- 1. What is the running time (using asymptotic notation) of the insert() operation for a heap-based priority queue? Briefly justify your answer.
- 2. Using figure 7.1 as a model, illustrate the operation of partition() on the array $A = \langle 13, 19, 9, 5, 12, 8, 7, 4, 21, 2, 6, 11 \rangle$.
- 3. In the video we claimed that $T(n) = T(n-100) + \Theta(n) = \Theta(n^2)$. Show that this is true using the substitution method.
- 4. Consider an array in which every element is within 3 positions of its sorted position. Thus, the array is *almost* sorted.
 - (a) Insertion sort is $O(n^2)$. Using the algorithm at the top of page 26 of the textbook, show the running time of the almost-sorted array.
 - (b) Give the recurrence for quicksort on the almost-sorted array. Don't worry about rounding. You can assume that each element is *exactly* 3 spots away from sorted order at each level of the recursion tree. Assume that partition() is $\Theta(n)$.
 - (c) What is the solution to the recurrence? You do not need to justify your answer.
- 5. Suppose that the splits at every level of quicksort are in the proportion 1α to α where $0 < \alpha \le 1/2$ is a constant. Show that the minimum depth of a leaf in the recursion tree is approximately $-\lg n/\lg \alpha$ and the maximum depth is approximately $\lg n/\lg(1-\alpha)$. Don't worry about integer round-off.
- 6. A random number generator can be expensive. Assuming the randomized version of quicksort splits every level perfectly in half, how many times is random() called for input size n?