

← [course home \(/table-of-contents\)](/table-of-contents)

You want to be able to access the *largest element* in a stack.↗

You've already implemented this Stack class:

```
class Stack(object):

    def __init__(self):
        """Initialize an empty stack"""
        self.items = []

    def push(self, item):
        """Push a new item onto the stack"""
        self.items.append(item)

    def pop(self):
        """Remove and return the last item"""
        # If the stack is empty, return None
        # (it would also be reasonable to throw an exception)
        if not self.items:
            return None

        return self.items.pop()

    def peek(self):
        """Return the last item without removing it"""
        if not self.items:
            return None
        return self.items[-1]
```

Python 2.7

Use your Stack class to **implement a new class MaxStack with a method `get_max()` that returns the largest element in the stack.** `get_max()` should not remove the item.

Your stacks will contain only integers.

Gotchas

What if we push several items in increasing numeric order (like 1, 2, 3, 4...), so that there is a *new max* after each `push()`? What if we then `pop()` each of these items off, so that there is a *new max* after each `pop()`? Your algorithm shouldn't pay a steep cost in these edge cases.

You should be able to get a runtime of $O(1)$ for `push()`, `pop()`, and `get_max()`.

Breakdown

A just-in-time approach is to have `get_max()` simply walk through the stack (popping all the elements off and then pushing them back on) to find the max element. This takes $O(n)$ time for each call to `get_max()`. But we can do better.

To get $O(1)$ time for `get_max()`, we could store the max integer as a member variable (call it `max`). But how would we keep it up to date?

For every `push()`, we can check to see if the item being pushed is larger than the current `max`, assigning it as our new `max` if so. But what happens when we `pop()` the current `max`? We could recompute the current `max` by walking through our stack in $O(n)$ time. So our worst-case runtime for `pop()` would be $O(n)$. We can do better.

What if when we find a new current `max` (`new_max`), instead of overwriting the old one (`old_max`) we held onto it, so that once `new_max` was popped off our stack we would know that our `max` was back to `old_max`?

What data structure should we store our set of `maxes` in? We want something where the last item we put in is the first item we get out ("last in, first out").

We can store our `maxes` in another stack!

Solution

We define *two* new stacks within our `MaxStack` class—`stack` holds all of our integers, and `maxes_stack` holds our "maxima." We use `maxes_stack` to keep our max up to date in constant time as we `push()` and `pop()`:

1. Whenever we `push()` a new item, we check to see if it's greater than or equal to the current max, which is at the top of `maxes_stack`. If it is, we also `push()` it onto `maxes_stack`.
2. Whenever we `pop()`, we also `pop()` from the top of `maxes_stack` if the item equals the top item in `maxes_stack`.

```
class MaxStack(object):

    def __init__(self):
        self.stack = Stack()
        self.maxes_stack = Stack()

    def push(self, item):
        """Add a new item onto the top of our stack."""
        self.stack.push(item)

        # If the item is greater than or equal to the last item in maxes_stack,
        # it's the new max! So we'll add it to maxes_stack.
        if self.maxes_stack.peek() is None or item >= self.maxes_stack.peek():
            self.maxes_stack.push(item)

    def pop(self):
        """Remove and return the top item from our stack."""
        item = self.stack.pop()

        # If it equals the top item in maxes_stack, they must have been pushed
        # in together. So we'll pop it out of maxes_stack too.
        if item == self.maxes_stack.peek():
            self.maxes_stack.pop()

        return item

    def get_max(self):
        """The last item in maxes_stack is the max item in our stack."""
        return self.maxes_stack.peek()
```

Complexity

$O(1)$ time for `push()`, `pop()`, and `get_max()`. $O(m)$ additional space, where m is the number of operations performed on the stack.

Bonus

Our solution requires $O(m)$ additional space for the second stack. But do we really need it?

Can you come up with a solution that requires $O(1)$ additional space? (It's tricky!)

What We Learned

Notice how in the solution we're *spending time* on `push()` and `pop()` so we can *save time* on `get_max()`. That's because we chose to optimize for the time cost of calls to `get_max()`.

But we could've chosen to optimize for something else. For example, if we expected we'd be running `push()` and `pop()` frequently and running `get_max()` rarely, we could have optimized for faster `push()` and `pop()` methods.

Sometimes the first step in algorithm design is *deciding what we're optimizing for*. Start by considering the expected characteristics of the input.

← [course home \(/table-of-contents\)](/table-of-contents)

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(</question/queue-two-stacks?course=fc1§ion=queues-stacks>)

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