

**Thesis proposal**



**Czech  
Technical  
University  
in Prague**

**F3**

**Faculty of Electrical Engineering  
Department of Measurement**

## **Radio position determination of the flying objects**

**Jakub Kákona**

**Supervisor: Doc. Dr. Ing. Pavel Kovář  
Field of study: Air Traffic Control  
Subfield: Radio navigation  
February 2017**



# Contents

<b>1 Motivation</b>	<b>1</b>	<b>3 Future work</b>	<b>19</b>
1.1 Main object parameters . . . . .	2	3.1 Expansion of used methods to other natural phenomena . . . . .	19
1.1.1 Artificial airspace targets . . . .	2	3.2 Proposed lightning detection system . . . . .	20
1.1.2 Natural radio-detectable objects	2	<b>A Bibliography</b>	<b>21</b>
1.2 Common position determination methods . . . . .	5		
1.2.1 Direction finding . . . . .	5		
1.2.2 Distance measurement . . . . .	5		
1.2.3 Velocity measurement . . . . .	7		
<b>2 Experimental verification</b>	<b>9</b>		
2.1 Meteor detection system . . . . .	9		
2.1.1 VOR Transmitters as signal sources . . . . .	12		
2.2 Hemispherical radiating pattern antenna design . . . . .	15		
2.2.1 Patch Antenna Design . . . . .	16		
2.2.2 Short-circuited quadrifilar helix . . . . .	16		
2.3 Meteor trajectory determination	16		





# Chapter 1

## Motivation

Radio position determination of flying objects is a standard radiolocation discipline which historically led to the development of radar systems. At present, the radar systems are mature enough to detect almost any type of radio-reflective artificial flying object in the atmosphere or near space. [1] Therefore the technology development is moving from the focus on radar sensitivity to system stability, reliability, and low operation costs leaving little space for scientific research. However, resulting applied technologies lead to new scientific possibilities of observations and measurement techniques which could bring new discoveries [3]. Unfortunately, due to a need of specific parameters for scientific measurement, an experiment-specific radar system is usually built. This approach is shown in recent scientific papers, which describe state of the art radio detection methods of natural phenomena. For example, a lightning detection systems like [18] uses specifically designed direction finding and time measurement receiver system. Another system is designed to be a meteor scatter receiver on the specific frequency and position [25]. By combining parameters required by these and possibly other systems a universal receiver useful for natural object detection a scientific radio-measurement apparatus could emerge. The source [3] describes the first and extremely expensive solution for this problem. The LOFAR station design and requirements are prohibitive for widespread scientific use, but a use of new techniques could scale down the station complexity and allows a small scale high-quality radio experiments.

## 1.1 Main object parameters

From a radar point of view, the terminology usually uses a term target instead of an object. The radar cross section (RCS; describing the ability to reflect radio waves), object distance and velocity are typical limiting parameters of the radar systems. These parameters vary largely depending on the measured target type and limit overall energy budget of the radar system.

### 1.1.1 Artificial airspace targets

A large group of possible radio reflective targets includes classical airspace objects like airplanes, unmanned aerial vehicles or satellites. These classical objects are detectable and localizable with already existing radar systems. Parameters like RCS and trajectory or velocity of these object are usually known from other sources simultaneously and therefore are not attracting much interest of radio scientist except utilizing this object category for system parameters verification. Otherwise, these objects are usually treated as noise in scientific measurements.

### 1.1.2 Natural radio-detectable objects

Several natural atmospheric or near space phenomena are expected to be localized by radio-waves. The list, for example, contains Solar system bodies, meteors, ionospheric fluctuations, solar flares, cosmic rays' particles and atmospheric electrical discharges. Not all of these natural phenomena have confirmed radio detection due to technical limitations or yet unknown physical principles [2]. But observation of natural phenomena are generally scientifically more valuable than artificial objects [6], [4]. Therefore the following text will be mainly focused on methods useful for natural phenomena measurement and detection.

### Reflective objects

The one of oldest known radio detection method is a backscatter radar. It is an ordinary type of radar which expects reflective targets (meteor trails

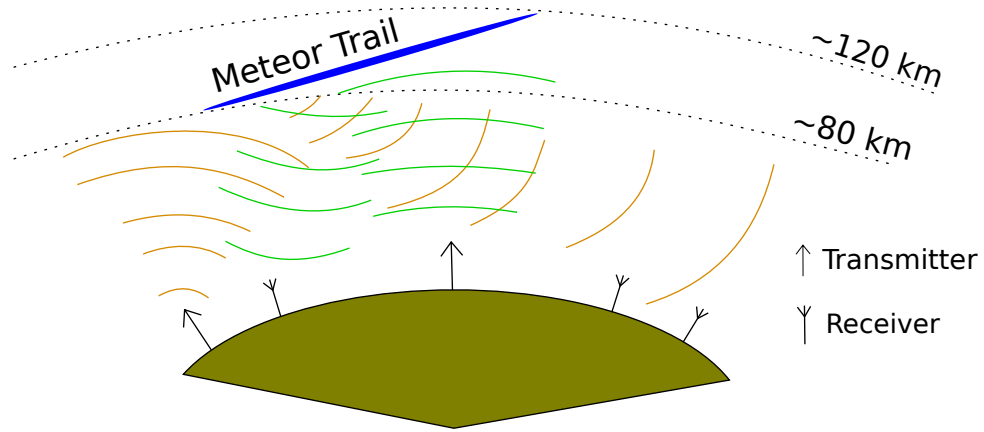
for example). Currently, several radars of this type are in operation to study meteors i. e. SkiYMet[10], CMOR [22].

Meteors, the atmospheric products of meteoroids traveling in space, are studied for many decades. Results of such research help us to understand the evolution of not only the planetary system but the interplanetary and possibly interstellar medium [5] as well. As the density of the interplanetary medium is low, great statistic and long-term continuous data set is necessary to describe its properties.

However, all mentioned [10],[22] monostatic or bistatic backscatter radars have little detection coverage, usually limited to the radar antenna field of view. Therefore these radar types observe only several spatially limited areas of the Earth's atmosphere. Besides the backscatter scientific radar systems, a multistatic scatter radio meteor detection networks have evolved [25],[8]. These forward scattering multistatic systems have a great advantage of a significant detection coverage. Unfortunately, the current spread of this technology is not sufficient to entirely cover the meteor flux in the Earth's atmosphere. However, the benefits of using this radio method are obvious - radio meteor detection capability is not dependent on the current weather and can work even during the daylight or nights with full Moon [24].

The main improvement of coverage which the forward scattering method brings originate in the fact that one or multiple radio-frequency transmitters can be cooperatively used simultaneously over the large area. Additionally, forward scattering geometry decreases the angle of reflection, therefore, increasing the available illuminating frequency of the transmitter.

The general principle of meteor observing by the forward scattering of radio waves off their trails is illustrated by the figure 1.1. A radio receiver with operating frequency range of 30-200MHz located at a proper distance (about 500-2000 km) from a transmitter. A curvature of the Earth or terrain features over this distance ensures there is no possibility of direct radio visibility. When a meteoroid enters the atmosphere, its meteor trail may reflect the radio waves emitted by the transmitter to the receiver. The signal can be received until the ionized meteor trail recombines. Reflections can last from tenths of a second to a few minutes, depending on used radio frequency and ionization density. The received signal characteristics are directly related to physical parameters of the meteoric event [23].



**Figure 1.1:** The method of radio meteor detection based on the forward scattering radar system

## ■ Emissive objects

Another object detection principle relies on the fact that some phenomena are radio emissive targets itself. A typical example of such object is thunderstorm lightning. The lightning detection and localization stations work on VLF, LF, and VHF radio bands. Specific frequency and bandwidth selected depend on the use case of the system. The long range lighting surveillance systems use VLF frequencies. Essentially all methods that provide accurate information about the location, polarity, and peak current of return strokes in the cloud to ground, lightning operates in this frequency range. This sensor type usually extracts a basic signal feature like time of trigger and amplitude by preset of waveform discrimination criteria [19]. Then the measured time and possible azimuth of received signal the event from multiple stations is processed in the central processing unit. The signal source is assumed to be point-like; therefore the spatial resolution of the best implementations of this technique are limited to sub-kilometer precision [21]. For more precise measurement a shorter wavelength is used the mostly from VHF band, where a combination of time of arrival and interferometry methods are used for reconstructing lighting channel [16], [17] .

The newer detection systems are exclusively based on proprietary Vaisala IMPACT [13] or TLS200/TSS928/LS7002 lightning sensors. Furthermore commercial off the shelf products are preferred systems for long-term sustainability [20]. Unfortunately, these systems are intended to be used in meteorological measurements and safety use. Therefore are not suitable for research of atmospheric phenomena. The only one exception to this trend I have found in the literature is lighting research which takes place in LOFAR project [14], [15].



## 1.2 Common position determination methods

If we want to estimate target position by radio signal reflected or transmitted by the target, we have only a small number of signal features which we could use to obtain the information about target coordinates. The best method to be used for determination of target position depends on the target type, the precision of measurement required and intended application. In most cases for an unknown flying object, we need to implement and combine several of the following general methods.

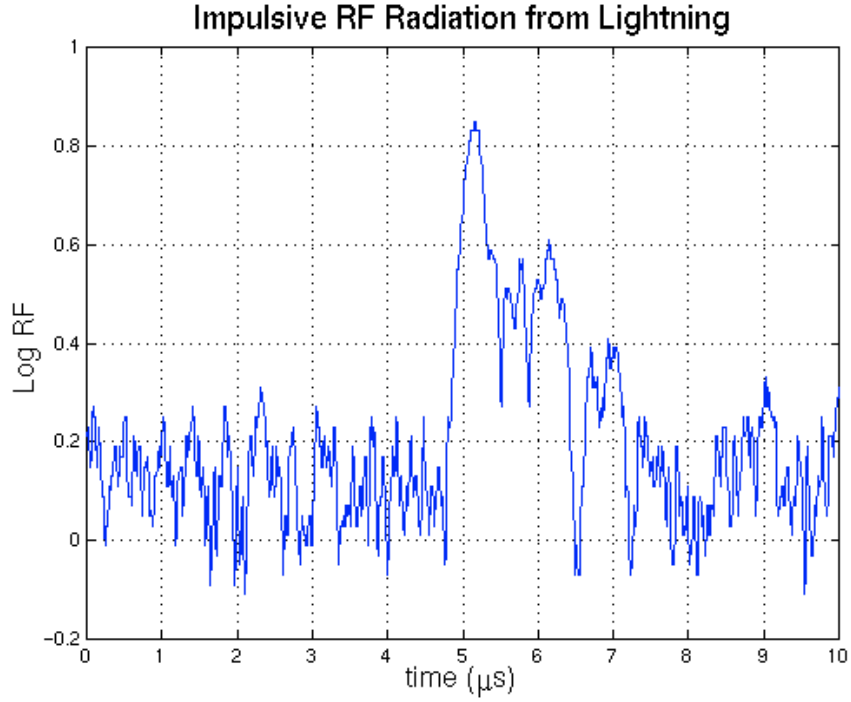
### 1.2.1 Direction finding

Radio direction finding is the oldest radio localization method. It uses receiver system sensitive to the angular orientation of the incoming signal. The target is then localized by combining angular information from multiple receivers. The direction sensitivity of a system was historically achieved by using a directional antenna. Nowadays the system usually uses antenna arrays consisting of antenna elements with a semi-omnidirectional radiating pattern, but angular information combining process is still based on triangulation.

### 1.2.2 Distance measurement

Localizing a target by radio distance measurement usually uses the time-variable radio signal, rarely a signal attenuation model. The target position is obtained by combining measured distances between the target and the receiver using geometrical trilateration or multilateration. The general limiting factor of this method is the requirement of a time-space variance of the radio signal which could not be achieved in every case. In some cases, a pulse signal could be used for distance measurement. This technique is used in almost all existing lightning localization networks. The distances are obtained by measurement of time of arrival (TOA) or time of group arrival (TOGA) respectively.

To determine the 3-dimensional structure and temporal development of a lightning discharge the system utilizes the basic technique employed by the lightning mapping array that has been developed and operated at Kennedy Space Center by Carl Lennon and Launa Maier. The LMA uses time of arrival



**Figure 1.2:** Hilbert envelope of a lightning discharge signal. Source: [18]

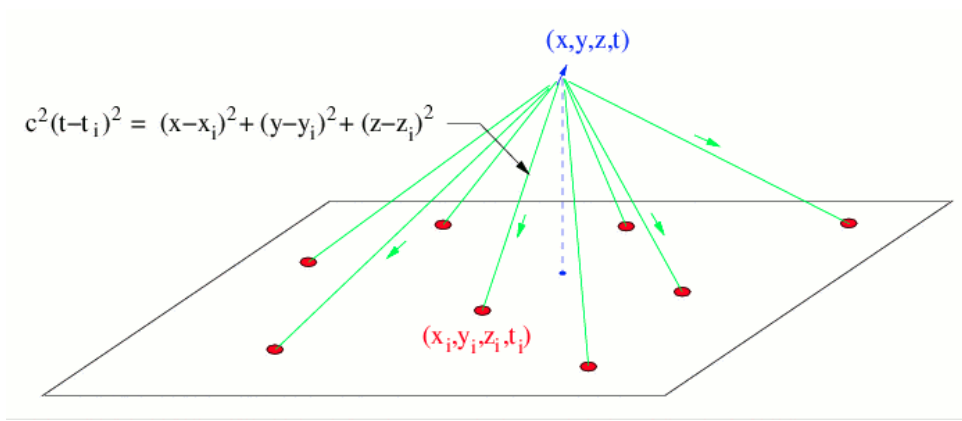
measurements to locate impulsive VHF radiation events during discharge. The figure 1.2 shows the VHF radiation for a portion of a normal lightning discharge. The sharp peaks in the Log RF plotted signal are produced by impulsive electrical breakdown events in small source regions [18].

If the time of arrival of the radiation from such an event is measured at four locations, the 3-dimensional position of the source region can be determined. If impulsive radiation occurs at location  $(x, y, z)$  and at time  $t$ , the time it is received at station  $i$  is

$$t_i = t + \frac{\text{sqrt}((x - x_i)^2 + (y - y_i)^2 + (z - z_i)^2)}{c} \quad (1.1)$$

where  $(x_i, y_i, z_i)$  is the position of station  $i$ .

By measuring the time of arrival of the radiation at least a four stations the four unknowns  $(x, y, z, t)$  can be determined. To provide for redundancy in the data (so a noise spike at one of the stations is not misidentified as a source of lightning) the system uses multiple receivers. The data from all stations is



**Figure 1.3:** Illustration of measured distances in TOA methods. Source: [18]

used to determine the location (and error in location) of the radiation source [18].

### 1.2.3 Velocity measurement

The key principle is a bistatic Doppler shift described by equation 1.2. The method is based on the fact that multiple receivers receiving the same signal reflected or generated by the same target have seen different Doppler shifted signal depending on the velocity vector of the target.

$$f = \frac{1}{\lambda} \frac{d}{dt} (R_{tx} + R_{rx}) \quad (1.2)$$

Where

- $f$  - Received frequency
- $\lambda$  - Radar transmitter operating frequency wavelength in meters
- $R_{tx}$  - Distance between the transmitter and the target
- $R_{rx}$  - Distance between the receiver and the target.

This method can localize only moving targets, but it is especially suitable for fast airspace targets which could not stop their movement due to physical laws restrictions.



## Chapter 2

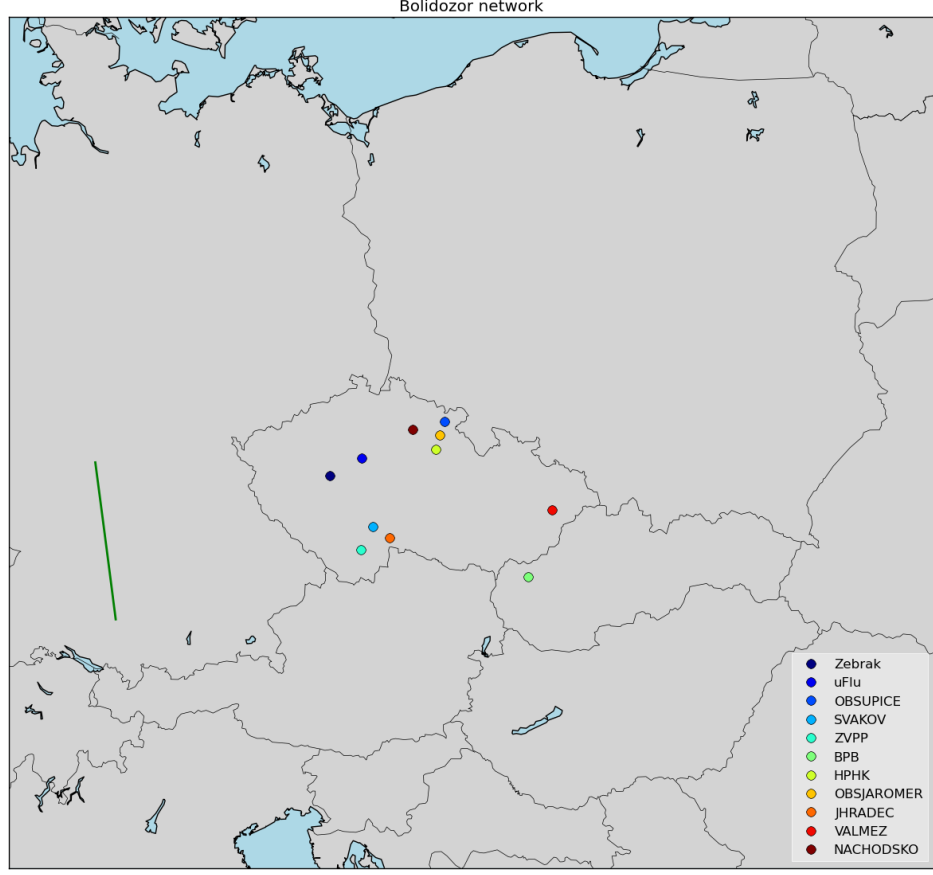
### Experimental verification

The following section describes a real experimental work, which was carried out to verify the natural phenomena detection hypotheses described above.

#### 2.1 Meteor detection system

Meteors were selected primarily as the core natural objects testing phenomenon because they have unusual properties like high velocities and a wide range of RCS. Proposed Bolidozor network [12] uses multistatic forward scattering approach which allows an efficient use of the radar transmitter energy to maximize the information value collected from the meteor reflection. The network currently uses GRAVES [27] transmitter located in France, which transmits a continuous wave (CW) signal at a frequency of 143.05 MHz. A radiation of the transmitter is directed mainly to the south hemisphere, but due to the imperfections of its antenna system, the signal from meteor reflections can be observed in almost all European countries. Therefore the transmitter is suitable for receivers' network operations with the aim of meteor trail detection and the development of algorithms for the calculation of meteor trajectory. Unfortunately, the use of a distance measurement method is not possible because the transmitter signal is only partially modulated in space by steering the transmit azimuth in several discrete sectors, but the exact method and timing of steering radar beam we can not control.

The use of such high-frequency beacon has one main advantage over the

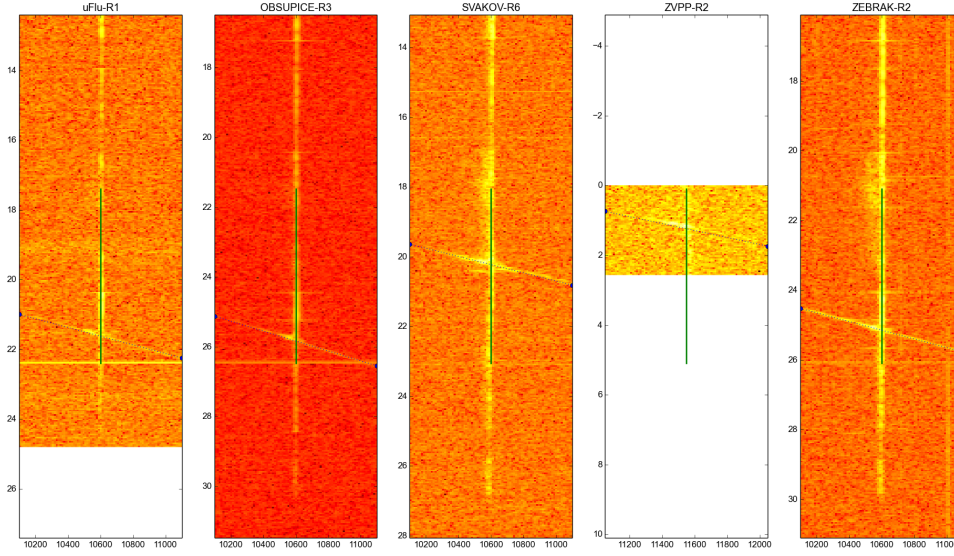


**Figure 2.1:** Bolidozor stations network

previous meteor detection experiments. Previous attempts used longer radio wavelengths in frequency range 20-50 MHz. Such long wavelengths were used to obtain a higher sensitivity to finer meteor trails. According to a simplified formula (2.1), where  $T$  is the exponential time constant and  $D$  is ambipolar diffusion coefficient and  $\lambda$  is wavelength [26]. The equation implies that at longer wavelengths we observe the meteor's echo for a longer period of time compared to shorter wavelengths. However, shorter wavelengths allow us to detect finer details of meteor trails.

$$T = \frac{\lambda^2}{16\pi^2 D} \quad (2.1)$$

The head echo of a meteor is usually called overdense due to its relatively high plasma frequency compared to used observation frequency ( $F_{obs}$ ) in the front of the meteoroid shock wave that is created in the air. This condition is expressed by the equation (2.2). However, if we use a frequency close to the



**Figure 2.2:** Example of meteor reflections for multiple stations - Spectrograms show the time aligned signal evolution over vertical axis. (The oldest data being at the bottom) Horizontal axis corresponds to the frequency. (Highest frequency on the right)

plasma frequency ( $f_{pe}$ ) of the meteor trail, we can distinguish the head echo and the meteor trail reflection because the Doppler shift is applied on the part of the reflected signal. This situation is shown in the figure 2.2 where head echoes are marked by sloped dotted lines. Static meteor trail reflections are indicated by straight vertical lines.

$$F_{obs} << f_{pe} = \frac{\sqrt{\frac{n_e e^2}{m \epsilon_0}}}{2\pi} \quad (2.2)$$

- $n_e$  is the number density of electrons
- $e$  is the elementary electrical charge
- $m$  is the effective mass of the electron
- $\epsilon_0$  is the permittivity of vacuum.

Obviously, not all parts of the meteor trail are observable from one station as the signal can be scattered to different directions non-specularly. However, if we use multiple receiving stations, we greatly increase the sensitivity, because several stations could be located in the reflection spots. Therefore it is very useful to have stations working as a cooperative detection network. The

network of stations has many advantages over a single transmitter - single receiver configuration. For example, it brings about robustness which allows operability even in a case that a part of the system is under a maintenance and therefore not functional.

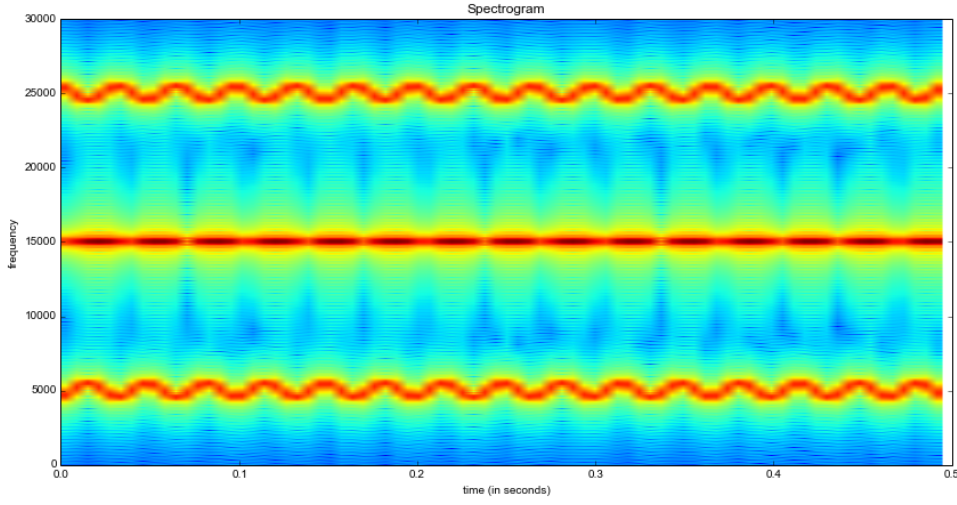
There also exist signal processing advantages, especially if we want to compute meteor parameters such as its velocity and trajectory from the meteor radio observation. All physical parameters we could determine from the single reflection are signal intensity and frequency shift in a given time which corresponds to an ionization intensity and bi-static velocity. Therefore we must combine information about one meteor event from multiple stations to obtain points in space corresponding to the meteor trajectory. We align the events according to time stamps. Therefore, a precise time synchronization between the stations is required. The exact required precision depends on the network geometry. However, if we want to work in 300 m distance resolution, which is typical for the current optical methods, we need the time precision on approximately the microseconds scale. Therefore, we needed to develop a high-performance receiver with specific parameters, in particular with a high quality of time synchronization. Tight time synchronization requirements between nodes increase the complexity of the receiver system. To simplify the development process we used MLAB open source electronic prototyping platform.

As a result, a new type of radio meteor detection system is being built, based on a new idea of distributed scientific measurement systems. At the moment Bolidozor network produces a large volume of valuable radioastronomical data ready for further processing. We currently have an extensive database of multi-station meteor reflections. Unfortunately, we have yet not reached a suitable network geometry to reliably obtain meteor position and trajectory by the known methods [36]. To overcome the missing algorithm issue, a further evolution of Bolidozor network should be focused on the research of the new trajectory estimation algorithms. We are also working on the network extension with the aim of extending its service area as well as increasing the station's density which should decrease data noise and improve the numerical stability of algorithms.

### 2.1.1 VOR Transmitters as signal sources

Although GRAVES military radar is a high power transmitter which easily allows basic detection of meteors, it is not an optimal system for meteor localization because it only has one transmitter, measurement method cannot be extended to the whole earth, and the transmitted signal is not suitably





**Figure 2.3:** VOR signal numerical model

modulated to allow a useful distance measurement. Therefore several other available transmitters are investigated, such as FM radio transmitters or VOR beacons.

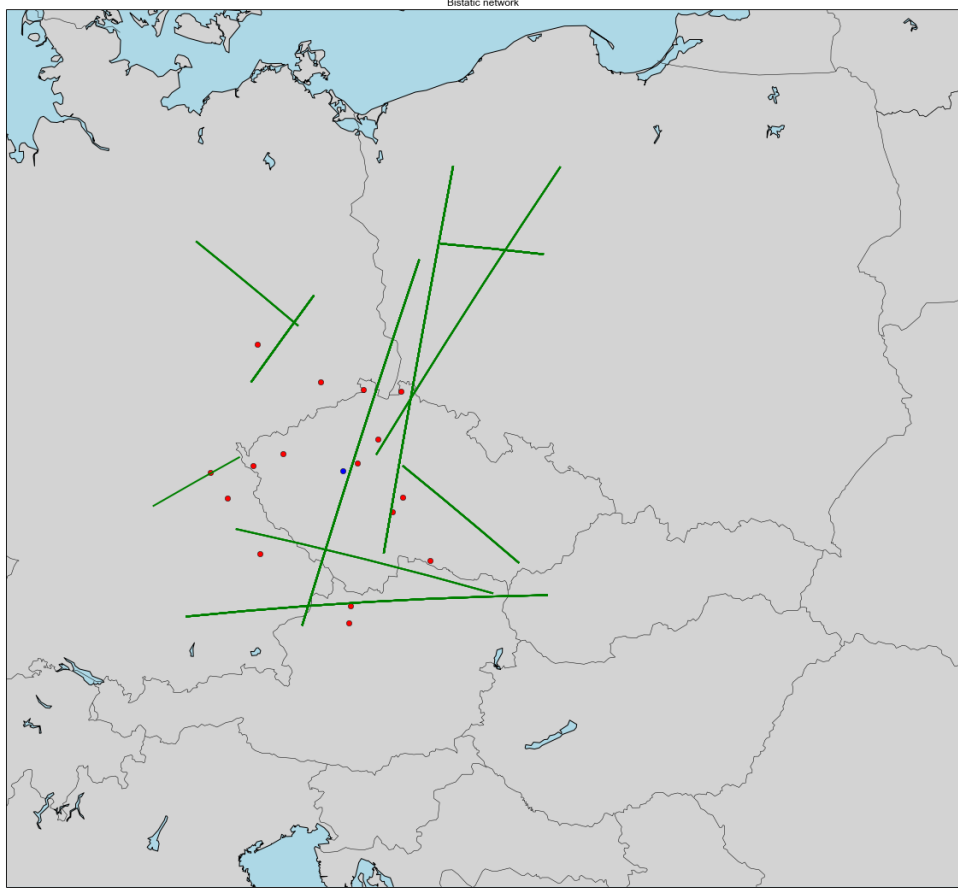
For feasibility study of meteor detection based on VOR beacons, a numerical signal model has been created. The spectrum of modeled signal is shown in figure 2.3.

This signal is expected to be reflected from an ionized meteor trail, and signal reflection will be detected and extracted from the noise using the VOR signal replica. An intensity of received reflected signal was modeled by using a standard radar equation 2.3.

$$P_r = \frac{P_t G_t G_r \lambda^2 \sigma}{(4\pi)^3 R_t^2 R_r^2 L} \quad (2.3)$$

Where

- $P_r$  — Received power in watts.
- $P_t$  — Peak transmit power in watts.
- $G_t$  — Transmitter antenna gain.
- $G_r$  — Receiver antenna gain.
- $\lambda$  — Radar operating frequency wavelength in meters.

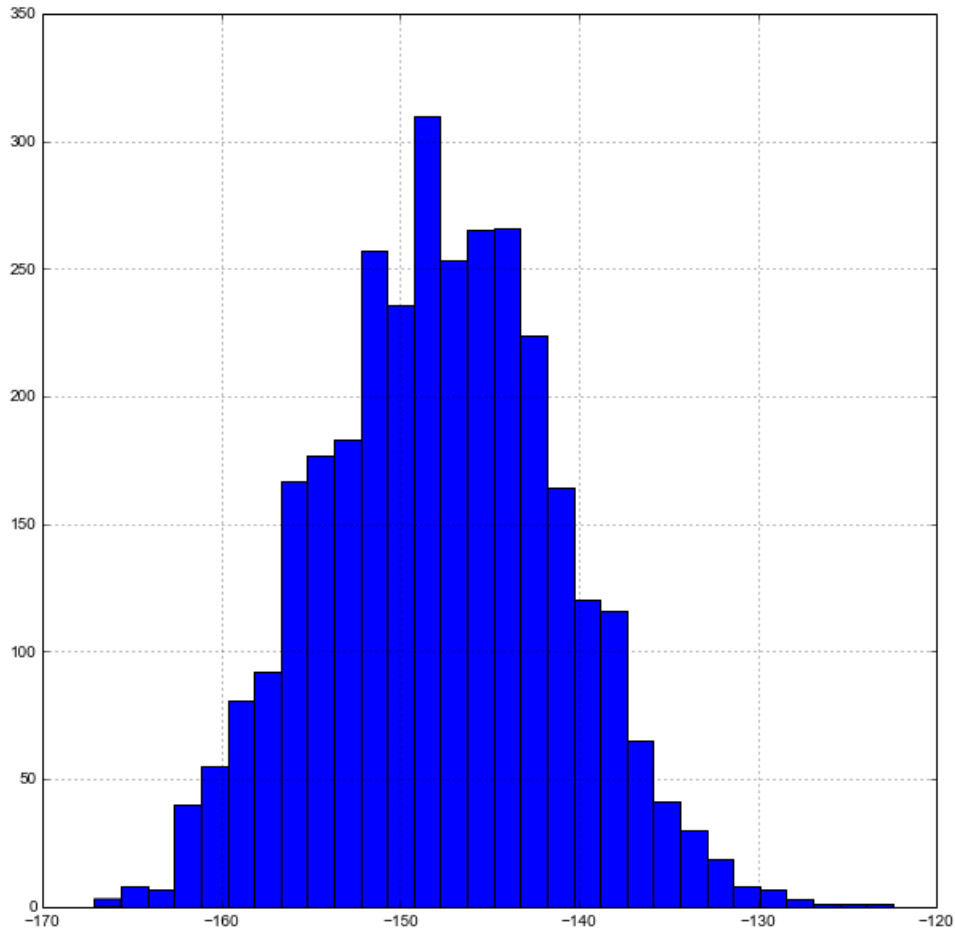


**Figure 2.4:** An example of random artificial meteor trajectories

- $\sigma$  — Target's nonfluctuating radar cross section in square meters.
- $L$  — General loss factor to account for both system and propagation loss.
- $R_t$  — Range from the transmitter to the target.
- $R_r$  — Range from the receiver to the target.

The model generates many meteor trajectories (figure 2.4 and calculates the signal power at receiver for point of closest approach. The resulting power histogram is shown in figure 2.5.

As could be seen from resulting histogram, the power of expected received signal is on the verge of the radio receiver sensitivity. Therefore the detection could work over only a relatively small distance, and receiver system must therefore properly handle the strong ground signal and weak reflected signal.



**Figure 2.5:** Distribution of expected signal power on receiver [dBm] on horizontal axis and meteor count on vertical axis.

Such desired behavior could be probably best achieved by use of an antenna with suitable direction sensitivity.

## 2.2 Hemispherical radiating pattern antenna design

A highly directional pattern antenna is usually used for radio meteor observations, but these types of antennas became impractical in cases where we have multiple transmitters such as VOR beacons, spread around a reception station. In that situation, the hemispherical sensitivity of the antenna is more valuable than the peak directional antenna gain. A hemispherical radiation pattern antenna should be the best solution. The symmetry of the radiation

pattern of such antenna allows easy construction of antenna arrays which could be used for angular measurement of received signals.

### ■ 2.2.1 Patch Antenna Design

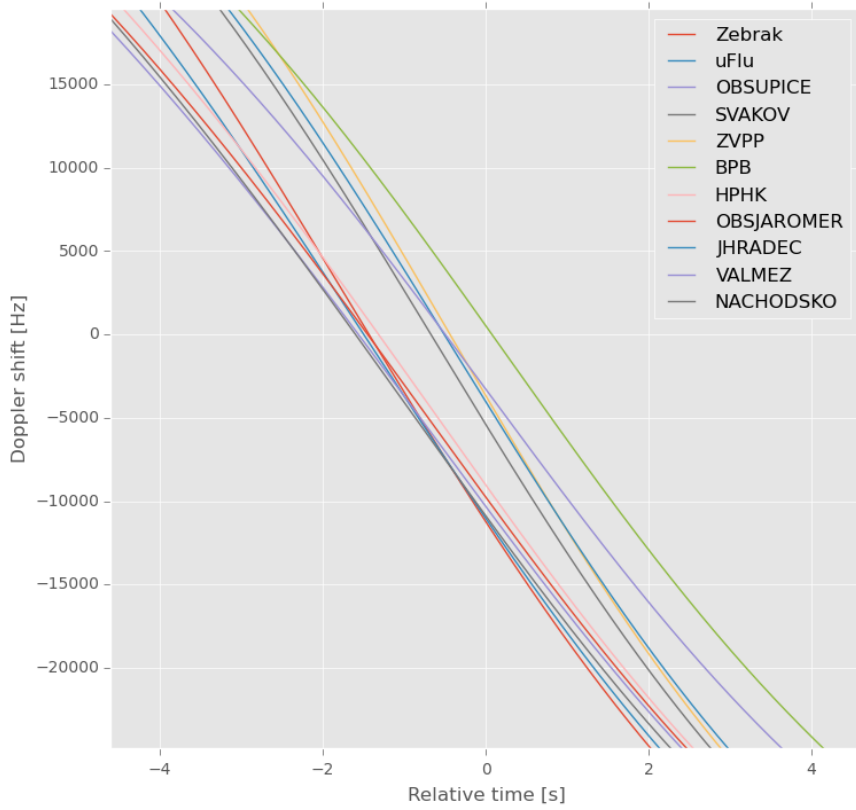
Patch antenna was initially examined due to an expectation of a simple construction and easy manufacturing. The antenna was experimentally constructed from wire mesh with a square grid. This grid was chosen as a compromise between antenna quality (surface conductivity) and the possibility of icing on antenna's surfaces. Real prototype of the antenna was made according to the computer model. Unfortunately, after the antenna's construction and verification, it was found that the antenna is very sensitive to deformation of patch base element and for a position of the central elevated element. Additionally, the central part must be a precise square to achieve a circular polarization.

### ■ 2.2.2 Short-circuited quadrifilar helix

Another antenna type was proposed to overcome the issues of the previous antenna design experiment. Short-circuited quadrifilar helix (SC-QHA) is a variant of a well-known self-phased quadrifilar helix antenna (SP-QHA). However, unlike the SP-QHA type, the SC-QHA has a narrower bandwidth which depends primarily on a bandwidth of a phasing network. Therefore the antenna could be more efficient for narrow band signals like meteor reflections. The antenna was numerically modeled in NEC2++ software.

## ■ 2.3 Meteor trajectory determination

Every radio illuminated meteor trajectory in the atmosphere creates its Doppler shift reflection footprint. This process could be described by a numerical model of Doppler shifts for points on the trajectory. For simplicity, the tested model expects constant velocity along a straight line of the meteor path which is divided into equidistant time samples. A numerical difference of path distances between transmitter, meteor, and receiver are computed, then velocity and Doppler shift value are obtained for every point of the trajectory.



**Figure 2.6:** Doppler shifts calculated for meteor ground path displayed in the figure 2.1.

The resulting figure of Doppler shifts calculated along the model meteor path radio-detectable on every existing station is shown in figure 2.6.

This signal model can be partially confirmed from Bolidozor meteor database where several meteor events are recorded on multiple stations. If we plot such meteor event in time aligned spectrogram, we obtain an image similar to the figure 2.2. Precise meteor trajectory estimation methods are investigated at the moment. One of the difficulties is a possible suboptimal geometry configuration and low inter-station events correlation.





## Chapter 3

### Future work

Although some meteor trajectory estimation algorithms are developed, the real precision of estimation is unknown because it needs a comparison with other trajectory estimation method. The best candidate will be probably optical measurement performed at the event which is detected by radio method and by optical observations. A journal publication can be expected as the future result of this experiment.

Algorithmic complexity of meteor trajectory estimation could be possibly reduced by introducing some additional information other than velocity measurements. The direction finding using phased antenna array is the most promising candidate for improving the measurement method because a distance measurement is not usable for meteors due to the lack of a globally available network of transmitters which allows direct distance measurement. However, distance measurement localization method could be used in the same system for natural phenomena which produce a wide-band time limited noise-like signal such as lightning.



### 3.1 Expansion of used methods to other natural phenomena

The analysis mentioned above of state of the art methods and systems leads to a conclusion that the dissertation should focus on multi-methodical detection and analysis of natural phenomena which is already the most promising

area for radio scientific research. Already obtained experiences can be used for detection other natural phenomena like lightning strikes which could be extremely useful for work at the CRREAT project which needs precise localization of atmospheric events to achieve its scientific goals. A publishable result could be expected according to CRREAT project roadmap because measurement of lightning position and its parameters are needed for describe the dependence on some other phenomena.

## ■ 3.2 Proposed lightning detection system

The source [14] suggests that the lightning pulses are strongly polarized where the polarization direction varies strongly for the individual peaks that form the total pulse. Combining the intensity and polarization information from many different antennas at different viewing angles on the discharge, the time structure, and direction of each charge movement can be determined. This forms the input for building a 4-D vector map of the discharge current showing for every step the position in space as well as the direction of the electric current and therefore giving detailed insight into the spatiotemporal development of the lightning. The shape of each pulse is related to the time-dependence and the distance over which the current flows.

The CRREAT team will perform measurements of the atmospheric radiation and ionization events on satellites, aircraft, unmanned aerial vehicles, monitoring cars and ground stations. The CRREAT project will contribute to improvement of space weather models, air transport safety and global navigation systems reliability.



## Appendix A

### Bibliography

- [1] Small and Short-Range Radar Systems, Gregory L. Charvat, CRC Press 2014, Pages 1–35, Print ISBN: 978-1-4398-6599-6, eBook ISBN: 978-1-4398-6600-9
- [2] F. G. Schröder, Instruments and Methods for the Radio Detection of High Energy Cosmic Rays, *DISSERTATION*, Tag der mündlichen Prüfung: 11. Februar 2011
- [3] K. Mikhailov, J. van Leeuwen, The LOFAR search for radio pulsars and fast transients in M33, M81 and M82, *Astrophysics of Galaxies*, A&A 593, A21 (2016), DOI: 10.1051/0004-6361/201628348
- [4] Radio detection of air showers with LOFAR and AERA - LOFAR key science project Cosmic Rays and Pierre Auger Collaborations (Hörandel, Jörg R. for the collaboration) JPS Conf.Proc. 9 (2016) 010004 arXiv:1509.04960 [astro-ph.HE]
- [5] MANN, I., PELLINEN-WANNBERG, A., MURAD, E., et. al. Dusty plasma effects in near earth space and interplanetary medium. *Space Science Reviews*, 2011, Vol. 161, Issue 1-4: 1-47 10.1007/s11214-011-9762-3
- [6] J. Stasielak, R. Engel, S. Baur, P. Neunteufel, R. Šmída, F. Werner, H. Wilczyński Feasibility of radar detection of extensive air showers *Astroparticle Physics*, Volume 73, 15 January 2016, Pages 14–27, astropartphys.2015.07.003
- [7] BLAND, PHILIP, A., The Desert Fireball Network *Astronomy & Geophysics*, vol. 45, number 5. pages 5.20-5.23 10.1046/j.1468-4004.2003.45520



- [19] Richard L. Dowden, James B. Brundell, Craig J. Rodger, VLF lightning location by time of group arrival (TOGA) at multiple sites *ournal of Atmospheric and Solar-Terrestrial Physics* 64 (2002) 817–830
- [20] William P. Roeder, Jon M. Saul, Four Dimensional Lightning Surveillance System: Status and Plans *22nd International Lighting Detection conference* (2012)
- [21] Kenneth L. Cummins, Martin J. Murphy, An Overview of Lightning Locating Systems: History, Techniques, and Uses, With an In-depth Look at the U.S. NLDN *IEEE Transaction on Electromagnetic Compatibility* (4/15/2009)
- [22] WEBSTER, A. R., BROWN, P. G., JONES, J., et. al. Canadian Meteor Orbit Radar (CMOR) *Atmos. Chem. Phys.*, 4, 679-684, 2004 [www.atmos-chem-phys.org/acp/4/679/](http://www.atmos-chem-phys.org/acp/4/679/) SRef-ID: 1680-7324/acp/2004-4-679
- [23] WISLEZ, J.-M., Forward scattering of radio waves off meteor trails *Proceedings of the International Meteor Conference*, Brandenburg, Germany, 1995, p. 99-117
- [24] CLEGG, J. A. ,HUGHES, V. A. A., LOVELL, C. B., The Daylight Meteor Streams of 1947 May-August *Monthly Notices of the Royal Astronomical Society*, Vol. 107, p.369
- [25] LAMY, H., ANCIAUX, M., RANVIER, S., Recent advances in the BRAMS network *Proceedings of the International Meteor Conference*, Mistelbach, Austria, 27-30 August 2015, Eds.: Rault, J.-L.; Roggemans, P., International Meteor Organization, ISBN 978-2-87355-029-5, pp. 171-175
- [26] POOLE, L. M. G., Duration distribution of radio echoes obtained from underdense shower meteor trains *Smithsonian Contributions to Astrophysics*, Vol. 11, p.181
- [27] ALLEN, T., A GRAVES Sourcebook, Version of 2013-08-07 [Online] Cited 2016-1-23. Available at: <http://fas.org/spp/military/program/track/graves.pdf>
- [28] HORKEL, M., CHROUST, J., JANAS, M., et. al. MLAB - The Modular Laboratory project. [Online] Cited 2016-1-23. Available at: <http://www.mlab.cz/>
- [29] STRAND-BERGESEN, B, et. al. SDR-Widget interface [Online] Cited 2016-1-23. Available at: <https://github.com/borgestrand/sdr-widget>
- [30] MELTON, J., Ghpsdr3 [Online] Cited 2016-1-23. Available at: <http://openhpsdr.org/wiki/index.php?title=Ghpsdr3>
- [31] UNIVERSAL SCIENTIFIC TECHNOLOGIES, s.r.o., Radio meteor detection station RMDS02D [Online] Cited 2016-1-23. Available at: <http://wiki.mlab.cz/doku.php?id=cs:rmds>

- [32] South Bohemian Czech astronomy society department *Czech astronomy society annual report 2015* Pages 40-46
- [33] PEREZ,GRANGER, F., BRIAN E., IPython: A System for Interactive Scientific Computing *Computing in Science & Engineering* 2007, vol 9.,number 3, Pages 21-29
- [34] RAGAN-KELLEY, M., PEREZ, F., GRANGER, B., et al., The Jupyter/IPython architecture: a unified view of computational research, from interactive exploration to communication and publication. *American Geophysical Union*, Fall Meeting 2014 12/2014
- [35] JONES E, OLIPHANT E, PETERSON P, et al. SciPy: Open Source Scientific Tools for Python 2001-, <http://www.scipy.org/> [Online; accessed 2016-03-07].
- [36] STEYAERT, C.,VERBELEN, F., et al., Meteor Trajectory from Multiple Station Head Echo Doppler Observations *WGN, the Journal of the IMO* 38:4 (2010)