

## MATH-253: HW1

Due on 1/22/2024

*Prof. Oleksandr Bobrovnikov (Sasha), Spring 2024, 1/22/2024*

Kaleb Burris

## 2.1

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- a)  $\overrightarrow{RP} = \langle -1 - (-3), 3 - 7 \rangle = \langle 2, -4 \rangle$   
 b)  $\overrightarrow{PQ} = 2\vec{i} - 4\vec{j}$

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- a)  $\overrightarrow{PQ} = \langle 2, 2 \rangle, \overrightarrow{PR} = -\overrightarrow{RP} = \langle -2, 4 \rangle.$

Therefore:

$$\begin{aligned} 2\overrightarrow{PQ} - 2\overrightarrow{PR} &= 2 \cdot \langle 2, 2 \rangle - 2 \cdot \langle -2, 4 \rangle \\ &= \langle 4, 4 \rangle - \langle -4, 8 \rangle \\ &= \langle 8, -4 \rangle \end{aligned}$$

- b)  $8\vec{i} - 4\vec{j}$

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$$\|\overrightarrow{PQ}\| = \sqrt{2^2 + 2^2} = \sqrt{8} = 2\sqrt{2}$$

- a)  $\langle 1, 1 \rangle$   
 b)  $\vec{i} + \vec{j}$

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$$\vec{v} = \langle 2 - (-1), 1 - (-3) \rangle = \langle 3, 4 \rangle$$

$$\|\langle v \rangle\| = \sqrt{3^2 + 4^2} = \sqrt{9 + 16} = \sqrt{25} = 5$$

$$\left\langle \frac{3}{5}, \frac{4}{5} \right\rangle$$

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$$\vec{v} = \langle x - 1, 0 - 1 \rangle = \langle x - 1, -1 \rangle$$

$$\|\vec{v}\| = \sqrt{10} = \sqrt{(x - 1)^2 + (-1)^2}$$

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