

# Lab3

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Submission deadline: August 16, 2023

## Question 1

I have assumed  $g(x)$  to be the uniform distribution in  $(0,1)$

**a)**

Since the process of generating a random variable distribution follows Geometric distribution (we have to get a random variable that satisfies the given condition  $u \geq \frac{f(X)}{cg(X)}$ ) and the probability of satisfying this condition is  $\frac{1}{c}$ , the average number of iterations is  $c$ .

**b)**

Sample mean = 0.33331

$$\begin{aligned} E(X) &= \int_0^1 20x^2(1-x)^3 dx \quad (\text{substituting } x = \sin^2 \theta) \\ &= \frac{1}{3} \end{aligned}$$

**c)**

$$\begin{aligned} \text{Exact value} &= \int_{\frac{1}{4}}^{\frac{3}{4}} 20x^2(1-x)^3 dx \\ &= \frac{79}{128} \\ &= 0.61718 \end{aligned}$$

Value Calculated from sample = 0.6118

d)

Average number of iterations required from theory= $c=\frac{136}{64}=2.125$

Average number of iterations required for the sample=2.1397

e)

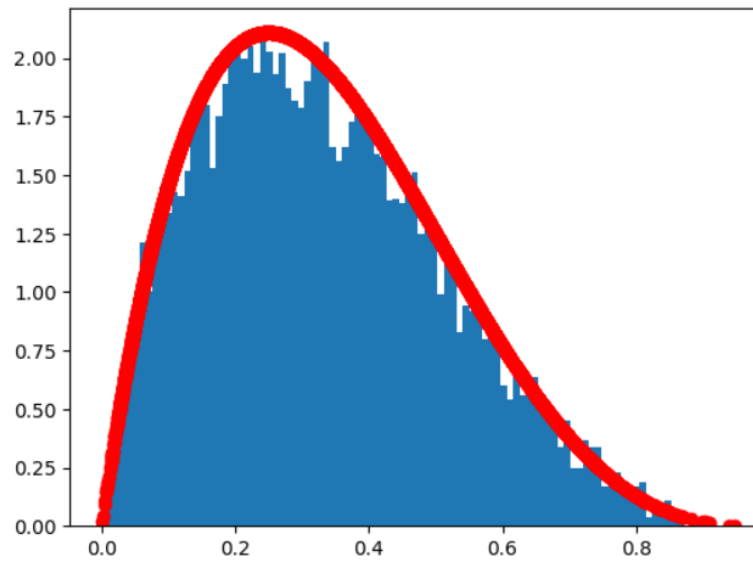


Figure 1: scatter plot vs histogram

f)

average number of iterations required has increased

for  $c_1=3$  it is 2.953

for  $c_2=5$  it is 5.035

## Question 2

I assumed dominating PDF to be the uniform distribution in  $(0,1)$  and  $\alpha=4$

$$f(x)=kx^{\alpha-1}e^{-x}$$

We have to find  $k$  such that

$$\int_0^1 f(x)dx = 1$$

On solving,

$$k = \frac{e}{6e-16}$$

As  $f(x)$  is an increasing function in  $(0,1)$ ,

$$\text{maximum value of } f(x) = \frac{1}{6e-16}$$

and therefore the rejection constant  $= \frac{1}{6e-16} = 3.229$

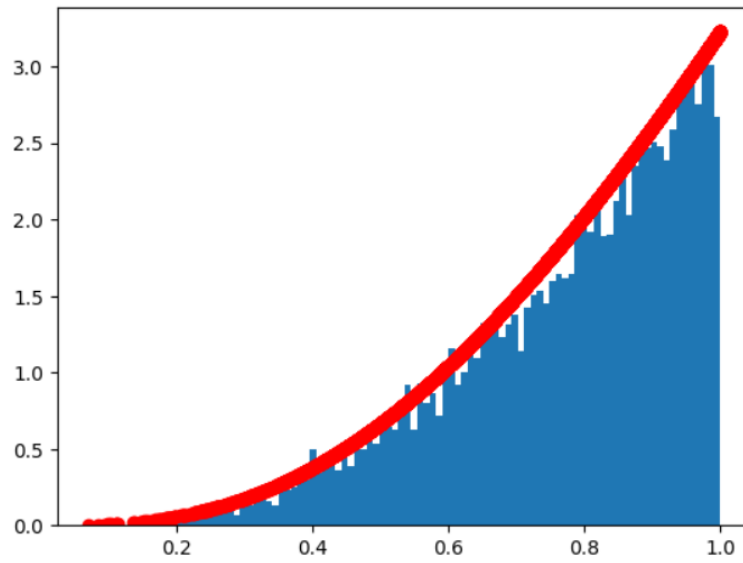


Figure 2: scatter plot vs histogram