

## BLG231E – Assignment 1

Name – Surname: Ö. Malik Kalembaşı

Student ID: 150180112

CRN: 11623

### Part 1

1.

a.

i)

$$B = 0010\ 0110 + 1 = 0 \cdot 2^0 + 1 \cdot 2^1 + 1 \cdot 2^2 + 0 \cdot 2^3 + 0 \cdot 2^4 + 1 \cdot 2^5 + 0 \cdot 2^6 + 1 = -39$$

max signed 8-bit positive integer is 127.

$$A - (-39) \leq 127$$

largest decimal value of **A = 88**

ii)

$$B = 0010\ 0110 + 1 = 0 \cdot 2^0 + 1 \cdot 2^1 + 1 \cdot 2^2 + 0 \cdot 2^3 + 0 \cdot 2^4 + 1 \cdot 2^5 + 0 \cdot 2^6 + 1 = -39$$

min signed 8-bit integer is -128.

$$A - B \geq -128$$

smallest decimal value of **A = -128**

b.

decimal value of A = 88

binary representation of A = 0101 1000

A – B

<b>0</b> 101 1000		<b>0</b> 101 1000
- <b>1</b> 101 1001	(2's complement)	+ <b>0</b> 010 0111
		<b>0</b> 111 1111

(bold digits give the signs)

there is no overflow, result is valid.

c.

i)

max unsigned 8-bit positive integer is 255.

$$A - B = C$$

$$B = 1101\ 1001 = 1 \cdot 2^0 + 0 \cdot 2^1 + 0 \cdot 2^2 + 1 \cdot 2^3 + 1 \cdot 2^4 + 0 \cdot 2^5 + 1 \cdot 2^6 + 1 \cdot 2^7 = 217$$

$$C \leq 1111\ 1111 \quad \text{and} \quad A \leq 1111\ 1111$$

largest unsigned 8-bit binary value of **A = 1111 1111**

ii)

min unsigned 8-bit binary number is 0000 0000.

$$A - B = C$$

$$B = 1101\ 1001 = 1 \cdot 2^0 + 0 \cdot 2^1 + 0 \cdot 2^2 + 1 \cdot 2^3 + 1 \cdot 2^4 + 0 \cdot 2^5 + 1 \cdot 2^6 + 1 \cdot 2^7 = 217$$

$$0000\ 0000 \leq C \quad \text{and} \quad 0000\ 0000 \leq A$$

$$A - B \leq 0000\ 0000$$

smallest unsigned 8-bit binary value of **A = B = 1101 1001**

2.

a.

i)

$$A = 1011\ 1100$$

(bold digit gives the sign, negative)

$$1011\ 1100 \quad (2\text{'s complement})$$

$$0100\ 0011 \quad (\text{add } 1)$$

$$0100\ 0100 \quad 68$$

so, decimal value of A = -68

max signed 8-bit integer is 127.

$$A + B \leq 127$$

largest signed 8-bit decimal value of **B = 127**

ii)

decimal value of A = -68

min signed 8-bit integer is -128.

$$A + B \geq -128$$

$$A + (-68) \geq -128$$

smallest signed 8-bit decimal value of **B = -60**

**b.**

smallest decimal value of B is -60

binary representation of B = **1**100 0100

(bold digit give the sign, negative)

$$A = 1011\ 1100$$

$$1011\ 1100$$

$$+ \underline{1100\ 0100}$$

$$\textcolor{red}{1}1000\ 0000$$

(9th digit is ignored; bold digit gives the sign, negative)

## Part 2

**3.**

**a.**

$$E(a, b, c) = ab'c + abc' + abc + a'bc$$

$$\textbf{abc} + abc' + \textbf{ab}'c + a'bc \quad (\text{commutative})$$

$$\textbf{ab}(\textbf{c} + \textbf{c}') + ab'c + a'bc \quad (\text{distributivity})$$

$$ab(\textbf{1}) + ab'c + a'bc \quad (\text{inverse})$$

$$\textbf{ab} + ab'c + a'bc \quad (\text{identity})$$

$$ab + ab'c + a'bc + \textbf{abc} \quad (\text{idempotence})$$

$$ab + ab'c + \textbf{abc} + \textbf{a}'bc \quad (\text{commutative})$$

$$ab + a\textbf{cb}' + a\textbf{cb} + a'bc \quad (\text{commutative})$$

$$ab + a\textbf{c}(\textbf{b}' + \textbf{b}) + a'bc \quad (\text{distributivity})$$

$$ab + ac(\textbf{b} + \textbf{b}') + a'bc \quad (\text{commutative})$$

$$ab + ac(\textbf{1}) + a'bc \quad (\text{inverse})$$

$$ab + a\textbf{c} + a'bc \quad (\text{identity})$$

$$ab + ac + a'bc + \textbf{abc} \quad (\text{idempotence})$$

$$ab + ac + \textbf{bca}' + \textbf{bca} \quad (\text{commutative})$$

$ab + ac + \mathbf{bc(a' + a)}$	(distributivity)	
$ab + ac + bc(\mathbf{a + a'})$	(commutative)	
$ab + ac + bc(\mathbf{1})$	(inverse)	
$ab + ac + \mathbf{bc}$	(identity)	<b>(final expression)</b>

**b.**

$$E(a, b, c, d) = a'bd' + bcd + abc' + ab'd + bc'd' + ad + a'bc$$

$$a'bd' + \mathbf{bcd} + abc' + ab'd + bc'd' + \mathbf{ad} + \mathbf{a'bc} \quad (\text{consensus theorem respect to a})$$

$$a'bd' + abc' + ab'd + bc'd' + ad + a'bc \quad (\text{consensus term is removed})$$

$$\mathbf{a'bd'} + abc' + ab'd + \mathbf{bc'd'} + ad + \mathbf{a'bc} \quad (\text{consensus theorem respect to c})$$

$$abc' + ab'd + bc'd' + ad + a'bc \quad (\text{consensus term is removed})$$

$$\mathbf{abc'} + ab'd + \mathbf{bc'd'} + \mathbf{ad} + a'bc \quad (\text{consensus theorem respect to d})$$

$$ab'd + bc'd' + ad + a'bc \quad (\text{consensus term is removed})$$

$$\mathbf{ab'd} + bc'd' + \mathbf{ad} + a'bc \quad (\text{absorption})$$

$$bc'd' + ad + a'bc \quad \mathbf{(final expression)}$$