

1. $f(0.25)=1.189069$
absolute error=1.060930

2.

a)

at $t=10$:

position(in feet)=7.425028

speed(in feet per second)=48.381736

b) at $t=5.6488025$ s, it crosses the speed limit for first time(found roots of $f(x)-55\text{miles/hr}=0$)

c) max speed of the car: 119.4173(found $f'(x)$ values for all x such that $f''(x)=0$)

3.

a) $f(0.43)\sim 2.4777, f'(0.43)\sim 3.4366$

b) $f(0.25)\sim 1.1965, f'(0.25)\sim 0.3915$

4.

The spline polynomials have the coefficients(in the order $x^3, x^2, x, 1$):

[12.373172074666664, 27.795675786666663, 18.627197749333334, 4.066688837333333]

[-12.496177903999998, -9.508349181333331, -0.024814734666666, 0.958020090000000]

[13.313368901333329, -9.508349181333331, -0.024814734666667, 0.958020090000000]

5.

a)

Using natural spline:

at $t=10$ s:

position(in feet): 772.7556477639466

speed(in feet per second): 70.998616874135564

b)

Using clamped spline:

at $t=10$ s:

position(in feet): 772.7812192723696

speed(in feet per second): 71.074483775811188