§4.4 Exponential Distributions

The Exponential Distribution. The random variable X has an exponential distribution with facts:

$$X \sim \exp(\lambda), \quad \lambda > 0$$
 (1)

$$f(x,\lambda) = \begin{cases} \lambda \cdot e^{-\lambda x} & \text{if } x > 0\\ 0 & \text{otherwise} \end{cases}$$
 (2)

$$\mathbb{E}(X) = \frac{1}{\lambda} \tag{3}$$

$$var(X) = \frac{1}{\lambda^2} \tag{4}$$

§4.6 Normal Probability Plots

"Normal probability plots" are used to check an assumption of normality.

A new type of notation: If x_1, x_2, \dots, x_n is a list of numbers, we define $x_{(1)}$ to be the smallest, $x_{(2)}$ to be the smallest, and so on. $x_{(n)}$ is the largest.

Example:
$$\{4, 1, 7, 12, 3, 9\} \rightarrow x_{(1)} = 1, x_{(2)} = 3, \dots x_{(6)} = 12$$

Normal probability plots have one point per observation: for the i^{th} point,

- the *x*-coordinate is $\mathbb{E}(Z_{(i)})$ where $Z \sim N(0,1)$, and
- the y-coordinate is $x_{(i)}$, the i^{th} smallest data value.

We'll use R to create the normal probability plots. Here's how we'll interpret the points:

If the points in the normal probability plot lie on the (approximately) straight line, then the data are consistent with an underlying normal population.

Otherwise, the data are inconsistent with an underlying normal population.