Miami-Dade County Public Schools Florida's B.E.S.T. Mathematics Grade 8 - Achievement Level Descriptor Tables

TABLE OF CONTENTS (BY BENCHMARK)	
MA.8.NSO.1.1	Page 2
MA.8.NSO.1.2	Page 3
MA.8.NSO.1.3	Page 4
MA.8.NSO.1.4	Page 5
MA.8.NSO.1.5	Page 5
MA.8.NSO.1.6	Page 6
MA.8.NSO.1.7	Page 7
MA.8.AR.1.1	Page 8
MA.8.AR.1.2	Page 8
MA.8.AR.1.3	Page 9
MA.8.AR.2.1	Page 9
MA.8.AR.2.2	Page 10
MA.8.AR.2.3	Page 10
MA.8.AR.3.1	Page 11
MA.8.AR.3.2	Page 11
MA.8.AR.3.3	Page 12
MA.8.AR.3.4	Page 12
MA.8.AR.3.5	Page 13
MA.8.AR.4.1	Page 14
MA.8.AR.4.2	Page 14
MA.8.AR.4.3	Page 15
MA.8.F.1.1	Page 16
MA.8.F.1.2	Page 17
MA.8.F.1.3	Page 17
MA.8.GR.1.1	Page 18
MA.8.GR.1.2	Page 19
MA.8.GR.1.3	Page 20
MA.8.GR.1.4	Page 20
MA.8.GR.1.5	Page 21
MA.8.GR.1.6	Page 21
MA.8.GR.2.1	Page 22
MA.8.GR.2.2	Page 23
MA.8.GR.2.3	Page 24
MA.8.GR.2.4	Page 25
MA.8.DP.1.1	Page 26
MA.8.DP.1.2	Page 27
MA.8.DP.1.3	Page 27
MA.8.DP.2.1	Page 28
MA.8.DP.2.2	Page 29
MA.8.DP.2.3	Page 30

(Return to the Table of Contents)

MA.8.NSO.1.1 (Context: Mathematical)

Extend previous understanding of rational numbers to define irrational numbers within the real number system. Locate an approximate value of a numerical expression involving irrational numbers on a number line.

Example: Within the expression $1 + \sqrt{30}$, the irrational number $\sqrt{30}$ can be estimated to be between 5 and 6 because 30 is between 25 and 36. By considering $(5.4)^2$ and $(5.5)^2$, a closer approximation for $\sqrt{30}$ is 5.5. So, the expression $1 + \sqrt{30}$ is equivalent to about 6.5.

Benchmark Clarifications

Clarification 1: Instruction includes the use of number line and rational number approximations, and recognizing pi (π) as an irrational number.

Clarification 2: Within this benchmark, the expectation is to approximate numerical expressions involving one arithmetic operation and estimating square roots or pi (π) .

Assessment Limits

Irrational numbers are limited to pi (π) and square roots.

Approximate values of square roots must be based on the value of the square roots of neighboring perfect squares.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
identifies numbers as rational or irrational.	defines irrational numbers within the real number system and locates an approximate value of an irrational number on a number line.	defines irrational numbers within the real number system and locates an approximate value of a two-term numerical expression involving irrational numbers on a number line.	defines irrational numbers within the real number system and locates an approximate value of a numerical expression involving irrational numbers on a number line and explains their reasoning.

(Return to the <u>Table of Contents</u>)

MA.8.NSO.1.2 (Context: Mathematical)

Plot, order and compare rational and irrational numbers, represented in various forms.

Benchmark Clarifications

Clarification 1: Within this benchmark, it is not the expectation to work with the number e.

Clarification 2: Within this benchmark, the expectation is to plot, order and compare square roots and cube roots.

Clarification 3: Within this benchmark, the expectation is to use symbols (<, > or =).

Assessment Limits

Items must include at least one irrational number or radical. Irrational numbers are limited to pi (π) , square roots, and cube roots.

Items requiring the student to compare fractions with irrational numbers or decimals are limited to fractions that result in a terminating decimal.

Items may use the words "is less than," "is greater than," or "is equal to."

Approximate values of square roots must be based on the value of the square roots of neighboring perfect squares.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
given an irrational square root or cube root, determines the integer values it lies between.	plots, orders, and compares, using <, >, =, rational and irrational numbers (when roots are included, roots will have the same index).	plots, orders, and compares, using <, >, =, rational and irrational numbers represented in various forms (must include at least one square root and one cube root).	explains and justifies how to plot, order, and compare rational and irrational numbers represented in various forms.

(Return to the <u>Table of Contents</u>)

MA.8.NSO.1.3 (Context: Mathematical)

Extend previous understanding of the Laws of Exponents to include integer exponents. Apply the Laws of Exponents to evaluate numerical expressions and generate equivalent numerical expressions, limited to integer exponents and rational number bases, with procedural fluency.

Example: The expression $\frac{2^4}{2^7}$ is equivalent to 2^{-3} which is equivalent to $\frac{1}{8}$.

Benchmark Clarifications

Clarification 1: Refer to the K-12 Formulas (Appendix E) for the Laws of Exponents.

Assessment Limits

Items must incorporate a negative exponent in either the given expression or the student-generated expression.

Items requiring the student to evaluate numerical expressions must incorporate at least one Law of Exponents or a negative exponent.

Items will require the student to evaluate a numerical expression with negative exponents, generate an equivalent expression, or generate and evaluate an expression.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
applies the Laws of Exponents to identify equivalent numerical expressions, limited to integer exponents and rational number bases, and applies one property from the Law of Exponents.	applies the Laws of Exponents to evaluate numerical expressions and identify equivalent numerical expressions, limited to integer exponents and rational number bases.	applies the Laws of Exponents to evaluate numerical expressions and generate equivalent numerical expressions, limited to integer exponents and rational number bases, with procedural fluency.	analyzes an error in the application of the Laws of Exponents used to evaluate numerical expressions and justifies the reasoning.

(Return to the <u>Table of Contents</u>)

MA.8.NSO.1.4 (Context: Mathematical & Real-World)

Express numbers in scientific notation to represent and approximate very large or very small quantities. Determine how many times larger or smaller one number is compared to a second number.

Example: Roderick is comparing two numbers shown in scientific notation on his calculator. The first number was displayed as 2.3147E27 and the second number was displayed as 3.5982E - 5. Roderick determines that the first number is about 10^{32} times bigger than the second number.

Benchmark Clarifications

No Benchmark Clarifications

Assessment Limits

Items may require the student to rewrite numbers in scientific notation or in standard form.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
given two numbers in scientific notation with different powers of 10, determines which one is larger or smaller.	scientific notation to represent and approximate very large quantities.	expresses numbers in scientific notation to represent and approximate very large or very small quantities and determines how many times larger or smaller one number is compared to a second number.	(intentionally left blank)

MA.8.NSO.1.5 (Context: Mathematical)

Add, subtract, multiply, and divide numbers expressed in scientific notation with procedural fluency.

Example: The sum of 2.31×10^{15} and 9.1×10^{13} is 2.401×10^{15} .

Benchmark Clarifications

Clarification 1: Within this benchmark, for addition and subtraction with numbers expressed in scientific notation, exponents are limited to within 2 of each other.

Assessment Limits

Items may require the student to rewrite numbers in scientific notation or in standard form.

Numbers are limited to the thousandths place or less when expressed in scientific notation.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
scientific notation in the same power of 10		adds, subtracts, multiplies, and divides numbers expressed in scientific notation.	adds, subtracts, multiplies, and divides numbers expressed in scientific notation, including combinations of these operations.

(Return to the <u>Table of Contents</u>)

MA.8.NSO.1.6 (Context: Real-World)

Solve real-world problems involving operations with numbers expressed in scientific notation.

Benchmark Clarifications

Clarification 1: Instruction includes recognizing the importance of significant digits when physical measurements are involved.

Clarification 2: Within this benchmark, for addition and subtraction with numbers expressed in scientific notation, exponents are limited to within 2 of each other.

Assessment Limits

Items may require the student to rewrite numbers in scientific notation or in standard form.

Numbers are limited to the thousandths place or less when expressed in scientific notation.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
subtracting numbers expressed in scientific notation in the same power of 10 wherein the	problems by adding and subtracting numbers expressed in scientific notation in the same power of 10, and	solves real-world problems by adding, subtracting, multiplying, and dividing numbers expressed in scientific notation.	solves real-world problems by adding, subtracting, multiplying, and dividing numbers expressed in scientific notation and interprets the solution	
	numbers expressed in scientific notation.	Scientific fiolation.	in the context of the situation.	

(Return to the Table of Contents)

MA.8.NSO.1.7 (Context: Mathematical & Real-World)

Solve multi-step mathematical and real-world problems involving the order of operations with rational numbers including exponents and radicals.

Example: The expression $(-\frac{1}{2})^2 + \sqrt{(2^3 + 8)}$ is equivalent to $\frac{1}{4} + \sqrt{16}$ which is equivalents to $\frac{1}{4} + 4$ which is equivalent to $\frac{17}{4}$.

Benchmark Clarifications

Clarification 1: Multi-step expressions are limited to 6 or fewer steps.

Clarification 2: Within this benchmark, the expectation is to simplify radicals by factoring square roots of perfect squares up to 225 and cube roots of perfect cubes from -125 to 125.

Assessment Limits

Decimals are limited to the thousandths place or less.

Expressions must be given and must incorporate a negative exponent and/or a radical.

The value of the radicand must be a perfect square or perfect cube.

Integer exponents are limited to values between –3 and 3, inclusive.

Expressions that include the use of both fractions and decimals must use fractions that only result in a terminating decimal.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
with up to 4 steps involving the order of	mathematical and real- world problems with up to 5 steps involving the order of operations with rational numbers including integer	mathematical and real- world problems with up to 6 steps involving the order of operations with rational numbers including exponents and radicals.	solves and explains multi-step mathematical and real-world problems with up to 6 steps and justifies each step in applying the order of operations with rational numbers including exponents and radicals.	

(Return to the <u>Table of Contents</u>)

MA.8.AR.1.1 (Context: Mathematical)

Apply the Laws of Exponents to generate equivalent algebraic expressions, limited to integer exponents and monomial bases.

Example: The expression $(3x^3y^{-2})^3$ is equivalent to $27x^9y^{-6}$.

Benchmark Clarifications

Clarification 1: Refer to the K-12 Formulas (Appendix E) for the Laws of Exponents.

Assessment Limits

Items are limited to the use of monomials and one-term algebraic expressions involving multiplication and/or division.

Items are limited to the use of no more than two variables.

Items including one variable are limited to no more than three laws.

Items including two different variables are limited to the application of no more than two Laws of Exponents.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
Exponents to identify equivalent algebraic expressions, using integer exponents and monomial bases using	applies the Laws of Exponents to identify equivalent algebraic expressions, using positive exponents and monomial bases using laws of exponents.	equivalent algebraic expressions, using integer exponents and	applies the Laws of Exponents to generate equivalent algebraic expressions, limited to integer exponents and monomial bases using laws of exponents and provides justification.

MA.8.AR.1.2 (Context: Mathematical)

Apply properties of operations to multiply two linear expressions with rational coefficients.

Example: The product of (1.1 + x) and (-2.3x) can be expressed as $-2.53x-2.3x^2$ or $-2.3x^2-2.53x$.

Benchmark Clarifications

Clarification 1: Problems are limited to products where at least one of the factors is a monomial.

Clarification 2: Refer to Properties of Operations, Equality and Inequality (Appendix D).

Assessment Limits

No Assessment Limits

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
operations to multiply two linear expressions with integer coefficients where both factors are	operations to multiply two linear expressions with rational coefficients where both factors are	applies properties of operations to multiply two linear expressions with rational coefficients where one factor is a monomial.	(intentionally left blank)

(Return to the <u>Table of Contents</u>)

MA.8.AR.1.3 (Context: Mathematical)

Rewrite the sum of two algebraic expressions having a common monomial factor as a common factor multiplied by the sum of two algebraic expressions.

Example: The expression $99x-11x^3$ can be rewritten as $11x(9-x^2)$ or as $-11x(-9+x^2)$.

Benchmark Clarifications

No Benchmark Clarifications

Assessment Limits

Algebraic expressions must be given.

Items are limited to the use of no more than two different variables.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
monomial factor in the sum of two algebraic expressions.	algebraic expressions, identifies the equivalent expression having a common monomial factor as a common factor	having a common monomial factor with a common factor multiplied by the sum of two algebraic expressions.	rewrites the sum of two algebraic expressions having a common monomial factor in different ways (including factoring out the GCF) with a common factor multiplied by the sum of two algebraic expressions.

MA.8.AR.2.1 (Context: Mathematical)

Solve multi-step linear equations in one variable, with rational number coefficients. Include equations with variables on both sides.

Benchmark Clarifications

Clarification 1: Problem types include examples of one-variable linear equations that generate one solution, infinitely many solutions or no solution.

Assessment Limits

Items including one equation must give the equation and include more than two procedural steps to solve.

Items including multiple equations must give the equations and at least one of the given equations will include more than two procedural steps to solve.

Items may require the student to state whether there is one solution, no solution, or infinite solutions.

tieris may require the student to state whether there is one solution, no solution, or infinite solutions.				
	Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5	
	equations in one variable, with variables on both sides of the equation and rational number coefficients that generate	equations in one variable, with rational number coefficients that generate one solution, no solution, or infinitely many solutions.	with rational number	

(Return to the <u>Table of Contents</u>)

MA.8.AR.2.2 (Context: Mathematical)

Solve two-step linear inequalities in one variable and represent solutions algebraically and graphically.

Benchmark Clarifications

Clarification 1: Instruction includes inequalities in the forms $px\pm q > r$ and $p(x\pm q) > r$, where p, q and r are specific rational numbers and where any inequality symbol can be represented.

Clarification 2: Problems include inequalities where the variable may be on either side of the inequality.

Assessment Limits

Inequalities must be given, will be presented in the forms $px \pm q > r$ or $p(x \pm q) > r$, and will use the relational symbols >, \geq , <, or \leq .

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
inequalities in one variable with whole number coefficients and represents solutions algebraically.	inequalities in one variable with positive rational coefficients and	inequalities in one variable and represents solutions algebraically and graphically.	solves two-step linear inequalities in one variable and represents solutions algebraically and graphically and interprets the solution in context of the situation.	

MA.8.AR.2.3 (Context: Mathematical)

Given an equation in the form of $x^2 = p$ and $x^3 = q$, where p is a whole number and q is an integer, determine the real solutions.

Benchmark Clarifications

Clarification 1: Instruction focuses on understanding that when solving $x^2 = p$, there is both a positive and negative solution.

Clarification 2: Within this benchmark, the expectation is to calculate square roots of perfect squares up to 225 and cube roots of perfect cubes from -125 to 125.

Assessment Limits

Items will not require the student to simplify square roots of nonperfect squares, simplify cube roots of nonperfect cubes, or approximate roots.

Items are limited to one procedural step to isolate the variable.

Items may require the student to give both the positive and negative solutions for the form $x^2 = p$.

			•	
	Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5	
given an equation in the form of $x^2 = p$, where p is a perfect square between 0 and 225, determines a positive solution.	is a perfect cube between 0 and 125, determines a positive	form of $x^2 = p$ and $x^3 = q$, where p is perfect square between 0 and 225 and q is a perfect cube between -125 and 225, determines positive and negative solutions.	form of $x^2 = p$ and $x^3 = q$, where p is perfect square between 0 and 225 and q is a perfect cube between -125 and 225,	

(Return to the Table of Contents)

MA.8.AR.3.1 (Context: Mathematical & Real-World)

Determine if a linear relationship is also a proportional relationship.

Benchmark Clarifications

Clarification 1: Instruction focuses on the understanding that proportional relationships are linear relationships whose graph passes through the origin.

Clarification 2: Instruction includes the representation of relationships using tables, graphs, equations and written descriptions.

Assessment Limits

Items will present a relationship as a table, a graph, an equation, or a written description.

Items presented as a written description must state that the relationship is linear and will require the student to identify whether it is proportional.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
linear relationship is also a proportional relationship from a graph.	linear relationship is also a proportional relationship using tables and	determines whether a linear relationship is also a proportional relationship using written descriptions.	(intentionally left blank)

MA.8.AR.3.2 (Context: Mathematical)

Given a table, graph or written description of a linear relationship, determine the slope.

Benchmark Clarifications

Clarification 1: Problem types include cases where two points are given to determine the slope.

Clarification 2: Instruction includes making connections of slope to the constant of proportionality and to similar triangles represented on the coordinate plane.

Assessment Limits

All values for x-and y-coordinates used to determine slope must be integers.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
given a graph of a linear relationship involving integer values , determines the slope.	given a table of a linear relationship involving integer values, determines the slope.	written description of a linear relationship involving rational values, determines the slope.	given a table, graph, or written description of a linear relationship involving rational values, determines the slope, and explains the connection between slope and the constant of proportionality or explains the connection between slope and similar triangles on the coordinate plane.

(Return to the Table of Contents)

MA.8.AR.3.3 (Context: Mathematical)

Given a table, graph or written description of a linear relationship, write an equation in slope-intercept form.

Benchmark Clarifications

No Benchmark Clarifications

Assessment Limits

Items must state that the given table, graph, or written description represents a linear relationship.

Tables must include at least two points.

Graphs may include at least two exact points marked on the line and may be labeled with coordinates.

Graphs must have integral y-intercepts.

All values for x- and y-coordinates used to determine slope must be integers.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
relationship, identifies the equivalent equation in slope-intercept form.	the y-intercept), graph, or written description (including ordered pairs	given a table, graph, or written description of a linear relationship, writes the equation in slope- intercept form.	(intentionally left blank)	

MA.8.AR.3.4 (Context: Mathematical)

Given a mathematical or real-world context, graph a two-variable linear equation from a written description, a table, or an equation in slope-intercept form.

Benchmark Clarifications

No Benchmark Clarifications

Assessment Limits

Items must use integral values for y-intercepts.

Coordinate points within tables and written descriptions must be integers.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
given a two-variable linear equation in slope-intercept form, identifies the graph that represents the given linear equation.	given a mathematical context, graphs a two-variable linear equation from a table, or an equation in slope-intercept form.	given a mathematical or real-world context, graphs a two-variable linear equation from a written description, a table, or an equation in slope-intercept form.	(intentionally left blank)

(Return to the <u>Table of Contents</u>)

MA.8.AR.3.5 (Context: Real-World)

Given a real-world context, determine and interpret the slope and y-intercept of a two-variable linear equation from a written description, a table, a graph or an equation in slope-intercept form.

Example: Raul bought a palm tree to plant at his house. He records the growth over many months and creates the equation h = 0.21m + 4.9, where h is the height of the palm tree in feet and m is the number of months. Interpret the slope and y-intercept from his equation.

Benchmark Clarifications

Clarification 1: Problems include conversions with temperature and equations of lines of fit in scatter plots.

Assessment Limits

Items will require the student to find and interpret the slope, the y-intercept, or both.

Items will not require the student to write an equation or graph a line on a given coordinate plane.

Variables must be defined in context.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
given a real-world context, determines the slope and y-intercept of a two-variable linear equation from an equation in slope-intercept form.	involving integer values, determines and interprets the slope and y-intercept of a two-variable linear equation from a written description, a table, a	given a real-world context involving rational values, determines and interprets the slope and y-intercept of a two-variable linear equation from a written description, a table, a graph, or an equation in slope-intercept form.	(intentionally left blank)

(Return to the Table of Contents)

MA.8.AR.4.1 (Context: Mathematical)

Given a system of two linear equations and a specified set of possible solutions, determine which ordered pairs satisfy the system of linear equations.

Benchmark Clarifications

Clarification 1: Instruction focuses on the understanding that a solution to a system of equations satisfies both linear equations simultaneously.

Assessment Limits

Items must present the system of equations, and equations must be in slope-intercept form.

Items must present possible solutions as integral ordered pairs.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
solution to a system of equations can be represented as an ordered pair.	linear equations that has one solution with integer values and a specified set of possible solutions, determines the	linear equations and a specified set of possible solutions, determines the ordered pairs that satisfy the system of linear equations.		

MA.8.AR.4.2 (Context: Mathematical)

Given a system of two linear equations represented graphically on the same coordinate plane, determine whether there is one solution, no solution or infinitely many solutions.

Benchmark Clarifications

No Benchmark Clarifications

Assessment Limits

Items may present the system of equations using slope-intercept form.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
when given a system of two linear equations represented graphically, identifies the solution .	linear equations represented graphically on the same coordinate plane, determines whether there is one solution.	linear equations represented graphically on the same coordinate plane, determines	given a system of two linear equations represented graphically on the same coordinate plane, determines and provides a justification as to whether there is one solution, no solution, or infinitely many solutions.

(Return to the **Table of Contents**)

MA.8.AR.4.3 (Context: Mathematical & Real-World)

Given a mathematical or real-world context, solve systems of two linear equations by graphing.

Benchmark Clarifications

No Benchmark Clarifications

Assessment Limits

When equations are given, the equations must be in slope-intercept form with integral y-intercepts.

Items that require the student to graph and find the point of intersection will have the coordinates of the solution as integers.

Given a system of equations, items may require the student to approximate the non-integer solution.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
	real-world context, solves systems of two linear equations by graphing; solutions are integers.	systems of two linear equations by graphing; solutions can be		

(Return to the <u>Table of Contents</u>)

MA.8.F.1.1 (Context: Mathematical)

Given a set of ordered pairs, a table, a graph or mapping diagram, determine whether the relationship is a function. Identify the domain and range of the relation.

Benchmark Clarifications

Clarification 1: Instruction includes referring to the input as the independent variable and the output as the dependent variable.

Clarification 2: Within this benchmark, it is the expectation to represent domain and range as a list of numbers or as an inequality.

Assessment Limits

Items will present the domain and range as a list of values in braces or as an inequality.

Items may refer to input as the independent variable or domain, and to output as the dependent variable or range.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
given a graph or mapping diagram , determines whether the relationship is a function.	pairs, a table, a graph, or mapping diagram, determines whether the relationship is a function, and given a set of ordered pairs, a table, or mapping diagram, identifies the domain	mapping diagram, determines whether the relationship is a function and determines the domain and range of	given a set of ordered pairs, a table, a graph, or mapping diagram, determines whether the relationship is a function, determines the independent and dependent variables, and identifies the domain and range of the relation as a list of numbers or as a simple inequality (e.g. x ≥ 1) and interprets the domain constraints in terms of the context.	

(Return to the <u>Table of Contents</u>)

MA.8.F.1.2 (Context: Mathematical & Real-World)

Given a function defined by a graph or an equation, determine whether the function is a linear function. Given an input-output table, determine whether it could represent a linear function.

Benchmark Clarifications

Clarification 1: Instruction includes recognizing that a table may not determine a function.

Assessment Limits

Items will present a relationship as a table, a graph, an equation, or a written description.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
19		given a function defined by an input-output table,	(intentionally left blank)
	determines whether the	determines whether the	
linear function.		table could represent a	
	function.	linear function.	

MA.8.F.1.3 (Context: Real-World)

Analyze a real-world written description or graphical representation of a functional relationship between two quantities and identify where the function is increasing, decreasing or constant.

Benchmark Clarifications

Clarification 1: Problem types are limited to continuous functions.

Clarification 2: Analysis includes writing a description of a graphical representation or sketching a graph from a written description.

Assessment Limits

Items may require the student to identify increasing, decreasing, or constant intervals from a graph.

Intervals will not be expressed in inequality or interval notation.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
given a specific section of a graph that represents a function, analyzes the specific section as increasing or decreasing.	representation of a functional relationship between two quantities and identifies where the function is increasing, decreasing, or constant.	written description or graphical representation of a functional relationship between two quantities and identifies	analyzes a real-world written description of a functional relationship between two quantities and draws a graph to identify where the function is increasing, decreasing, or constant.	

(Return to the <u>Table of Contents</u>)

MA.8.GR.1.1 (Context: Mathematical & Real-World)

Apply the Pythagorean Theorem to solve mathematical and real-world problems involving unknown side lengths in right triangles.

Benchmark Clarifications

Clarification 1: Instruction includes exploring right triangles with natural-number side lengths to illustrate the Pythagorean Theorem.

Clarification 2: Within this benchmark, the expectation is to memorize the Pythagorean Theorem.

Clarification 3: Radicands are limited to whole numbers up to 225.

Assessment Limits

Items will not present triangles on a coordinate plane.

Items will not require the student to simplify square roots of nonperfect squares.

Nonperfect square roots may be represented in radical form or as an approximation.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
			applies the Pythagorean	
			Theorem more than	
mathematical problem to		world problems involving		
find the hypotenuse of a		unknown side lengths in		
right triangle resulting in	lengths in right triangles.		world problems involving	
a whole number.			unknown side lengths in	
			right triangles.	

(Return to the <u>Table of Contents</u>)

MA.8.GR.1.2 (Context: Mathematical & Real-World)

Apply the Pythagorean Theorem to solve mathematical and real-world problems involving the distance between two points in a coordinate plane.

Example: The distance between (-2,7) and (0, 6) can be found by creating a right triangle with the vertex of the right angle at the point (-2, 6). This gives a height of the right triangle as 1 unit and a base of 2 units. Then using the Pythagorean Theorem, the distance can be determined from the equation $1^2 + 2^2 = c^2$, which is equivalent to $5 = c^2$. So, the distance is $\sqrt{5}$ units.

Benchmark Clarifications

Clarification 1: Instruction includes exploring right triangles with natural-number side lengths to illustrate the Pythagorean Theorem.

Clarification 2: Within this benchmark, the expectation is to memorize the Pythagorean Theorem.

Clarification 3: Radicands are limited to whole numbers up to 225.

Assessment Limits

Items will not require the student to simplify square roots of nonperfect squares.

Nonperfect square roots may be represented in radical form or as an approximation.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
Theorem to solve mathematical problems involving the distance between two points in the first quadrant of a	Theorem to solve mathematical problems involving the distance between two points in a coordinate plane when the two points are shown as part of a right triangle.	Theorem to solve mathematical and real-world problems involving the distance between two points with a given coordinate plane.	

(Return to the <u>Table of Contents</u>)

MA.8.GR.1.3 (Context: Mathematical & Real-World)

Use the Triangle Inequality Theorem to determine if a triangle can be formed from a given set of sides. Use the converse of the Pythagorean Theorem to determine if a right triangle can be formed from a given set of sides.

Benchmark Clarifications

No Benchmark Clarifications

Assessment Limits

Limit real-world context to simple situations when using the converse of the Pythagorean Theorem.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
(intentionally left blank)	Inequality Theorem to determine whether a triangle can be formed from a given set of sides.	determine whether a triangle can be formed from a given set of sides and uses the converse of the Pythagorean Theorem to determine	given three side lengths that do not make a triangle, determine which side should be changed to form a triangle, and uses the converse of the Pythagorean Theorem to determine whether a given triangle is a right triangle.

MA.8.GR.1.4 (Context: Mathematical)

Solve mathematical problems involving the relationships between supplementary, complementary, vertical or adjacent angles.

Benchmark Clarifications

No Benchmark Clarifications

Assessment Limits

Angle measures may be expressed as numerical values or algebraic expressions.

Items including an algebraic expression that represents an unknown angle must determine the unknown angle measure.

angle measure.			
Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
complementary, vertical, or adjacent angles with numerical angle	solves mathematical problems with one relationship between supplementary, complementary, vertical, or adjacent angles with numerical angle measures.	solves mathematical problems involving multiple relationships between supplementary, complementary, vertical, or adjacent angles with numerical angle measures.	solves mathematical problems involving the relationships between supplementary, complementary, vertical, or adjacent angles with at least one angle measures given as an algebraic expression.

(Return to the <u>Table of Contents</u>)

MA.8.GR.1.5 (Context: Mathematical)

Solve problems involving the relationships of interior and exterior angles of a triangle.

Benchmark Clarifications

Clarification 1: Problems include using the Triangle Sum Theorem and representing angle measures as algebraic expressions.

Assessment Limits

Angle measures may be expressed as numerical values or algebraic expressions.

Items including an algebraic expression that represents an unknown angle must determine the unknown angle measure.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
(intentionally left blank)	solves problems involving	solves problems involving	solves problems involving	
	the relationships of	the relationships of	the relationships of	
	interior angles of a	interior and exterior	interior and exterior	
	triangle.	angles of a triangle when		
		one angle measure is	multiple angle measures	
		given as an algebraic	are given as algebraic	
		expression.	expressions.	

MA.8.GR.1.6 (Context: Mathematical)

Develop and use formulas for the sums of the interior angles of regular polygons by decomposing them into triangles.

Benchmark Clarifications

Clarification 1: Problems include representing angle measures as algebraic expressions.

Assessment Limits

Angle measures may be expressed as numerical values or algebraic expressions.

Items including an algebraic expression that represents an unknown angle must determine the unknown angle measure.

<u> </u>				
Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
numerical angle measures, identifies the corresponding equation	the sums of interior angles of regular polygons by	polygons by decomposing them into triangles.	develops and uses formulas for the sums of the interior angles of regular polygons by decomposing them into triangles; includes finding a missing angle measure and includes representing angle measures as algebraic expressions.	

(Return to the **Table of Contents**)

MA.8.GR.2.1 (Context: Mathematical)

Given a preimage and image generated by a single transformation, identify the transformation that describes the relationship.

Benchmark Clarifications

Clarification 1: Within this benchmark, transformations are limited to reflections, translations, or rotations of images.

Clarification 2: Instruction focuses on the preservation of congruence so that a figure maps onto a copy of itself.

Assessment Limits

Items will not use the coordinate plane.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
image generated by a translation, identifies the transformation that	image generated by a reflection, identifies the transformation that describes the	image generated by a rotation, identifies the transformation that describes the relationship.	given a preimage and image generated by a single transformation, analyzes the transformation that describes the relationship and recognizes that translations, rotations, and reflections preserve congruence.

(Return to the <u>Table of Contents</u>)

MA.8.GR.2.2 (Context: Mathematical)

Given a preimage and image generated by a single dilation, identify the scale factor that describes the relationship.

Benchmark Clarifications

Clarification 1: Instruction includes the connection to scale drawings and proportions.

Clarification 2: Instruction focuses on the preservation of similarity and the lack of preservation of congruence when a figure maps onto a scaled copy of itself unless the scaling factor is 1.

Assessment Limits

Items will not ask the student to find the lengths of missing sides using a scale factor.

Items will not use the coordinate plane.

	Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5		
given a preimage and image generated by a single dilation, identifies the scale factor of the dilation as less than 1 or greater than 1.	generating a single dilation, identifies the corresponding	given a preimage and image generated by a single dilation, identifies the scale factor of the dilation.	given a preimage and image generated by a single dilation, identifies the scale factor that describes the relationship, and recognizes and explains that dilations do not preserve congruence unless the scale factor is 1.		

(Return to the <u>Table of Contents</u>)

MA.8.GR.2.3 (Context: Mathematical)

Describe and apply the effect of a single transformation on two-dimensional figures using coordinates and the coordinate plane.

Benchmark Clarifications

Clarification 1: Within this benchmark, transformations are limited to reflections, translations, rotations or dilations of images.

Clarification 2: Lines of reflection are limited to the x-axis, y-axis or lines parallel to the axes.

Clarification 3: Rotations must be about the origin and are limited to 90°, 180°, 270° or 360°.

Clarification 4: Dilations must be centered at the origin.

Assessment Limits

Rotations must include the direction of rotation with the angle of rotation.

Transformations will not be given as ordered pair rules.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
dimensional figure	transformation, either a reflection over the x- or y-axis or translation, on two-dimensional figures using the coordinate plane.		(intentionally left blank)

(Return to the Table of Contents)

MA.8.GR.2.4 (Context: Mathematical & Real -World)

Solve mathematical and real-world problems involving proportional relationships between similar triangles.

Example: During a Tampa Bay Lightning game one player, Johnson, passes the puck to his teammate, Stamkos, by bouncing the puck off the wall of the rink. The path of the puck creates two line segments that form hypotenuses for each of two similar right triangles, with the height of each triangle the distance from one of the players to the wall of the rink. If Johnson is 12 feet from the wall and Stamkos is 3 feet from the wall. How far did the puck travel from the wall of the rink to Stamkos if the distance traveled from Johnson to the wall was 16 feet?

Benchmark Clarifications

No Benchmark Clarifications

Assessment Limits

Given dimensions of figures in items must be the same unit.

	Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5		
between similar triangles	problems involving proportional relationships between similar triangles where a diagram is provided and the scale factor is a whole or rational number.	solves mathematical or real-world problems involving proportional relationships between similar triangles with or without a diagram where the scale factor is a whole or rational number.	solves mathematical or real-world problems involving proportional relationships between similar triangles, having at least one side represented as an algebraic expression, where a diagram is not provided and the scale factor is a rational number.		

(Return to the <u>Table of Contents</u>)

MA.8.DP.1.1 (Context: Real-World)

Given a set of real-world bivariate numerical data, construct a scatter plot or a line graph as appropriate for the context.

Example: Jaylyn is collecting data about the relationship between grades in English and grades in mathematics. He represents the data using a scatter plot because he is interested if there is an association between the two variables without thinking of either one as an independent or dependent variable.

Example: Samantha is collecting data on her weekly quiz grade in her social studies class. She represents the data using a line graph with time as the independent variable.

Benchmark Clarifications

Clarification 1: Instruction includes recognizing similarities and differences between scatter plots and line graphs, and on determining which is more appropriate as a representation of the data based on the context.

Clarification 2: Sets of data are limited to 20 points.

Assessment Limits

Data sets will include between 5 and 20 points, inclusive.

Items will state whether a scatter plot or line graph is to be constructed based on the intent of the given context.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
bivariate numerical data, identifies the corresponding scatter plot	bivariate numerical data, constructs either a	bivariate numerical data,	given a set of real-world bivariate numerical data, justifies whether the construction of a scatter plot or a line graph is appropriate for the context.

(Return to the <u>Table of Contents</u>)

MA.8.DP.1.2 (Context: Real-World)

Given a scatter plot within a real-world context, describe patterns of association.

Benchmark Clarifications

Clarification 1: Descriptions include outliers; positive or negative association; linear or nonlinear association; strong or weak association.

Assessment Limits

Items will not require the student to determine strong vs. weak association.

Items will use wording of association exclusively when describing as linear, nonlinear, positive, or negative.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
identifies a positive or negative association and any outliers .	identifies a positive or negative association and whether it is strong or weak and has any	given a scatter plot within a real-world context, describes patterns of association, including linear or nonlinear and any outliers.	(intentionally left blank)

MA.8.DP.1.3 (Context: Mathematical & Real-World)

Given a scatter plot with a linear association, informally fit a straight line.

Benchmark Clarifications

Clarification 1: Instruction focuses on the connection to linear functions.

Clarification 2: Instruction includes using a variety of tools, including a ruler, to draw a line with approximately the same number of points above and below the line.

Assessment Limits

Items will not require the student to write or determine the equation of a line of fit.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
(intentionally left blank)	identifies a straight line	linear association, informally fits a straight line.	linear association,

(Return to the Table of Contents)

MA.8.DP.2.1 (Context: Real-World)

Determine the sample space for a repeated experiment.

Benchmark Clarifications

Clarification 1: Instruction includes recording sample spaces for repeated experiments using organized lists, tables or tree diagrams.

Clarification 2: Experiments to be repeated are limited to tossing a fair coin, rolling a fair die, picking a card randomly from a deck with replacement, picking marbles randomly from a bag with replacement and spinning a fair spinner.

Clarification 3: Repetition of experiments is limited to two times except for tossing a coin.

Assessment Limits

Items may present sample spaces as an organized list, a table, or a tree diagram.

Items including a deck of cards are not limited to a standard 52-card deck, and may include, but are not limited to, cards containing names, letters of the alphabet, a variety of colors, or the like.

Items including a fair die are not limited to a standard 6-sided die and may include a variety of sides.

Items including a fair die are not limited to including consecutive sequential numbers and may include repeated or not repeated, colors, shapes, words, numbers, or the like.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
space for a repeated experiment, that is repeated two	space for a repeated experiment involving a coin, a die , or a given fair spinner.	space for a repeated experiment including		

(Return to the Table of Contents)

MA.8.DP.2.2 (Context: Real-World)

Find the theoretical probability of an event related to a repeated experiment.

Benchmark Clarifications

Clarification 1: Instruction includes representing probability as a fraction, percentage, or decimal.

Clarification 2: Experiments to be repeated are limited to tossing a fair coin, rolling a fair die, picking a card randomly from a deck with replacement, picking marbles randomly from a bag with replacement and spinning a fair spinner.

Clarification 3: Repetition of experiments is limited to two times except for tossing a coin.

Assessment Limits

Probability will be represented using a fraction, percent, or decimal.

Items including a deck of cards are not limited to a standard 52-card deck, and can include, but are not limited to, cards containing names, letters of the alphabet, a variety of colors, or the like.

Items including a fair die are not limited to a standard 6-sided die and can include a variety of sides.

Items including a fair die are not limited to including consecutive sequential numbers and can include repeated or not repeated, colors, shapes, words, numbers, or the like. Descriptions representing an experiment are not limited to the repetition of two trials.

Achievement Level Descriptors			
Level 2	Level 3	Level 4	Level 5
finds the theoretical probability of an event related to a repeated experiment, which include tossing a fair coin or rolling a fair die, and expresses that probability as a fraction.	probability of an event related to a repeated experiment, which include tossing a fair coin, rolling a fair die, picking a card randomly from a deck with replacement, picking marbles randomly from a bag with replacement, and spinning a fair spinner, and expresses that probability as a fraction.	probability of an event related to a repeated experiment, which include tossing a fair coin, rolling a fair die, picking a card randomly from a deck with replacement, picking marbles randomly from a bag with replacement, and spinning a fair spinner, and expresses that probability as a percentage and/or as a	
	randomly from a bag with replacement, and spinning a fair spinner, and expresses that probability as a fraction.	marbles randomly from a bag with replacement, and spinning a fair spinner, and expresses that probability as a	

(Return to the Table of Contents)

MA.8.DP.2.3 (Context: Real-World)

Solve real-world problems involving probabilities related to single or repeated experiments, including making predictions based on theoretical probability.

Example: If Gabriella rolls a fair die 300 times, she can predict that she will roll a 3 approximately 50 times since the theoretical probability is $\frac{1}{\epsilon}$.

Example: Sandra performs an experiment where she flips a coin three times. She finds the theoretical probability of landing on exactly one head as $\frac{3}{8}$. If she performs this experiment 50 times (for a total of 150 flips), predict the number of repetitions of the experiment that will result in exactly one of the three flips landing on heads.

Benchmark Clarifications

Clarification 1: Instruction includes making connections to proportional relationships and representing probability as a fraction, percentage, or decimal.

Clarification 2: Experiments to be repeated are limited to tossing a fair coin, rolling a fair die, picking a card randomly from a deck with replacement, picking marbles randomly from a bag with replacement and spinning a fair spinner.

Clarification 3: Repetition of experiments is limited to two times except for tossing a coin.

Assessment Limits

Probability will be represented using a fraction, percent, or decimal.

Items including a deck of cards are not limited to a standard 52-card deck, and can include, but are not limited to, cards containing names, letters of the alphabet, a variety of colors, or the like.

Items including a fair die are not limited to a standard 6-sided die and can include a variety of sides.

Items including a fair die are not limited to including consecutive sequential numbers and can include repeated or not repeated, colors, shapes, words, numbers, or the like. Descriptions representing an experiment are not limited to the repetition of two trials.

Achievement Level Descriptors				
Level 2	Level 3	Level 4	Level 5	
solves real-world problems involving probabilities related to single experiments involving coins, dice, or a given fair spinner.	problems involving probabilities related to single or repeated experiments involving coins, dice, or a given fair spinner, including making predictions	solves real-world problems involving probabilities related to single or repeated experiments, including experiments that involve replacement, including making predictions based on theoretical probability	(intentionally left blank)	