**1.** Suppose  $f(x) = x^2 - x$  what is the average value of f on [-1,1]?

$$\overline{f} = \frac{1}{b-a} \int_{a}^{b} f(x) dx \quad \text{where} \quad f(x) = x^{2} - x$$

$$\Rightarrow \overline{f} = \frac{1}{1 - (-1)} \int_{-1}^{1} (x^{2} - x) dx = \frac{1}{2} \left( \frac{x^{3}}{3} - \frac{x^{2}}{2} \right) \Big|_{-1}^{1}$$

$$= \left( \frac{2x^{3} - 3x^{2}}{12} \right) \Big|_{-1}^{1} = \left( -\frac{1}{12} \right) - \left( -\frac{5}{12} \right) = \frac{4}{12} = \boxed{\frac{1}{3} \approx 0.\overline{333}}$$

**2.** Evaluate  $2 + 4 + 6 + \cdots + 100$ .

$$2+4+6+\dots+100 = \sum_{n=1}^{50} 2n = 2\sum_{n=1}^{50} n$$
Using  $\sum_{n=1}^{k} n = \frac{k(k+1)}{2}$ ;  $\Rightarrow$   $2\left(\frac{50(51)}{2}\right) = \boxed{2,550}$ 

 $3. \quad \text{Evaluate } \int (7 + e^x)^5 e^x dx$ 

$$\int (7 + e^x)^5 e^x dx$$

$$let \quad u = 7 + e^x \quad du = e^x dx$$

$$\Rightarrow \int u^5 du = \frac{1}{6}u^6 + C = \boxed{\frac{1}{6}(7 + e^x)^6 + C}$$

**4.** Evaluate  $\int_{-1}^{1} (3+x)^4 dx$ 

$$\int_{-1}^{1} (3+x)^{4} dx$$

$$let \quad u = 3+x; \quad du = dx$$

$$u_{lower} = 3 + (-1) = 2; \quad u_{upper} = 3 + 1 = 4$$

$$\Rightarrow \int_{-1}^{1} u^{4} du = \frac{1}{5} u^{5} \Big|_{2}^{4} = \frac{4^{5}}{5} - \frac{2^{5}}{5} = \boxed{198.4}$$

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