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| Anti-Lock braking system Name: Kalyani Patil ID: 2005001 |  |
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## Introduction

Antilock braking system (ABS) prevent brakes from locking during braking. During sever braking situation or on slippery roadways when driver presses the break to hard the wheels approach lockup, the ABS takes over here. The ABS modulate braking torque applied on wheels independent of the pedal force to bring the wheel speed back to the optimal level.

It allows driver to control the car easier, even on roads with low adhesion, such as wet, snowy, muddy roads. ABS system takes vehicle speed and wheel speed as input to find slip ratio and with the help of controller it modulates braking torque to prevent wheel from lockup.

## Mathematical Model

### Vehicle Model

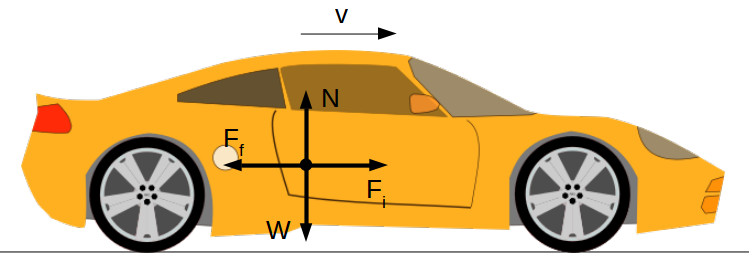


Figure 1: Various forces acting on vehicle during braking.

For horizontal direction:

Ff = Friction force between wheel and ground.

Fi = Inertia of vehicle.

For vertical direction:

N = Normal force.

W = Vehicle weight.

Friction force is given as:

The vehicle’s weight is:

Therefore,

m = Total vehicle mass.

g = Gravitational acceleration.

Inertial force on vehicle is:

### Wheel Model

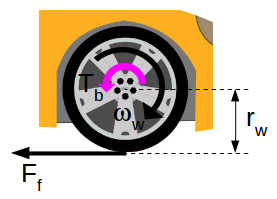


Figure 2: Forces acting on wheel.

During braking when driver applies braking torque (Tb) to the wheels. The friction force Ff applies an opposite torque on wheel.

Wheel acceleration can be given by:

Wheel speed can be obtained by integrating above equation.

### Wheel Slip

Wheel slip(s) is given by:

This function is implemented by MATLAB function block.

Wv is equivalent angular speed of car, and it is given by:

### Friction Coefficient

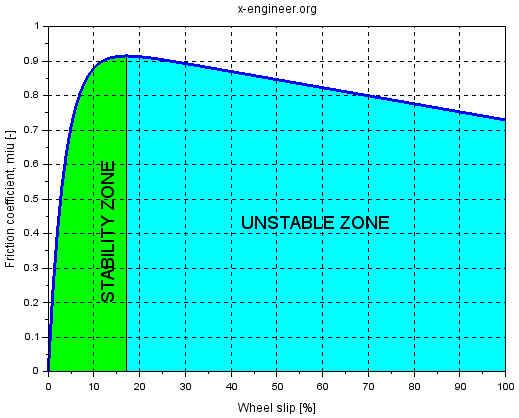


Figure 3: Friction coefficient stability zone.

Above graph shows the relation between friction coefficient and wheel slip (s). We can observe that at around 20% slip ratio friction coefficient is maximum. Hence, ABS system will try to keep slip ratio at 20% to avoid lockup.

The fiction coefficient can be given as:

This equation is implemented using MATLAB function block.

s = Slip

A, B, C, D = Value depends on type of road.

### Controller

We set target slip of 0.2. A slip error is calculated by subtracting actual slip from target slip. To avoid action of controller at low-speed actual slip is only used when vehicle speed is higher than minimum speed (Vmin).

Depending on the error controller will output:

* 1, if s>0
* 0, if s==0
* -1, if s<0

The hydraulic system is modeled using first order transfer function, with the amplification factor K and time constant T.

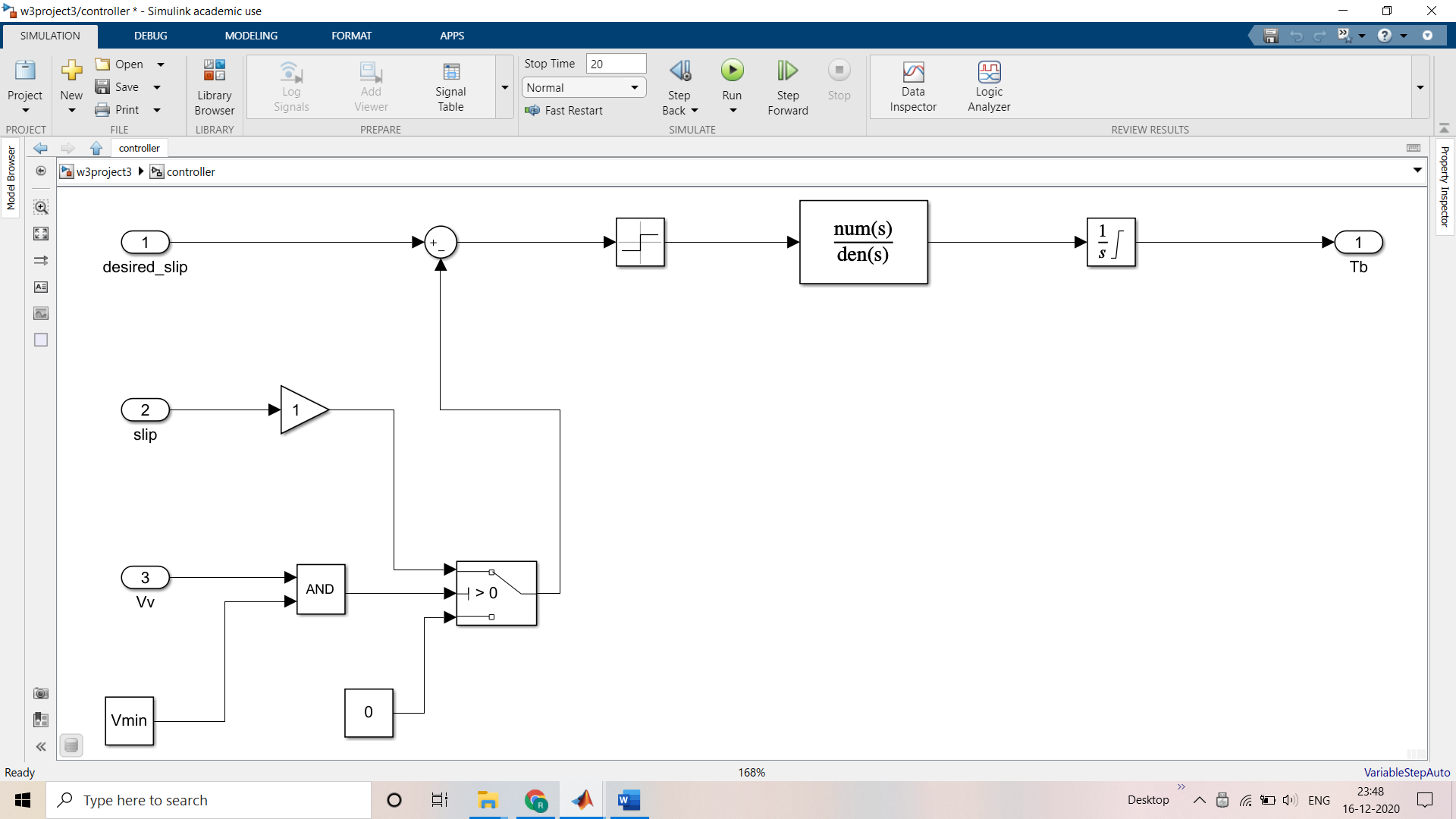


Figure 4: Controller design in Simulink.