

Part I

1. Evaluate $\int_1^\infty \frac{1}{1+x^2} dx$

$$\begin{aligned}\int_1^\infty \frac{1}{1+x^2} dx &= \lim_{a \rightarrow \infty} \int_1^a \frac{1}{1+x^2} dx \\ \lim_{a \rightarrow \infty} \int_1^a \frac{1}{1+x^2} dx &= \lim_{a \rightarrow \infty} \left[\arctan(x) \right]_1^a = \lim_{a \rightarrow \infty} \arctan(a) - \arctan(1) \\ &= \frac{\pi}{2} - \frac{\pi}{4} = \boxed{\frac{\pi}{4}}\end{aligned}$$

Part II