

Assignment 2 : Q2: Report

Question 2 Denoising Phantom Magnetic Resonance Image

Part a,b,c,d

Complex gaussian noise model is implemented along with different priors like quadratic, discontinuity adaptive huber function, huber function. Codes for the same can be found in code folder of question 2. “myDenoiser.m” contains the relevant information.

Reporting

Part a

RRMSE between noisy and noiseless image: 0.2931

Part b

Optimal Values for Quadratic Prior

Optimal Value of alpha = 0.231

Description	alpha	RRMSE
alpha_optimal	0.231	0.23359
1.2*alpha_optimal	0.2772	0.23523
0.8*alpha_optimal	0.1848	0.23455

Optimal Values for Huber Prior

Optimal Value of alpha = 1

Optimal Value of Gamma = 0.01

Description	(alpha,gamma)	RRMSE
alpha_optimal,gamma_optimal	(1,0.01)	0.079497
1.2*alpha_optimal,gamma_optimal	(1,0.01)	0.079497
0.8*alpha_optimal,gamma_optimal	(0.8,0.01)	0.24494
alpha_optimal,1.2*gamma_optimal	(1,0.012)	0.087185
alpha_optimal,0.8*gamma_optimal	(1,0.008)	0.080729

Optimal Values for Discontinuity adaptive huber Prior


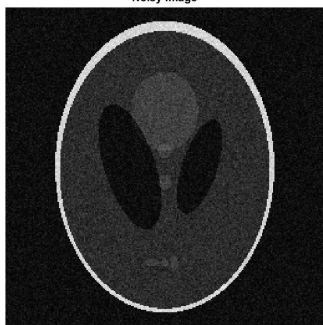
Optimal Value of $\alpha = 0.999$
 Optimal Value of $\gamma = 0.008$


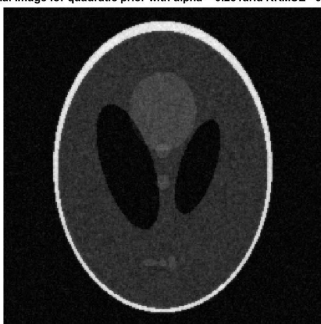




Description	(α, γ)	RRMSE
$\alpha_{\text{optimal}}, \gamma_{\text{optimal}}$	(0.999, 0.008)	0.094544
$1.2 * \alpha_{\text{optimal}}, \gamma_{\text{optimal}}$	(1, 0.008)	0.14487
$0.8 * \alpha_{\text{optimal}}, \gamma_{\text{optimal}}$	(0.7992, 0.008)	0.2518
$\alpha_{\text{optimal}}, 1.2 * \gamma_{\text{optimal}}$	(0.999, 0.0096)	0.13452
$\alpha_{\text{optimal}}, 0.8 * \gamma_{\text{optimal}}$	(0.999, 0.0064)	0.11971

Looking at the table we can conclude that optimal values are indeed local minima for objective function.

Part c

Corresponding images for Different Type of Prior

Description	Noiseless	Specific
Noisy		

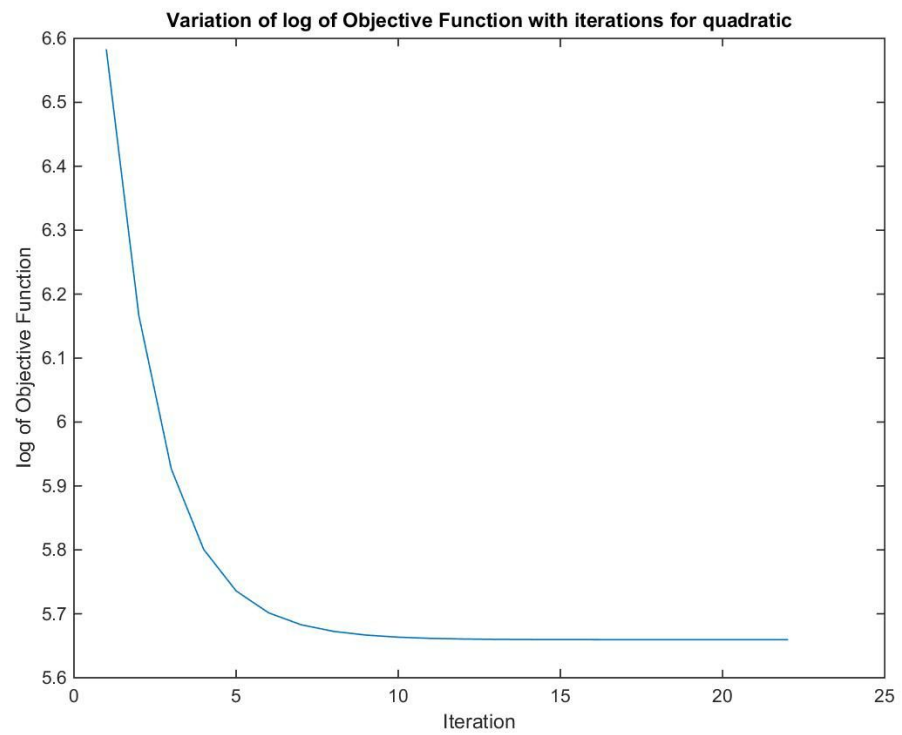
Quadratic Prior	<p>Noiseless Image</p> 	<p>Optimal Image for quadratic prior with $\alpha = 0.231$ and $RRMSE = 0.23359$</p> 
Huber Prior	<p>Noiseless Image</p> 	<p>Optimal Image for huber prior with $\alpha = 0.999$ and $\gamma = 0.01$ and $RRMSE = 0.079571$</p> 
Discontinuity adaptive function Prior	<p>Noiseless Image</p> 	<p>Optimal Image for disc_dapt_function prior with $\alpha = 0.999$ and $\gamma = 0.008$ and $RRMSE = 0.094544$</p> 

Part d

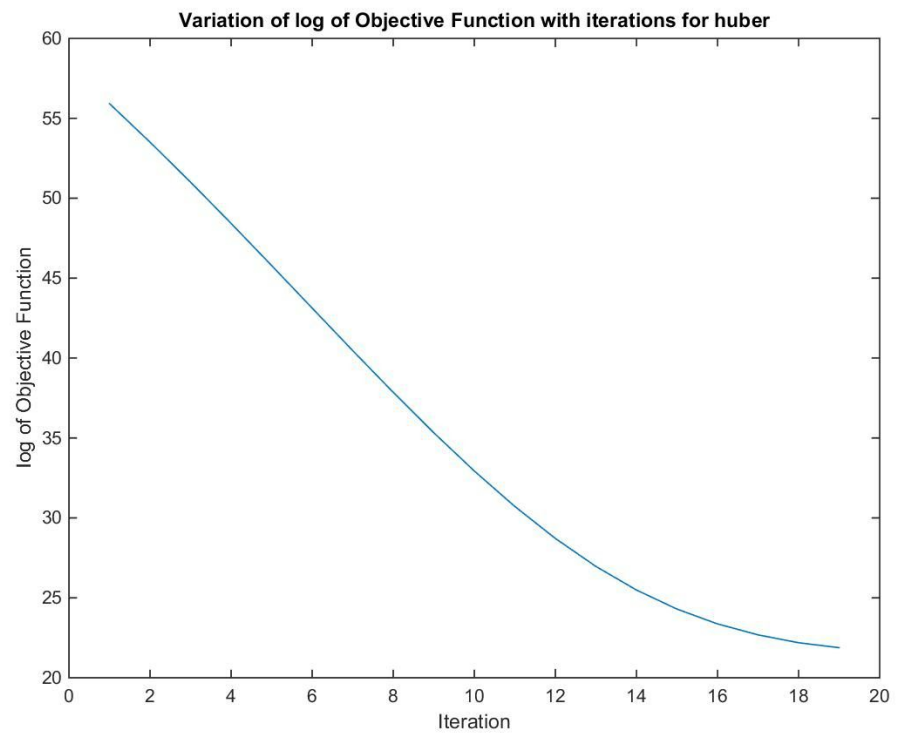
Corresponding plots of Objective Function for Different Type of Prior

Prior Type	Plot of log of Objective Function
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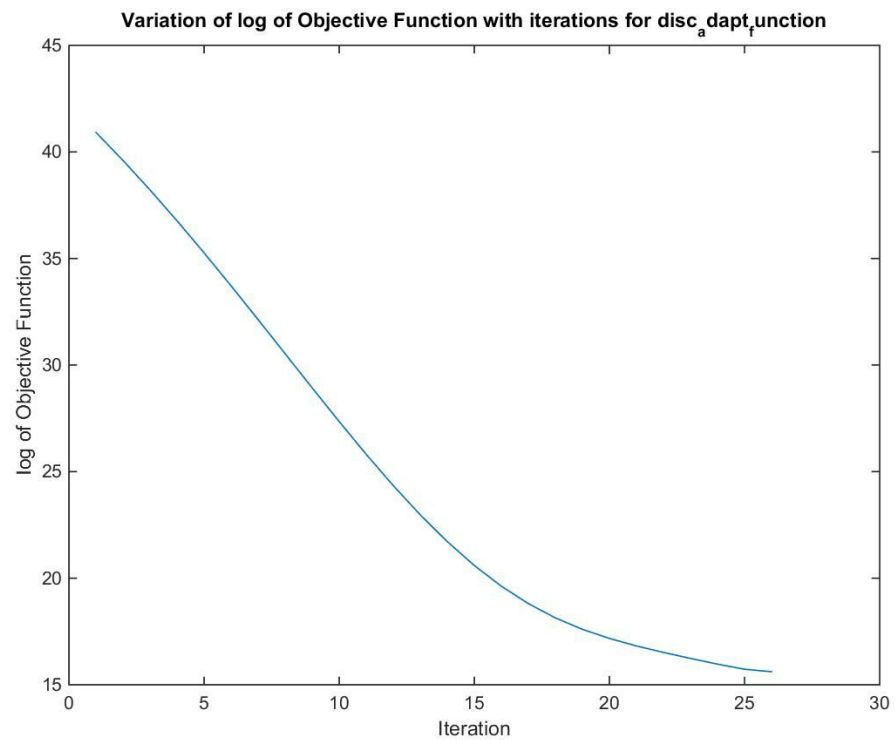
Quadratic



Huber



Discontinuity-Adaptive Huber Prior



Disclaimer

All the images and corresponding plots in high resolution can be found in 'images' folder of question 2. Sub folder are made for different priors and you can locate optimal images and objective function plot.