

## Data and the plug-in principle

```
{r setup, include=FALSE} knitr::opts_chunk$set(cache=TRUE)
```

1

```
return_probs <- function(row){
  row <- as.numeric(row)

  product_1 <- p_v1_v11[,1][row[1]+1]* p_v2_v11[,1][row[2]+1]* p_v3_v11[,1][row[3]+1]* p_v4_v11[,1][row[4]+1]
  product_2 <- p_v1_v11[,2][row[1]+1]* p_v2_v11[,2][row[2]+1]* p_v3_v11[,2][row[3]+1]* p_v4_v11[,2][row[4]+1]
  product_3 <- p_v1_v11[,3][row[1]+1]* p_v2_v11[,3][row[2]+1]* p_v3_v11[,3][row[3]+1]* p_v4_v11[,3][row[4]+1]

  c(P_1*product_1, P_2*product_2, P_3*product_3)

}

binary_data <- read.csv('naive_bayes_binary.csv')
binary_data_train <- binary_data[1:(length(binary_data$V1)/2),]
binary_data_test <- binary_data[2501:5000,]
true_values <- binary_data_test$V11
binary_data_test <- binary_data_test[1:10]

#create tables of all variables and derive their conditional probs

table_v1_v11 <- table(binary_data_train$V1, binary_data_train$V11)
table_v2_v11 <- table(binary_data_train$V2, binary_data_train$V11)
table_v3_v11 <- table(binary_data_train$V3, binary_data_train$V11)
table_v4_v11 <- table(binary_data_train$V4, binary_data_train$V11)
table_v5_v11 <- table(binary_data_train$V5, binary_data_train$V11)
table_v6_v11 <- table(binary_data_train$V6, binary_data_train$V11)
table_v7_v11 <- table(binary_data_train$V7, binary_data_train$V11)
table_v8_v11 <- table(binary_data_train$V8, binary_data_train$V11)
table_v9_v11 <- table(binary_data_train$V9, binary_data_train$V11)
table_v10_v11 <- table(binary_data_train$V10, binary_data_train$V11)
```

```

# table_vecs <-

p_v1_v11 <- prop.table(table_v1_v11,2)
p_v2_v11 <- prop.table(table_v2_v11,2)
p_v3_v11 <- prop.table(table_v3_v11,2)
p_v4_v11 <- prop.table(table_v4_v11,2)
p_v5_v11 <- prop.table(table_v5_v11,2)
p_v6_v11 <- prop.table(table_v6_v11,2)
p_v7_v11 <- prop.table(table_v7_v11,2)
p_v8_v11 <- prop.table(table_v8_v11,2)
p_v9_v11 <- prop.table(table_v9_v11,2)
p_v10_v11 <- prop.table(table_v10_v11,2)

number_1 <- sum(binary_data_train$V11 ==1)
number_2 <- sum(binary_data_train$V11 ==2)
number_3 <- sum(binary_data_train$V11 ==3)

P_1 <- number_1/length(binary_data_train$V11)
P_2 <- number_2/length(binary_data_train$V11)
P_3 <- number_3/length(binary_data_train$V11)

probs_v11_numbers <- c(P_1, P_2, P_3)

results <- c()
for (i in 1:length(binary_data_test$V1)) {
  temp <- return_probs(binary_data_test[i,])
  results <- c(results, match(max(temp), temp))
}

```

## 2

a)

```

library('rpart')
library('rpart.plot')
student_data <- read.csv('student/student-mat.csv', sep=';')

student_data$class <- ifelse(student_data$G3 > 10,0,1)
new_dat <- student_data[1:30]
new_dat <- cbind(new_dat, student_data[34])

sample_ind <- sample(nrow(new_dat),nrow(new_dat)*0.70)
train <- new_dat[sample_ind,]

```

```

test <- new_dat[-sample_ind,]

set.seed(100)
fit <- rpart(formula = class~., data = train, method = "class", control = rpart.control(cp = 0.01))

printcp(fit)

test$pred <- predict(fit, test, type = "class")

#pruning
fit_pruned <- prune(fit, cp = 0.038)
test$pred <- predict(fit_pruned, test, type = "class")

rpart.plot(fit_pruned)

```

b)

training error = root node error X relative error

training error =  $0.47 * 0.62 = 0.2914$

generalisation error =  $0.47 * 0.6641 = 0.3121$

c)

d)

```

student_data_reg <- read.csv('student/student-mat.csv', sep=';')
new_dat <- student_data[1:30]
new_dat <- cbind(new_dat, student_data[33])

sample_ind <- sample(nrow(new_dat), nrow(new_dat)*0.70)
train_reg <- new_dat[sample_ind,]
test_reg <- new_dat[-sample_ind,]

set.seed(100)
fit_reg <- rpart(formula = G3~., data = train_reg, method = "anova", control = rpart.control(cp = 0.01))

printcp(fit_reg)

fit_pruned_reg <- prune(fit_reg, cp = 0.027)

rpart.plot(fit_pruned_reg)

```

## 4

a)

```
strange_data <- read.csv('strange_binary.csv')

set.seed(100)

fit_strange <- rpart(c~., data=strange_data, method='class', control = rpart.control(cp = 0))

plot(fit_strange)
fit_strange
printcp(fit_strange)

#           CP nsplit rel error xerror   xstd
# 1 0.0572917     0   1.00000 1.0000 0.10308
# 2 0.0312500     3   0.82812 1.0938 0.10540
# 3 0.0156250     4   0.79688 1.1094 0.10574
# 4 0.0078125     5   0.78125 1.1094 0.10574
# 5 0.0000000     9   0.75000 1.0781 0.10504

fit_pruned_strange <- prune(fit_strange, cp = 0.0312)
plot(fit_pruned_strange)

strange_predict <- predict(fit_pruned_strange, strange_data, type='class')
score <- mean(strange_predict == strange_data$c)

printcp(fit_pruned_strange)
```

The error on the test set will be different from that of training error. As you can see for the given tree,  $cp=0.00781$  looks the most optimal parametre with the least validation error. Here the validation is much more than training error. So it cannot be said that training and test will be the same for this tree.

## 6

```
classification_data <- read.csv('classification_accuracy.csv')

wins_decision_tree <- sum(classification_data$decision_tree > classification_data$svm) + sum(classification_data$decision_tree > classification_data$naive_bayes)
wins_svm <- sum(classification_data$svm > classification_data$decision_tree) + sum(classification_data$svm > classification_data$naive_bayes)
wins_naive_bayes <- sum(classification_data$naive_bayes > classification_data$svm) + sum(classification_data$naive_bayes > classification_data$decision_tree)

loss_decision_tree <- sum(classification_data$decision_tree < classification_data$svm) + sum(classification_data$decision_tree < classification_data$naive_bayes)
loss_svm <- sum(classification_data$svm < classification_data$decision_tree) + sum(classification_data$svm < classification_data$naive_bayes)
loss_naive_bayes <- sum(classification_data$naive_bayes < classification_data$svm) + sum(classification_data$naive_bayes < classification_data$decision_tree)
```

```
draw_decision_tree <- sum(classification_data$decision_tree == classification_data$svm) + s  
draw_svm <- sum(classification_data$svm == classification_data$decision_tree) + sum(classifi  
draw_naive_bayes <- sum(classification_data$naive_bayes == classification_data$svm) + sum(c
```