weight> //edge number 1
<node_1> <node_2> <weight> //edge number 2
...
...
...
<node_1> <node_2> <weight> //edge number <number of edges>

```

1.2.3 Matrices

```

<number of rows>
<number of columns>
<E> <E> <E> <E> ... <E> //space seperated row 1 of the matrix
<E> <E> <E> <E> ... <E> //space seperated row 2 of the matrix
...
...
...
<E> <E> <E> <E> ... <E> //space seperated row <number of rows> of the matrix

```

1.2.4 Vectors and Functions

1.2.4.1 Weight Vector

```

<number of edges> //number of edges
<node_1> <node_2> <weight> //edge number 1
<node_1> <node_2> <weight> //edge number 2
...
...
...
<node_1> <node_2> <weight> //edge number <number of edges>

```

1.2.4.2 Column Vector for system of linear equations (**b**)

```

<number of entries in vector> //number of vector entries
<element> // First element
<element> // Second element
...
...
...
<element> // <number of entries in vector>th element

```

1.2.5 Singleton Values

```

Error Parameter (**$epsilon$)
<epsilon> //Value of error parameter
Number of samples($N$)
<Number of samples> //Total number of samples

```

Chapter 2

File Index

2.1 File List

Here is a list of all documented files with brief descriptions:

src/naive/ NaivePLW.cpp	
One-sink Laplacian Solver Using Random Walks	5

Chapter 3

File Documentation

3.1 src/naive/NaivePLW.cpp File Reference

One-sink Laplacian Solver Using Random Walks.

```
#include <bits/stdc++.h>
```

Macros

- `#define nll ""`
empty string alias
- `#define br " "`
space alias
- `#define nl std::endl`
newline alias
- `#define in(a) std::cin >> a;`
single input alias
- `#define in2(a, b) std::cin >> a >> b;`
double input alias
- `#define in3(a, b, c) std::cin >> a >> b >> c;`
triple input alias
- `#define out(a) std::cout << a;`
single output alias
- `#define out2(a, b) std::cout << a << br << b;`
double output alias
- `#define out3(a, b, c) std::cout << a << br << b << br << c;`
triple output alias
- `#define outs(a) out2(a, nll)`
output with space alias
- `#define outn(a) std::cout << a << nl;`
output with newline alias

Functions

- `template<typename T >`
`void incontainer (std::vector< T > &v)`
Inputs space separated dynamic array.
- `template<typename T >`
`void outcontainer (std::vector< T > &v)`
Outputs space separated dynamic array.

- `template<typename T >`
`void inmatrix (std::vector< std::vector< T > > &v)`
Inputs space separated entries of newline separated dynamic arrays forming a matrix.
- `template<typename T >`
`void outmatrix (std::vector< std::vector< T > > &v)`
Outputs a matrix.
- `void DFS (int node, std::vector< int > &visited, int &cnt)`
Performs DFS on the graph storing connected counter in cnt.
- `bool checkConnected ()`
Check if the given graph is connected.
- `template<typename T >`
`bool cumDist ()`
Checks whether the.
- `void throwError (std::string err)`
Throws Error and exits the program.
- `template<typename T >`
`T distSelector (const std::vector< std::pair< double, T > > &dist)`
Sample from a given distribution.
- `void generateHittingTable (int start, int end)`
Generates Hitting Table between the two given vertices.
- `void init ()`
Initializes the chain.
- `void bootstrap ()`
Bootstraps the chain and finds s.
- `void runChainSerial ()`
Run the chain serially.
- `void runChain ()`
Run Phase two.
- `void end ()`
Completion Formalities.
- `template<typename T >`
`bool cumDist (const std::vector< std::pair< double, T > > &dist)`
Checks if the given array is a Cumulative distribution or not.
- `int main ()`
Main function.

Variables

- `int n`
Number of Nodes in Graph.
- `int m`
Number of Edges in Graph.
- `int s`
Vertex chosen via bootstrapping indicating high stationary prob. state.
- `int u`
The index of the sink vertex.
- `int timer = 0`
Timer for running the chain serially.
- `int N = -1`
Number of samples for bootstrapping.
- `int d = 5`
Stores the number of chains to run.

- double **sb**
Stores the sum of non-sink column vectors.
- double **eps** = 1
Stores the bound on error required.
- std::mutex **io_lock**
Declares variables for storing timestamps and durations if -DTIMER is passed as a flag.
- std::vector< int > **identity**
- std::vector< int > **X**
State vector for multi-dimension markov chain.
- std::vector< int > **Q**
Occupancy vector for each node.
- std::vector< double > **mu**
Error vector mu as per definition.
- std::vector< double > **b**
Column vector b as per definition.
- std::vector< double > **j**
Column vector j as per definition.
- std::vector< double > **D**
Stores total weight sum for the vertices.
- std::vector< std::pair< double, int > > **sources**
Distribution of sources.
- std::vector< std::vector< int > > **adj_list**
Adjacency list for the given graph.
- std::vector< std::tuple< int, int, double > > **edges**
List of edges of the graph.
- std::vector< std::vector< std::pair< double, int > > > **P**
- std::vector< std::vector< std::pair< double, int > > > **Cum_P**
Transition Matrix and Cumulative Transition Matrix.
- std::map< std::pair< int, int >, double > **weightMap**
Contains mapping from pair of nodes to their corresponding edge weight.
- std::map< std::pair< int, int >, std::vector< std::pair< double, int > > > **HittingTable**
Stores the computed hitting table distributions for different pair of nodes.

3.1.1 Detailed Description

One-sink Laplacian Solver Using Random Walks.

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Version

0.5

Date

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3.1.2 Function Documentation

3.1.2.1 bootstrap()

```
void bootstrap ( )
```

Bootstraps the chain and finds s.

Bootstrap runs the bootstrapping algorithm and finds the ideal vertex to start the chain from. < Default Initialization of the chain

- < Represents the vertices we picked
- < Picking a source
- < No paths between source sink pair
- < Generate a path between source and sink
- < Pick a vertex from the given distribution
- < Increment counter for the chosen vertex
- < Keeps check of maximum freq
- < Keeps track of best vertex
- < Update new maximum
- < Update new winner
- < Assign chosen vertex to s

3.1.2.2 checkConnected()

```
bool checkConnected ( )
```

Check if the given graph is connected.

Checks if the input is connected.

Returns

true Input Graph is connected

false Input Graph is not connected

- < This vector keeps track of visited nodes
- < Counter to keep track of number of visited nodes
- < DFS to update visited counter
- < Return true if all nodes have been visited, false otherwise

3.1.2.3 cumDist()

```
template<typename T >
```

```
bool cumDist (
```

```
    const std::vector< std::pair< double, T > > & dist )
```

Checks if the given array is a Cumulative distribution or not.

Template Parameters

<i>T</i>	Type of labels on each entity
----------	-------------------------------

Parameters

<i>dist</i>	Candidate distribution
-------------	------------------------

Returns

true Given candidate is a Cumulative distribution

false Given candidate is not a Cumulative distribution

- < checks previous entry
- < cumulative prob. distribution is monotonically increasing
- < update previous entry
- < last entry of the distribution should be 1

3.1.2.4 DFS()

```
void DFS (
    int node,
    std::vector< int > & visited,
    int & cnt )
```

Performs DFS on the graph storing connected counter in cnt.
Runs a Depth first search to mark all connected nodes.

Parameters

<i>node</i>	current node
<i>visited</i>	array indicating wether each node has been visited or not
<i>cnt</i>	counter indicating number of visited nodes

< increase counter indicating total number of connected vertices
< color of node is color_val
< Iterate through the neighbors of current node
< Node already visited
< Node not visited, apply DFS recursively

3.1.2.5 distSelector()

```
template<typename T >
T distSelector (
    const std::vector< std::pair< double, T > > & dist )
```

Sample from a given distribution.
Selects a given label from the distribution.

Template Parameters

<i>T</i>	Type of label in the distrtribution
----------	-------------------------------------

Parameters

<i>dist</i>	Cumulative probability distrtribution
-------------	---------------------------------------

Returns

T

< d1 represents the chosen random value
< first entry is the selected entry
< Temp variables for binary search
< Binary search for the interval of distribution in which d1 falls

3.1.2.6 end()

```
void end ( )
```

Completion Formalities.
Completes exit formalities. <std::cout << s << std::endl;

3.1.2.7 generateHittingTable()

```
void generateHittingTable (
    int start,
    int end )
```

Generates Hitting Table between the two given vertices.
 Generates Hitting table for vertices starting from start and ending at end.

Parameters

<i>start</i>	Starting vertex
<i>end</i>	Ending vertex

- < Initial vertex
- < start has been visited
- < Total number of vertices in the walk
- < Continue walking until we hit our target
- < Select next vertex from the transition matrix
- < increment occurrences of i1
- < increment vertex counter for the walk
- < Vector to generate Hitting table distribution
- < Generate Hitting Table Distribution

3.1.2.8 init()

```
void init ( )
```

Initializes the chain.

Initializes the variables, i.e.

Takes input < Temporary Int Variables

< Temporary Double Variables

< Input Number of nodes and Number of edges

< Initialize edges vector

< Initialize adjacency list vector

< Initialize Transition Matrix

< Initialize Cumulative Transition Matrix

< Initialize Total node weight tracker

< Input the edges

< Takes in the incident vertices and their edge-weight

< Setup adjacency list

< Setup adjacency list

< Map given edge weight

< Map given edge weight

< Add weight of given edges to total node weight

< Add weight of given edges to total node weight

< append given edge to the edges

< Check if the graph is connected

< Setting up the transition matrix for our markov chain

< Cumulative Probability counter

< Check if cumulative edge weight of a vertex is very low or 0

< Throw Error and exit

< Scan through all neighboring vertices

< Get the weight of the required edge

< Find relative weightage of this edge

< Add it's probability to the cumulative value

< If there's a chance to go from i to it, we push it in our transition matrix

< Update transition matrix

< Update the cumulative transition matrix

< Input the dimension of column vector, this should equal n

< Initialize b

< Initialize j

< Taking input bi

< Finding the sink

< Sum of all non-sink vertices

```

< Identified u
< Cumulative j
< Sink vertex
< j_sink = 0 by definition
< Using definition of j
< Updating cumulative value
< Making cumulative probability distribution
< Culumative j
< Initializing P[u]
< Initializing Cum_P[u]
< Push back non-zero j value into transition matrix
< Push back non-zero j value into transition matrix
< Build cumulative transition matrix for sink
< Input the error parameter
< std::cout << eps << std::endl;

```

3.1.2.9 main()

```
int main ( )
```

Main function.

Returns

int Exit status of the program

```
< std::ios_base::sync_with_stdio(false); std::cin.tie(NULL);
```

3.1.2.10 runChain()

```
void runChain ( )
```

Run Phase two.

runs the chain

3.1.2.11 runChainSerial()

```
void runChainSerial ( )
```

Run the chain serially.

Runs the chain serially. < t = t+1

```

< Choosing a dimension to update
< Check whether the update is lazy
< Select new vertex from distribution
< Increment occupancy for new vertex
< Decrement occupancy for previous vertex
< Increment in mu for previous vertex
< Increment in mu for new vertex
< Update mu[previous vertex]
< Update mu[new vertex]
< Update state of multi-dim markov chain

```

3.1.2.12 throwError()

```
void throwError (
    std::string err )
```

Throws Error and exits the program.

A utility function to throw errors and exit the program.

Parameters

<i>err</i>	Error encoded as string
------------	-------------------------

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