- 1. Let A,B,C,D be four distinct points on a line, in that order. The circles with diameters AC and BD intersect at X and Y. The line XY meets BC at Z. Let P be a point on the line XY other than Z. The line CP intersects the circle with diameter AC at C and M, and the line BP intersects the circle with diameter BD at B and N. Prove that the lines AM, DN, XY are concurrent.
- 2. Let a, b, c be positive real numbers such that abc = 1. Prove that

$$\frac{1}{a^3(b+c)} + \frac{1}{b^3(c+a)} + \frac{1}{c^3(a+b)} \ge \frac{3}{2}.$$

- 3. Determine all integers n > 3 for which there exist n points  $A_1, ...., A_n$  in the plane, no three collinear, and real numbers  $r_1, ..., r_n$  such that for  $1 \le i < j < k \le n$ , the area of  $\triangle A_i A_j A_k$  is  $r_i + r_j + r_k$ .
- 4. Find the maximum value of  $x_0$  for which there exists a sequence  $x_0, x_1, \dots, x_{1995}$  of positive reals with  $x_0 = x_{1995}$ , such that for  $i = 1, \dots, 1995$ ,

$$x_{i-1} + \frac{2}{x_{i-1}} = 2x_i + \frac{1}{x_i}.$$

- 5. Let ABCDEF be a convex hexagon with AB = BC = CD and DE = EF = FA, such that  $\angle BCD = \angle EFA = \pi/3$ . Suppose G and H are points in the interior of the hexagon such that  $\angle AGB = \angle DHE = 2\pi/3$ . Prove that  $AG + GB + GH + DH + HE \ge CF$ .
- 6. Let p be an odd prime number. How many p-element subsets A of  $\{1, 2, .... 2p\}$  are there, the sum of whose elements is divisible by p?