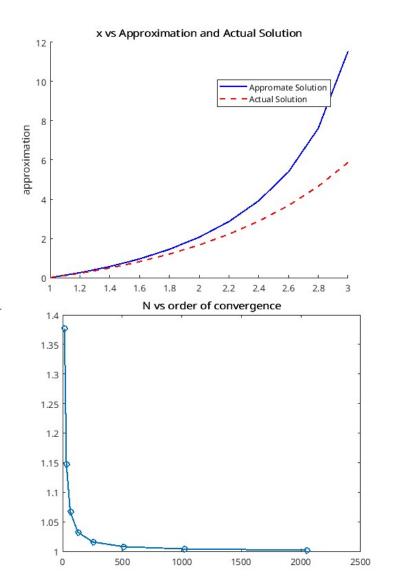
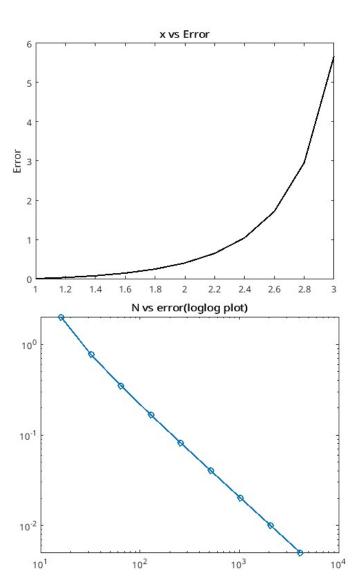
Q1)

(a)

Implicit Euler:

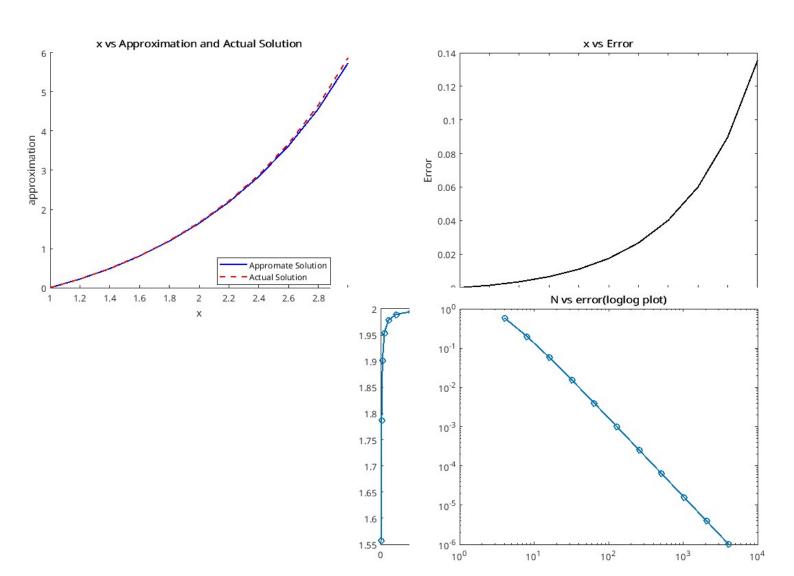
Implicit Euler Method:				
t	approximation	actual	error	
—				
1	0	Θ	0	
1.2	0.250454583026496	0.221242772757631	0.0292118102688649	
1.4	0.563305747476104	0.489681663750943	0.0736240837251615	
1.6	0.95352968025127	0.812752740561542	0.140776939689727	
1.8	1.4421515146776	1.19943864032594	0.242712874351662	
2	2.06047770329629	1.66128175572157	0.39919594757472	
2.2	2.85773744096705	2.21350181348063	0.644235627486413	
2.4	3.91683450001299	2.87655141999484	1.04028308001815	
2.6	5.39162138733281	3.67847533085185	1.71314605648097	
2.8	7.61470635189775	4.65866505823951	2.95604129365824	
3	11.5481105505512	5.87409997818417	5.67401057236705	





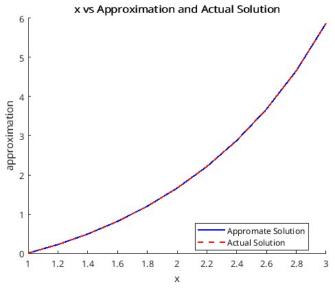
Runge Kutta 2nd Order

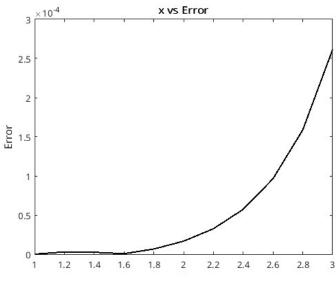
Runge Kutta Method 2 order:					
t	approximation	actual	error		
1	0	0	0		
1.2	0.219834710743802	0.221242772757631	0.00140806201382948		
1.4	0.486177046768206	0.489681663750943	0.00350461698273657		
1.6	0.806184891605961	0.812752740561542	0.00656784895558093		
1.8	1.18843925837304	1.19943864032594	0.0109993819529002		
2	1.64388892124877	1.66128175572157	0.0173928344727998		
2.2	2.18686089286093	2.21350181348063	0.0266409206197		
2.4	2.83643571306701	2.87655141999484	0.0401157069278355		
2.6	3.61849255493937	3.67847533085185	0.0599827759124798		
2.8	4.56889438371891	4.65866505823951	0.0897706745206071		
3	5.73864746521413	5.87409997818417	0.135452512970037		

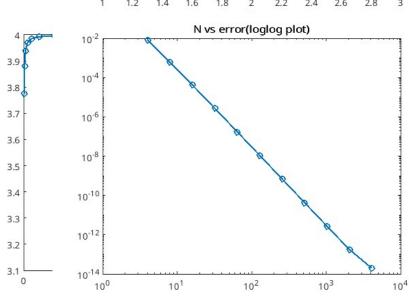


Runge Kutta 4th order

Runge Kutta Method 4 order:				
t	approximation	actual	error	
_				
1	Θ	Θ	9	
1.2	0.221245707288813	0.221242772757631	2.9345311814144e-06	
1.4	0.489684166443365	0.489681663750943	2.50269242257906e-06	
1.6	0.81275216202401	0.812752740561542	5.7853753210324e-07	
1.8	1.19943202163924	1.19943864032594	6.61868670004395e-06	
2	1.66126511544869	1.66128175572157	1.66402728811743e-05	
2.2	2.21346931657636	2.21350181348063	3.24969042724277e-05	
2.4	2.87649411454154	2.87655141999484	5.73054533026252e-05	
2.6	3.67837899609925	3.67847533085185	9.63347525999581e-05	
2.8	4.65850628368228	4.65866505823951	0.000158774557231567	
3	5.87383856983279	5.87409997818417	0.000261408351379444	

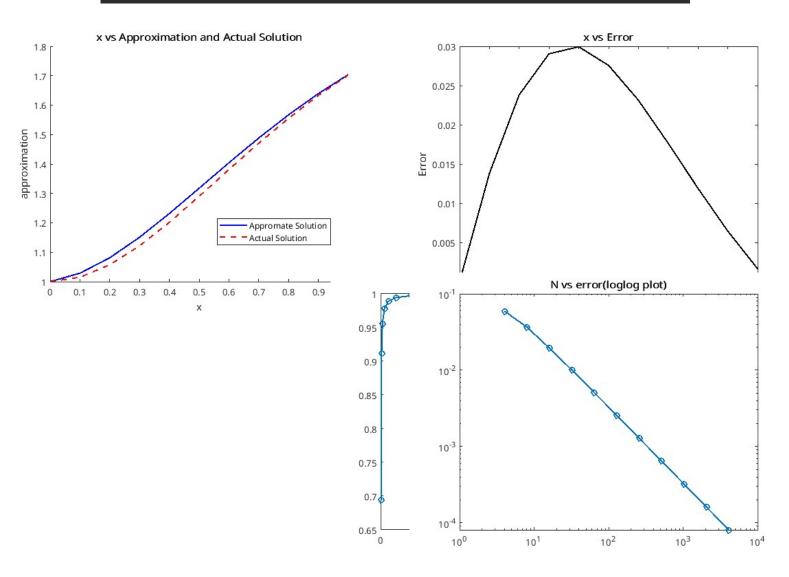






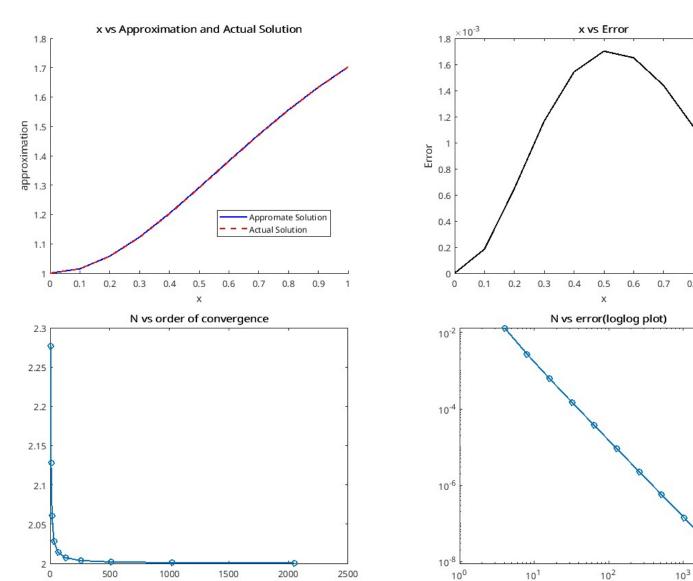
(b)Implicit Euler:

Implicit Euler Method:				
t	approximation	actual	error	
—				
Θ	1	1	Θ	
0.1	1.02860172615079	1.01481549985822	0.0137862262925679	
0.2	1.08098831062131	1.0571810074642	0.0238073031571016	
0.3	1.15074609870334	1.12169801826798	0.0290480804353561	
0.4	1.2314205216256	1.2014860103644	0.0299345112611962	
0.5	1.31736970673967	1.28980527630561	0.0275644304340572	
0.6	1.40405913082249	1.38093121544373	0.0231279153787602	
0.7	1.48805948728035	1.47041518539722	0.0176443018831272	
0.8	1.5669267611553	1.55503142343518	0.0118953377201196	
0.9	1.63905137779954	1.63261318178287	0.00643819601667794	
1	1.7035097441446	1.70187005276128	0.00163969138332076	



Runge Kutta 2nd Order

Runge Kutt t ——	a Method 2 order: approximation	actual	error
Θ	1	1	0
0.1	1.015	1.01481549985822	0.0001845001417764
0.2	1.05782895089288	1.0571810074642	0.000647943428678577
0.3	1.12286281792299	1.12169801826798	0.00116479965500993
0.4	1.20302831702477	1.2014860103644	0.00154230666036415
0.5	1.29150646848125	1.28980527630561	0.00170119217564579
0.6	1.38258169760259	1.38093121544373	0.00165048215885255
0.7	1.4718540869499	1.47041518539722	0.00143890155267368
0.8	1.55615483380428	1.55503142343518	0.00112341036909891
0.9	1.63336880578335	1.63261318178287	0.000755624000484012
1	1.70224778342493	1.70187005276128	0.000377730663653653



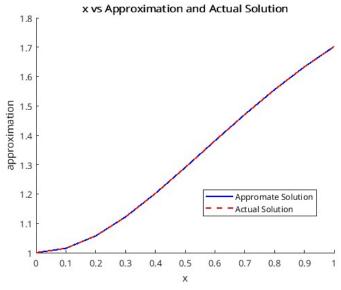
0.8

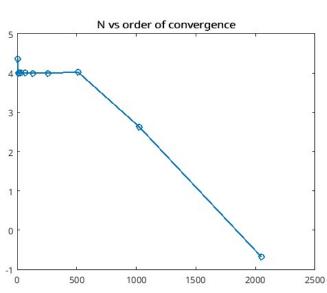
0.9

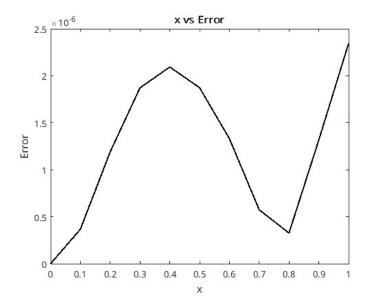
10⁴

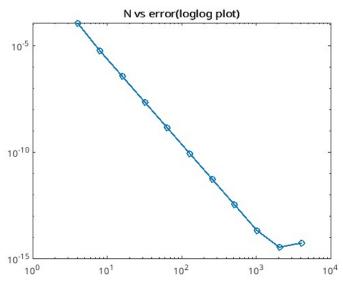
Runge Kutta 4th Order

Runge Kutta Method 4 order:				
t	approximation	actual	error	
_				
Θ	1	1	0	
0.1	1.01481586700284	1.01481549985822	3.67144615154302e-07	
0.2	1.05718219810417	1.0571810074642	1.19063996151247e-06	
0.3	1.12169988971777	1.12169801826798	1.87144978847087e-06	
0.4	1.20148810362448	1.2014860103644	2.09326007616362e-06	
0.5	1.28980714875618	1.28980527630561	1.87245057259311e-06	
0.6	1.38093254642537	1.38093121544373	1.33098163468404e-06	
0.7	1.47041575933439	1.47041518539722	5.73937165126992e-07	
0.8	1.55503109713822	1.55503142343518	3.26296961894457e-07	
0.9	1.63261186640638	1.63261318178287	1.31537648861979e-06	
1	1.70186770854212	1.70187005276128	2.3442191539047e-06	









Runge Kut t ——	ta Method 4 order: approximation	actual 	error
Θ	1	1	Θ
0.1	1.11422259959182	1.11422250235566	9.7236156237912e-08
0.2	1.25293090533928	1.2529306328511	2.72488182906372e-07
0.3	1.40845175999911	1.40845124727396	5.12725151002869e-07
0.4	1.57122625952187	1.5712254606242	7.98897670017951e-07
0.5	1.73049086605814	1.73048975851471	1.10754342430575e-06
0.6	1.87508832068056	1.87508690788131	1.41279924692483e-06
0.7	1.99434192183752	1.99434023319418	1.68864333693897e-06
0.8	2.07891995120454	2.0789180400345	1.91117004311181e-06
0.9	2.12161659014078	2.12161452944478	2.06069599562042e-06
1	2.11798166912361	2.11797954561299	2.12351061801286e-06

