

Answer 1

Constraint satisfaction Problem Vs Problem solving using search

>> In constraint satisfaction problem, we have a finite set of variables, nonempty domain of possible values for each variable and a finite set of constraints.

We wish to find an assignment that does not violate the constraints.

For problem solving using search, we have start state, goal state and some permissible actions. We wish to reach goal state following any path.

>> In constraint satisfaction, first constraints are discovered and propagated as far as possible throughout the system. Then, if there is still not a solution, search begins. Thus, it is a two step process.

In the latter approach, there is no propagation. We keep following path in the hope that it will lead to the goal state.

Cryptarithmic problem :

$$\begin{array}{r} \text{EAR} \\ + \text{EAR} \\ \hline \text{DRUM} \end{array}$$

Assumptions :-

- 1) The values for all the alphabets are distinct.
- 2) No alphabet has value 0 and value is single-digit.

$$\begin{array}{r} c_1 \\ \text{EAR} \\ c_2 \text{EAR} \\ \hline \text{DRUM} \end{array}$$

c_i 's denote the carry generated.

Initial state

M is even
 $\because D \neq 0$ and all values are single digit, carry ≤ 1
 $\Rightarrow C_3 = 1$
 $\Rightarrow D = 1$
 $U = (2A + C_1) \% 10$
 $R = (2E + C_2) \% 10$

let $R = 2$
 $\Rightarrow M = 4$
 $C_1 = 0$
 $U = (2A) \% 10$
 $2 = (2E + C_2) \% 10$
 M is even \Downarrow
 $E = 0$ or 1

let $R = 3$
 $\Rightarrow M = 6, C_1 = 0$
 $\because U$ is even
 $A = 2$ not possible
 (no value for E)
 $A = 4$ not possible
 (no value for E)
 $A = 6$ conflicts with U

let $R = 4$
 on
 Next page

For $C_2 = 0$ $E = 6$ [\because For $C_2 = 1$ not possible]
 $\because U$ is even
 and $C_2 = 0 \Rightarrow A < 5$
 $A = 3, 4$
 \downarrow
 U conflicts with E \downarrow conflicts with M
 No value possible for A .

$A = 7$
 $\Rightarrow U = 4$
 E no value of E possible
 $A = 8$
 U conflicts with M
 $A = 9$
 No value of E is possible.
 Hence,
 No value possible for A .

Initial state

 M is even

$D = 1$

$C_3 = 1$

$U = (2A + C_1) \% 10$

$R = (2E + C_2) \% 10$

$R = 2$

Not possible

$R = 3$

Not possible

$R = 4$

$\Rightarrow M = 8, C_1 = 0$

 $A = 2$ not possible $(U$ conflicts with $R)$

let $A = 3$

$\Rightarrow U = 6, C_2 = 0$

$10 + 4 = 2E + 0$

$\Rightarrow E = 7$

All alphabets are assigned values. No conflicts.

We stop here.

Finally, $A = 3$

$E = 7$

$U = 6$

$D = 1$

$M = 8$

$R = 4$

$C_1 = 0$

$C_2 = 0$

$C_3 = 1$

$$\begin{array}{r}
 \textcircled{0} \textcircled{0} \\
 7 \ 3 \ 4 \\
 \textcircled{1} \ 7 \ 3 \ 4 \\
 \hline
 1 \ 4 \ 6 \ 8
 \end{array}$$

$$\begin{array}{r}
 \text{EAR} \\
 + \text{EAR} \\
 \hline
 \text{DRUM}
 \end{array}$$

Answer 3.

Underestimation and overestimation of a heuristic function

A heuristic function gives an estimated cost of reaching goal state from current state.

let h = actual cost of getting from current state to goal state

h^* = estimate of h [our heuristic function].

Underestimation: When $h^* \leq h$

our heuristic function underestimates the cost of getting from current state to goal state.

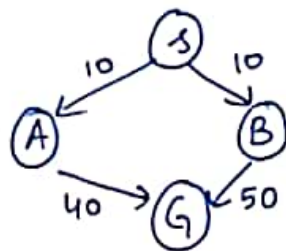
In this case, we always get the optimal solution.

Overestimation: When $h^* > h$

our heuristic function overestimates the cost of getting from current state to goal state.

In this case, we cannot guarantee finding the cheapest path solution unless we expand the entire graph until all paths are longer than the best solution.

Example:



For A* algorithm
 $f(n) = g(n) + h(n)$

$h^*(A) = 30$, $h^*(B) = 20$
 Underestimation

$S \rightarrow A$ $f(A) = 40$

$S \rightarrow B$ $f(B) = 30 \checkmark$

$S \rightarrow B \rightarrow G$ $f(G) = 60 < 40$

$S \rightarrow A \rightarrow G$ $f(G) = 50 \checkmark$

optimal solution obtained

$h^*(A) = 80$, $h^*(B) = 20$
 Overestimation

$S \rightarrow A$ $f(A) = 90$

$S \rightarrow B$ $f(B) = 30 \checkmark$

$S \rightarrow B \rightarrow G$ $f(G) = 80 \checkmark$

optimal solution
 is not reached

Conditions under which A^* algorithm gives optimal solution

- 1) A^* returns optimal solution if $h(n)$ is admissible - it never overestimates true cost to nearest goal.

$$h(n) \leq h^*(n).$$

As shown in previous example for $h(n) > h^*(n)$ optimal solution is not reached.

- 2) A^* return optimal solution if $h(n)$ is consistent - for every node n , every successor n' of n generated by action a ,

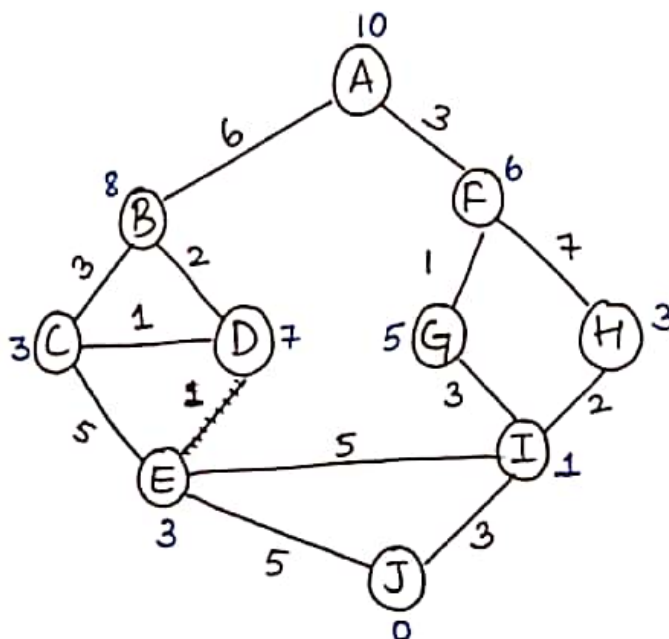
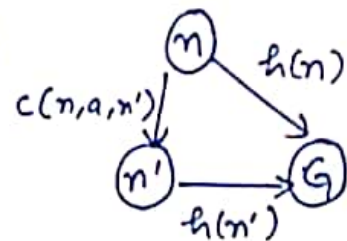
$$h(n) \leq c(n, a, n') + h(n')$$

let n' is successor of n , then

$$\begin{aligned} g(n') &= g(n) + c(n, a, n') \\ &= g(n) + c(n, a, n') + h(n') \\ &> g(n) + h(n) \\ &= f(n) \end{aligned}$$

$$f(n') > f(n)$$

$\Rightarrow f(n)$ is non decreasing along any path - which is desirable.



The numbers on edge represent distance between the nodes.

The numbers written on node represent heuristic value $h(n)$, where $n = A, B, \dots, J$

start state: A goal state: J

(a) Greedy best first search algorithm

Evaluation function $f(n) = h(n)$

Start state: A

Step 1: A is expanded to get B and F.

$h(B) > h(F)$.

Step 2: F is expanded to get G and H.

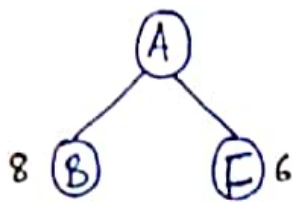
$h(G) > h(H)$

Step 3: H is expanded to get I.

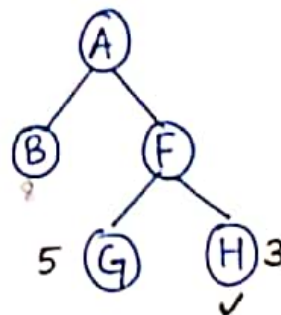
Step 4: I is expanded to get E and J.

$h(E) > h(J)$.

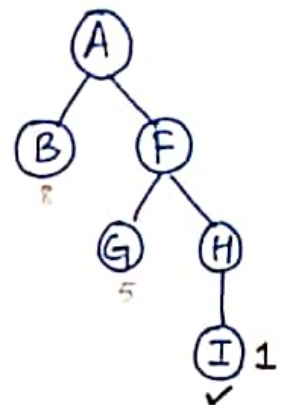
Goal state J is reached.



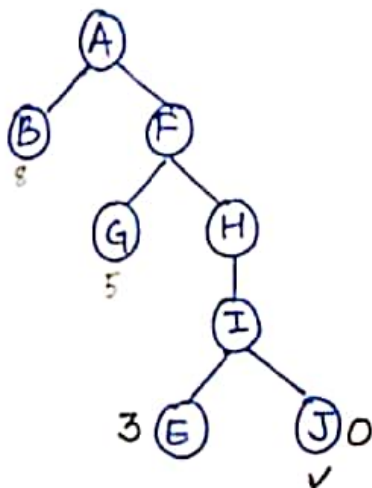
Step 1:



Step 2:



Step 3



Step 4.

Greedy best first search
on graph given

(b) A^* algorithm

start state: A

Evaluation function $f(n) = g(n) + h(n)$ step 1

A 10

$$A \rightarrow B \quad f(B) = 8 + 6 = 14$$

$$A \rightarrow F \quad f(F) = 6 + 3 = 9 \quad \checkmark$$

$$f(B) > f(F)$$

Path $A \rightarrow F$ is selected.step 2

$$A \rightarrow F \rightarrow G \quad f(G) = \overset{(3)}{9} + 1 + 5 = 9 \quad \checkmark$$

$$A \rightarrow F \rightarrow H \quad f(H) = \overset{(3)}{9} + 7 + 3 = 13$$

Out of $A \rightarrow B$, $A \rightarrow F \rightarrow G$ and $A \rightarrow F \rightarrow H$,path $A \rightarrow F \rightarrow G$ has smallest value of f .Path $A \rightarrow F \rightarrow G$ is selected.step 3

$$A \rightarrow F \rightarrow G \rightarrow I \quad f(I) = 7 + 1 = 8 \quad \checkmark$$

Out of $A \rightarrow B$, $A \rightarrow F \rightarrow H$ and $A \rightarrow F \rightarrow G \rightarrow I$,path $A \rightarrow F \rightarrow G \rightarrow I$ is selected as it has the smallest value of f .step 4

$$A \rightarrow F \rightarrow G \rightarrow I \rightarrow E \quad f(E) = 12 + 3 = 15$$

$$A \rightarrow F \rightarrow G \rightarrow I \rightarrow J \quad f(J) = 10 + 0 = 10$$

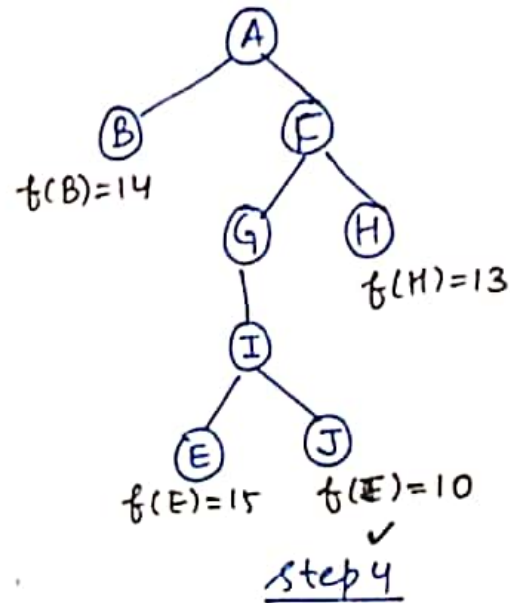
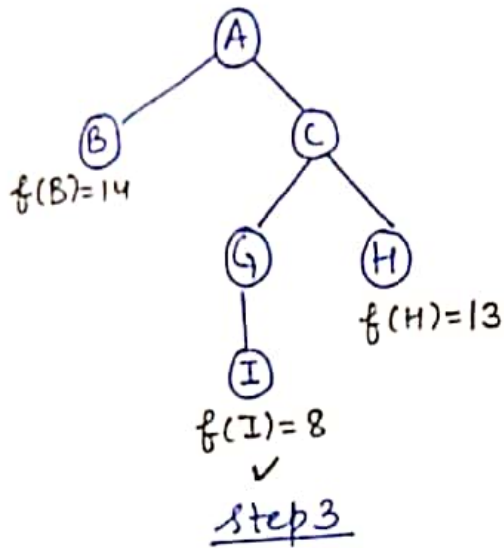
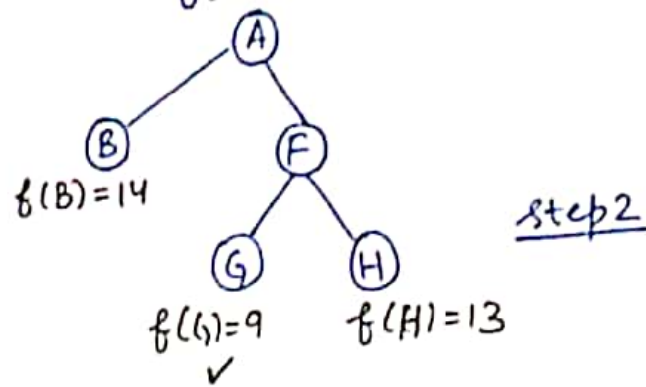
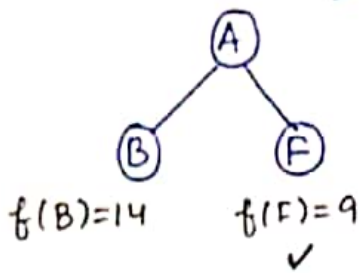
Out of paths $A \rightarrow B$, $A \rightarrow F \rightarrow H$, $A \rightarrow F \rightarrow G \rightarrow I \rightarrow E$ and $A \rightarrow F \rightarrow G \rightarrow I \rightarrow J$, path $A \rightarrow F \rightarrow G \rightarrow I \rightarrow J$ is selected, as it has the smallest value of f .

We have reached goal state J.

 \therefore We stop here.

n	$h(n)$
A	10
B	8
C	3
D	7
E	3
F	6
G	5
H	3
I	1
J	0

Diagrammatically,

A* algorithm on graph given

Answer 5

(a) Everyone who loves all animals is loved by someone
 S1 $\forall x [\forall y \text{ Animal}(y) \rightarrow \text{loves}(x, y)] \rightarrow [\exists z \text{ loves}(z, x)]$

Anyone who kills an animal is loved by noone.

S2 $\forall x [\exists y \text{ Animal}(y) \wedge \text{kills}(x, y) \rightarrow [\forall z \neg \text{loves}(z, x)]]$

John Jack loves all animals.

S3 $\forall x \text{ Animal}(x) \rightarrow \text{loves}(\text{Jack}, x)$

Either Jack or John killed the cat, who is named Pussy

S4 $\text{kills}(\text{Jack}, \text{Pussy}) \vee \text{kills}(\text{Ravi}, \text{Pussy}) \wedge \text{Cat}(\text{Pussy})$

Cats are animals.

S5 $\forall x (\text{Cat}(x) \rightarrow \text{Animal}(x))$

Predicates Used :

$\text{Animal}(x) : x$ is an animal

$\text{Cat}(x) : x$ is a cat

$\text{loves}(x, y) : x$ loves y

$\text{kills}(x, y) : x$ killed y

(b) Converting to Prenex Normal Form

S1: $\forall x [\forall y \neg \text{Animal}(y) \vee \text{loves}(x, y)] \rightarrow [\exists z \text{ loves}(z, x)]$
 $\forall x [\exists y \text{ Animal}(y) \wedge \neg \text{loves}(x, y)] \vee [\exists z \text{ loves}(z, x)]$

S2: $\forall x [\forall y \neg \text{Animal}(y) \vee \neg \text{kills}(x, y)] \vee [\forall z \neg \text{loves}(z, x)]$

S3: $\forall x \neg \text{Animal}(x) \vee \text{loves}(\text{Jack}, x)$

S4: $\text{kills}(\text{Jack}, \text{Pussy}) \vee \text{kills}(\text{Ravi}, \text{Pussy}) \wedge \text{Cat}(\text{Pussy})$

S5: $\forall x \neg \text{Cat}(x) \vee \text{Animal}(x)$

(c) Skolemize the formulae

$$S1: \forall x [\text{Animal}(F(x)) \wedge \neg \text{loves}(x, F(x))] \vee \text{loves}(G(x), x)$$

Removing universal quantifier,

$$= [\text{Animal}(F(a)) \wedge \neg \text{loves}(a, F(a))] \vee \text{loves}(G(a), a)$$

$$= [\text{Animal}(F(a)) \vee \text{loves}(G(a), a)] \wedge$$

$$[\neg \text{loves}(a, F(a)) \vee \text{loves}(G(a), a)]$$

$$S2: \neg \text{Animal}(b) \vee \neg \text{kills}(a, b) \vee \neg \text{loves}(c, a)$$

$$S3: \neg \text{Animal}(a) \vee \text{loves}(\text{Jack}, a)$$

$$S4: \text{kills}(\text{Jack}, \text{Pussy}) \vee \text{kills}(\text{John}, \text{Pussy}) \wedge \text{Cat}(\text{Pussy})$$

$$S5: \neg \text{Cat}(a) \vee \text{Animal}(a)$$

Finally, In CNF

$$S1 \quad 1. \text{Animal}(F(a)) \vee \text{loves}(G(a), a)$$

$$S1 \quad 2. \neg \text{loves}(a, F(a)) \vee \text{loves}(G(a), a)$$

$$S2 \quad 3. \neg \text{Animal}(b) \vee \neg \text{kills}(a, b) \vee \neg \text{loves}(c, a)$$

$$S3 \quad 4. \neg \text{Animal}(a) \vee \text{loves}(\text{Jack}, a)$$

$$S4 \quad 5. \text{kills}(\text{Jack}, \text{Pussy}) \vee \text{kills}(\text{John}, \text{Pussy})$$

$$S4 \quad 6. \text{Cat}(\text{Pussy})$$

$$S5 \quad 7. \neg \text{Cat}(a) \vee \text{Animal}(a)$$

(d) Who killed Pussy?

1. $\text{Animal}(f(a)) \vee \text{loves}(g(a), a)$
2. $\neg \text{loves}(a, f(a)) \vee \text{loves}(g(a), a)$
3. $\neg \text{Animal}(b) \vee \neg \text{kills}(a, b) \vee \neg \text{loves}(c, a)$
4. $\neg \text{Animal}(a) \vee \text{loves}(\text{Jack}, a)$
5. $\text{kills}(\text{Jack}, \text{Pussy}) \vee \text{kills}(\text{John}, \text{Pussy})$
6. $\text{Cat}(\text{Pussy})$
7. $\neg \text{Cat}(a) \vee \text{Animal}(a)$
8. $\text{Animal}(\text{Pussy})$ Using 6 & 7
9. $\text{loves}(\text{Jack}, \text{Pussy})$ Using 4 & 8
10. $\neg \text{kills}(\text{Jack}, \text{Pussy})$ Using 3, 8 & 9
11. $\text{kills}(\text{John}, \text{Pussy})$ Using 5 & 11

Hence, using resolution algorithm, we inferred following :-

$\neg \text{kills}(\text{Jack}, \text{Pussy}) \rightarrow$ Jack did not kill Pussy

$\text{kills}(\text{John}, \text{Pussy}) \rightarrow$ John killed Pussy.

Who killed Pussy? John.

Answer 6.

Differentiate the following

(a) Turing Test approach vs Rational ^{agent} approach

It concerns on acting humanly.

How human acts in a given situation.

Human behavior is well adapted for one specific environment and is defined by sum of total of things that human do.

This approach gives optimal solution since solvable by humans.

It concerns on acting rationally.

Acting so as to achieve one's goals, given one's beliefs.

It is more amenable to scientific development as the standard of rationality is clearly defined and completely general.

This approach gives the best expected outcome if best outcome is not achievable.

(b) Knowledge based systems vs Expert systems

It uses reasons and a knowledge base to solve complex problems.

It is divided into Logic, Frames, Rules or Semantic Networks for knowledge representation.

It represent knowledge in a declarative way.

It emulates decision-making ability of a human expert.

It is divided into two subsystems: the knowledge base and inference engine. (rule interpreter).

It ~~is~~ represents knowledge as if-then rules.

Example: MYCIN system.

(c) Best first search ✓

It is informed search strategy - it has additional information available (about the goal).

It uses an evaluation function $f(n)$.

It selects the node which has lowest value of $f(n)$.

It uses advantages of both breadth first and depth first search.

Breadth first search.

It is uninformed search strategy - uses only the information available in the problem definition.

It does not use any evaluation function.

It expands/selects the shallowest unexpanded node.

It does not resemble to depth first search.

(d) Hill climbing search ✓

It is informed search - has additional information about the goal.

It is a local search algorithm and checks only the immediate neighbours and selects the most promising node from them.

It may fail to find a solution due to local maximum, plateau or ridge.

It stops if there are no successor states with better values than the current state.

Iterative deepening search

It is uninformed search - has no information other than problem definition.

It performs depth-first search up to a certain "depth limit" and keeps increasing it after each iteration.

It always find solution, if solution exists.

It stops if goal node is found or when all the possibilities (depth) are executed/exhausted.

(e) Substitution vs Unification

A substitution is a finite set of the form $\{t_1/v_1, t_2/v_2, \dots, t_n/v_n\}$ where every variable v_i is different from term t_i and no two elements in the set have the same variable after the stroke symbol.

It does not use disagreement set.

There is no predefined goal, substitution is applied to 'unify' terms and formulae.

It allows use of $\{f(x)|x\}$ i.e., it is a valid substitution.

Unification is a process of determining and applying a certain substitution to a set of expressions in order to make them identical.

It requires a notion of disagreement set.

The goal is to find a most general unifier (m.g.u.)

It does not allow use of $\{f(x)|x\}$ since it would not lead to obtaining m.g.u.

(f) Model based agent vs

It keeps some internal state that depends on the percept history.

It takes the decision based on how its actions affect the world.

The goal cannot be updated.

No planning involved.

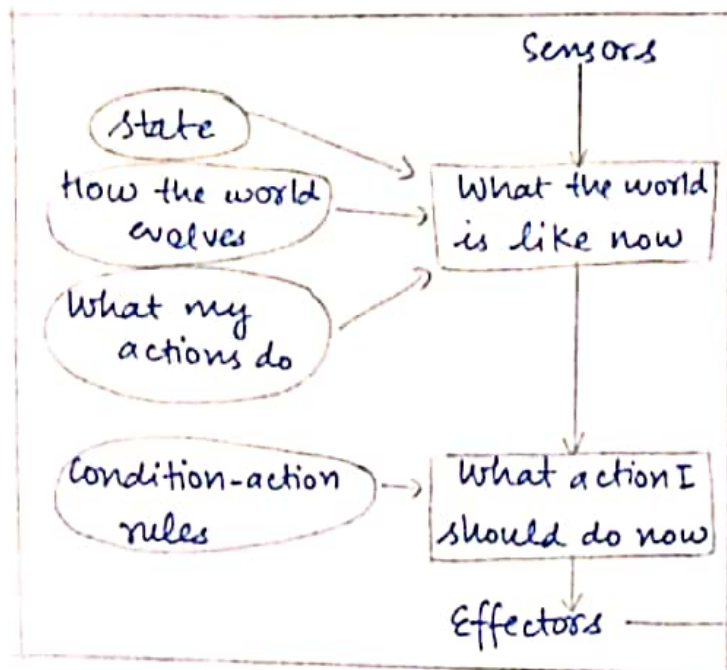
Goal based agent

It is an extension of model based agent, it also uses goals, info in addition to internal state.

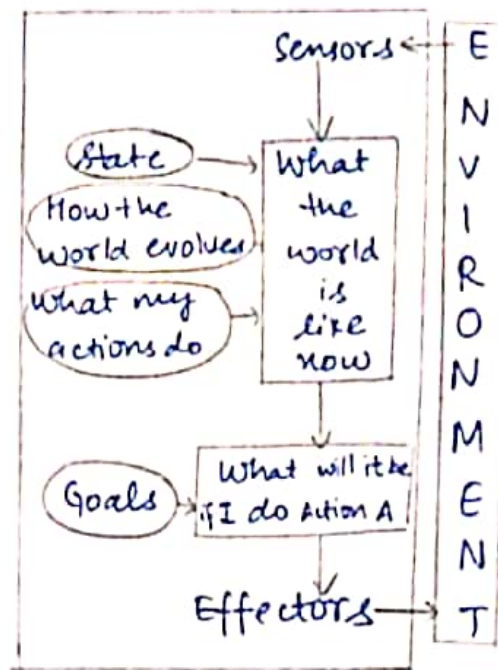
It takes the decision on the basis of I am happy?

The goal can be updated.

It performs planning and searching.



Model Based Agent



Goal Based Agent

(g) Problem solving using search vs Planning

It searches the state space of possible actions, starting from initial state.

In this the problem is solved in order. It follows any path that it believes will lead it to goal state - not subgoal state.

There is no subgoaling, so problem is not divided into chunks.

It involves task of coming up with a sequence of actions that will achieve a goal component of planning system.

The planner does not have to solve the problem in order - it can suggest actions to solve any subgoals at anytime.

The planner assumes that most part of the world are independent so they can be stripped apart and solved individually.