

1)

q	lower rectangle rule
a	0.03125
b	-0.25
c	-0.4
d	0
e	0.2432

2)

q	mid point rule	trapezoid rule	simpsons 1/3rd rule
a	0.1582	0.26562	0.19401
b	-0.26667	-0.26786	-0.26706
c	-0.67532	-0.86667	-0.73911
d	1.8039	4.1433	2.5837
e	-0.011895	-0.037024	-0.020272

3)

lower rectangle rule	trapezoid rule	simpsons 1/3rd rule	simpsons 3/8th rule
4	3	3.13333333333333	3.13846153846154

4)ans=7.125

5)

$$f(x) = x \ln(x)$$

$$f'(x) = 1 + \ln(x)$$

$$f''(x) = 1/x$$

$$f'''(x) = -1/x^2$$

$$f''''(x) = 2/x^4$$

$$\max_{1 \leq x \leq 2} f''(x) = 1$$

$$\max_{1 \leq x \leq 2} f''''(x) = 2$$

Here  $m = 10^{-5}$   
 $(\text{actual} - \text{calculated}) / \text{actual} \leq \pm m$   
 $(\text{actual} - \text{calculated}) / \text{calculated} \leq (1 / (1 \pm m) - 1)$   
 $\text{actual} - \text{calculated} = \text{error}$

a) Composite Trapezoidal rule:  
 $\text{error} = (-h^2(b-a)/12)f''(c_n) \leq (-h^2/12)$   
 $n = 115$   
 $h = 0.0086$   
 $\text{area} = 0.636298728771027$

b) Composite Simpson's rule:

$$\text{error} = (-h^4(b-a)/180)f''(c_n) \leq (-h^4/90)$$

$$n=7$$

$$h=0.1428$$

$$\text{area}=0.636294469092996$$

c) Composite Midpoint rule:

$$\text{error} = (-h^2(b-a)/24)f''(c_n) \leq (-h^2/24)$$

$$n=81$$

$$h=0.0123$$

$$\text{area}=0.636289959200426$$

6) length of the track in feet is (using composite trapezoid rule): 9855