Miami-Dade County Public Schools Florida's B.E.S.T. Mathematics

Grade 6 - Achievement Level Descriptor Tables

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MA.6.NSO.1.1 (Context: Mathematical)

Extend previous understanding of numbers to define rational numbers. Plot, order and compare rational numbers.

Benchmark Clarifications

Clarification 1: Within this benchmark, the expectation is to plot, order and compare positive and negative rational numbers when given in the same form and to plot, order and compare positive rational numbers when given in different forms (fraction, decimal, percentage).

Clarification 2: Within this benchmark, the expectation is to use symbols (<. > or =).

Assessment Limits

Items requiring the student to plot, order, and/or compare numbers in the same form must contain at least one negative value.

Items requiring the student to plot, order, and/or compare numbers in different forms are limited to fractions that result in a terminating decimal.

Items may use the words "is less than," "is greater than," or "is equal to."

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
defines a rational number; plots, orders, and compares integers.	defines a rational number; plots, orders, and compares positive and negative rational numbers when given in the same form.	defines a rational number; plots, orders, and compares positive rationale numbers when given in different forms.	defines a rational number; explains and justifies how to plot, order, and compare positive and negative rational numbers when given in the same form and when positive rational numbers are represented in different forms.

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MA.6.NSO.1.2 (Context: Mathematical & Real-World)

Given a mathematical or real-world context, represent quantities that have opposite direction using rational numbers. Compare them on a number line and explain the meaning of zero within its context.

Example: Jasmine is on a cruise and is going on a scuba diving excursion. Her elevations of 10 feet above sea level and 8 feet below sea level can be compared on a number line, where 0 represents sea level.

Benchmark Clarifications

Clarification 1: Instruction includes vertical and horizontal number lines, context referring to distances, temperatures and finances and using informal verbal comparisons, such as, lower, warmer or more in

Clarification 2: Within this benchmark, the expectation is to compare positive and negative rational numbers when given in the same form.

Assessment Limits

Items will not require the student to perform operations.

Items may use, but are not limited to, contexts involving distance, temperature, or finance.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
given a mathematical context, represents quantities on a horizontal number line that have opposite direction using rational numbers.	given a mathematical or real-world context, represents and compares quantities on a number line that have opposite direction using rational numbers.	given a mathematical or real-world context, represents quantities that have opposite direction using rational numbers, compares the quantities on a number line, and explains the meaning of zero within its context.	(intentionally left blank)

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MA.6.NSO.1.3 (Context: Mathematical & Real-World)

Given a mathematical or real-world context, interpret the absolute value of a number as the distance from zero on a number line. Find the absolute value of rational numbers.

Benchmark Clarifications

Clarification 1: Instruction includes the connection of absolute value to mirror images about zero and to opposites.

Clarification 2: Instruction includes vertical and horizontal number lines and context referring to distances, temperature and finances.

Assessment Limits

Items will not require the student to perform arithmetic operations.

Items may use, but are not limited to, contexts involving distance, temperature, or finance.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
finds the absolute value of a rational number.	given a mathematical context, interprets the absolute value of a rational number as the distance from zero on a number line.	given a real-world context, interprets the absolute value of a rational number as the distance from zero on a number line.	given a real-world context, interprets and explains the meaning of the absolute value of a rational number in its context.

MA.6.NSO.1.4 (Context: Mathematical & Real-World)

Solve mathematical and real-world problems involving absolute value, including the comparison of absolute value.

Example: Michael has a lemonade stand which costs \$10 to start up. If he makes \$5 the first day, he can determine whether he made a profit so far by comparing | - 10|and |5|.

Benchmark Clarifications

Clarification 1: Absolute value situations include distances, temperatures and finances.

Clarification 2: Problems involving calculations with absolute value are limited to two or fewer operations.

Clarification 3: Within this benchmark, the expectation is to use integers only.

Assessment Limits

Items may use, but are not limited to, contexts involving distance, temperature, or finance.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
solves mathematical problems with one step involving absolute value; or compares absolute values.	solves mathematical problems with one step involving absolute value, including the comparison of absolute value.	solves mathematical problems with two steps or real-world problems with up to two steps involving absolute value, including the comparison of absolute value.	solves and explains mathematical or real- world problems with up to two steps involving absolute value, including the justification of the comparison of absolute value.

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MA.6.NSO.2.1 (Context: Mathematical)

Multiply and divide positive multi-digit numbers with decimals to the thousandths, including using a standard algorithm with procedural fluency.

Benchmark Clarifications

Clarification 1: Multi-digit decimals are limited to no more than 5 total digits.

Assessment Limits

Decimals that are multiplied or divided by 0.1 or 0.01 must be to at least the hundredths place.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
multiplies and divides positive multi-digit numbers with decimals to the hundredths .	multiplies positive multidigit numbers with decimals to the thousandths, including using a standard algorithm, and divides positive multi-digit numbers with decimals to hundredths, including using a standard algorithm.	multiplies and divides positive multi-digit numbers with decimals to the thousandths, including using a standard algorithm with procedural fluency.	analyzes an error in the multiplication or division computation using a standard algorithm and justifies the reasoning.

MA.6.NSO.2.2 (Context: Mathematical)

Extend previous understanding of multiplication and division to compute products and quotients of positive fractions by positive fractions, including mixed numbers, with procedural fluency.

Benchmark Clarifications

Clarification 1: Instruction focuses on making connections between visual models, and the relationship between multiplication and division, reciprocals and algorithms.

Assessment Limits

Items requiring the student to multiply a fraction by a fraction must have at least one fraction with a denominator greater than 20.

Items will not divide a unit fraction by a whole number or a whole number by a unit fraction.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
using models, computes products of positive fractions and computes quotients involving unit fractions and fractions.	with or without models, computes products and quotients of positive fractions, involving at least one unit fraction.	computes products and quotients of positive fractions, including mixed numbers with procedural fluency.	computes products and quotients of positive fractions by positive fractions, including mixed numbers with procedural fluency and explains relationship between multiplication and division, reciprocals, and algorithms.

MA.6.NSO.2.3 (Context: Real World)

Solve multi-step real-world problems involving any of the four operations with positive multi-digit decimals or positive fractions, including mixed numbers.

Benchmark Clarifications

Clarification 1: Within this benchmark, it is not the expectation to include both decimals and fractions within a single problem.

Assessment Limits

Context will not include money, perimeter, or area.

Items will use at least two different operations but will not use addition and subtraction only.

Items with decimals must include one to at least the hundredths.

When multiplying fractions, at least one fraction must have a denominator greater than 20.

Items will not include a numerical expression.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
solves two-step real-world problems involving addition, subtraction, and multiplication with positive multi-digit decimals or positive fractions.	solves two-step real-world problems involving any of the four operations with positive multi-digit decimals or positive fractions.	solves multi-step real-world problems involving any of the four operations with positive multi-digit decimals or positive fractions, including mixed numbers.	solves multi-step real-world problems involving any of the four operations with positive multi-digit decimals or positive fractions, including mixed numbers, and interprets the solution in the context of the situation.

MA.6.NSO.3.1 (Context: Mathematical & Real-World)

Given a mathematical or real-world context, find the greatest common factor and least common multiple of two whole numbers.

Example: Adam works out every 8 days and Susan works out every 12 days. If both Adam and Susan work out today, how many days until they work out on the same day again?

Benchmark Clarifications

Clarification 1: Within this benchmark, expectations include finding greatest common factor within 1,000 and least common multiple with factors to 25.

Clarification 2: Instruction includes finding the greatest common factor of the numerator and denominator of a fraction to simplify the fraction.

Assessment Limits

N/A

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
given a mathematical context, finds the greatest common factor within 500 or least common multiple with factors to 15 of two whole numbers.	given a mathematical context, finds the greatest common factor within 1000 and least common multiple with factors to 25 of two whole numbers.	given a real-world context, finds the greatest common factor within 1000 and least common multiple with factors to 25 of two whole numbers.	given a mathematical or real-world context, finds the greatest common factor within 1000 and least common multiple with factors to 25 of two whole numbers and explains the relationship between the greatest common factor and rewriting equivalent fractions.

MA.6.NSO.3.2 (Context: Mathematical & Real-World)

Rewrite the sum of two composite whole numbers having a common factor, as a common factor multiplied by the sum of two whole numbers.

Benchmark Clarifications

Clarification 1: Instruction includes using the distributive property to generate equivalent expressions.

Assessment Limits

The common factor will not exceed 1000.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
identifies the common factor between the sum of two composite whole numbers.	identifies the sum of two composite whole numbers having a common factor, as a common factor multiplied by the sum of two whole numbers.	rewrites the sum of two composite whole numbers having a common factor as a common factor multiplied by the sum of two whole numbers.	rewrites the sum of two composite whole numbers having a common factor, as a common factor multiplied by the sum of two whole numbers and justifies rewriting it multiple ways.	

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MA.6.NSO.3.3 (Context: Mathematical)

Evaluate positive rational numbers and integers with natural number exponents.

Benchmark Clarifications

Clarification 1: Within this benchmark, expectations include using natural number exponents up to 5.

Assessment Limits

Items must include an expression having only a positive rational base and a natural number exponent.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
evaluates positive whole numbers with natural number exponents up to 5.	evaluates positive rational numbers with natural number exponents up of 5.	evaluates positive rational numbers and integers with natural number exponents up to 5.	uses reasoning to determine the unknown exponential value when given an equation with a known integer base equal to an equivalent value.

MA.6.NSO.3.4 (Context: Mathematical)

Express composite whole numbers as a product of prime factors with natural number exponents.

Benchmark Clarifications

No Benchmark Clarificati	ions		
	Assessm	ent Limits	
N/A			
	Achievement Le	evel Descriptors	
Level 2	Level 3	Level 4	Level 5
identifies composite whole numbers as products of single prime factors.	expresses two-digit composite whole numbers as products of prime factors.	expresses composite whole numbers as products of prime factors using natural number exponents.	(intentionally left blank)

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MA.6.NSO.3.5 (Context: Mathematical)

Rewrite positive rational numbers in different but equivalent forms including fractions, terminating decimals and percentages.

Example: The number $1\frac{5}{8}$ can be written equivalently as 1.625 or 162.5%.

Benchmark Clarifications

Clarification 1: Rational numbers include decimal equivalence up to the thousandths place

Assessment Limits

N/A

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
identifies equivalent forms of positive terminating decimals with fraction notation with denominators of 1000.	identifies equivalent forms of positive rational numbers including fractions, terminating decimals, and percentages.	rewrites positive rational numbers in different but equivalent forms including fractions, terminating decimals, and percentages.	rewrites positive rational numbers in equivalent forms including fractions, terminating decimals, and percentages, and explains the relationship between representations.

MA.6.NSO.4.1 (Context: Mathematical)

Apply and extend previous understandings of operations with whole numbers to add and subtract integers with procedural fluency.

Benchmark Clarifications

Clarification 1: Instruction begins with the use of manipulatives, models and number lines working towards becoming procedurally fluent by the end of grade 6.

Clarification 2: Instruction focuses on the inverse relationship between the operations of addition and subtraction. If p and q are integers, then p - q = p + (-q) and p + q = p - (-q).

Assessment Limits

Items involving addition must incorporate at least one negative integer.

Items involving subtraction must incorporate at least one negative integer or can include positive integers wherein the subtrahend is larger than the minuend.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
(intentionally left blank)	using a visual model such as manipulatives or a number line, adds and subtracts integers.	adds and subtracts integers with procedural fluency.	adds and subtracts integers with procedural fluency and explains and justifies why the inverse relationship exists between addition and subtraction with integers using properties of operations.	

MA.6.NSO.4.2 (Context: Mathematical)

Apply and extend previous understandings of operations with whole numbers to multiply and divide integers with procedural fluency.

Benchmark Clarifications

Clarification 1: Instruction includes the use of models and number lines and the inverse relationship between multiplication and division, working towards becoming procedurally fluent by the end of grade

Clarification 2: Instruction focuses on the understanding that integers can be divided, provided that the divisor is not zero, and every quotient of integers (with non-zero divisor) is a rational number. If p and q are integers where integers where $q \neq 0$, then $-(\frac{p}{q}) = -\frac{p}{q}$, $-(\frac{p}{q}) = \frac{p}{-q}$ and $\frac{p}{q} = \frac{-p}{-q}$.

Assessment Limits

Items must incorporate at least one negative integer.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
(intentionally left blank)	using a visual model such as manipulatives or a number line, multiplies and divides integers.	multiplies and divides integers with procedural fluency.	multiplies and divides integers with procedural fluency and explains why the inverse relationship exists between multiplication and division with integers using properties of operations.	

MA.6.AR.1.1 (Context: Mathematical & Real-World)

Given a mathematical or real-world context, translate written descriptions into algebraic expressions and translate algebraic expressions into written descriptions.

Example: The algebraic expression 7.2x-20 can be used to describe the daily profit of a company who makes \$7.20 per product sold with daily expenses of \$20.

Benchmark Clarifications

No Benchmark Clarifications

Assessment Limits

Algebraic expressions or written descriptions must include at least one but no more than two unknowns.

Items will not require the student to perform operations.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
given a mathematical context, translates written descriptions into linear algebraic expressions limited to one term.	given a mathematical or real-world context, translates written descriptions into linear algebraic expressions limited to one term and translates linear algebraic expressions limited to one term into written descriptions.	given a mathematical or real-world context, translates written descriptions into linear algebraic expressions limited to two terms and translates linear algebraic expressions limited to two terms into written descriptions.	given a mathematical or real-world context, analyzes an error in the translation of a written description into a linear algebraic expression or in the translation of a linear algebraic expression into a written description and justifies the reasoning.	

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MA.6.AR.1.2 (Context: Mathematical & Real-World)

Translate a real-world written description into an algebraic inequality in the form of x > a, x < a, $x \ge a$ or $x \le a$. Represent the inequality on a number line.

Example: Mrs. Anna told her class that they will get a pizza if the class has an average of at least 83 out of 100 correct questions on the semester exam. The inequality $g \ge 83$ can be used to represent the situation where students receive a pizza and the inequality g < 83 can be used to represent the situation where students do not receive a pizza.

Benchmark Clarifications

Clarification 1: Variables may be on the left or right side of the inequality symbol.

Assessment Limits

Items may require the student to perform operations.

Given context should be continuous.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
represents an algebraic inequality on a number line wherein the variable is on the left side of the inequality.	translates a real- world written description into algebraic inequality form and represents that inequality on a number line.	translates a real-world written description into algebraic inequality form and represents an inequality with the variable on the right or left side of the inequality on a number line.	translates a real-world written description into algebraic inequality form and represents an inequality with the variable on the right or left side of the inequality on a number line and translates an algebraic inequality into a real-world written description.

MA.6.AR.1.3 (Context: Mathematical)

Evaluate algebraic expressions using substitution and order of operations.

Example: Evaluate the expression $2a^2 - \frac{b}{r}$, where a = -1 and b = 5.

Benchmark Clarifications

Clarification 1: Within this benchmark, the expectation is to perform all operations with integers.

Clarification 2: Refer to Properties of Operations, Equality and Inequality (Appendix D).

Assessment Limits

Items will not include more than three variables.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
evaluates algebraic expressions using substitution and order of operations with one variable and using	evaluates algebraic expressions using substitution and order of operations with one variable and	evaluates algebraic expressions using substitution and order of operations with two or more	evaluates algebraic expressions using substitution and order of operations and justifies using the
positive integers.	any integer.	variables and any integer.	order of operations.

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MA.6.AR.1.4 (Context: Mathematical & Real-World)

Apply the properties of operations to generate equivalent algebraic expressions with integer coefficients.

Example: The expression 5(3x + 1) can be rewritten equivalently as 15x + 5.

Benchmark Clarifications

Clarification 1: Properties include associative, commutative, and distributive.

Clarification 2: Refer to Properties of Operations, Equality and Inequality (Appendix D).

Assessment Limits

Items must include an expression with only one or two variables where coefficients, factors, and terms are integers only.

Items will require the student to use one, all, or a combination of the associative property, distributive property, commutative property, or arithmetic operations to generate equivalent expressions.

property, communication, and an arrangement to generate a quantum and processing					
	Achievement Level Descriptors				
Level 2 Level 3 Level 4 Level 5					
applies properties of	applies properties of	applies properties of	explains how the		
operations to identify	operations to generate	operations to generate	properties of operations		
equivalent algebraic	equivalent algebraic	equivalent algebraic	generate equivalent		
expressions with	expressions	expressions	algebraic expressions.		
positive integer	with positive integer	with integer			
coefficients.	coefficients.	coefficients.			

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MA.6.AR.2.1 (Context: Mathematical & Real-World)

Given an equation or inequality and a specified set of integer values, determine which values make the equation or inequality true or false.

Example: Determine which of the following values make the inequality x + 1 < 2 true: -4, -2, 0, 1.

Benchmark Clarifications

Clarification 1: Problems include the variable in multiple terms or on either side of the equal sign or inequality symbol.

Assessment Limits

Coefficients and constants in equations or inequalities must be integer values only.

Items will only use one-variable linear equations or inequalities but may include the variable in more than one term.

Items may represent equations or inequalities with the variable on either side or both sides of the equal sign or inequality symbol.

Items may present sets of integer values using braces. Items will use the relational symbols >, >, <, or < when presenting inequalities.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
given an equation or inequality and a specified set of positive integers, determines which values make the equation or inequality true or false.	given an equation or inequality and a specified set of integers, determines which values make the equation or inequality true or false, including variables in multiple terms.	given an equation or inequality and a specified set of integers, determines which values make the equation or inequality true or false, including variables in multiple terms and variables on either side of the equal sign or inequality symbol.	(intentionally left blank)	

MA.6.AR.2.2 (Context: Mathematical & Real-World)

Write and solve one-step equations in one variable within a mathematical or real-world context using addition and subtraction, where all terms and solutions are integers.

Example: The equations -35 + x = 17, 17 = -35 + x and 17 - x = -35 can represent the question "How many units to the right is 17 from -35 on the number line?"

Benchmark Clarifications

Clarification 1: Instruction includes using manipulatives, drawings, number lines and inverse operations.

Clarification 2: Instruction includes equations in the forms x + p = q and p + x = q, where x, p and q are any integer.

Clarification 3: Problems include equations where the variable may be on either side of the equal sign.

Assessment Limits

Items will require the student to write an equation, solve an equation, or write and solve an equation.

Items must incorporate a negative integer in either the given equation and/or the solution.

Equations will be represented in the form x + p = q or p + x = q, where x, p, and q are any integer.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
given a visual model such as a number line, solves for a variable in a one-step equation within a mathematical context using addition or subtraction, where all terms and solutions are positive integers.	without a visual model, solves for a variable in a one-step equation within a mathematical context using addition and subtraction, where all terms and solutions are integers.	writes and solves for a variable in an equation within a mathematical or realworld context using addition and subtraction, where all terms and solutions are integers, including variables on either side of the equal sign.	identifies multiple representations of the same equation using addition and subtraction, demonstrating how multiple equations can answer the same question.	

MA.6.AR.2.3 (Context: Mathematical & Real-World)

Write and solve one-step equations in one variable within a mathematical or real-world context using multiplication and division, where all terms and solutions are integers.

Benchmark Clarifications

Clarification 1: Instruction includes using manipulatives, drawings, number lines and inverse operations.

Clarification 2: Instruction includes equations in the forms $\frac{x}{p} = q$, where $p \neq 0$, and px = q.

Clarification 3: Problems include equations where the variable may be on either side of the equal sign.

Assessment Limits

Items will require the student to write an equation, solve an equation, or write and solve an equation.

Equations will be represented in the form px=q or $\frac{x}{p}=q$, where $p \neq 0$.

p 4,				
	Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5	
given a visual model such as a number line, solves for a variable in a one-step equation within a mathematical context using multiplication and division, where all terms and solutions are positive integers.	without a visual model, solves for a variable in a one-step equation within a mathematical context using multiplication and division, where all terms and solutions are integers.	writes and solves for a variable in an equation within a mathematical or realworld context using multiplication and division, where all terms and solutions are integers, including variables on either side of the equal sign.	identifies multiple representations of the same equation using multiplication and division, demonstrating how multiple equations can answer the same question.	

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MA.6.AR.2.4 (Context: Mathematical)

Determine the unknown decimal or fraction in an equation involving any of the four operations, relating three numbers, with the unknown in any position.

Example: Given the equation $\frac{9}{8} = x - \frac{1}{8}$, x can be determined to be $\frac{10}{8}$ because $\frac{10}{8}$ is $\frac{1}{8}$ more than $\frac{9}{8}$.

Benchmark Clarifications

Clarification 1: Instruction focuses on using algebraic reasoning, drawings, and mental math to determine unknowns.

Clarification 2: Problems include the unknown and different operations on either side of the equal sign. All terms and solutions are limited to positive rational numbers.

Assessment Limits

Items will not require the student to relate numbers in different forms.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
using a visual model, determines the unknown decimals or fractions in an equation involving any of the four operations, relating three numbers, with the unknown in any position.	without a visual model, determines the unknown decimals or fractions in an equation involving any of the four operations, relating three numbers, with the unknown in any position.	determines the unknown decimals or fractions, including mixed numbers and fractions greater than one, in an equation involving any of the four operations, relating three numbers, with the unknown in any position, including the unknown and different operations on either side of the equal sign.	describes how comparative relational thinking is used to determine the unknown decimal or fraction, including mixed numbers and fractions greater than one, in an equation involving any of the four operations, relating three numbers, with the unknown in any position, including the unknown and different operations on either side of the equal sign.

MA.6.AR.3.1 (Context: Real-World)

Given a real-world context, write and interpret ratios to show the relative sizes of two quantities using appropriate notation: $\frac{a}{b}$, a to b, or a:b where $b \ne 0$.

Benchmark Clarifications

Clarification 1: Instruction focuses on the understanding that a ratio can be described as a comparison of two quantities in either the same or different units.

Clarification 2: Instruction includes using manipulatives, drawings, models and words to interpret part-to-part ratios and part-to-whole ratios.

Clarification 3: The values of a and b are limited to whole numbers.

Assessment Limits

Presentation of context in items does not determine the order of the ratio.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
given a real-world context, writes part-to-part ratios to show the relative sizes of two quantities in the same units using appropriate notation: a/b, a to b, or a:b where b ≠ 0.	given a real-world context, writes and interprets part-to-part and part-to- whole ratios to show the relative sizes of two quantities in the same units using appropriate notation: a/b, a to b, or a:b where b ≠ 0.	given a real-world context, writes and interprets part-to-part and part-to- whole ratios to show the relative sizes of two quantities in the different units using appropriate notation: a/b , a to b, or a:b where $b \neq 0$.	(intentionally left blank)

MA.6.AR.3.2 (Context: Real-World)

Given a real-world context, determine a rate for a ratio of quantities with different units. Calculate and interpret the corresponding unit rate.

Example: Tamika can read 500 words in 3 minutes. Her reading rate can be described as $\frac{500 \ words}{3 \ minutes}$ which is equivalent to the unit rate of $166\frac{2}{3}$ words per minute.

Benchmark Clarifications

Clarification 1: Instruction includes using manipulatives, drawings, models and words and making connections between ratios, rates and unit rates.

Clarification 2: Problems will not include conversions between customary and metric systems.

Assessment Limits

Presentation of context in items does not determine the order of the ratio.

Items will not require the student to convert units.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
using a visual model and given a real-world context, identifies a rate for a ratio of quantities with different units.	with or without a visual model, given a real-world context, calculates a rate for a ratio of quantities with different units.	given a real-world context, calculates and interprets a unit rate for a ratio of quantities with different units.	(intentionally left blank)

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MA.6.AR.3.3 (Context: Mathematical & Real-World)

Extend previous understanding of fractions and numerical patterns to generate or complete a two- or three-column table to display equivalent part-to-part ratios and part-to-part-to-whole ratios.

Example: The table below expresses the relationship between the number of ounces of yellow and blue paints used to create a new color. Determine the ratios and complete the table.

Yellow (part)	1.5	3		9
Blue (part)	2	4		
New color (whole)			12	21

Benchmark Clarifications

Clarification 1: Instruction includes using two-column tables (e.g., a relationship between two variables) and three-column tables (e.g., part-to-part-to-whole relationship) to generate conversion charts and mixture charts.

Assessment Limits

N/A

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
uses a two- or three- column table to display equivalent part-to-part ratios and part-to-part-to-whole ratios.	completes a two- or three-column table to display equivalent part- to-part ratios and part- to-part-to-whole ratios.	generates a two- or three-column table to display equivalent part- to-part ratios and part- to-part-to-whole ratios.	interprets and explains the relationship between ratios presented in a two- or three-column table.	

MA.6.AR.3.4 (Context: Mathematical & Real-World)

Apply ratio relationships to solve mathematical and real-world problems involving percentages using the relationship between two quantities.

Example: Gerald is trying to gain muscle and needs to consume more protein every day. If he has a protein shake that contain 32 grams and the entire shake is 340 grams, what percentage of the entire shake is protein? What is the ratio between grams of protein and grams of non-protein?

Benchmark Clarifications

Clarification 1: Instruction includes the comparison of $\frac{part}{whole}$ to $\frac{percent}{100}$ in order to determine the percent, the part or the whole.

Assessment Limits

Items will only require the student to determine the percent, the part, or the whole.

Items will not require the student to convert units.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
identifies ratio relationships to solve mathematical problems involving percentages using the relationship between two quantities.	applies ratio relationships to solve mathematical problems involving percentages using the relationship between two quantities.	applies ratio relationships to solve real-world problems involving percentages using the relationship between two quantities.	explains the relationship between the percent, the part, and the whole and how it generates equivalent ratios.	

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MA.6.AR.3.5 (Context: Mathematical & Real-World)

Solve mathematical and real-world problems involving ratios, rates and unit rates, including comparisons, mixtures, ratios of lengths and conversions within the measurement system.

Benchmark Clarifications

Clarification 1: Instruction includes the use of tables, tape diagrams and number lines.

Assessment Limits

Items will not require the student to convert between systems.

Items must state the relationship of quantities as a ratio, rate, or unit rate using words or the form $\frac{a}{b}$, a to b, or a:b where $b \neq 0$.

Items will not require the student to only convert measurements.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
using visual models, solves mathematical and real-world problems involving ratios, rates, and unit rates.	solves mathematical problems involving ratios, rates, and unit rates, including comparisons and mixtures.	solves mathematical or real-world problems involving ratios, rates, and unit rates, including comparisons, mixtures, and ratios of lengths and a conversion within the same measurement system.	solves mathematical or real-world problems involving ratios, rates, and unit rates, including comparisons, mixtures, ratios of lengths and more than one conversion within the same measurement system.

MA.6.GR.1.1 (Context: Mathematical)

Extend previous understanding of the coordinate plane to plot rational number ordered pairs in all four quadrants and on both axes. Identify the x- or y- axis as the line of reflection when two ordered pairs have an opposite x- or y- coordinate.

Benchmark Clarifications

No Benchmark Clarifications

Assessment Limits

Items that require the student to plot points in the first quadrant will not use whole number values for the coordinates.

Coordinate planes must be scaled appropriately for given ordered pairs

obordinate planes must be sealed appropriately for given ordered pairs.				
Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
Plots integer ordered	Plots rational number	Plots rational number	Plots rational number	
pairs in all four	ordered pairs in all four	ordered pairs in all four	ordered pairs in all four	
quadrants and on both	quadrants and on both	quadrants and on both	quadrants and on both	
axes.	axes.	axes and identifies the	axes; identifies and	
		x- or y-axis as the line	explains why the x- or	
		of reflection when two	y-axis is the line of	
		ordered pairs have an	reflection when two	
		opposite x- or y-	ordered pairs have an	
		coordinate.	opposite x- or y-	
			coordinate.	

MA.6.GR.1.2 (Context: Mathematical & Real-World)

Find distances between ordered pairs, limited to the same x-coordinate or the same y-coordinate, represented on the coordinate plane.

Benchmark Clarifications

No Benchmark Clarifications

Assessment Limits

Items that require the student to find distance between points must have the same *x*-coordinate or the same *y*-coordinate.

Items may use all four quadrants.

Ordered pairs must be integers.

Items may present the ordered pairs on a coordinate plane.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
Finds distances	Finds distances	Finds distances	(intentionally left blank)
between integer	between ordered pairs	between ordered pairs	
ordered pairs, limited	of rational numbers,	of rational numbers,	
to either the same x-	limited to the same y-	limited to the same y-	
coordinate or y-	coordinate or the	coordinate or the same	
coordinate in the same	same x-coordinate, in	x-coordinate, in any	
quadrant.	the same quadrant,	quadrant, represented	
	represented on a	on a coordinate plane.	
	coordinate plane.		

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MA.6.GR.1.3 (Context: Mathematical & Real-World)

Solve mathematical and real-world problems by plotting points on a coordinate plane, including finding the perimeter or area of a rectangle.

Benchmark Clarifications

Clarification 1: Instruction includes finding distances between points, computing dimensions of a rectangle or determining a fourth vertex of a rectangle.

Clarification 2: Problems involving rectangles are limited to cases where the sides are parallel to the axes.

Assessment Limits

Items that require the student to find distance between points must have the same *x*-coordinate or the same *y*-coordinate.

Items may use all four quadrants.

Ordered pairs must be integers.

Items may present the ordered pairs on a coordinate plane.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
Solves mathematical	Solves mathematical or	Solves mathematical or	Solves mathematical	
problems by plotting	real-world problems by	real-world problems by	and real-world	
integer ordered pairs	plotting ordered pairs	plotting ordered pairs	problems including	
on a coordinate plane.	of rational numbers on	of rational numbers on	determining the fourth	
	a coordinate plane,	a coordinate plane,	vertex of a rectangle.	
	including finding the	including finding the		
	perimeter or area of a	perimeter or area of a		
	rectangle contained in	rectangle with vertices		
	one quadrant.	in multiple quadrants.		

MA.6.GR.2.1 (Context: Mathematical)

Derive a formula for the area of a right triangle using a rectangle. Apply a formula to find the area of a triangle.

Benchmark Clarifications

Clarification 1: Instruction focuses on the relationship between the area of a rectangle and the area of a right triangle.

Clarification 2: Within this benchmark, the expectation is to know from memory a formula for the area of a triangle.

Assessment Limits

Items must give the vertical height for all triangles.

	3			
Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
Identifies the	Applies the formula for	Derives a formula for	Justifies the	
relationship between	the area of a triangle to	the area of a right	relationship between	
the area of a rectangle	find the area of a	triangle using a	the area of a rectangle	
and the area of a right	triangle.	rectangle and applies	and the area of a right	
triangle.		that formula to find the	triangle.	
		area of a triangle.		

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MA.6.GR.2.2 (Context: Mathematical & Real-World)

Solve mathematical and real-world problems involving the area of quadrilaterals and composite figures by decomposing them into triangles or rectangles.

Benchmark Clarifications

Clarification 1: Problem types include finding area of composite shapes and determining missing dimensions.

Clarification 2: Within this benchmark, the expectation is to know from memory a formula for the area of a rectangle and triangle.

Clarification 3: Dimensions are limited to positive rational numbers.

Assessment Limits

When finding area of composite shapes that decompose into rectangles only, dimensions of the rectangles must overlap, have at least one fraction, or have at least one decimal.

Given quadrilaterals will not be rectangles or squares.

Items must give the vertical height for all triangles.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
Solves mathematical problems with positive integers involving the area of quadrilaterals by decomposing them into triangles or rectangles.	Solves mathematical problems with positive rational numbers involving the area of composite figures by decomposing them into triangles or rectangles.	Solves mathematical or real-world problems with positive rational numbers involving the area of quadrilaterals and composite figures by decomposing them into triangles or rectangles or finds a missing side when	Solves mathematical or real-world problems with positive rational numbers involving the area of quadrilaterals and composite figures by decomposing the shapes in different ways and showing how they are
		given the area.	equivalent.

MA.6.GR.2.3 (Context: Mathematical & Real-World)

Solve mathematical and real-world problems involving the volume of right rectangular prisms with positive rational number edge lengths using a visual model and a formula.

Benchmark Clarifications

Clarification 1: Problem types include finding the volume or a missing dimension of a rectangular prism.

Assessment Limits

Items must include at least one fractional or decimal edge length.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
Solves mathematical	Solves mathematical	Solves mathematical or	(intentionally left blank)
problems with a given	problems with a given	real-world problems	
visual model or using a	visual model or using a	involving the volume	
formula, finds the	formula, finds the	of right rectangular	
volume of a right	volume of a right	prisms with positive	
rectangular prism with	rectangular prism with	rational number edge	
one positive rational	positive rational	lengths or finds a	
number as edge length.	number edge lengths .	missing edge length	
		when given a volume.	

MA.6.GR.2.4 (Context: Mathematical & Real-World)

Given a mathematical or real-world context, find the surface area of right rectangular prisms and right rectangular pyramids using the figure's net.

Benchmark Clarifications

Clarification 1: Instruction focuses on representing a right rectangular prism and right rectangular pyramid with its net and on the connection between the surface area of a figure and its net.

Clarification 2: Within this benchmark, the expectation is to find the surface area when given a net or when given a three-dimensional figure.

Clarification 3: Problems involving right rectangular pyramids are limited to cases where the heights of triangles are given.

Clarification 4: Dimensions are limited to positive rational numbers.

Assessment Limits

Items will not require the student to find surface area using the formula.

Items may give a three-dimensional figure and require the student to identify the appropriate net with dimensions and find the surface area.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
Given a mathematical	Given a mathematical	Given a mathematical	(intentionally left blank)
context, finds the	context, finds the	or real-world context,	
surface area of right	surface area of right	finds the surface area	
rectangular prisms and	rectangular prisms and	of right rectangular	
right rectangular	right rectangular	prisms and right	
pyramids given the	pyramids using the	rectangular pyramids	
figure's net using	figure's net using	using the figure's net	
positive integers.	dimensions with one	using positive rational	
	rational number.	numbers.	

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MA.6.DP.1.1 (Context: Real-World)

Recognize and formulate a statistical question that would generate numerical data.

Example: The question "How many minutes did you spend on mathematics homework last night?" can be used to generate numerical data in one variable.

Benchmark Clarifications

No Benchmark Clarification

Assessment Limits

N/A

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
(intentionally left blank)	recognizes statistical questions that would generate numerical data.	formulates statistical questions that would generate numerical data.	explains what makes a question statistical.

MA.6.DP.1.2 (Context: Real-World)

Given a numerical data set within a real-world context, find and interpret mean, median, mode and range.

Example: The data set {15, 0, 32, 24, 0, 17, 42, 0, 29, 120, 0, 20}, collected based on minutes spent on homework, has a mode of 0.

Benchmark Clarifications

Clarification 1: Numerical data is limited to positive rational numbers.

Assessment Limits

Data sets are limited to no more than 20 data points.

Items will not require the student to calculate mean with data sets containing more than 10 data points.

Items must present numerical data as a set using braces, graphically, or in a table.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
given a numerical data	given a numerical data	given a numerical data	(intentionally left blank)
set limited to positive	set within a real-world	set within a real-world	
integers, within a real-	context, finds mean,	context, finds and	
world context, finds	median, mode, and	interprets mean,	
mean, median, mode,	range.	median, mode, and	
and range.		range.	

MA.6.DP.1.3 (Context: Real-World)

Given a box plot within a real-world context, determine the minimum, the lower quartile, the median, the upper quartile and the maximum. Use this summary of the data to describe the spread and distribution of the data.

Example: The middle 50% of the population can be determined by finding the interval between the upper quartile and the lower quartile.

Benchmark Clarifications

Clarification 1: Instruction includes describing range, interquartile range, halves, and quarters of the data.

Assessment Limits

Items may require the student to describe box plots using the words "symmetry", "skewed", "minimum", "maximum", "median", "lower" or "upper quartile", "outlier(s)", "range", "interquartile range", "halves", or "quarters."

Items may use vertical or horizontal number lines.

nems may use vertical of menzonial marries.			
Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
given a box plot within	given a box plot within	given a box plot within	(intentionally left blank)
a real-world context,	a real-world context,	a real-world context,	
determines the	determines the	uses this summary of	
minimum, the lower	interquartile range and	the data to describe	
quartile, the median,	range.	the spread and	
the upper quartile, and		distribution.	
the maximum.			

MA.6.DP.1.4 (Context: Real-World)

Given a histogram or line plot within a real-world context, qualitatively describe and interpret the spread and distribution of the data, including any symmetry, skewness, gaps, clusters, outliers and the range.

Benchmark Clarifications

Clarification 1: Refer to K-12 Mathematics Glossary (Appendix C).

Assessment Limits

Items will not require the student to calculate statistical measures or describe a plot using a statistical value, except range.

Items may require the student to describe the representation using the words "symmetry", "skewed", "gap(s)", "cluster(s)", "outliers", or "range."

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
given a histogram or	given a histogram or	given a histogram or	(intentionally left blank)
line plot within a real-	line plot within a real-	line plot within a real-	
world context,	world context,	world context,	
describes the spread	qualitatively describes	qualitatively describes	
and distribution of the	the spread and	and interprets the	
data including any	distribution of the	spread and distribution	
symmetry, skewness,	data, including any	of the data, including	
and the range.	symmetry, skewness,	any symmetry,	
	gaps, clusters, outliers,	skewness, gaps,	
	and the range.	clusters, outliers, and	
		the range.	

MA.6.DP.1.5 (Context: Real-World)

Create box plots and histograms to represent sets of numerical data within real-world contexts.

Example: The numerical data set {15, 0, 32, 24, 0, 17, 42, 0, 29, 120, 0, 20}, collected based on minutes spent on homework, can be represented graphically using a box plot.

Benchmark Clarifications

Clarification 1: Instruction includes collecting data and discussing ways to collect truthful data to construct graphical representations.

Clarification 2: Within this benchmark, it is the expectation to use appropriate titles, labels, scales and units when constructing graphical representations.

Clarification 3: Numerical data is limited to positive rational numbers.

Assessment Limits

Items will not require the student to calculate statistical measures outside of those needed to create a box plot, when necessary.

Data sets are limited to no more than 20 data points.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
identifies histograms	Identifies box plots and	creates box plots and	creates box plots and	
to corresponding sets	histograms to	histograms to	histograms to	
of numerical data	corresponding sets of	represent the set of the	represent and	
within real-world	numerical data	numerical data within	interpret sets of	
contexts.	within real-world	real-world contexts.	numerical data within	
	contexts.		real-world contexts;	
			distinguishes between	
			truthful and deceptive	
			data.	

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MA.6.DP.1.6 (Context: Real-World)

Given a real-world scenario, determine and describe how changes in data values impact measures of center and variation.

Benchmark Clarifications

Clarification 1: Instruction includes choosing the measure of center or measure of variation depending on the scenario.

Clarification 2: The measures of center are limited to mean and median. The measures of variation are limited to range and interquartile range.

Clarification 3: Numerical data is limited to positive rational numbers.

Assessment Limits

Items that require choosing a measure of center or measure of variation must be based on the effect of changes made to the data set.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
given a real-world	given a real-world	given a real-world	(intentionally left blank)
scenario, describes	scenario, determines	scenario, determines	
how changes in data	and describes how	and describes how	
values impact	changes in data values	changes in data values	
measures of center.	impact measures of	impact measures of	
	center; identifies	center and variation;	
	measures of center	identifies measures of	
	appropriate for the	center and variation	
	scenario.	appropriate for the	
		scenario.	