Data structures



Algorithms eBook part 2

byAdam Higherstein

Dynamical Data Structures

Linked list

Heap memory is used.

Can grow and shrink (basic arrays have fixes size)

You can add new elements to the beginning of linked list, or to the end or to the middle.

Element can be removed from the beginning, from the end and from the middle.

Very flexible data structures!

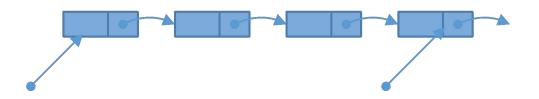
Singly linked list

One direction only

Dynamical Data Structures

Example: let's create this

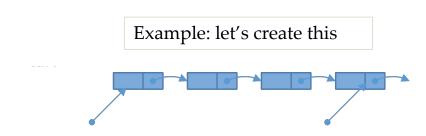
Linked list

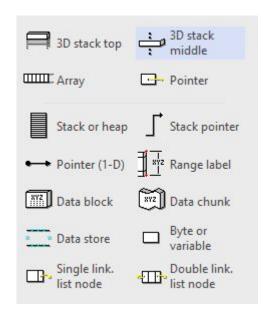


Dynamical Data Structures

Linked list

What tool to use? E.g. Ms Visio has symbols for memory objects



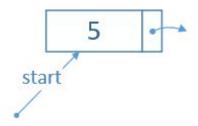


Example: let's create this

Dynamical Data Structures

Linked list

Let's create our example list step by step



First element is created and reference start point to it

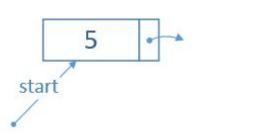
Example: let's create this

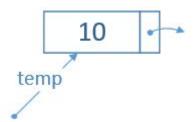
Dynamical Data Structures

Linked list

Let's create our example list step by step

First element is created and reference start point to it





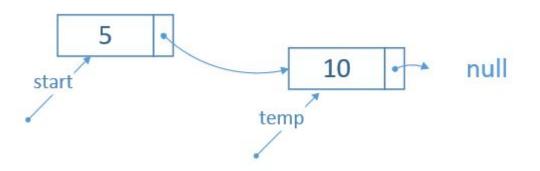
Second element is created by using an extra reference named temp

Example: let's create this

Dynamical Data Structures

Linked list

Let's create our example list step by step



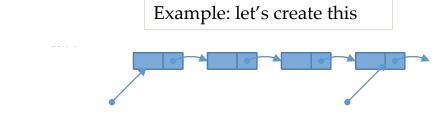
Let's connect new element to our list.

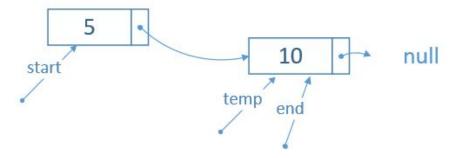
And if we do not know if there are coming new elements, we add there null_last element points to null

Dynamical Data Structures

Linked list

Let's create our example list step by step





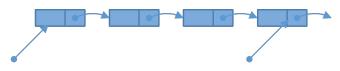
We put there also reference to mark the Last element

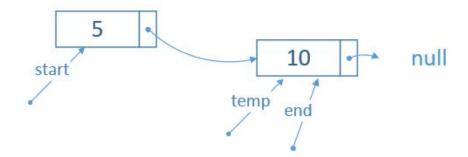
Dynamical Data Structures

Linked list

Let's create our example list step by step next element, value is 400



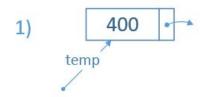


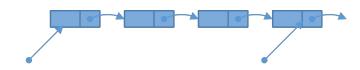


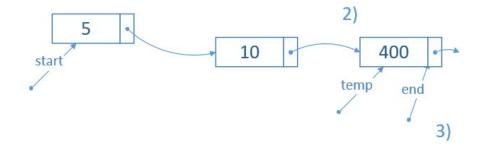
Dynamical Data Structures

Linked list

Let's create our example list step by step next element, value is 400



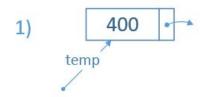


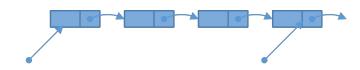


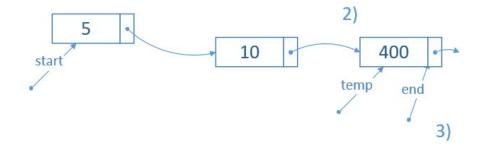
Dynamical Data Structures

Linked list

Let's create our example list step by step next element, value is 400



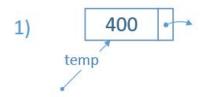


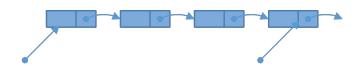


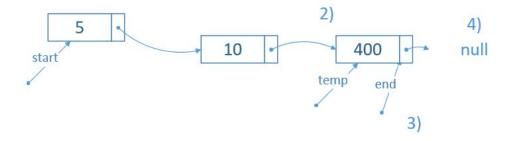
Dynamical Data Structures

Linked list

Let's create our example list step by step next element, value is 400



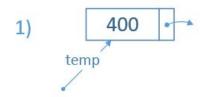


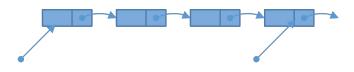


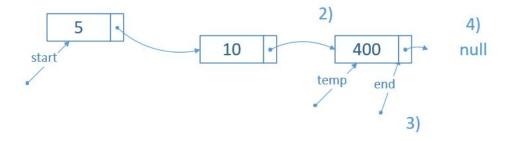
Dynamical Data Structures

Linked list

Let's create our example list step by step Go on and the final element there!



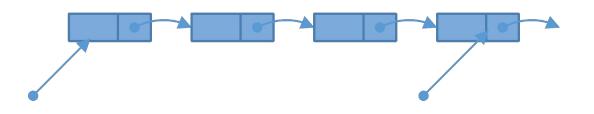




Dynamical Data Structures

Linked list

Let's create our example list step by step Result

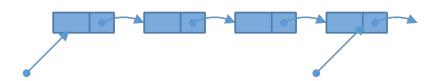


Dynamical Data Structures

Linked list

Code 1)

```
class Element
{
    public int data;
    public Element next;
}
```

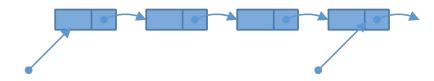


Dynamical Data Structures

Linked list

Code 2)

```
class Element
{
    public int data;
    public Element next;
}
```



```
Element start = new Element();
start.data = 5;

Element temp = new Element();
temp.data = 10;

start.next = temp;
temp.next = null;

Element end = temp;
```

Dynamical Data Structures

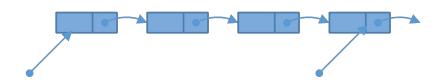
Linked list

Code 3)

```
Element end = temp;

temp = new Element();
temp.data = 400;

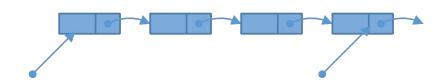
end.next = temp;
end = temp;
end.next = null;
```



Dynamical Data Structures

Linked list

Now: go on and complete the code. Then: print values!



Dynamical Data Structures

Linked list

Heap memory is used.

Can grow and shrink (basic arrays have fixes size)

You can add new elements to the beginning of linked list, or to the end or to the middle.

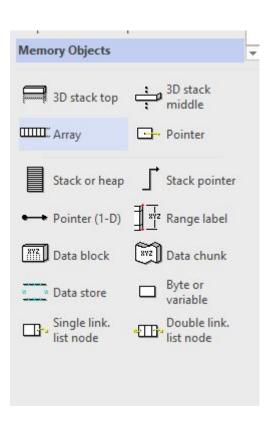
Element can be removed from the beginning, from the end and from the middle.

Very flexible data structures!

Dynamical Data Structures

Doubly linked list

Ms Visio has memory object symbols!



Dynamical Data Structures

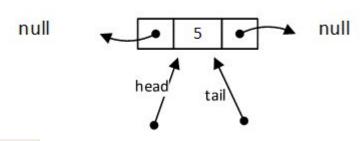
```
Class Element
{
    public int data;
    public Element next;
    public Element prev;
}
```

```
null 5 nu
```

Dynamical Data Structures

Doubly linked list

```
Class Element
{
    public int data;
    public Element next;
    public Element prev;
}
```

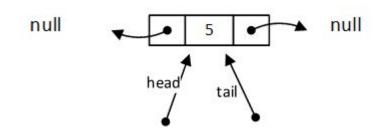


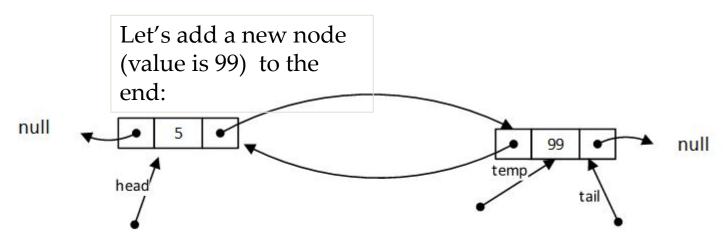
Create the 1. element

```
Element head = new Element();
head.data = 5;
head.next = null;
head.prev = null;
Element tail = head;
```

Dynamical Data Structures

```
Class Element
{
    public int data;
    public Element next;
    public Element prev;
}
```



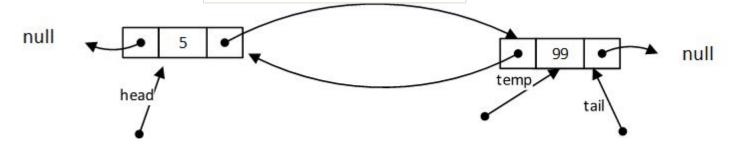


Dynamical Data Structures

Doubly linked list

```
Class Element
{
    public int data;
    public Element next;
    public Element prev;
}
```

Let's add a new node (value is 99) to the end:



Code

```
Element temp = new Element();
temp.data = 99;
tail.next = temp;
temp.prev = tail;
tail = tail.next;
tail.next = null;
```

Dynamical Data Structures

Doubly linked list

```
Class Element
{
    public int data;
    public Element next;
    public Element prev;
}
```

Here is node with value 200 added:

```
temp = new Element();
temp.data = 200;
tail.next = temp;
temp.prev = tail;
tail = tail.next;
tail.next = null;
```

Dynamical Data Structures

Doubly linked list

```
Class Element
{
    public int data;
    public Element next;
    public Element prev;
}
```

Here is node with value 200 added:

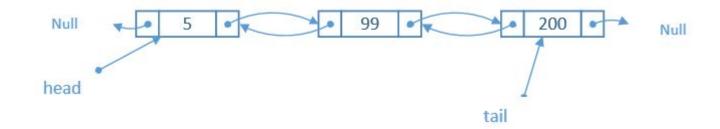
```
head

temp = new Element();
temp.data = 200;
tail.next = temp;
temp.prev = tail;
tail = tail.next;
tail.next = null;
```

Dynamical Data Structures

Doubly linked list

```
Class Element
{
    public int data;
    public Element next;
    public Element prev;
}
```

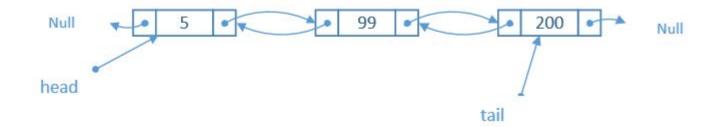


```
// printing, way 1
Console.WriteLine("{0}", head.data);
Console.WriteLine("{0}", head.next.data);
Console.WriteLine("{0}", head.next.next.data);
```

Dynamical Data Structures

Doubly linked list

```
Class Element
{
    public int data;
    public Element next;
    public Element prev;
}
```

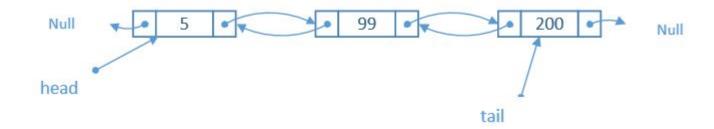


```
// printing, way 2
for (Element k = head; k != null; k = k.next )
    Console.WriteLine("{0}", k.data);
```

Dynamical Data Structures

Doubly linked list

```
Class Element
{
    public int data;
    public Element next;
    public Element prev;
}
```

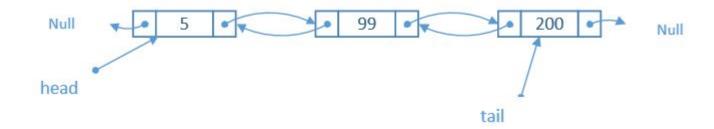


```
// printing, reverse order
Console.WriteLine("{0}", tail.data);
Console.WriteLine("{0}", tail.prev.data);
Console.WriteLine("{0}", tail.prev.prev.data);
```

Dynamical Data Structures

Doubly linked list

```
Class Element
{
    public int data;
    public Element next;
    public Element prev;
}
```

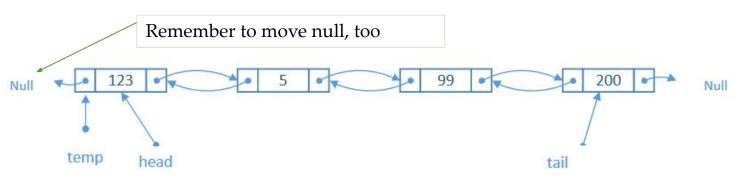


```
// printing, reverse order
for (Element k = tail; k != null; k = k.prev)
    Console.WriteLine("{0}", k.data);
```

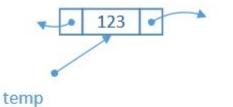
Dynamical Data Structures

Doubly linked list

```
Class Element
{
    public int data;
    public Element next;
    public Element prev;
}
```



Add new node to the beginning



Create the new node by using a temporary reference...

Connect to the beginning...

Move head to point to the new first node

Dynamical Data Structures

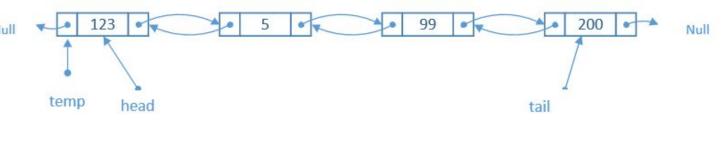
```
Class Element
{
    public int data;
    public Element next;
    public Element prev;
}
```

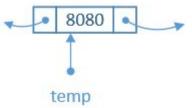
```
Remember to move null, too
temp
      head
                                             tail
 // new to the beginning
temp = new Node();
temp.data = 123;
head.prev = temp;
temp.next = head;
head = temp;
head.prev = null;
```

Dynamical Data Structures

```
// add element with 8080 after element 5
    temp = new Node();
    temp.data = 8080;

for (Node x = head; x != null; x = x.next)
    {
        if (x.data == 5)
        {
            temp.next = x.next;
            x.next.prev = temp;
            x.next = temp;
            temp.prev = x;
            break;
        }
}
```





Dynamical Data Structures

```
// add element with 8080 after element 5
    temp = new Node();
    temp.data = 8080;

for (Node x = head; x != null; x = x.next)
{
    if (x.data == 5)
    {
        temp.next = x.next;
        x.next.prev = temp;
        temp.prev = x;
        break;
    }
}
```

Dynamical Data Structures

```
// add element with 8080 after element 5
    temp = new Node();
    temp.data = 8080;

for (Node x = head; x != null; x = x.next)
{
    if (x.data == 5)
    {
        temp.next = x.next;
        x.next.prev = temp;
        temp.prev = x;
        break;
    }
}
```

Dynamical Data Structures

```
// add element with 8080 after element 5
                                                                    123
                                                                                                                              200
                                                                                                                                          Null
     temp = new Node();
     temp.data = 8080;
     for (Node x = head; x != null; x = x.next)
                                                                                                8080
                                                                                                                        tail
         if (x.data == 5)
             temp.next = x.next;
                                                                                                temp
             x.next.prev = temp;
             x.next = temp;
             temp.prev = x;
             break;
```

Dynamical Data Structures

Doubly linked list

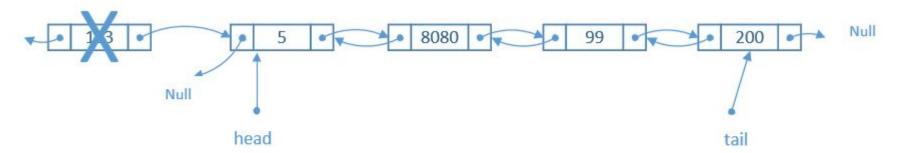
```
// add element with 8080 after element 5
    temp = new Node();
    temp.data = 8080;

for (Node x = head; x != null; x = x.next)
{
    if (x.data == 5)
    {
        temp.next = x.next;
        x.next.prev = temp;
        x.next = temp;
        temp.prev = x;
        break;
}
```

Dynamical Data Structures

Doubly linked list

Remove 1. node

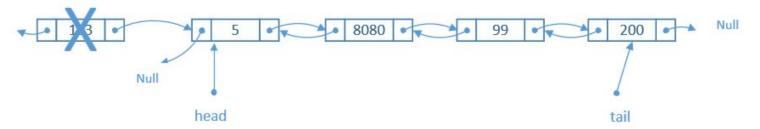


Remove from the beginning: move head to point to the second node... Mov null to point to the new starting node

Dynamical Data Structures

Doubly linked list

Remove 1. node



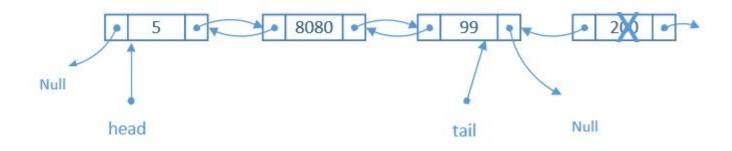
Remove from the beginning: move head to point to the second node... Mov null to point to the new starting node

```
// remove from the beginning
head = head.next;
head.prev = null;
```

Dynamical Data Structures

Doubly linked list

Remove the last node



```
// from the end
tail = tail.prev;
tail.next = null;
```

Dynamical Data Structures

Doubly linked list

Remove from a random position

```
// remove 8080
for (Node x = head; x != null; x = x.next)
    if (x.data == 8080)
    {
        x.prev.next = x.next;
        x.next.prev = x.prev;
        break;
}
```

Dynamical Data Structures

Doubly linked list

Try them!

Hopefully you learned a bit about linked lists!

Create nodes more practical Add attributes and methods Study collections that programming environment offers: you can use even them as base classes ...

Create own stacks and queues..

Dynamical Data Structures

Binary tree

Heap memory is used.

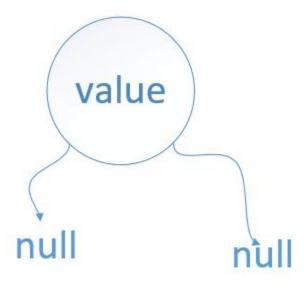
Can grow and shrink (basic arrays have fixes size)

You can add new elements to the beginning of linked list, or to the end or to the middle.

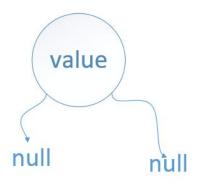
Element can be removed from the beginning, from the end and from the middle.

Very flexible data structures!

Dynamical Data Structures



Dynamical Data Structures



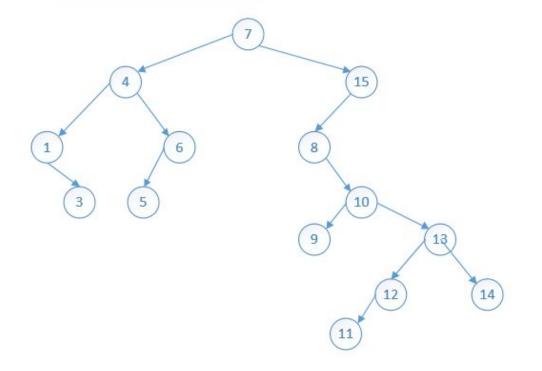
```
class BinaryTree
{
    public int data;
    public BinaryTree leftChild;
    public BinaryTree rightChild;
}
```

Dynamical Data Structures

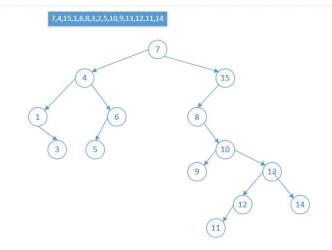
Binary tree

```
class BinaryTree
{
   public int data;
   public BinaryTree leftChild;
   public BinaryTree rightChild;
}
```

7,4,15,1,6,8,3,2,5,10,9,13,12,11,14

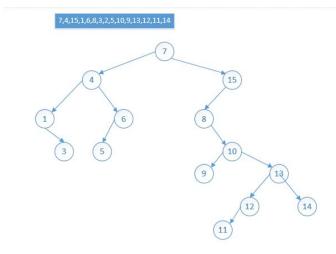


Dynamical Data Structures



```
public static void add (BinaryTree bt, int valu
boolean noplace = true;
BinaryTree newNode = new BinaryTree();
newNode.data = value;
newNode.leftChild = null;
newNode.rightChild = null;
while (noplace == true)
 if (value < bt.data)
   if (bt.leftChild == null)
    noplace= false;
   else bt = bt.leftChild;
 else
    if (bt.rightChild == null)
      noplace = false;
    else bt = bt.rightChild;
if (value < bt.data)
  bt.leftChild = newNode;
else
bt.rightChild= newNode;
```

Dynamical Data Structures

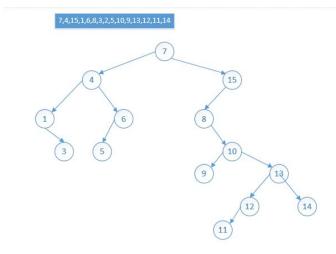


```
int[] values = {7,4,15,1,6,8,3,2,5,10,9,13,12,11,14};
BinaryTree bt = new BinaryTree();
bt.data = values[0];
bt.leftChild = null; bt.rightChild = null;
BinaryTree tree = bt;

for (int k = 1; k < values.length; k++)
{
   add(tree, values[k]);
}</pre>
```

Dynamical Data Structures

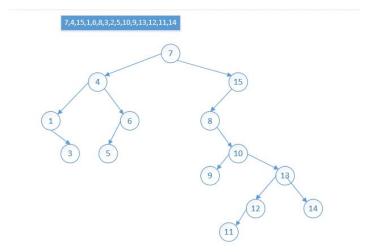
orders

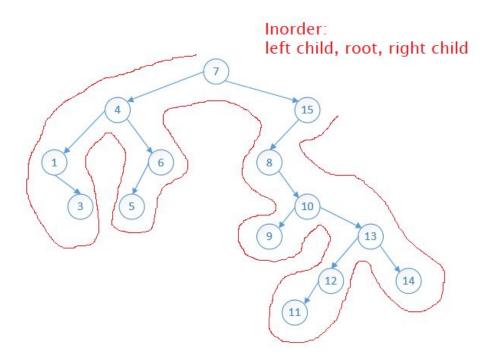


```
public static void inorderPrint(BinaryTree bt)
     if (bt == null)
          return;
      inorderPrint(bt.leftChild);
     System.out.print(" " + bt.data);
inorderPrint(bt.rightChild);
 public static void preorderPrint(BinaryTree bt)
     if (bt == null)
          return;
     System.out.print(" " + bt.data);
preorderPrint(bt.leftChild);
     preorderPrint(bt.rightChild);
 public static void postorderPrint(BinaryTree bt)
     if (bt == null)
          return;
     postorderPrint(bt.leftChild);
     postorderPrint(bt.rightChild);
System.out.print(" " + bt.data);
```

Dynamical Data Structures

orders

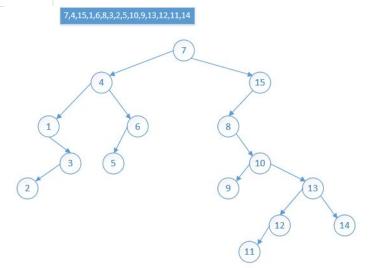




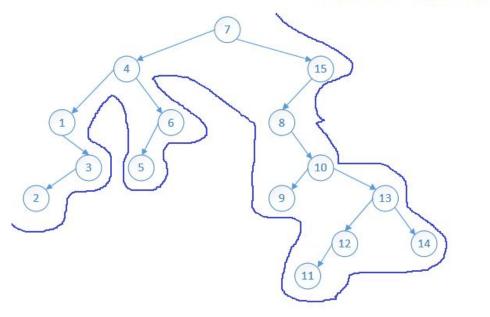
Dynamical Data Structures

orders

Binary tree



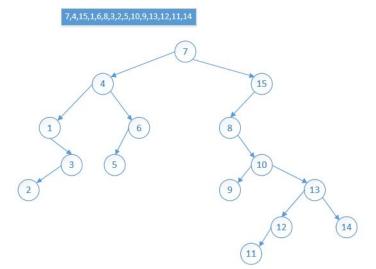
Postorder: left child – right child – root



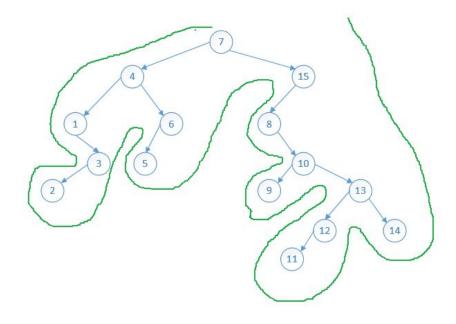
Dynamical Data Structures

orders

Binary tree

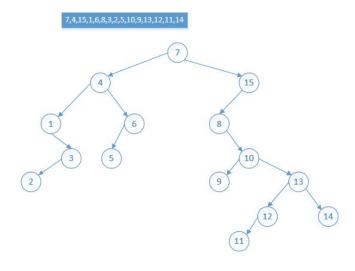


Predorder: root – left child – right child



Dynamical Data Structures

Binary tree



orders

INORDER

1 2 3 4 5 6 7 8 9 10 11 12 13 14 15

POSTORDER

2 3 1 5 6 4 9 11 12 14 13 10 8 15 7

PREORDER

7 4 1 3 2 6 5 15 8 10 9 13 12 11 14

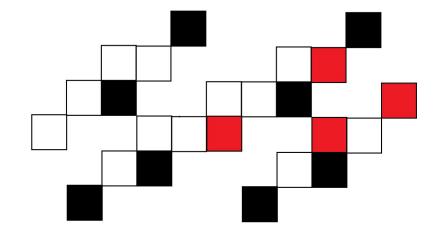
Try them!

Where are binary trees used?

Order makes them fast in searching...

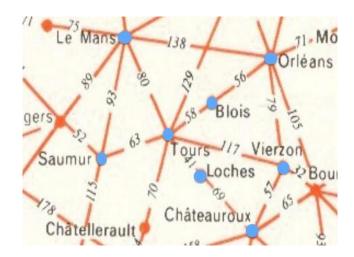
Add once – read many

Edsger Dijkstra shortest routes demo



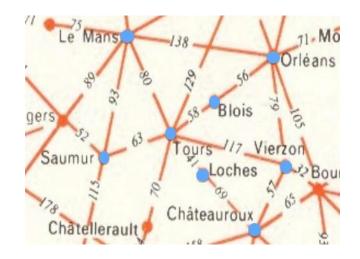
Edsger Dijkstra shortest routes demo Dijkstra Example
Shortest routes from Le Mans to other cities!

Map of France is here:

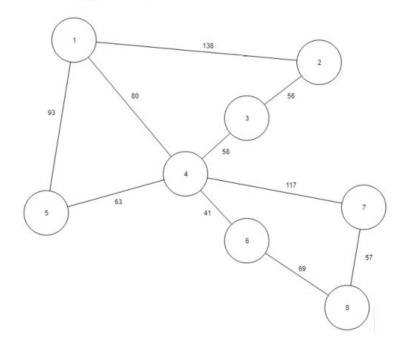


Blue circles are cities. We start from Le Mans.

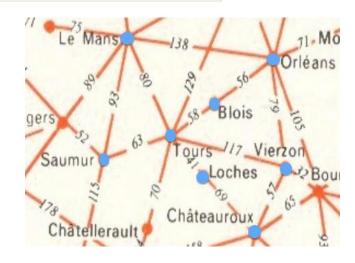
Edsger Dijkstra shortest routes demo



Here the network/graph as a diagram:



Edsger Dijkstra shortest routes demo



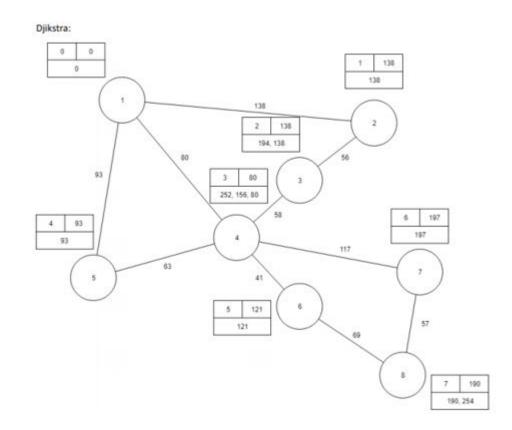
Here the network/graph as a matrix:

	1	2	3	4	5	6	7	8
1	0	138	INF	80	93	INF	INF	INF
2	138	0	56	INF	INF	INF	79	INF
3	INF	56	0	58	INF	INF	INF	INF
4	80	INF	58	0	63	41	117	INF
5	93	INF	INF	63	0	INF	INF	INF
6	INF	INF	INF	41	INF	0	INF	69
7	INF	79	INF	117	INF	INF	0	57
8	INF	INF	INF	INF	INF	69	57	0

Edsger Dijkstra shortest routes demo Here is the solution matrix: note priority queue

Round nr	Current node			Queue (priority queue)		
1	1	2,4,5	2(true, 138, 1), 4(true, 80, 1),5(true,93,1)	4(true, 80, 1), 5(true, 93, 1), 2(true, 138, 1)		
2 4	4	3,5,6,7	3(true,58,4) => 138	5(true, 93, 1)		
	80		5(true,63,4) => 143 NO	6(true,121,4)		
			6(true,41,4) => 121	2(true, 138, 1)		
			7(true,117,4) =>197	3(true,138,4)		
			NF 80 30560	7(true,197,4)		
3	5	1, 4	1 NO	6(true,121,4)		
93	93		4 NO	2(true, 138, 1)		
			Aspens:	3(true,138,4)		
3			4	7(true,197,4)		
4 6	6	4,8	4 NO	2(true, 138, 1)		
	121	2.5	8(true, 121 + 69, 6)	3(true,138,4)		
			10 10 10 10 10 10 10 10 10 10 10 10 10 1	8(true, 190, 6)		
			D.	7(true,197,4)		
5	2	1,3	1 NO	3(true,138,4)		
	138		3(true, 138+56, true) NO	8(true, 190, 6)		
				7(true,197,4)		
	3	2,4	2 NO	8(true, 190, 6)		
	138	647	3 NO	7(true,197,4)		
S	8	6,7	7 NO	7(true,197,4)		
	190		7 NO			
8	7	4,8	4 NO			
	197		8 NO			

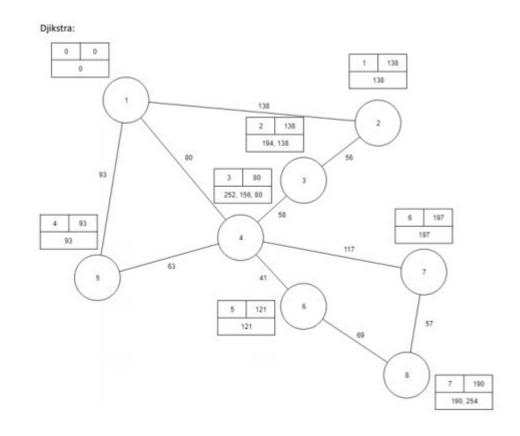
Edsger Dijkstra shortest routes demo



Edsger Dijkstra shortest routes demo

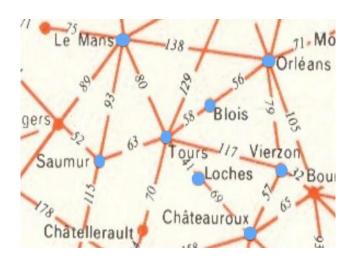
Results of the code:

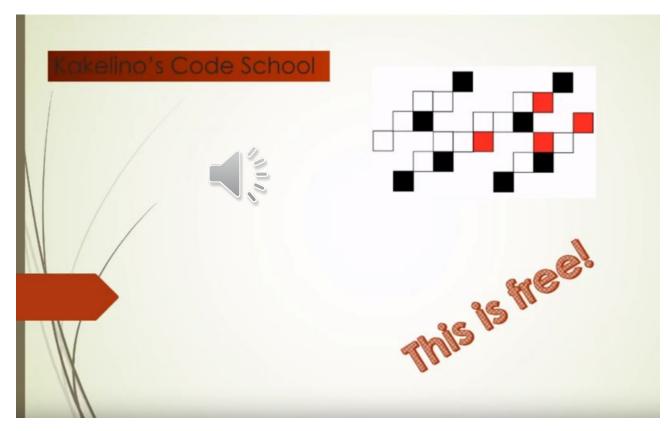
0..0 -> 0 0..1.. -> 138 0..3..2.. -> 138 0..3.. -> 80 0..4.. -> 93 0..3..5.. -> 121 0..3..6.. -> 197 0..3..5..7.. -> 190



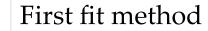
Edsger Dijkstra shortest routes demo

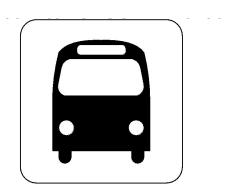
Try to simulate it!





Bin packing





Bin packing

Here are passenger groups 11 groups First fit method

Bin packing

First group has 8 persons: put persons to bus 1





First fit method

Bin packing

Second group has 7 persons: put persons to bus 1, too







First fit method

-

Bin packing

3. group has 14 persons: put persons to bus 2







Bin packing

4. group has9 persons:put persons to bus 3





First fit method

Bin packing

5. group has6 persons:put persons to bus 2, too



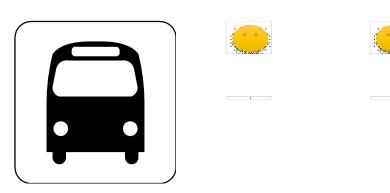




First fit method

Bin packing

6. group has9 persons:put persons to bus 3, too



First fit method

First fit method

Bin packing

7. group has 5 persons: put persons to bus 1, too









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Bin packing

8. group has 15 persons: put persons to bus 4



BUS 4

First fit method



Bin packing

9. group has6 persons:put persons to bus 5





First fit method

First fit method

Bin packing

10. group has7 persons:put persons to bus 5, too







Bin packing

11. group has 8 persons: put persons to bus 6





First fit method

That's all folks!!

This is a free version, part 2, of algorithms...

Final, completed version, real eBook, is coming soon!