

=====

»»»> 6f13a32dc5871f11859c2d625c5db8b60520ef89

Find the radius and interval of convergence for both of the following:

1 $\sum \frac{x^2}{k3^k}$

$$\sqrt[k]{\left| \frac{x^2}{k3^k} \right|} = \frac{\sqrt[k]{x^2}}{\sqrt[k]{k3^k}} = \frac{\sqrt[k]{x^2}}{3}$$

$$\lim_{k \rightarrow \infty} \frac{\sqrt[k]{x^2}}{3} < 3 \Rightarrow \lim_{k \rightarrow \infty} x^{\frac{2}{k}} < 9 \Rightarrow x^0 < 9 \Rightarrow 1 < 9$$

Radius = ∞ Interval = $(-\infty, \infty)$

2. $\sum \frac{(x-2)^k}{5k^2 4^4}$

$$\left| \frac{\frac{(x-2)^k}{5k^2 4^4}}{\frac{(x-2)^{k+1}}{5(k+1)^2 4^4}} \right| = \left| \frac{(x-2)^k}{5k^2 4^4} \frac{5(k+1)^2 4^4}{(x-2)^{k+1}} \right| = \left| \frac{1}{k^2} \frac{(k+1)^2}{x-2} \right| = \left| \frac{\sqrt{(k+1)^2}}{\sqrt{k^2(x-2)}} \right| = \frac{k+1}{k\sqrt{x-2}}$$

$$\frac{k+1}{k\sqrt{x-2}} \rightarrow \frac{1}{\sqrt{x-2}} \Rightarrow \frac{1}{\sqrt{x-2}} < 1 \Rightarrow 1 < \sqrt{x-2} \Rightarrow 1 < x-2 \Rightarrow 3 < x$$

Note: at $x = 3$, $\sum \frac{(3-2)^k}{5k^2 4^4} = \frac{1}{5(4^4)} \sum \frac{1}{k^2}$ the series converges by P-Series

Radius = ∞ Interval = $[3, \infty)$