$$\langle \Phi_0 | \hat{H} | \Phi_i^a \rangle = a \sqrt{i} + a \sqrt{k}$$