



NPTEL ONLINE CERTIFICATION COURSES

CONTROL AND TUNING METHODS IN SMPCs

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Electrical Engineering Department, IIT KHARAGPUR

Module 03: Fixed Frequency Control Methods

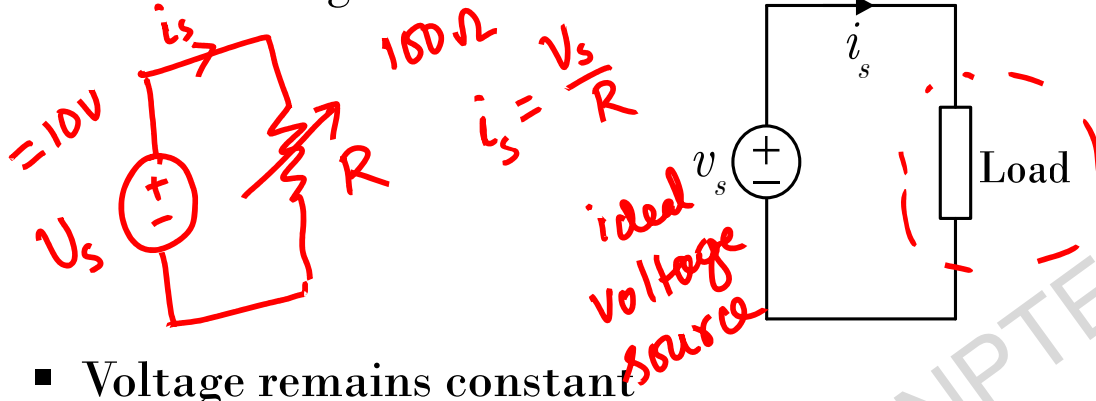
Lecture 13: Converter's Objectives and Control Implications using MATLAB Models

Concepts Covered

- Understanding behavior of a practical source while driving a SMPC
- Scalable MATLAB model development with a practical source
- Understanding converter objectives and control implications
- Power-stage design guidelines and few power designer tools
- MATLAB case studies to understand control requirements

Understanding a Voltage Source

- Ideal voltage source

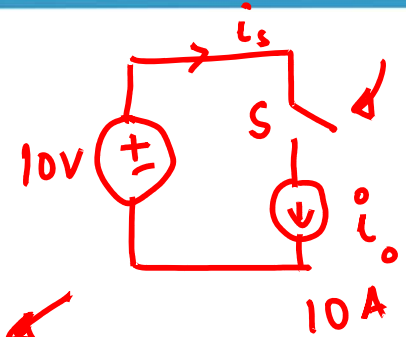
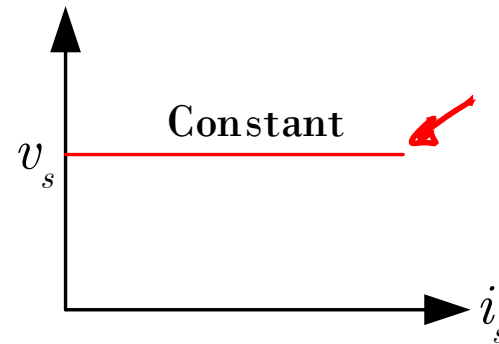


- Voltage remains constant

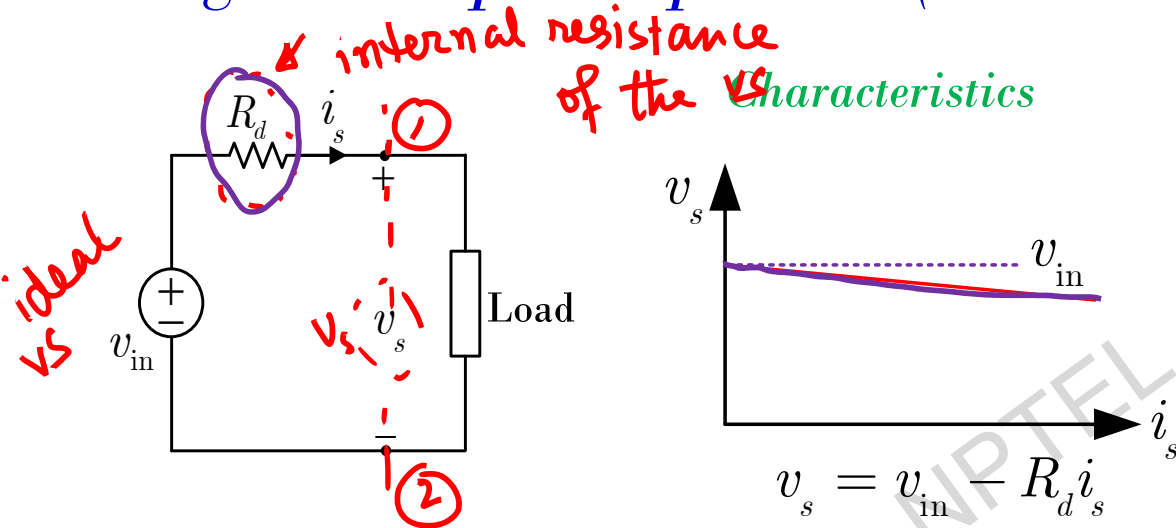
- Irrespective of current magnitude ➤ Relates to DC output impedance
- Irrespective of current profile ➤ Relates to AC output impedance

Ideal voltage source: Zero output impedance, infinite bandwidth!!

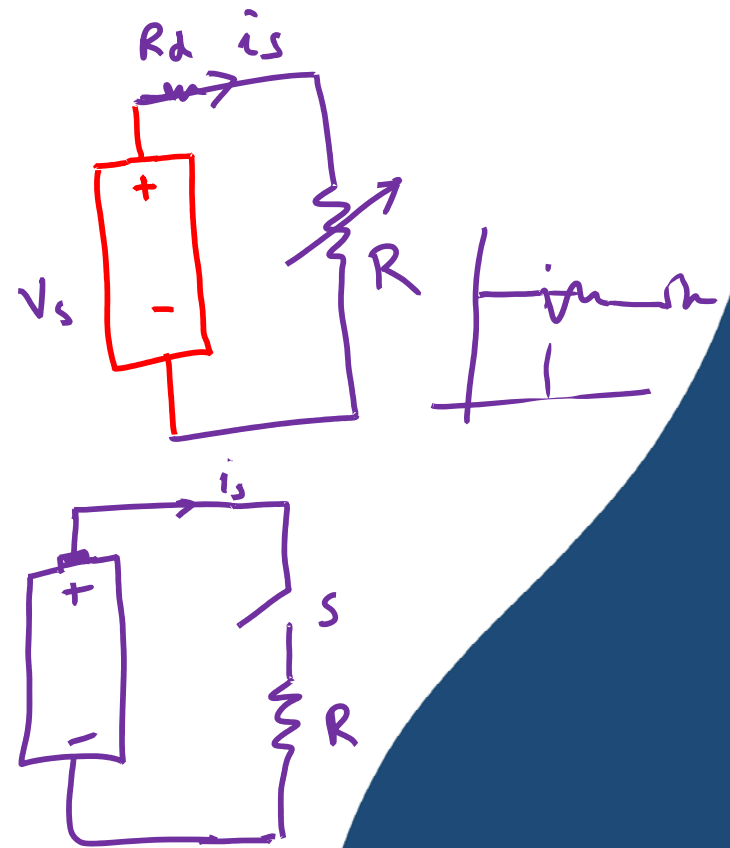
Characteristics



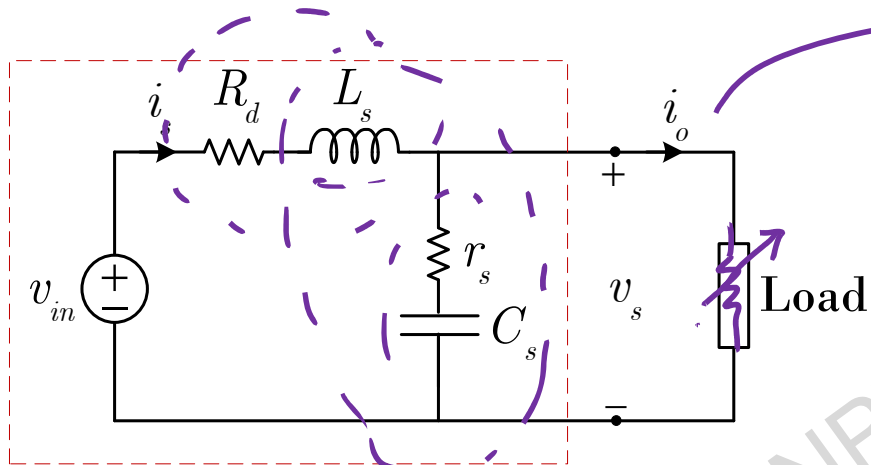
Adding DC Output Impedance (resistance)



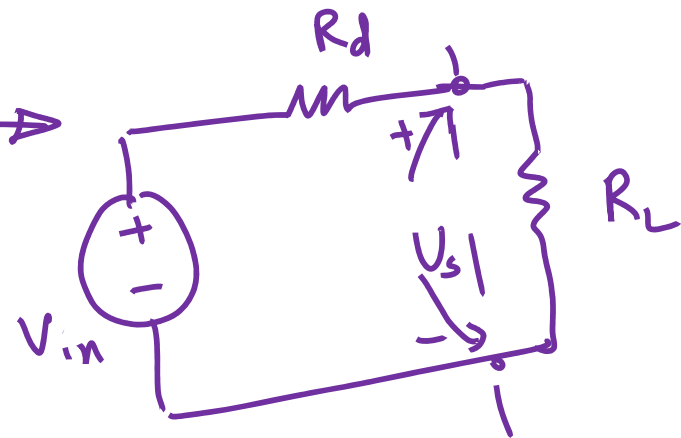
- This captures load regulation aspects.
- But, it does not capture transient effects.
- This model still assumes infinite bandwidth!!!



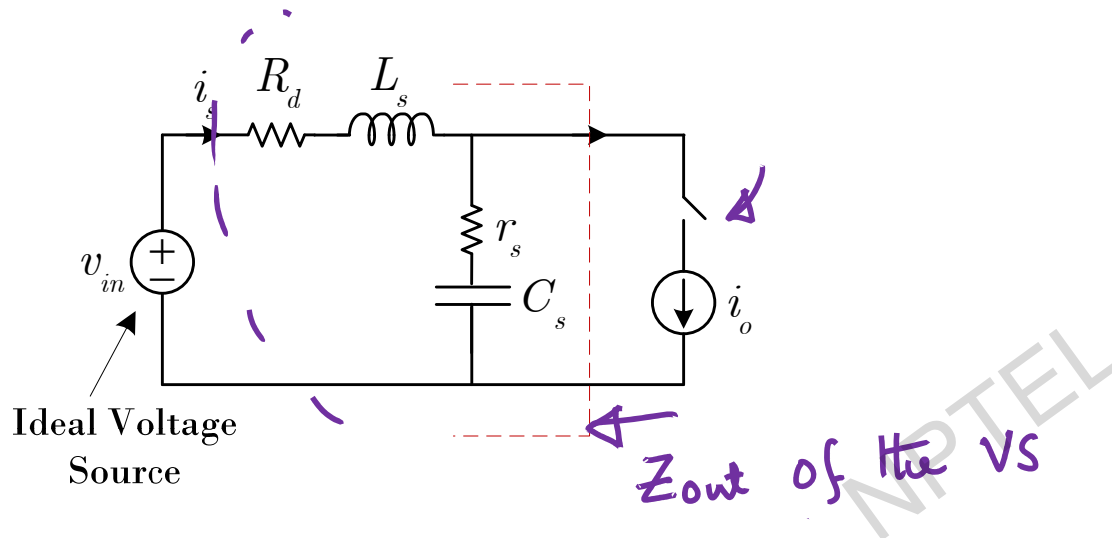
Adding Frequency Dependent Terms



Practical Voltage Source

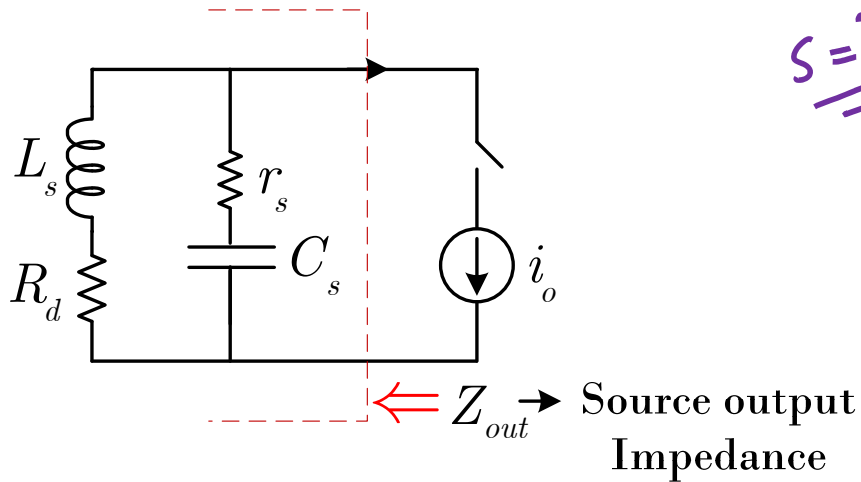


AC Small-Signal Modeling Output Impedance of Voltage Source



- For AC model, consider perturbations and replace DC quantities by zero
 - ideal voltage source: short circuited
 - ideal current source: open circuited

AC Small-Signal Modeling Output Impedance of Voltage Source



$$s = j\omega$$

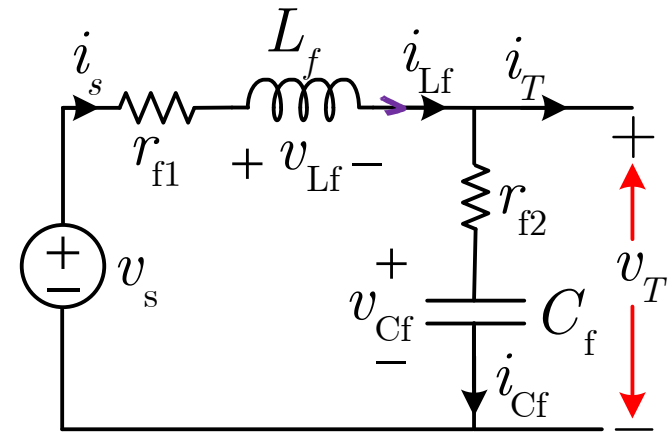
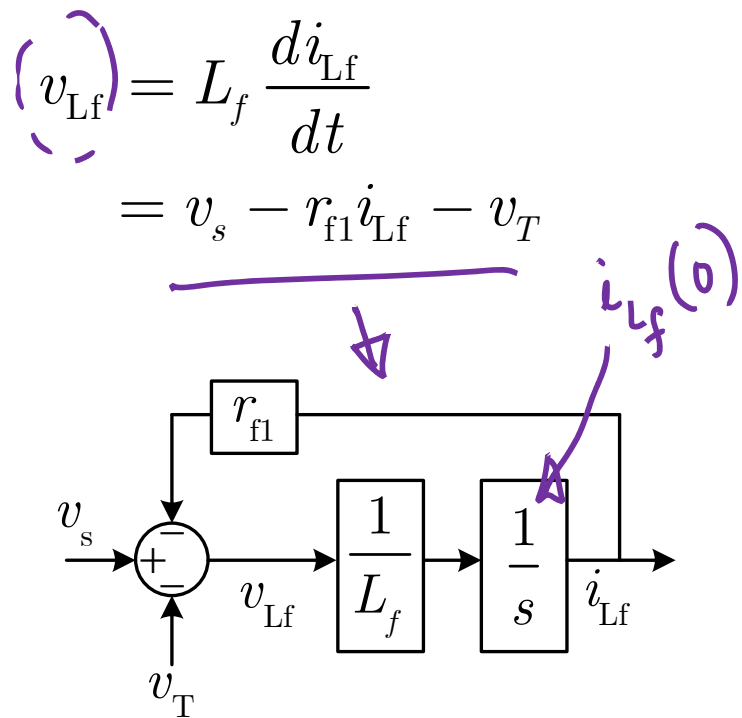
$$Z_{out}(0)$$

$$Z_{out}(s) = R_d \times \frac{\left(1 + \frac{s}{\omega_{zc}}\right) \left(1 + \frac{s}{\omega_{zl}}\right)}{1 + \frac{s}{Q_s \omega_s} + \frac{s^2}{\omega_s^2}}$$

$$\omega_{zc} = \frac{1}{r_s C_s}, \quad \omega_{zl} = \frac{R_d}{L_s}$$

$$\omega_n = \sqrt{\frac{R_d}{r_s}} \times \frac{1}{\sqrt{L_s C_s}}, \quad Q_s = \frac{Z_{cs}}{(R_d + r_s)}, \quad Z_{cs} = \sqrt{\frac{L_s}{C_s}}$$

MATLAB Model Development of a Practical Voltage Source

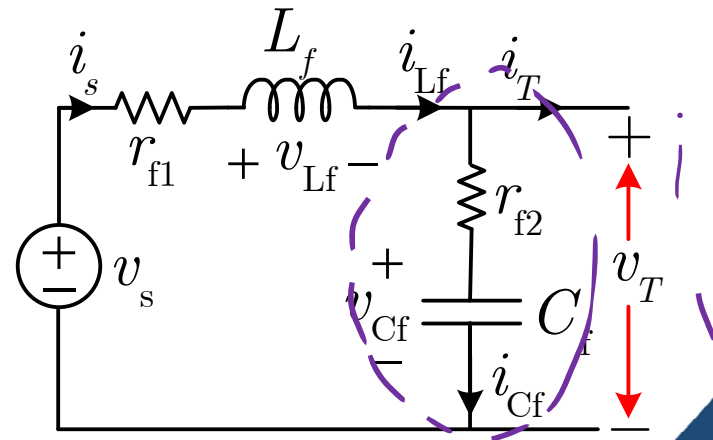
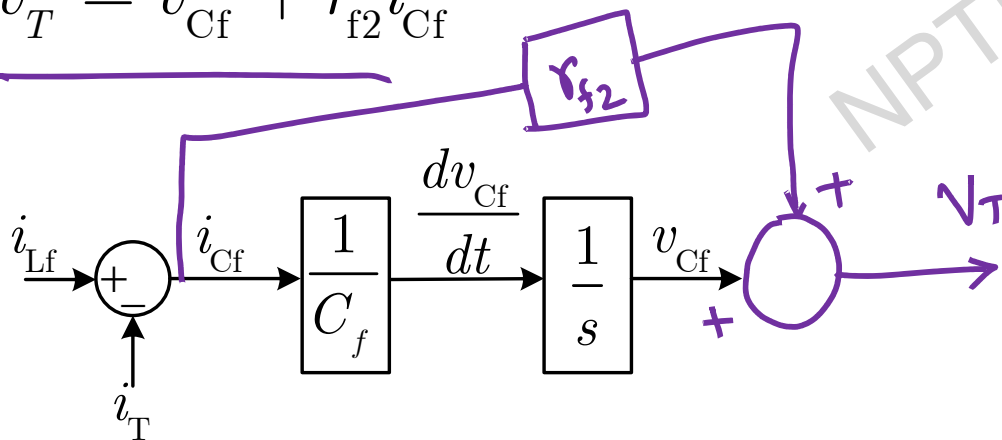


NPTEL

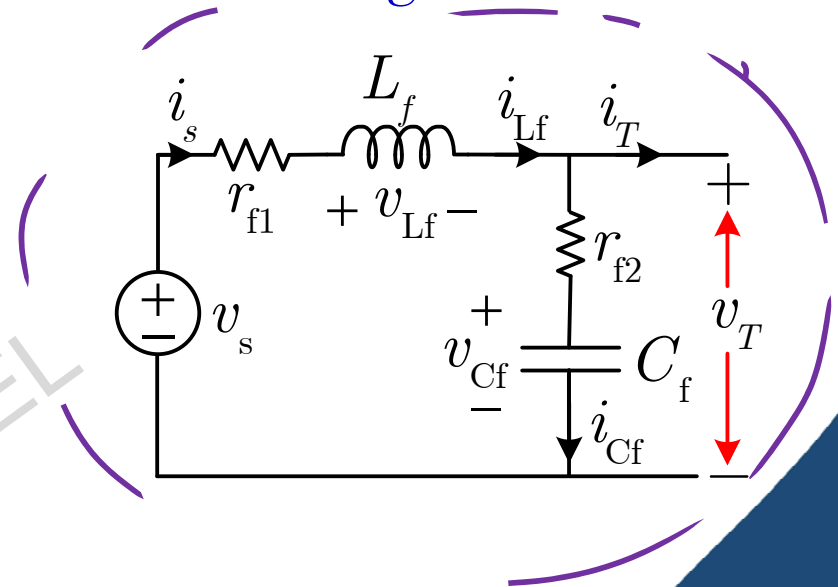
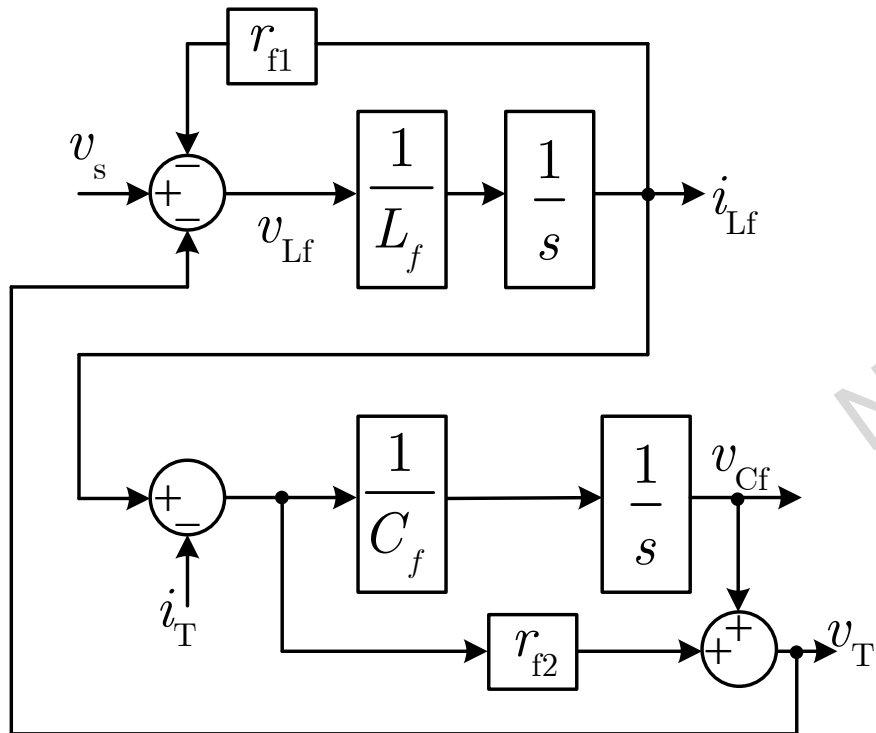
MATLAB Model Development of a Practical Voltage Source

$$\underline{C_f \frac{dv_{Cf}}{dt} = i_{Cf} = i_{Lf} - i_T}$$

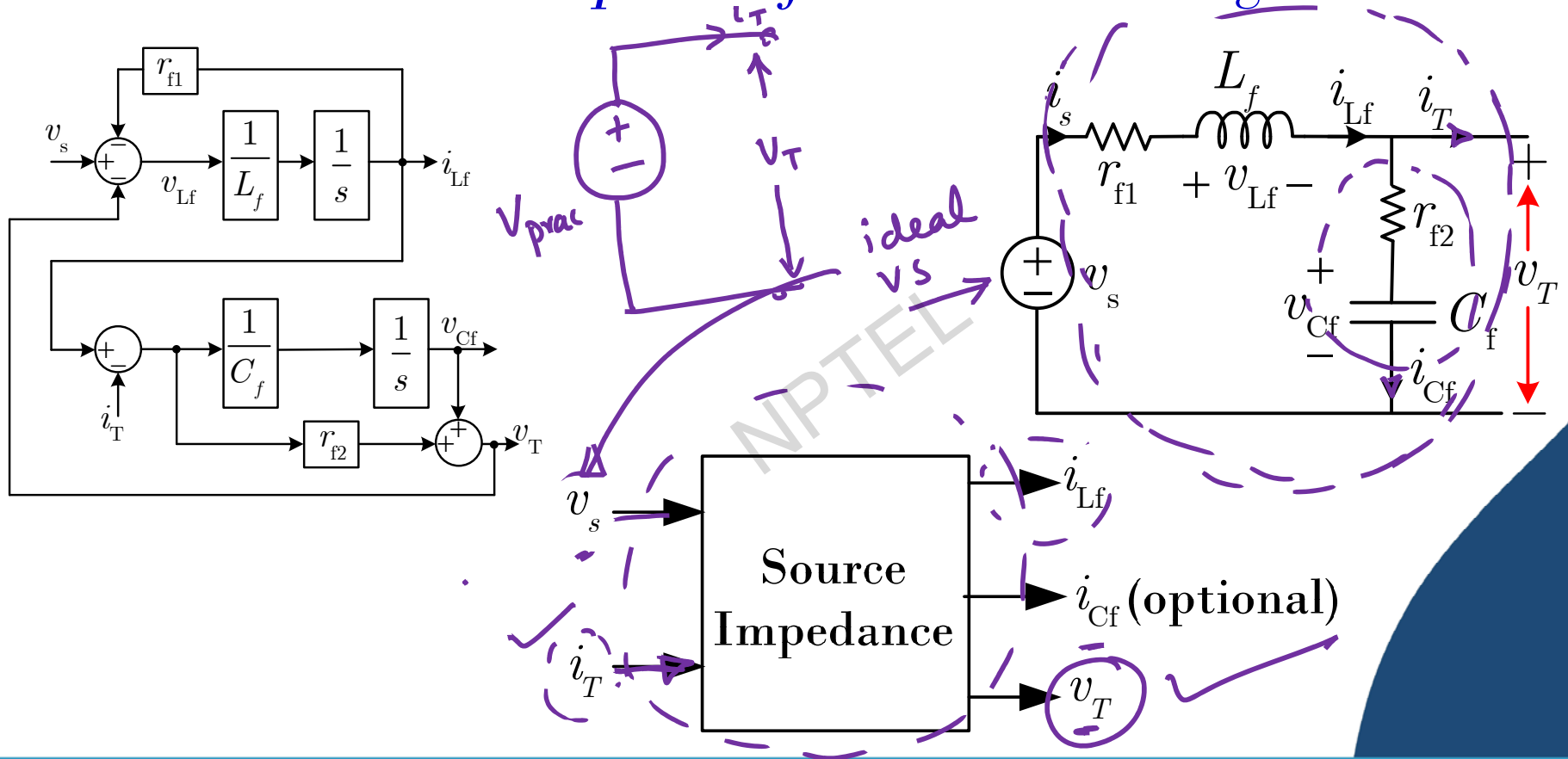
$$\underline{v_T = v_{Cf} + r_{f2} i_{Cf}}$$



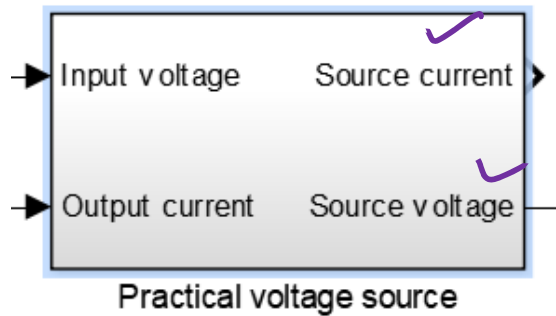
MATLAB Model Development of a Practical Voltage Source



MATLAB Model Development of a Practical Voltage Source

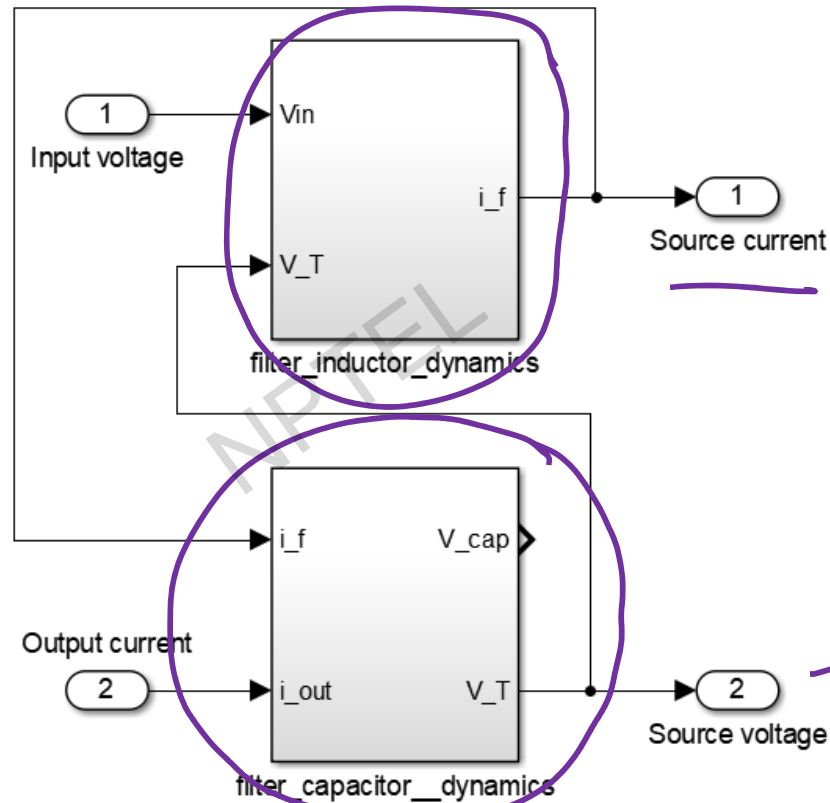


Practical Voltage Source Parameters for Simulation

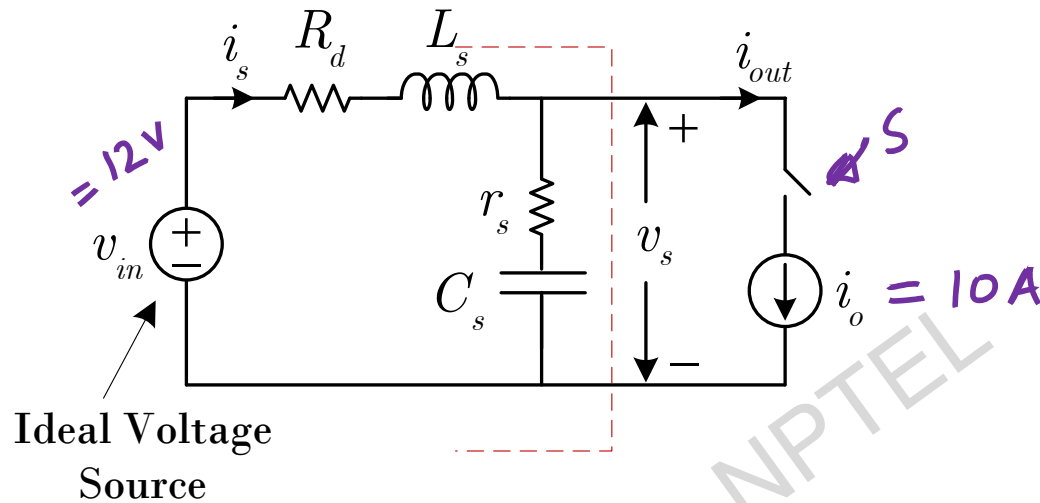


$L_f = 0.02 \text{e-}6;$
 $C_f = 100 \text{e-}6;$
 $r_{f1} = 2 \text{e-}3;$
 $r_{f2} = 2 \text{e-}3;$

20 nH

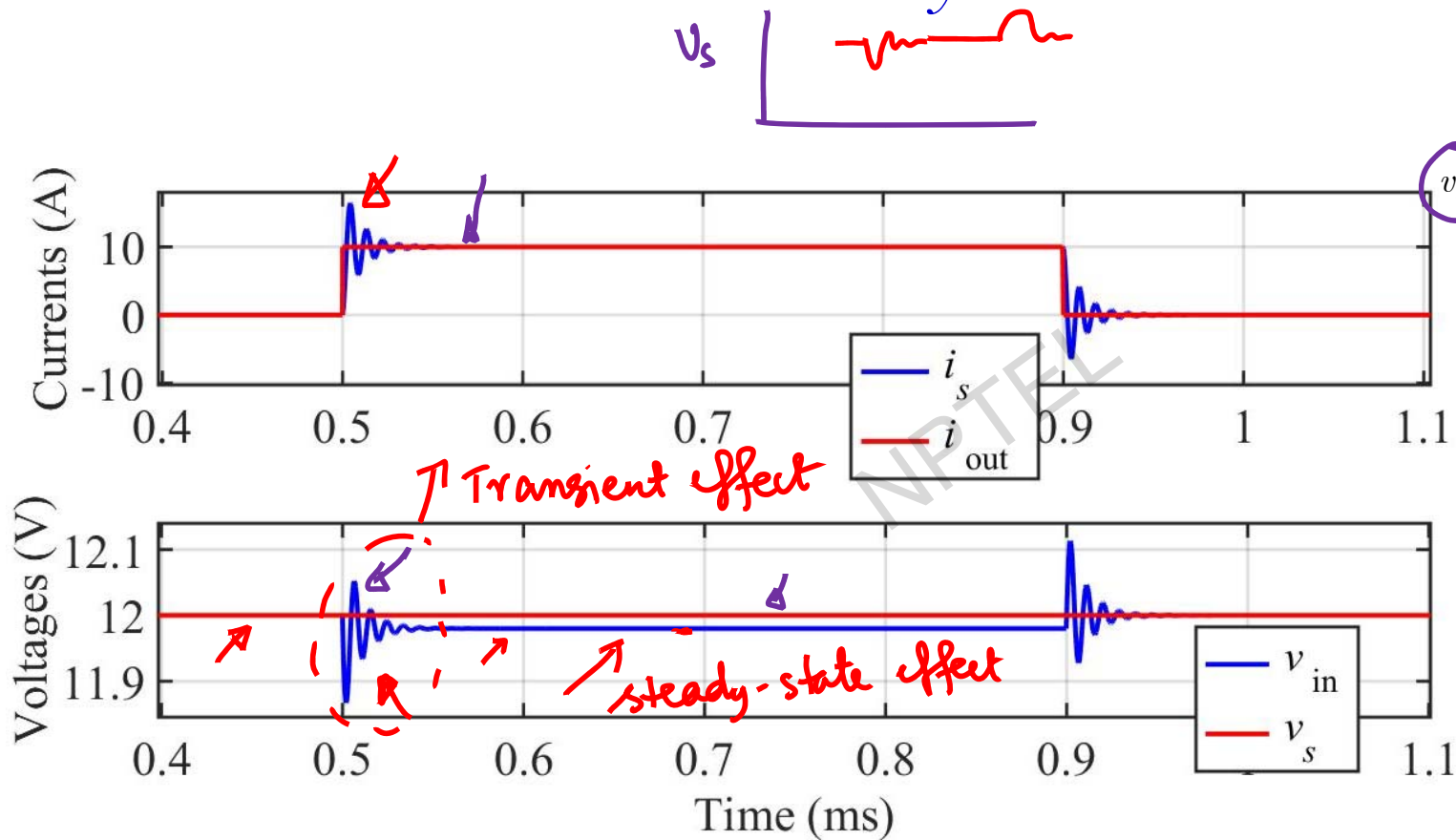


MATLAB Simulation Case Study – Practical Voltage Source



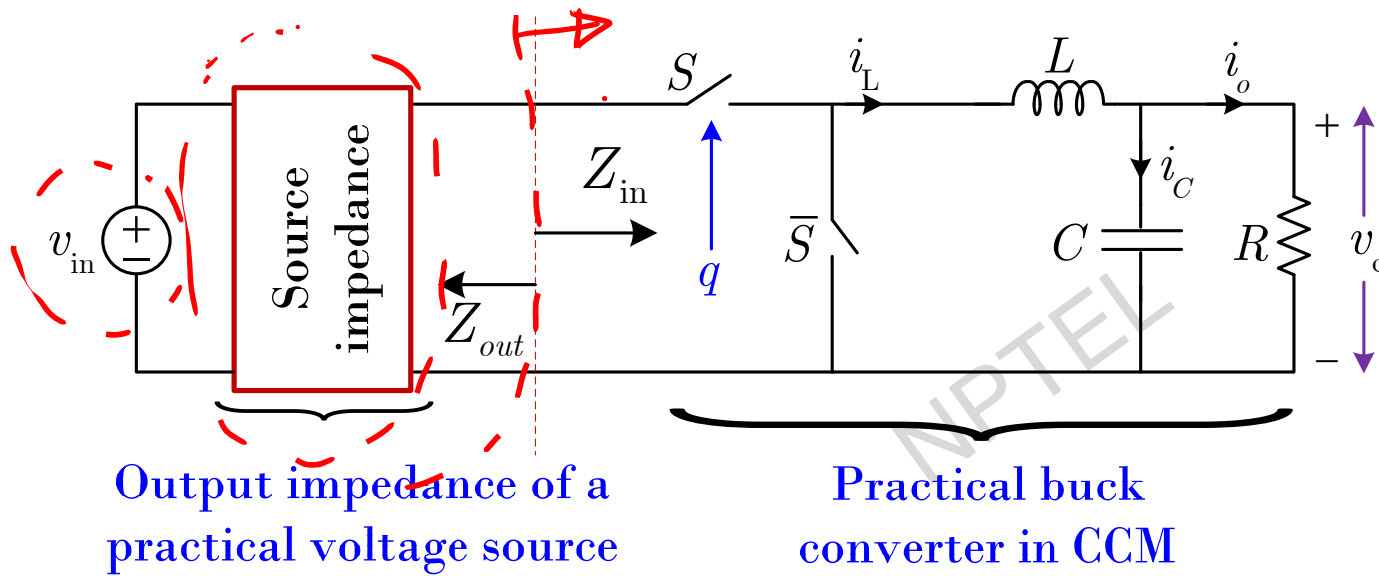
- Consider a pulsating load current profile
- Apply periodic load step-up and step-down

MATLAB Simulation Case Study – a Practical Voltage Source

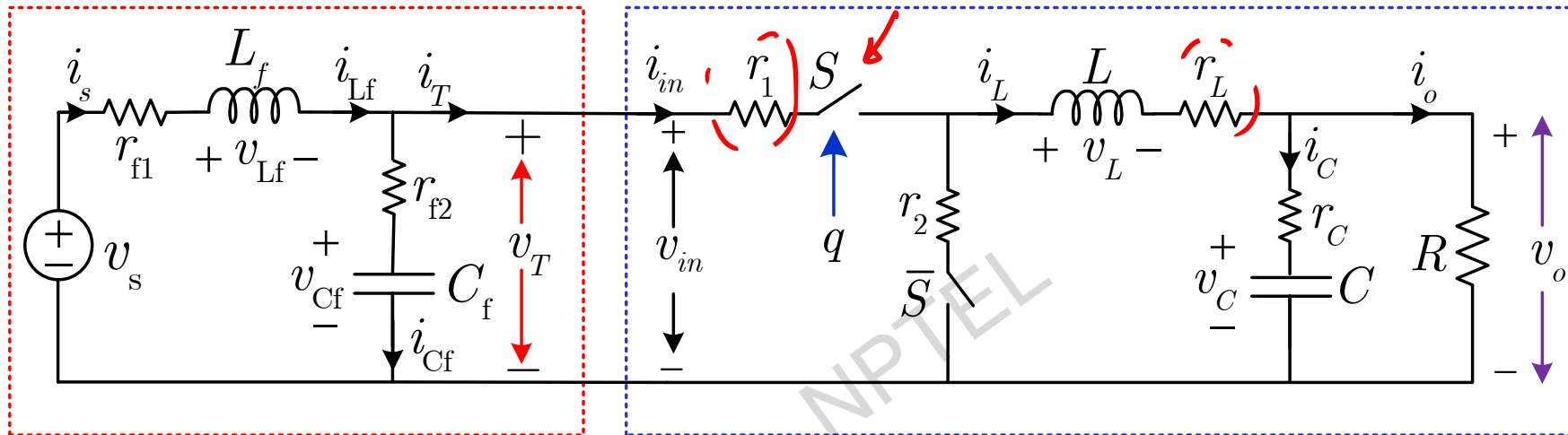


constant current load

Practical Source Driving a Buck Converter

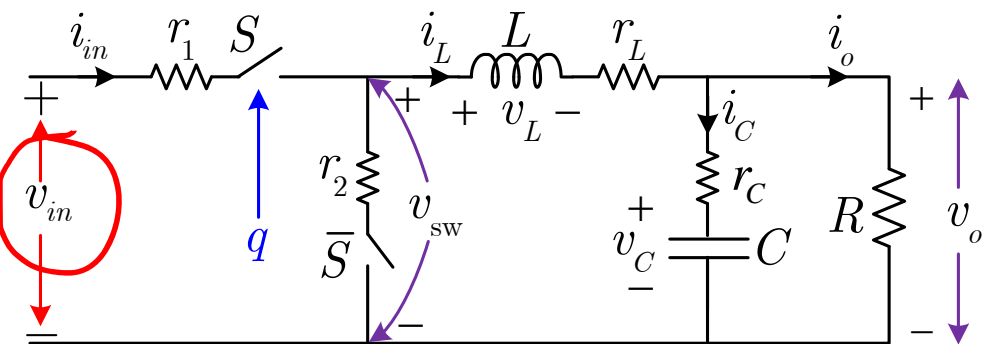


Practical Voltage Source Driving Practical Synchronous Buck Converter



Practical voltage source

Practical Synchronous Buck Converter



Synchronous buck converter

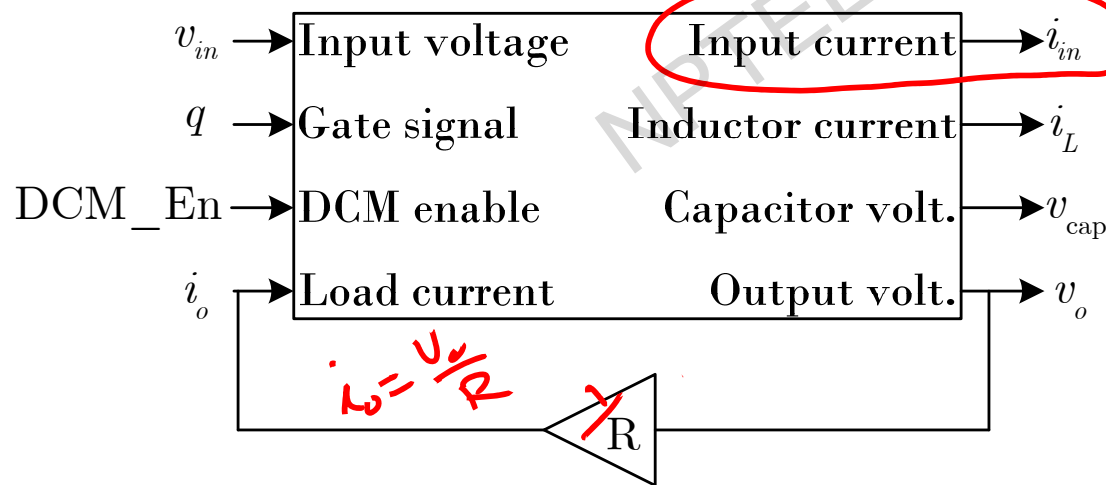
$$q = 1$$

$$q = 0$$

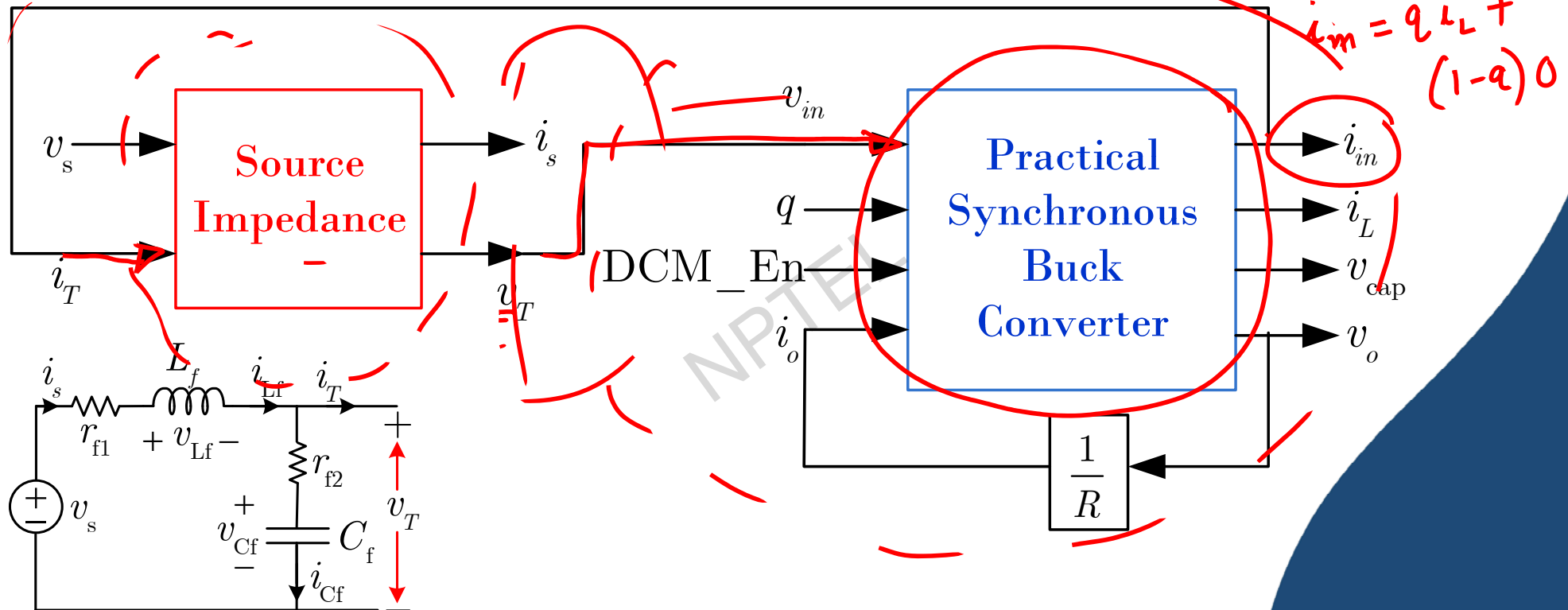
Input voltage v_{in} – source dependent

$$i_{in} = q \times (i_L) + (1 - q) \times 0 = q \times i_L$$

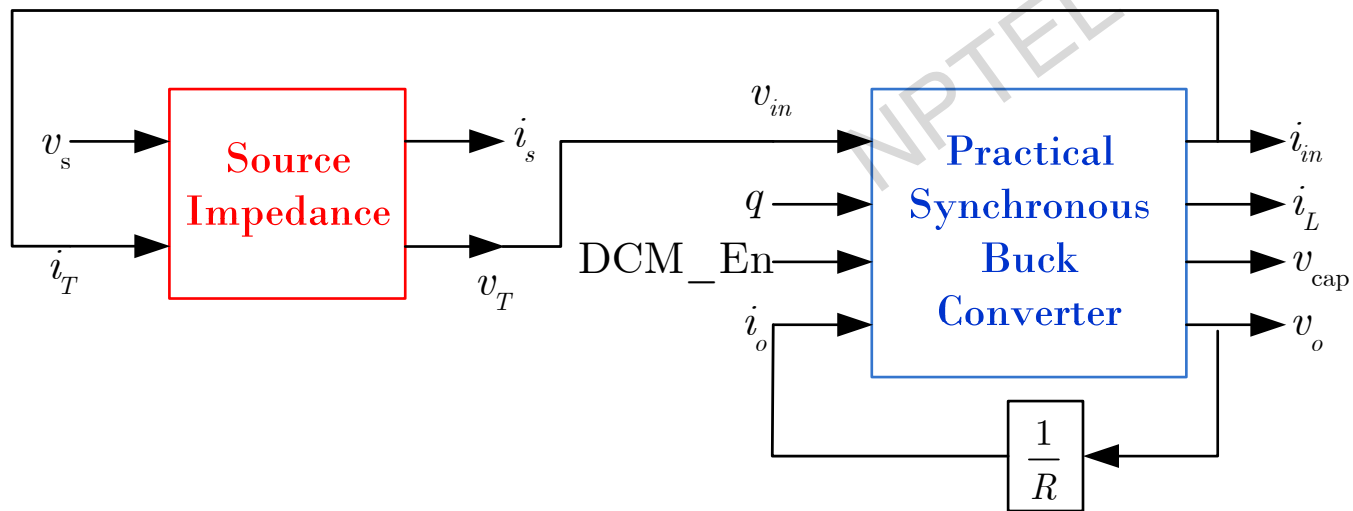
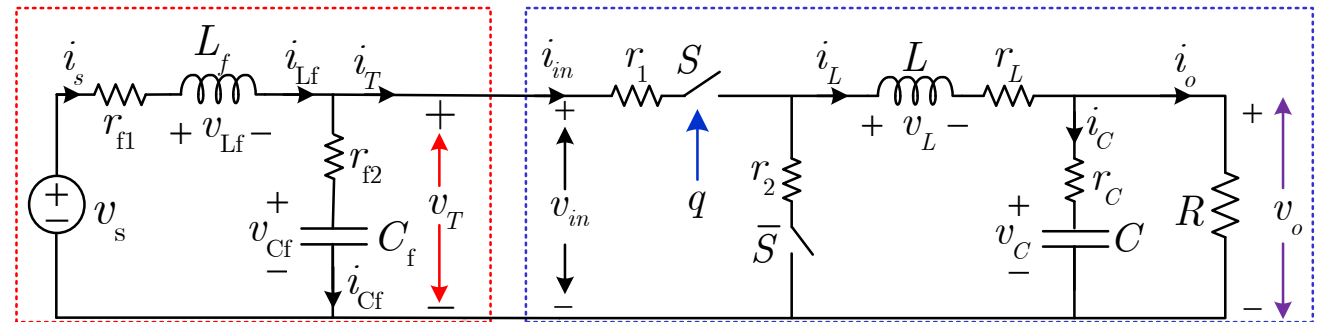
Input current i_{in} – dependent on i_L and q



MATLAB Model Development of a Practical Voltage Source



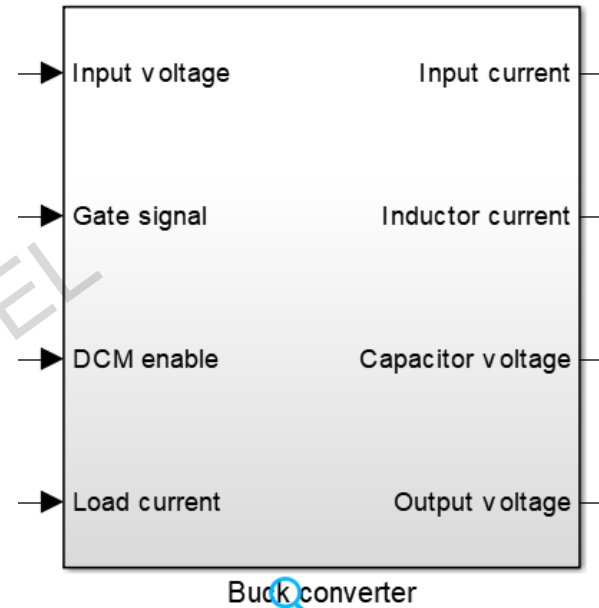
MATLAB Model Development of a Practical Voltage Source



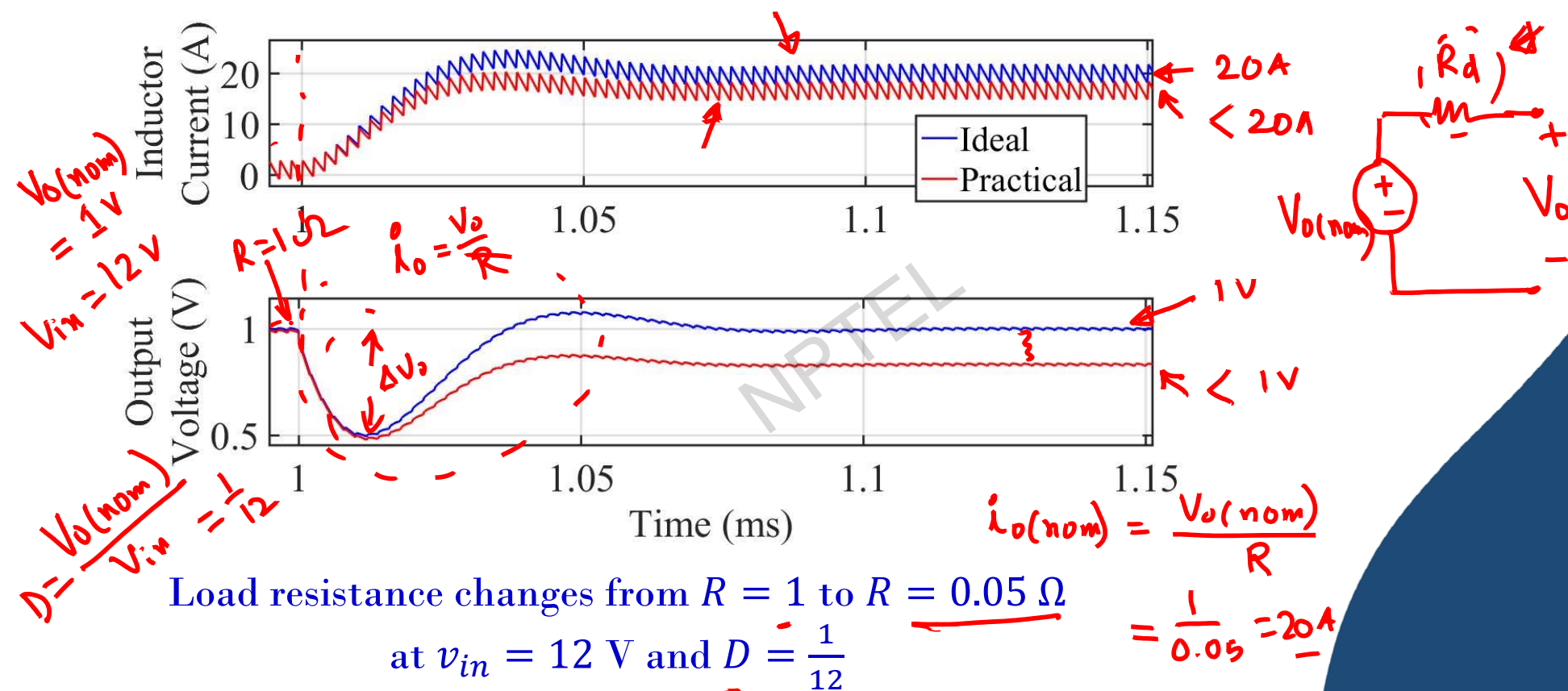
Synchronous Buck Converter Parameters for Simulation

```
L=0.5e-6;      % output inductance
C=200e-6;      % output capacitance
T=2e-6;        % switching time period
r_L=5e-3;      % inductor DCR
r_1=5e-3;      % High-side MOSFET on resistance
r_2=5e-3;      % Low-side MOSFET on resistance
r_d=r_2;       % diode on resistance
v_d=0.55;      % diode voltage drop
r_C=3e-3;      % capacitor ESR
Vin=12;        % nominal input voltage
Vref=1;        % reference output voltage
Io_max =20;    % maximum load current
```

parameters for the buck conv.



Simulation Case Study – Understanding Performance Requirements

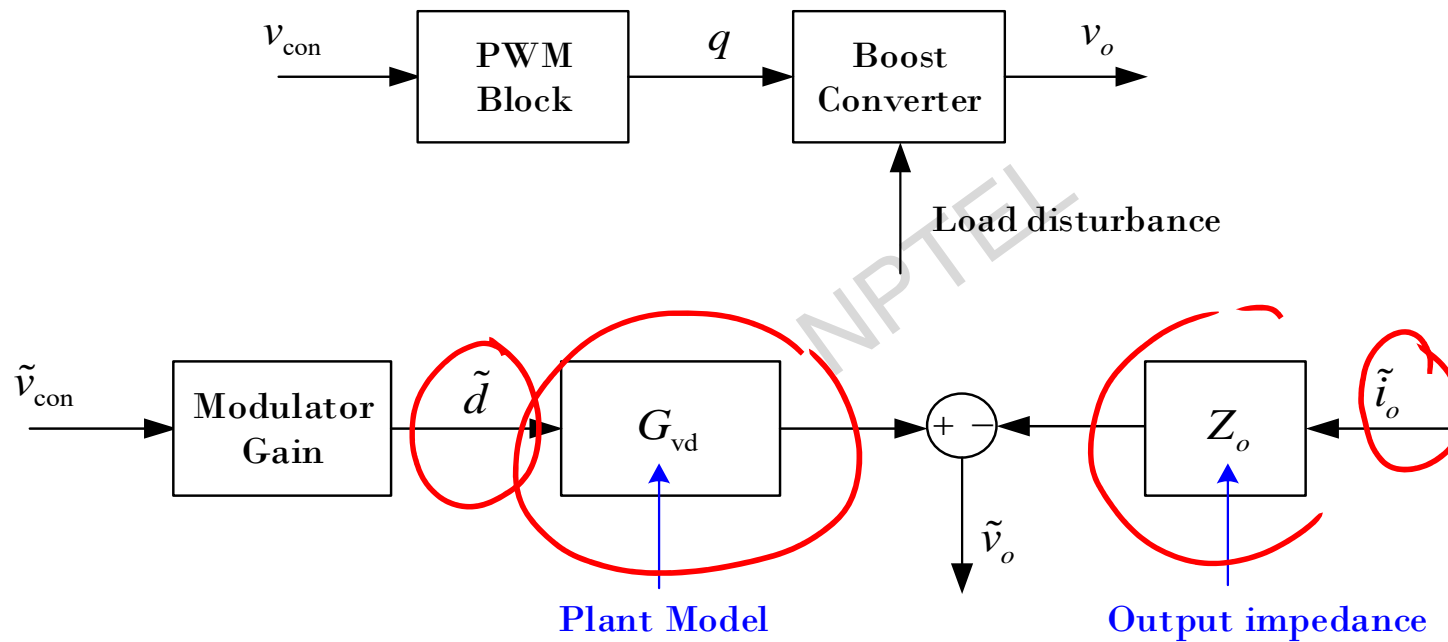


More Simulation Case Studies – Live Demonstration

- Buck converter operation using ideal and practical voltage sources
- Understanding conducted EMI effects
- Understanding transient response – supply, load, duty steps
- Understanding start-up behavior
- Understanding short circuit and open circuit behavior
- Understanding control requirements

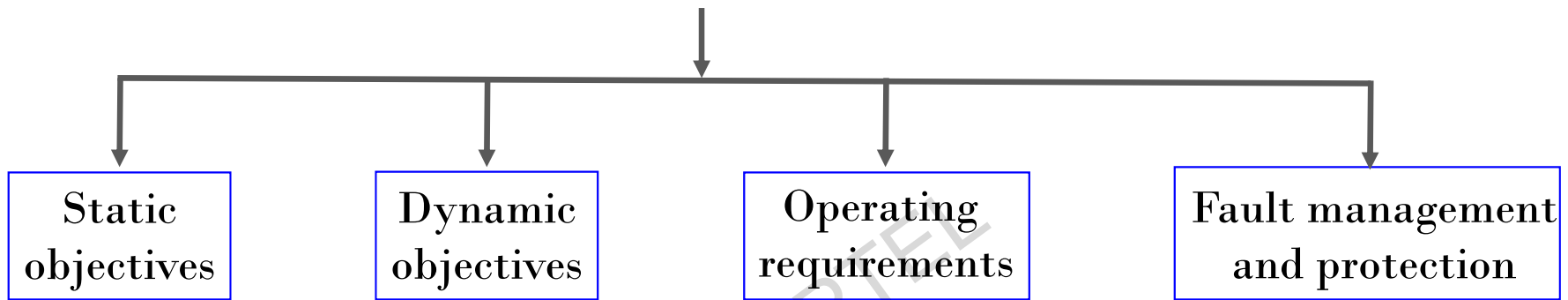
Understanding Dynamic Requirements

Conceptual understanding of load disturbance



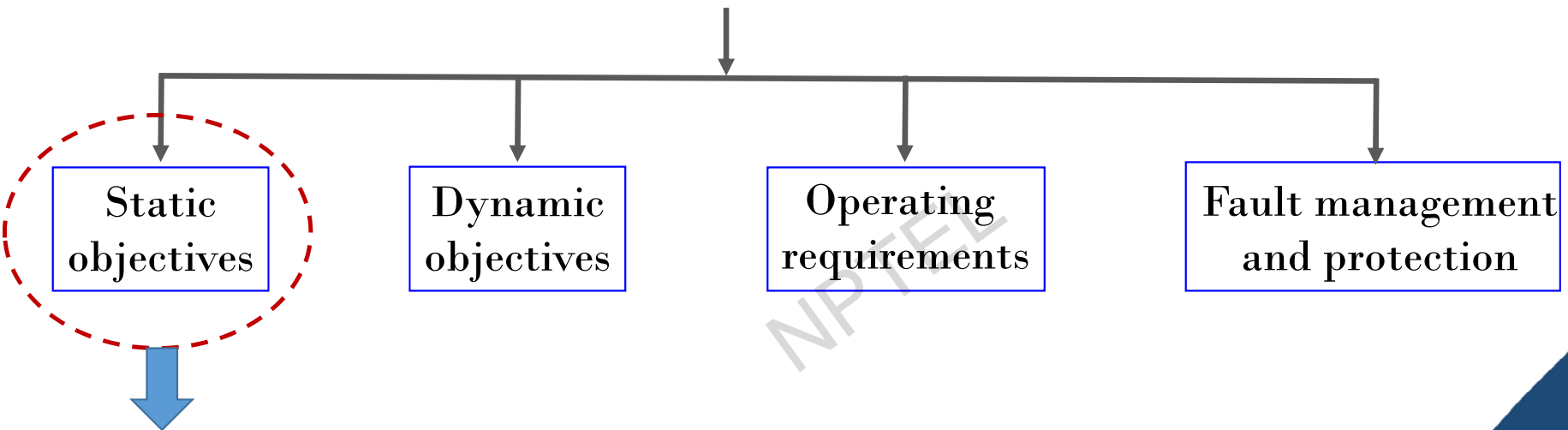
Understanding Converter's Objectives

Types of objectives



Understanding Converter's Objectives

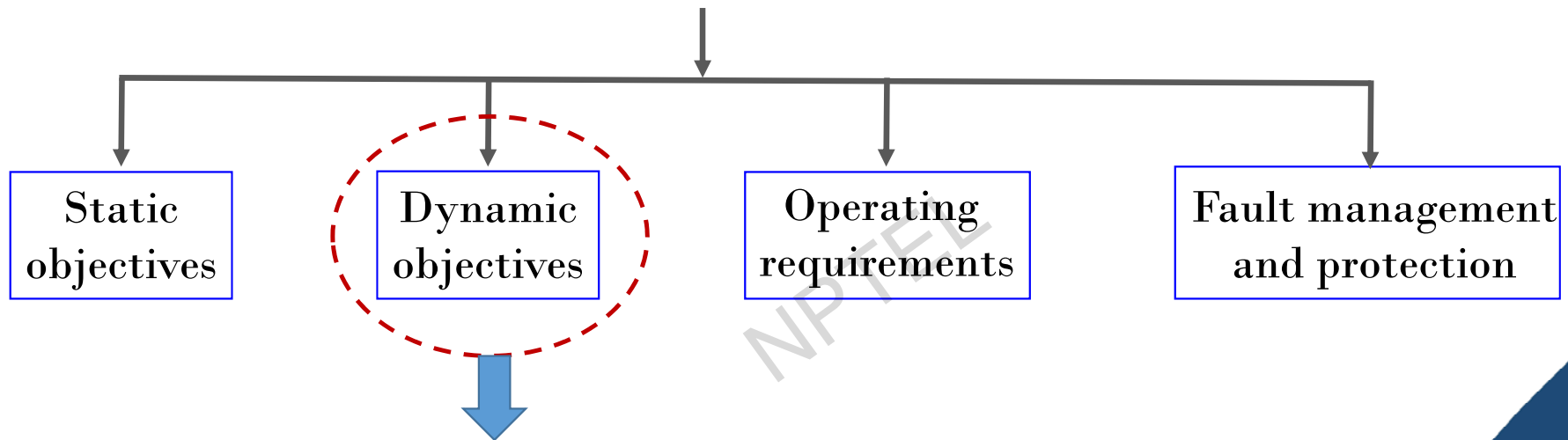
Types of objectives



Steady-state requirements and specifications

Understanding Converter's Objectives

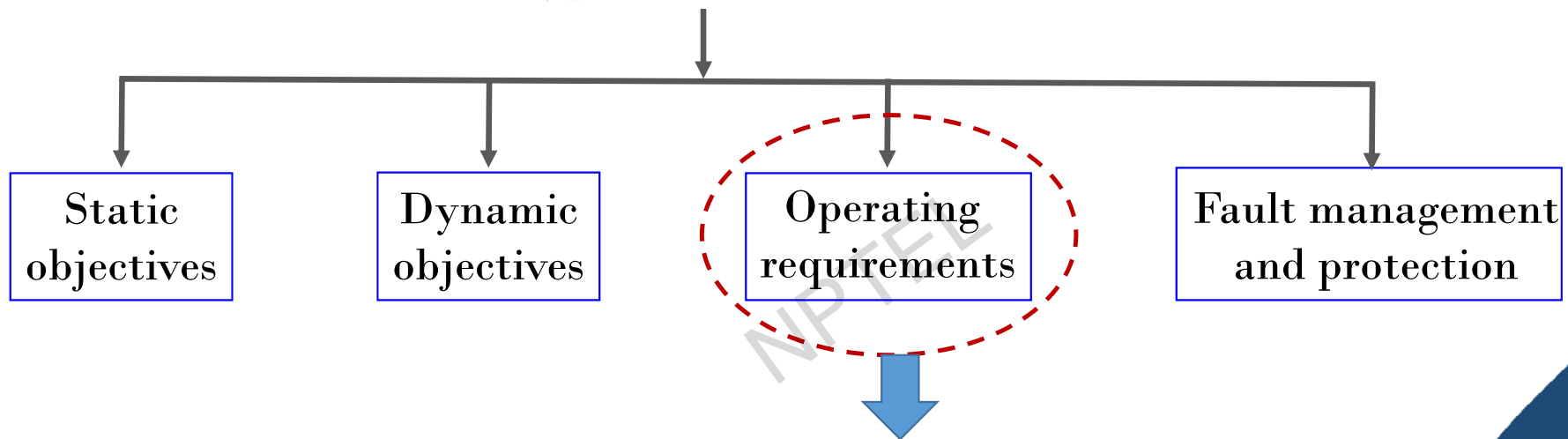
Types of objectives



Transient requirements and specifications

Understanding Converter's Objectives

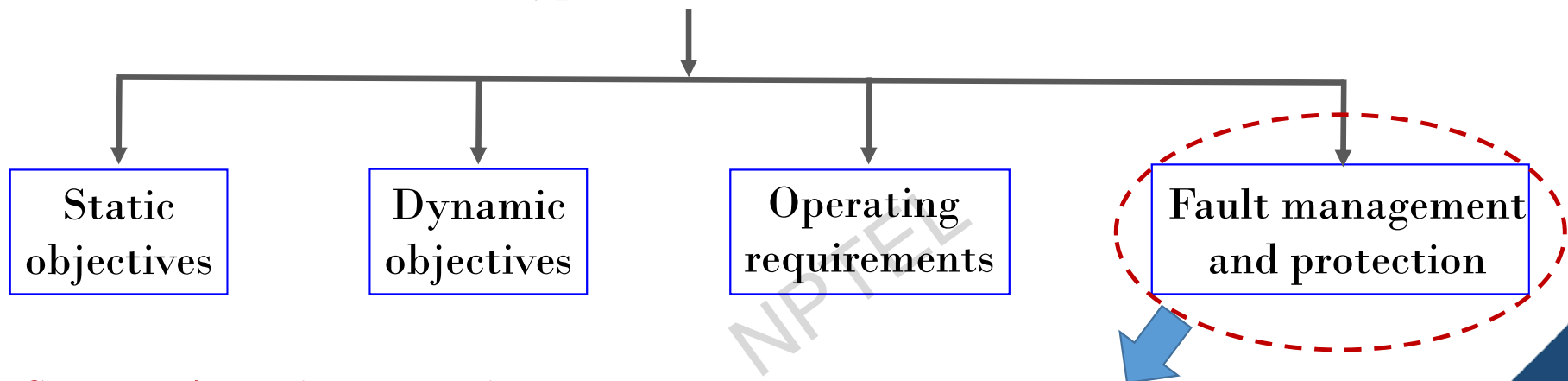
Types of objectives



- Conducted EMI compliance requirements and specifications
- Power-up sequencing – soft start, sequencing multiple converters
- Interrupt redundancy, hot swapping for fail-safe operations

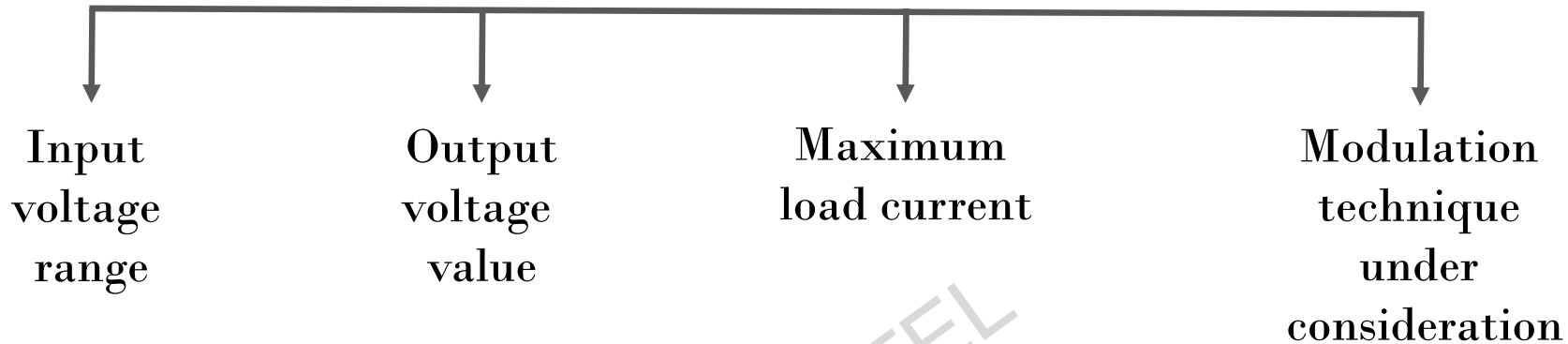
Understanding Converter's Objectives

Types of objectives



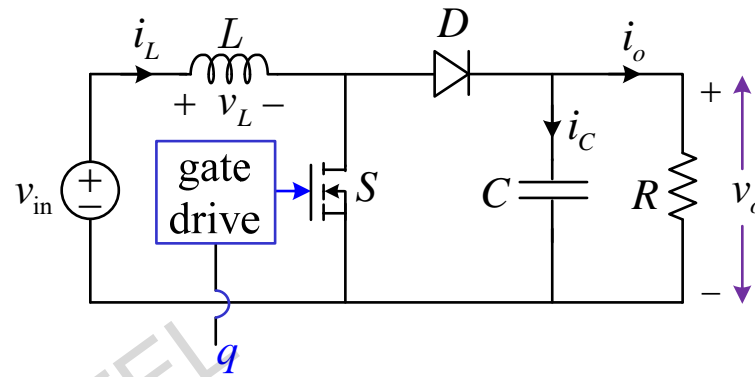
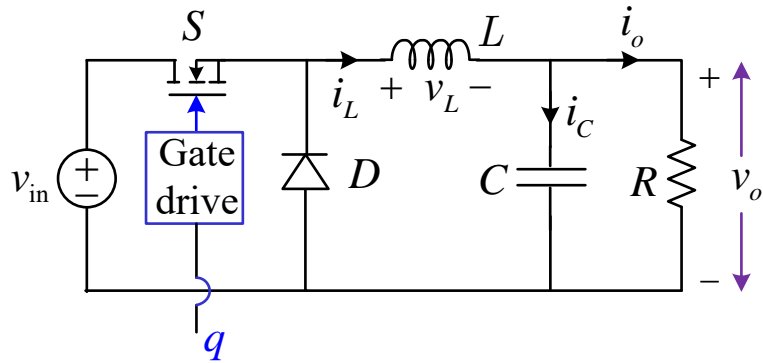
- **Strat-up/inrush current limit – current protection circuit**
- **Mean-time-to-failure – reliability aspect**
- **Thermal protection and heat distribution**
- **Packaging and cooling (active/passive) techniques**

Important Steady-State Requirements



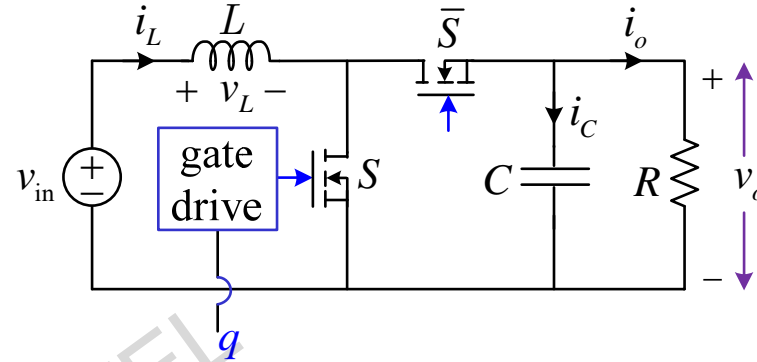
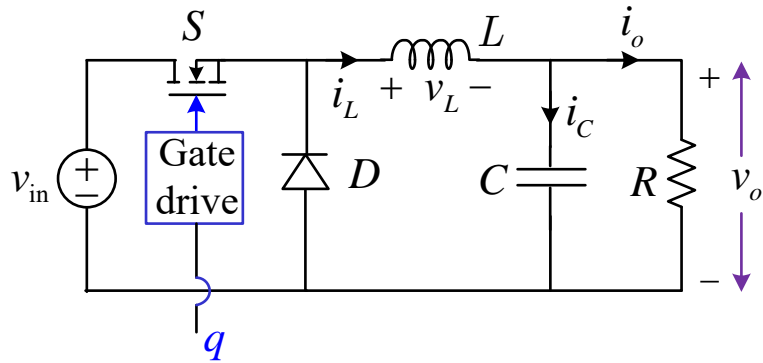
- *Range of input voltage* – worst-case current ripple, losses, device ratings
- *Nominal output voltage* – tolerable range, voltage regulation/ripple aspects
- *Maximum load current* – phase count, current ratings, losses, load step
- *Modulation technique* – frequency range, design rules, filter design

Power Stage Design Summary



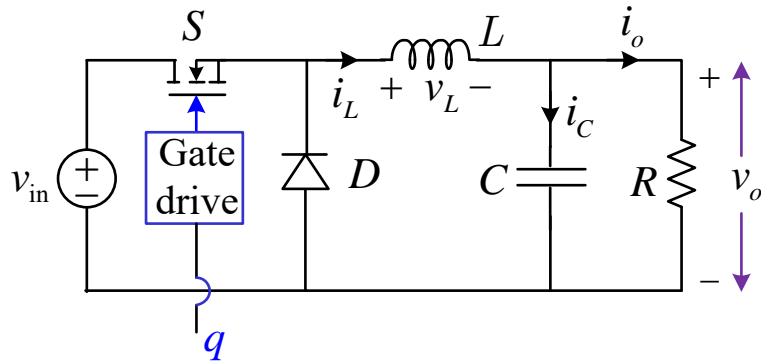
- Range of input voltage – worst-case current ripple, losses, device ratings
- Nominal output voltage – tolerable range, voltage regulation/ripple aspects
- Maximum load current – current ratings, phase count, losses, load step
- Modulation technique – frequency range, design rules, filter design

Few Commercial Power Stage Design Tools



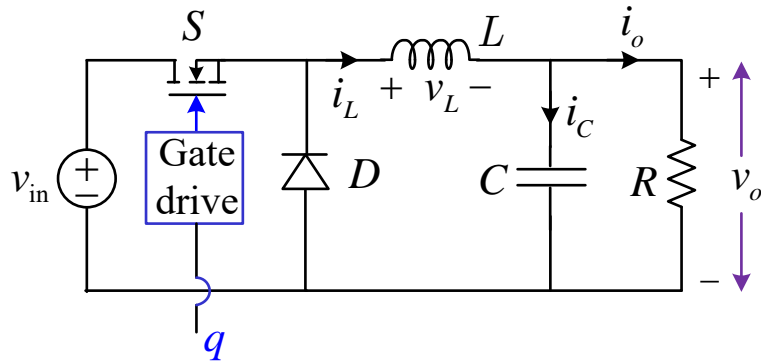
- *Texas Instruments Webench* – [link here](#)
- *STMicroelectronics eDesignSuite* – [link here](#)
- *Infineon Designer powered by TINA Cloud* – [link here](#)
- *On Semiconductor WebDesigner+Power* – [link here](#)

Example of Buck Converter Power Stage Design



- *Input voltage range* – 8 to 15 V with 12 V nominal
- *Nominal output voltage* – 1 V nominal with 2 % ripple limit
- *Maximum load current* – 20 A nominal and nearly 100 mA lower limit
- *Modulation technique* – single or combined multi-mode techniques

Buck Converter: Power Stage Inductor Design

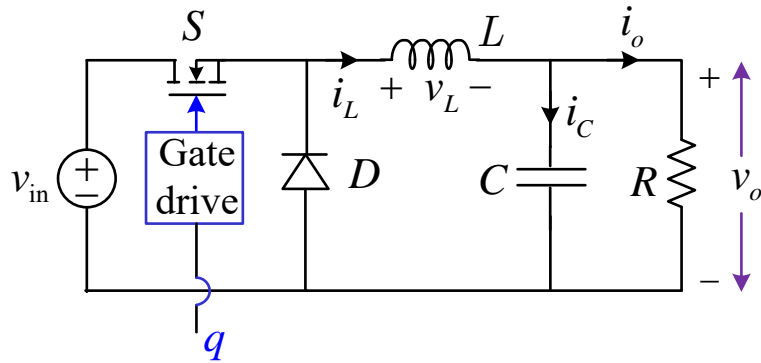


$$\Delta i_L = \frac{V_o}{Lf_{sw}} \times (1 - D)$$

Current ripple is maximum at minimum $D \rightarrow$ highest v_{in}

- Ripple inductor current (20% of maximum load current) = 4 A
- Minimum duty ratio (at maximum input voltage) = $1/15 =$ 0.067
- Nominal switching frequency (under high load) = 500 kHz
- Minimum inductor value (at 1 V output) = 467 nH

Buck Converter: Power Stage Design



$$\Delta v_o = \left(\frac{(1-D)V_o}{8LCf_{sw}^2} \right) + \underbrace{r_C \Delta i_L}_{\text{ESR effect}}$$

Current ripple is maximum at minimum $D \rightarrow$ highest v_{in}

- *Ripple output voltage (2% of nominal output voltage) = 20 mV*
- *Worst-case ripple at maximum input voltage*
- *Minimum output capacitor (at **3 mΩ ESR**) = 117 uF*
- *Inductor and capacitor: L = 0.5 uF, C=200 uF*

Understanding Operating Requirements

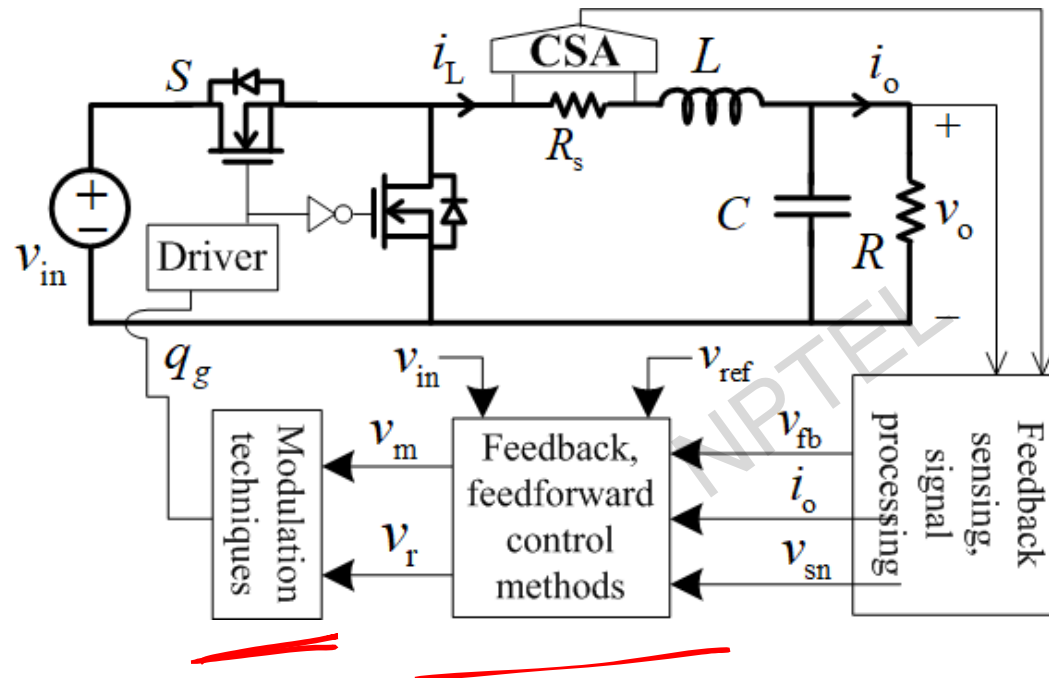
- Electromagnetic interference (EMI) – [reference link](#)
- Power-up sequencing – [reference link](#)
- Hot plugging – [reference link](#)

Fault Management and Protection

- Inductor (and switch) current limit
- Inrush/ start-up current limit
- Thermal protection
- Packaging and cooling requirements
- Health monitoring

→ Digital twin

Overview of Feedback/Feedforward Control Methods



S. Kapat & P. Krein, "A Tutorial and Review Discussions ...", *IEEE Open J. Power Electronics*

Summary

- Impedance aspects of a practical voltage source – discussed
- Scalable and plug-and-play MATLAB model development
- MATLAB case studies to demonstrate control requirements
- Power-stage design guidelines and few power designer tools



**THANK
YOU !**



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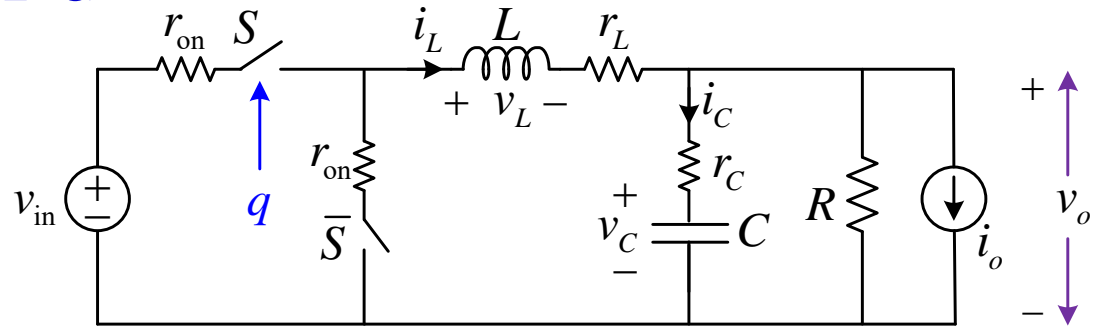
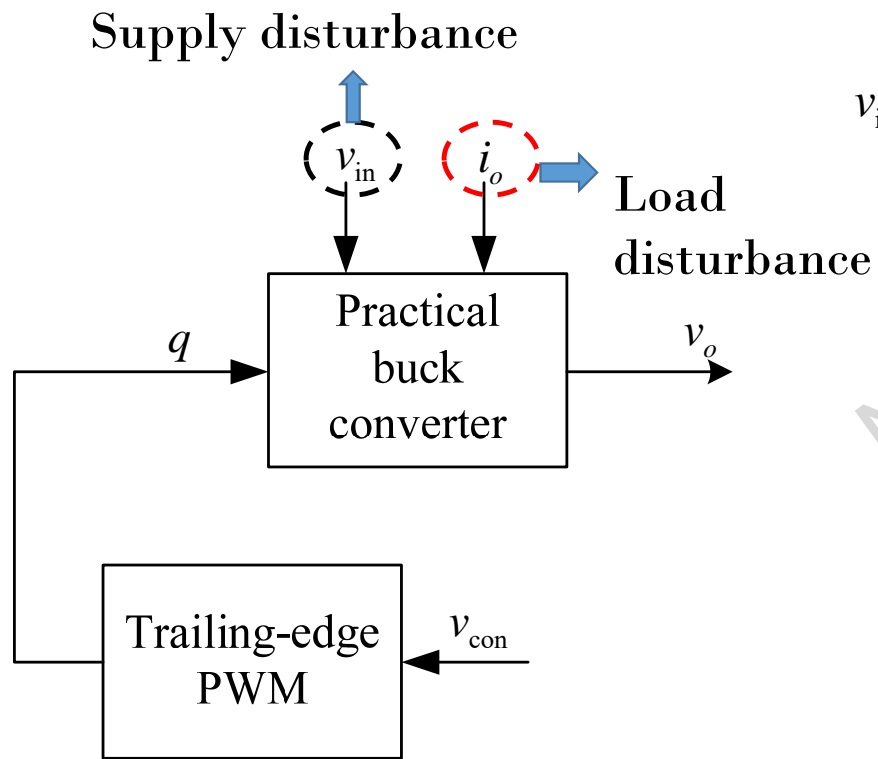
Module 03: Fixed Frequency Control Methods

Lecture 14: Feedforward Control in SMPC and MATLAB Simulation

Concepts Covered

- Sources of disturbances in SMPCs
- Disturbance rejection using feedforward action
- Supply disturbance rejection and MATLAB simulation
- Load disturbance rejection and MATLAB simulation
- Understanding need for feedback control

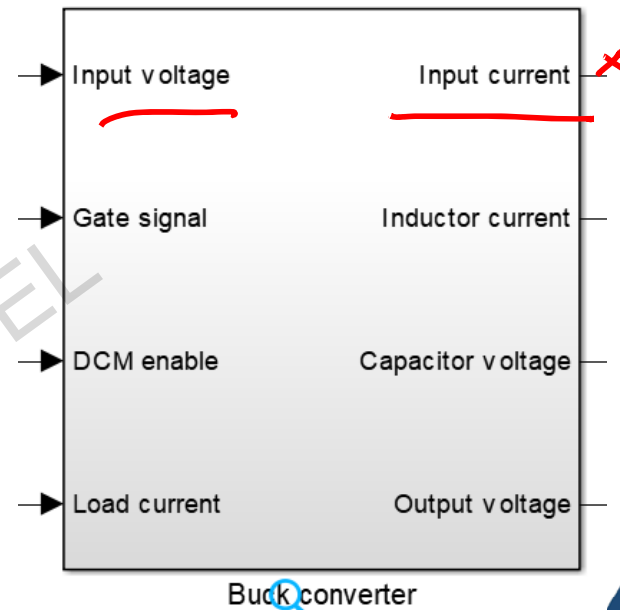
Sources of Disturbance in SMPC



NPTTEL

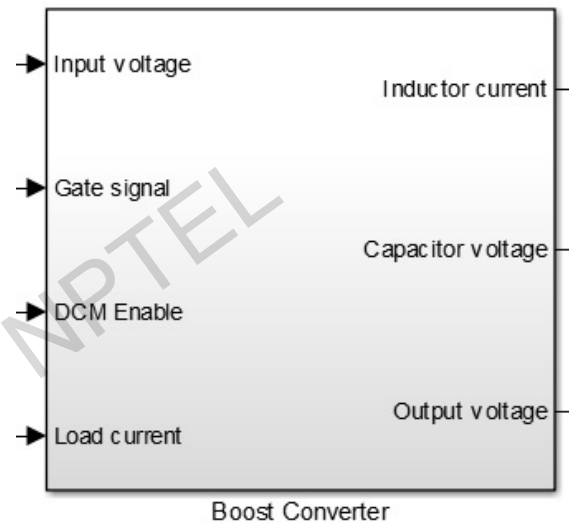
Synchronous Buck Converter Parameters for Simulation

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C=200e-6;      % output capacitance
T=2e-6;        % switching time period
r_L=5e-3;      % inductor DCR
r_1=5e-3;      % High-side MOSFET on resistance
r_2=5e-3;      % Low-side MOSFET on resistance
r_d=r_2;        % diode on resistance
v_d=0.55;      % diode voltage drop
r_C=3e-3;      % capacitor ESR
Vin=12;         % nominal input voltage
Vref=1;         % reference output voltage
Io_max =20;    % maximum load current
```



Synchronous Boost Converter Parameters for Simulation

```
L=2e-6;  
C=100e-6;  
T=2e-6;  
r_L=0*10e-3;  
r_d=0*10e-3;  
v_d=0*0.7;  
r_1=0*5e-3;  
r_2=0*5e-3;  
r_C=0*5e-3;  
Vin=3.6;  
Vref=5;
```



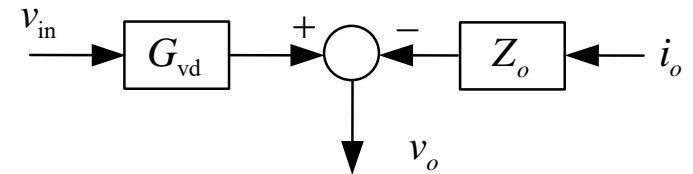
Effects of Supply and Load Disturbances – MATLAB Simulation

Observations:

Supply step transient

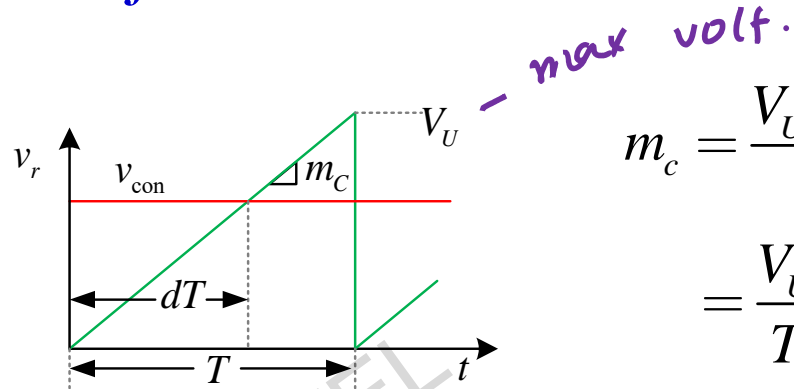
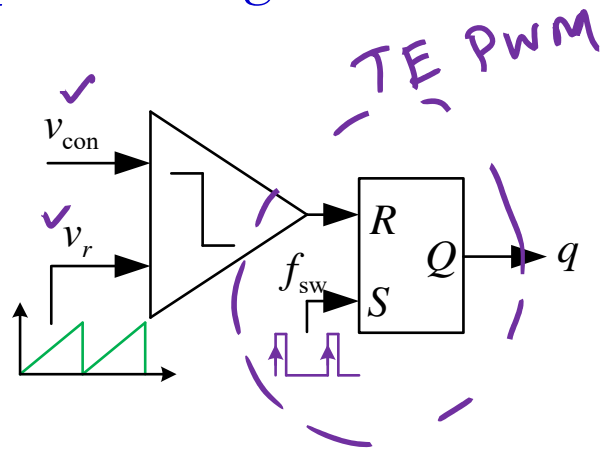
↓
Significant impact on
output voltage as well
as inductor current

Impact is visible even for
sinusoidal excitation



Buck converter

Input Voltage Disturbance Rejection in a Buck Converter



$$m_c = \frac{V_U - V_L}{T}$$

$$= \frac{V_U}{T} \quad (\because V_L = 0)$$

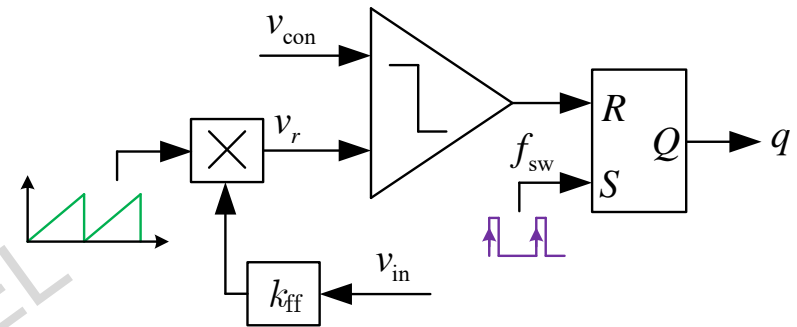
$$\frac{dT}{T} = \frac{v_{con}}{V_U} \Rightarrow d = \left(\frac{1}{V_U} \right) \times v_{con}$$

$v_{in} \rightarrow v_{in} + \Delta v_{in}$ ■ Objective is to reject disturbance of v_{in} change

Input Voltage Disturbance Rejection (contd...)

$$v_o = dv_{in} = \underbrace{\left(\frac{1}{V_U} \right)}_{F_m} \times v_{con} \times v_{in}$$

(modulator gain)



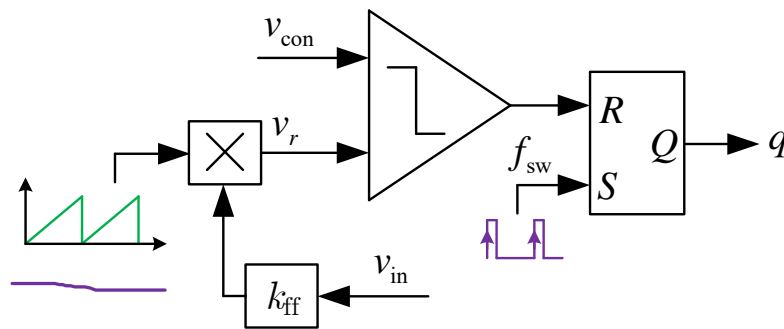
- Objective is to make Δv_o even without changing v_{con}

Let, $V_U = k_{ff} v_{in}$

$$v_o = \frac{1}{k_{ff} v_{in}} \times v_{in} \times v_{con} \Rightarrow v_o = \frac{v_{con}}{k_{ff}} \rightarrow \text{Insensitive to input voltage variation}$$

Input Voltage Disturbance Rejection in a Boost Converter

Simple extension of the previous input voltage feedforward



$$v_{in} \rightarrow v_{in} + \Delta v_{in}$$

$$v_o = \frac{1}{1-d} \times v_{in}$$

$$v_o = \frac{1}{1 - \frac{v_{con}}{V_U}} \times v_{in}$$

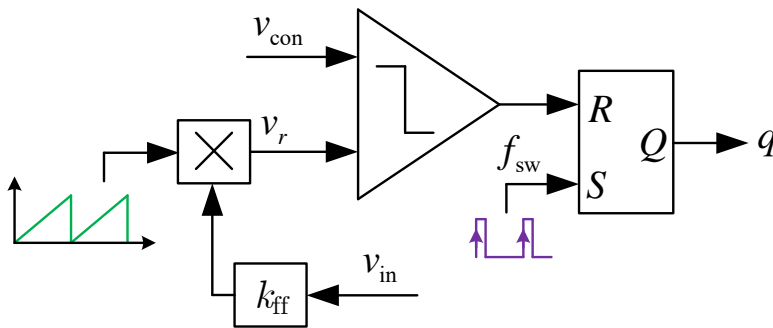
$$d = \frac{V_{con}}{V_m}$$

V_U

- Objective: Supply disturbance rejection using $V_U = k_{ff} \times v_{in}$

Input Voltage Disturbance Rejection in a Boost Converter

Simple extension of the previous input voltage feedforward



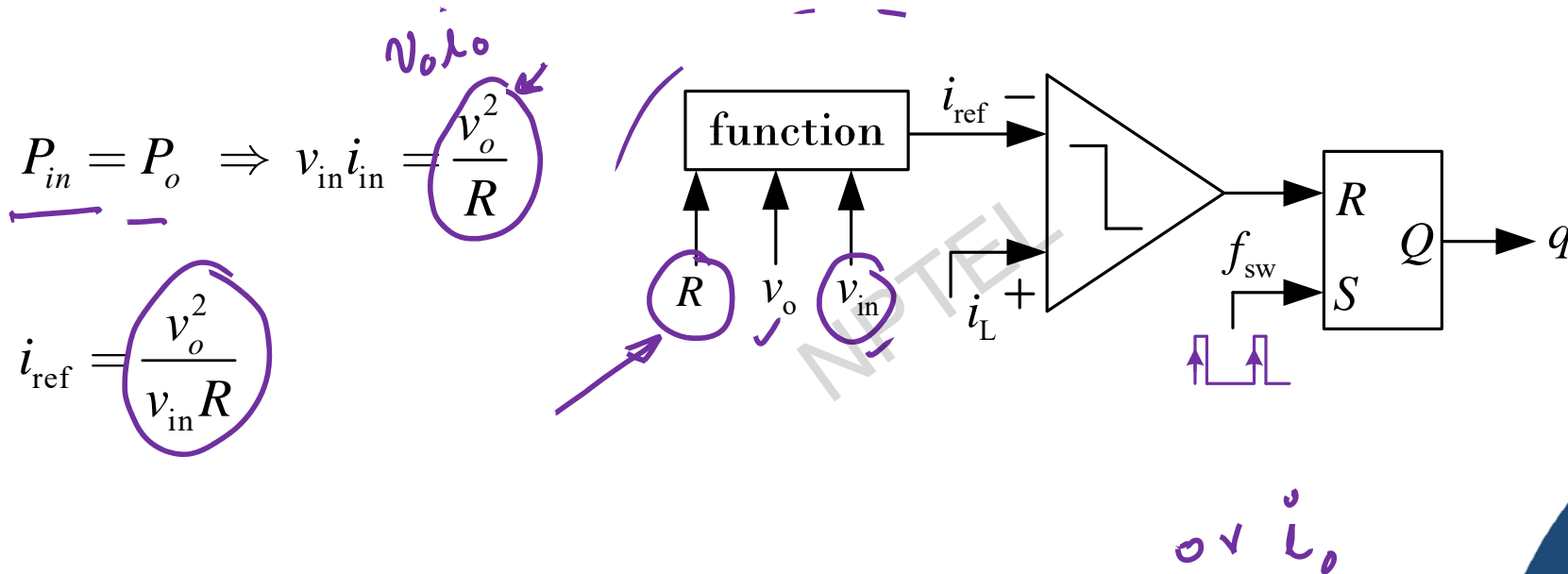
$$v_o = \frac{1}{1 - \frac{v_{\text{con}}}{V_U}} \times v_{\text{in}} = \frac{V_U}{V_U - v_{\text{con}}} \times v_{\text{in}}$$

$$v_o = \frac{k_{ff} v_{\text{in}}}{k_{ff} v_{\text{in}} - v_{\text{con}}} \times v_{\text{in}}$$

- Observation: **Supply disturbance cannot be rejected!!**

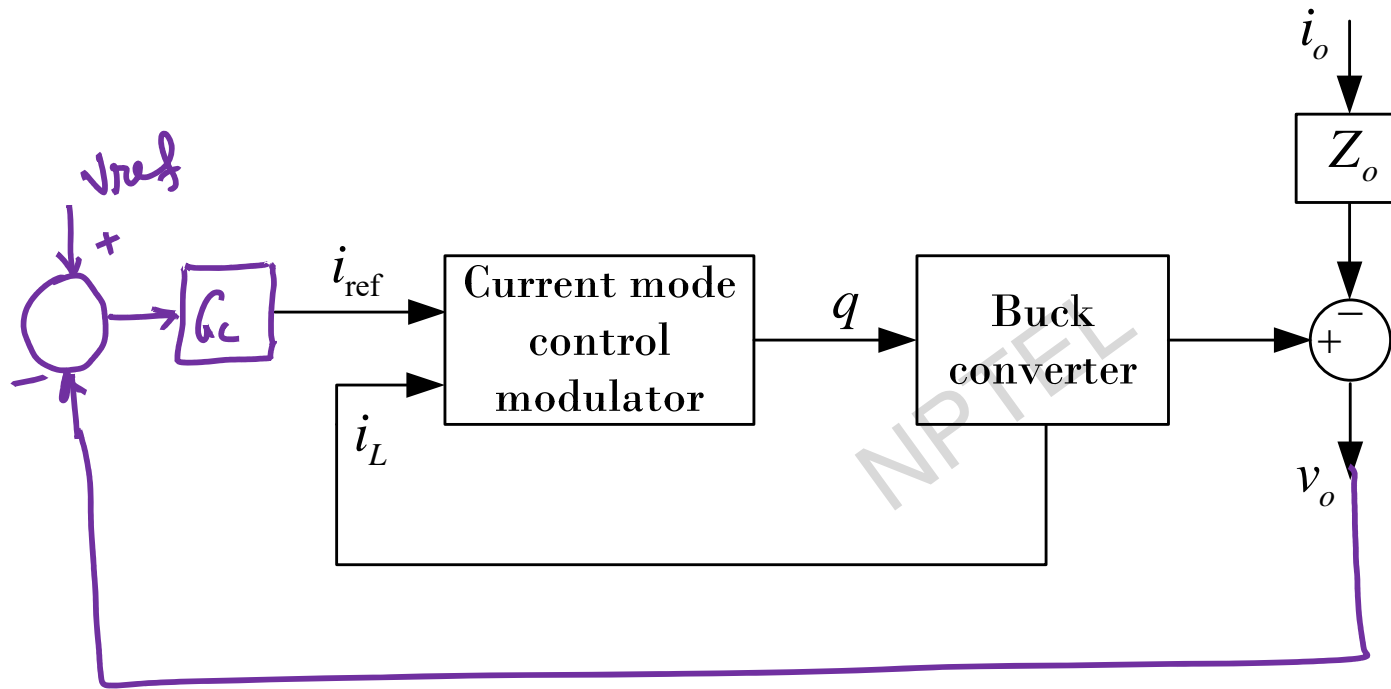
Input Voltage Disturbance Rejection in a Boost Converter

Alternative method using current control and power balance

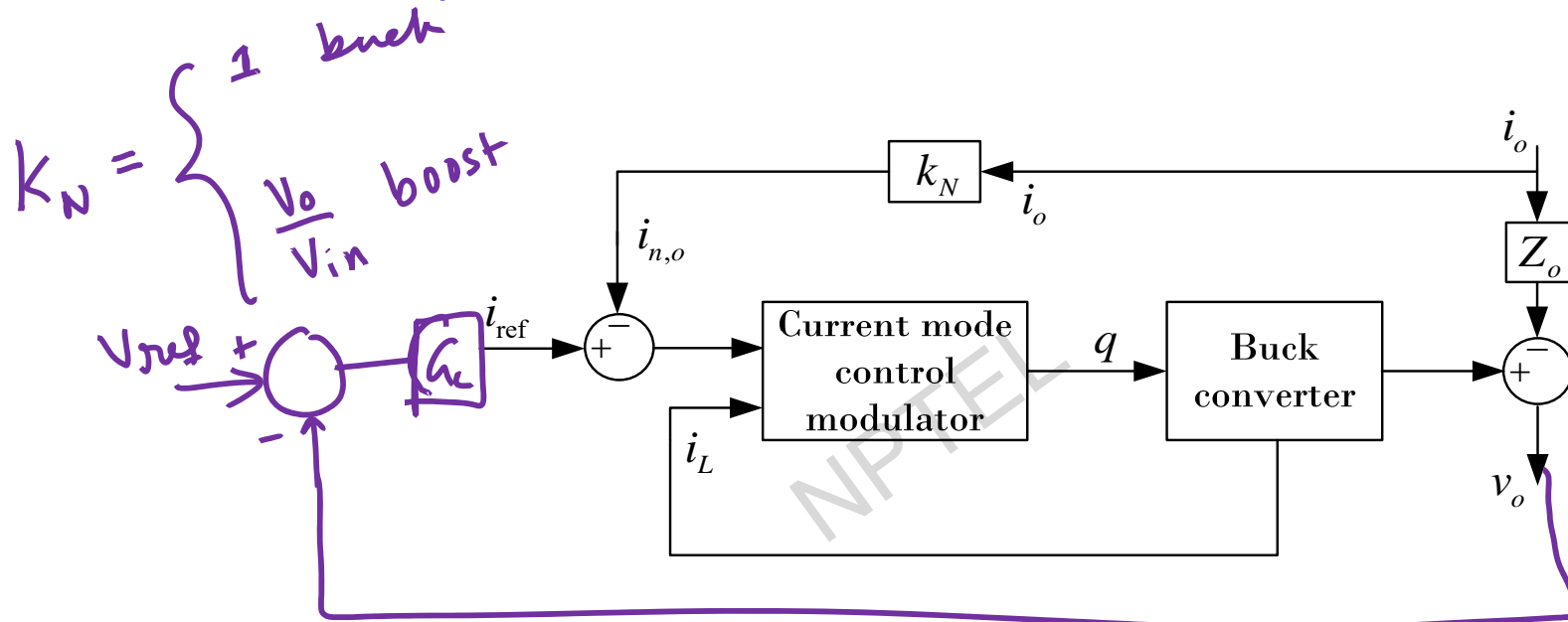


- Limitation: **Non-robust due to difficulty in measuring R !!**

Load Disturbance in CMC



Load Current Feedforward in CMC



- Repeat the earlier simulation using CMC using load feedforward

Limitations of Feedforward Control in SMPC

- Feedforward control offers excellent disturbance rejection
- Requires accurate parameter information – non-robust
- Poor regulation performance with practical parasitic
- Unmodelled dynamics may be problematic
- Feedforward control alone is not suitable for SMPCs

Summary

- Sources of disturbances in SMPCs – identified
- Effects of supply and load disturbance – discussed
- Input voltage and load current feedforward – demonstrated
- Feedforward control non-robust, feedback control seems essential
- Combined feedback and feedforward control – to be discussed



**THANK
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NPTEL ONLINE CERTIFICATION COURSES

CONTROL AND TUNING METHODS IN SMPCs

Dr. Santanu Kapat

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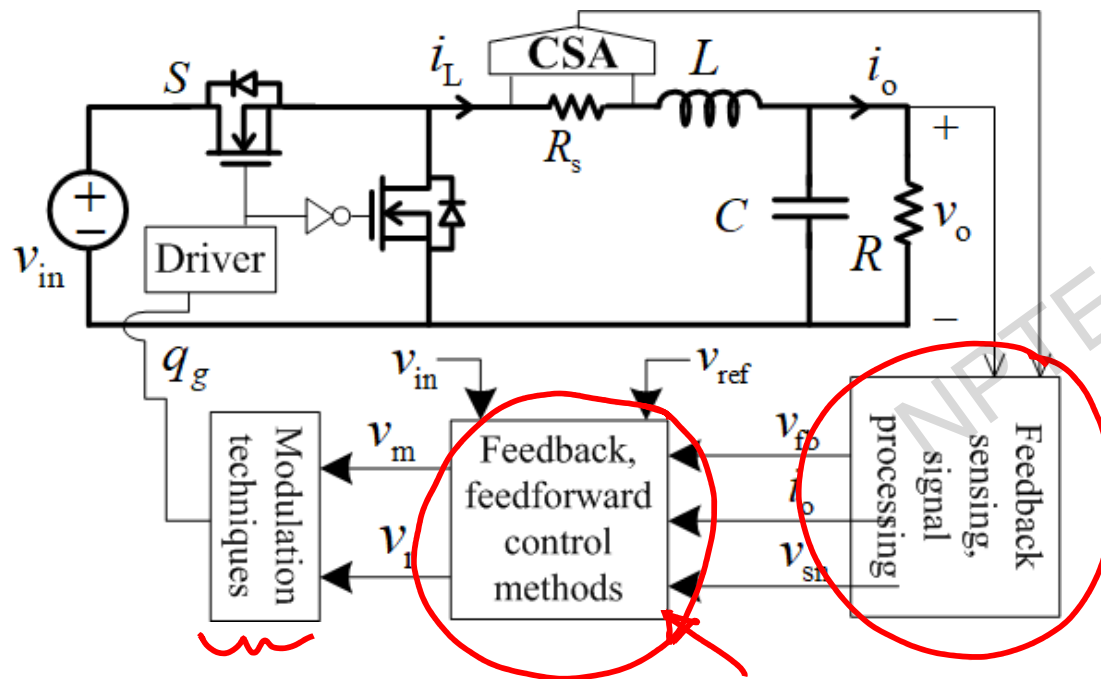
Module 03: Fixed Frequency Control Methods

Lecture 15: Single and Multi Loop Feedback Control Methods

Concepts Covered

- Conventional negative feedback control
- Link with voltage feedback control in SMPC
- PWM voltage mode control – single loop feedback control
- PWM current mode control – two-loop feedback control
- Discussions on advantages and limitations

Overview of Feedback/Feedforward Control Methods

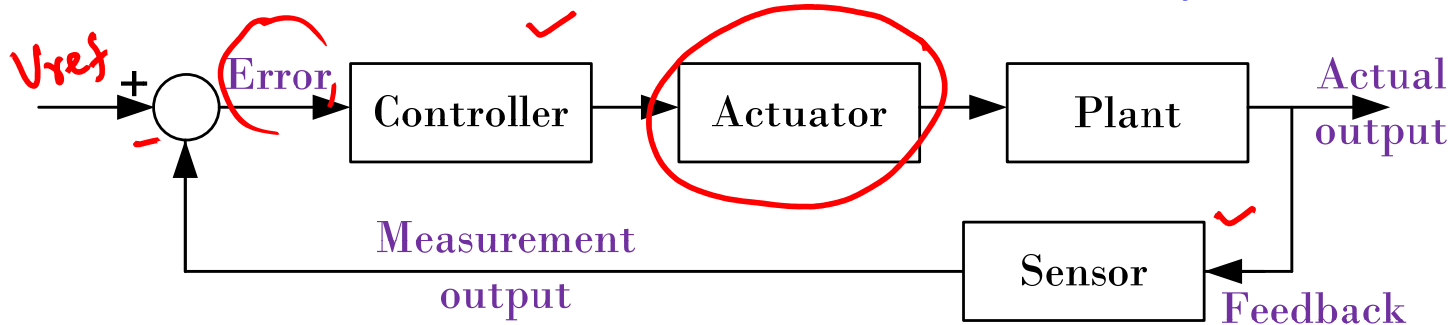


Objectives

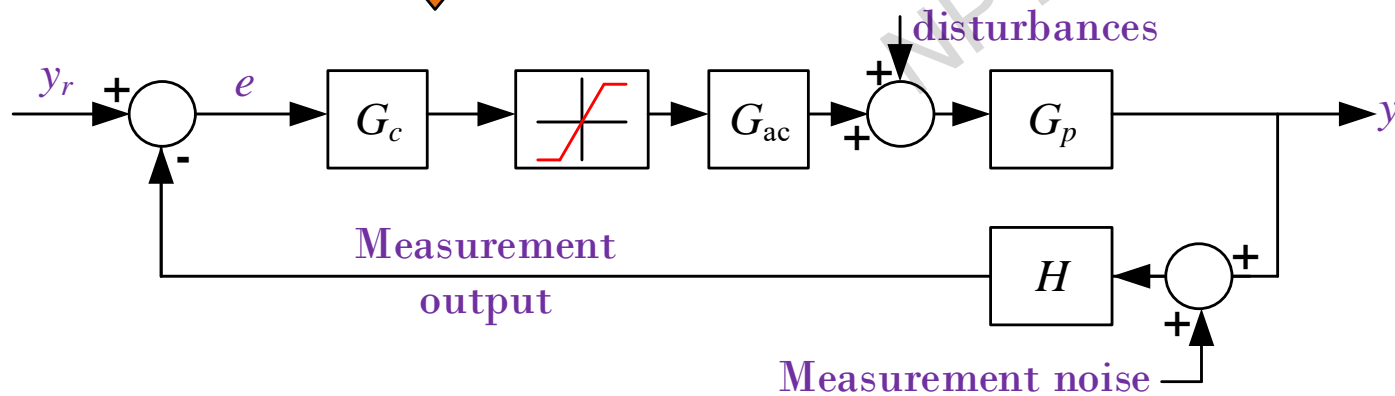
- Well-damped and fast response
- Good disturbance rejection
- Tight voltage regulation
- Soft-start at power-up

S. Kapat & P. Krein, "A Tutorial and Review Discussions ...", *IEEE Open J. Power Electronics*

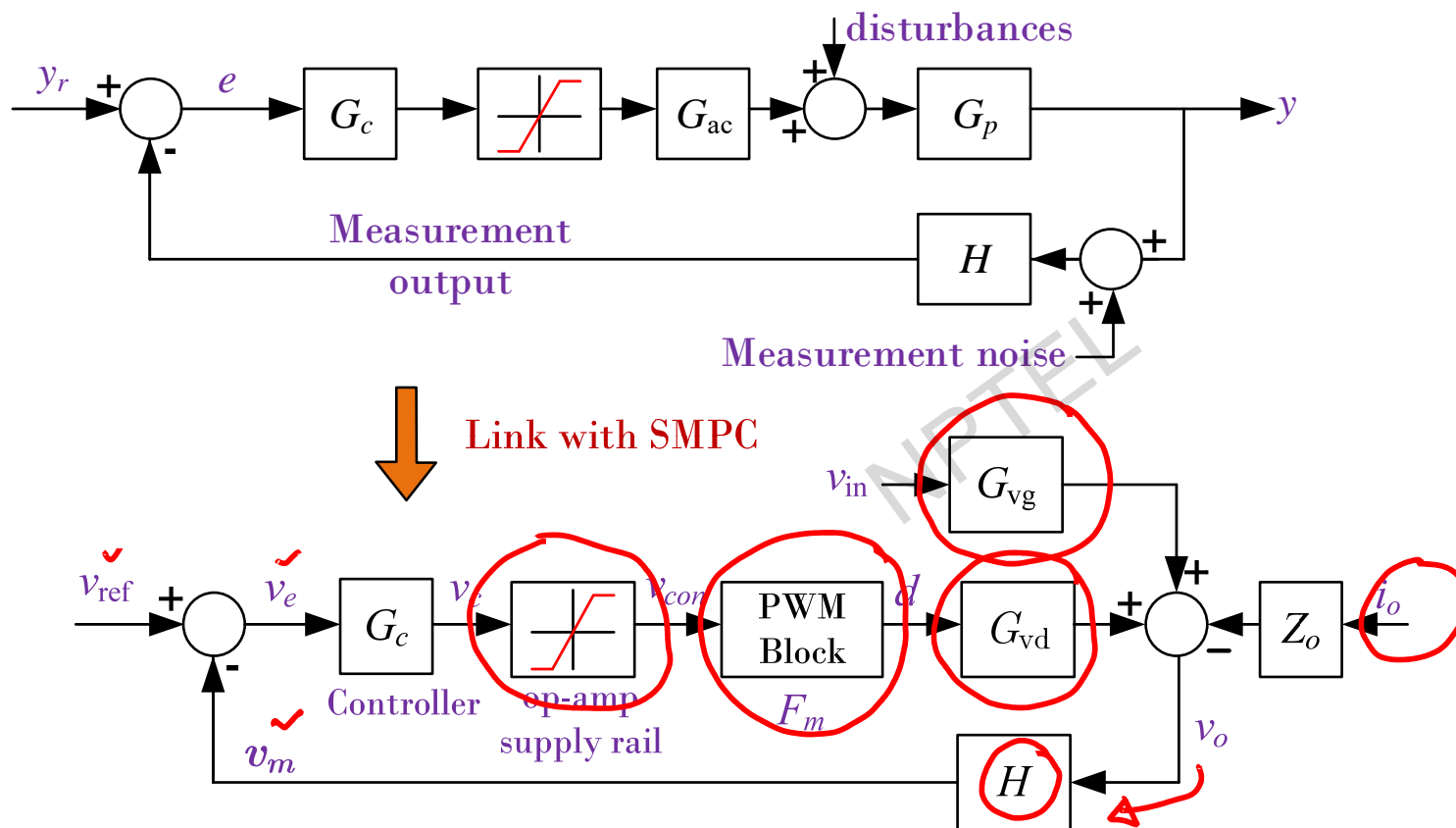
Single Loop Feedback Control – Sources of Disturbance



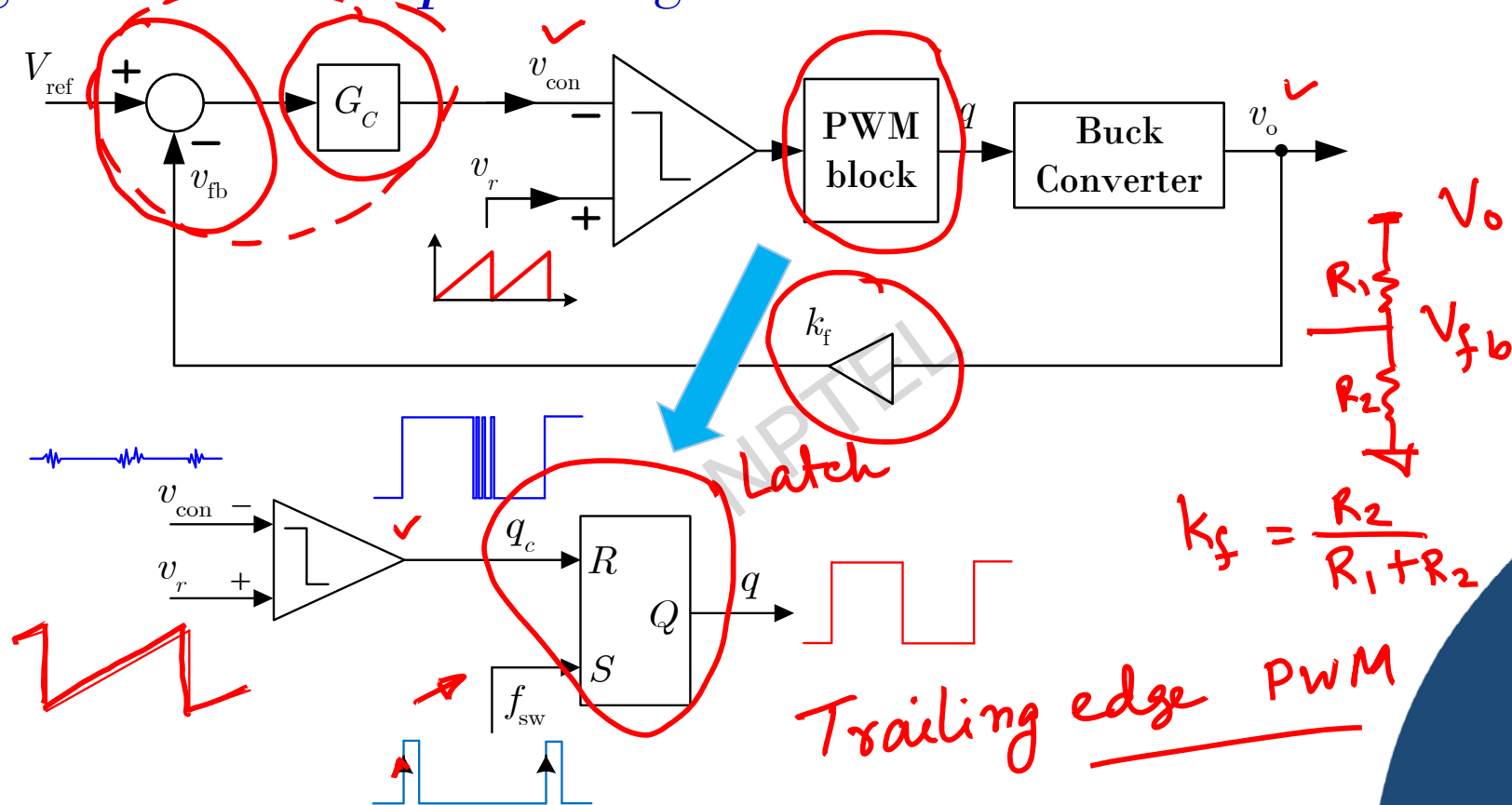
Source of disturbance and noise



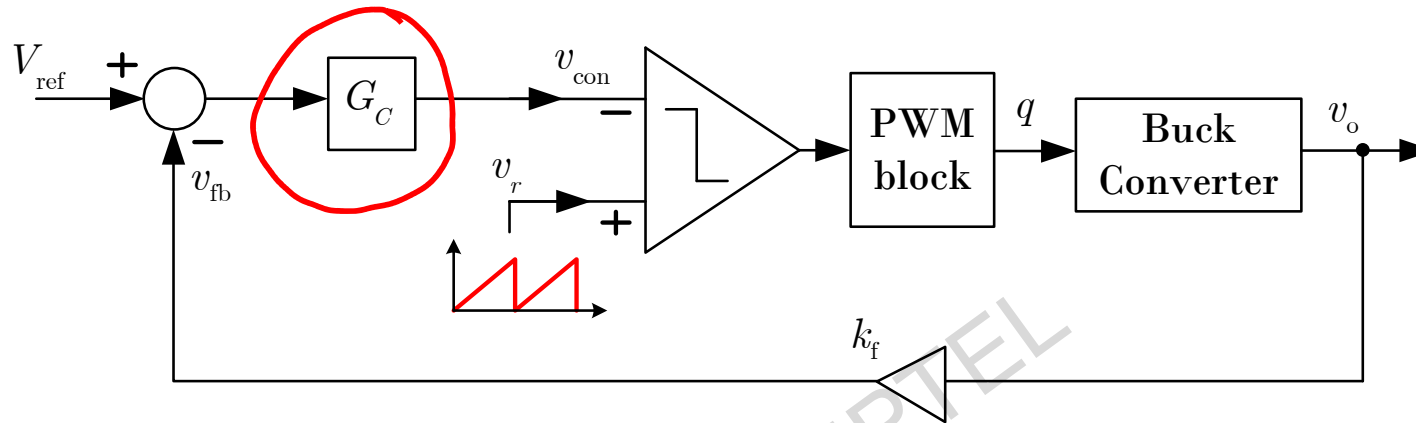
Single Loop Feedback Control – Link with SMPC



Single Feedback Loop – Voltage Mode Control

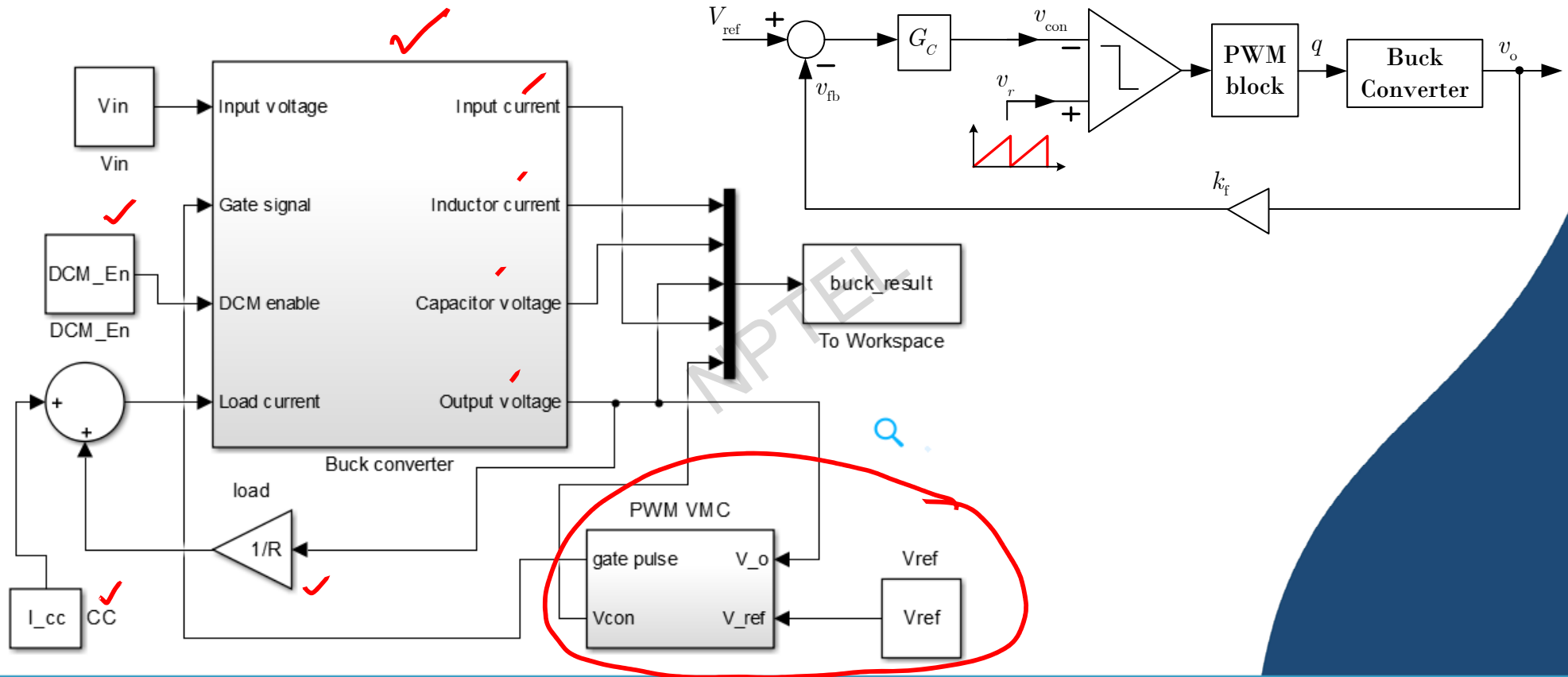


Voltage Mode Control (VMC) – A Start-up Case Study

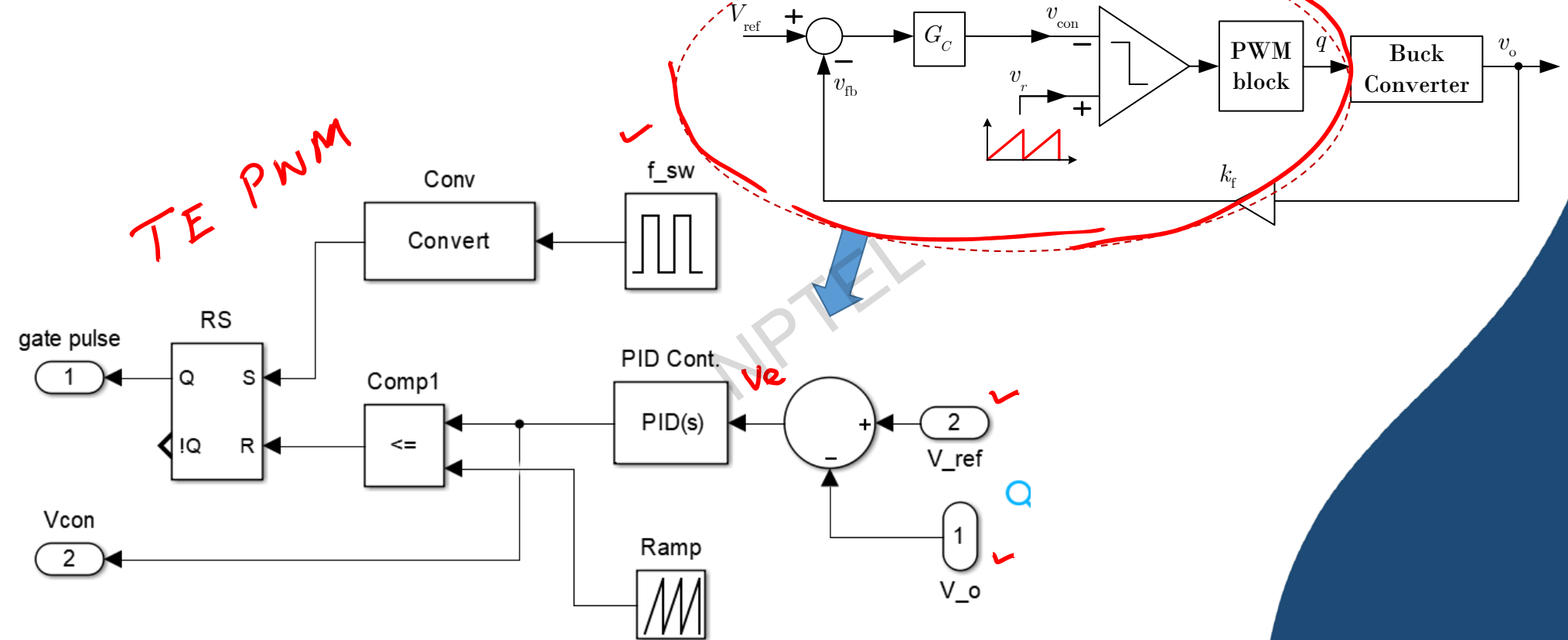


- Consider a PID controller $G_C(s) = \overset{\checkmark}{K_P} + \frac{\overset{\checkmark}{K_I}}{s} + \frac{\overset{\checkmark}{K_D}s}{\tau_D s + 1}$
- Implement VMC in MATLAB and simulate a start-up case study

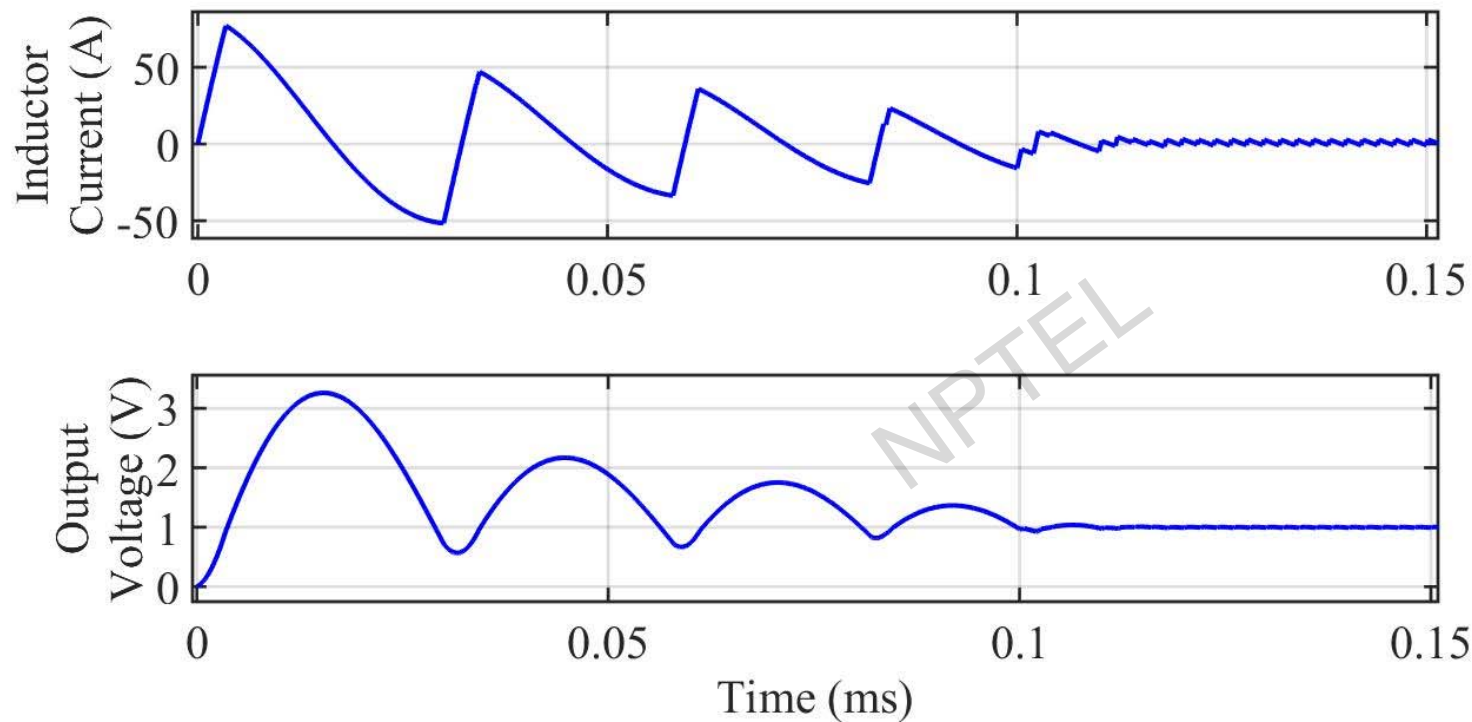
MATLAB Implementation of VMC



MATLAB Implementation of VMC



Simulating a Start-up Case Study under VMC

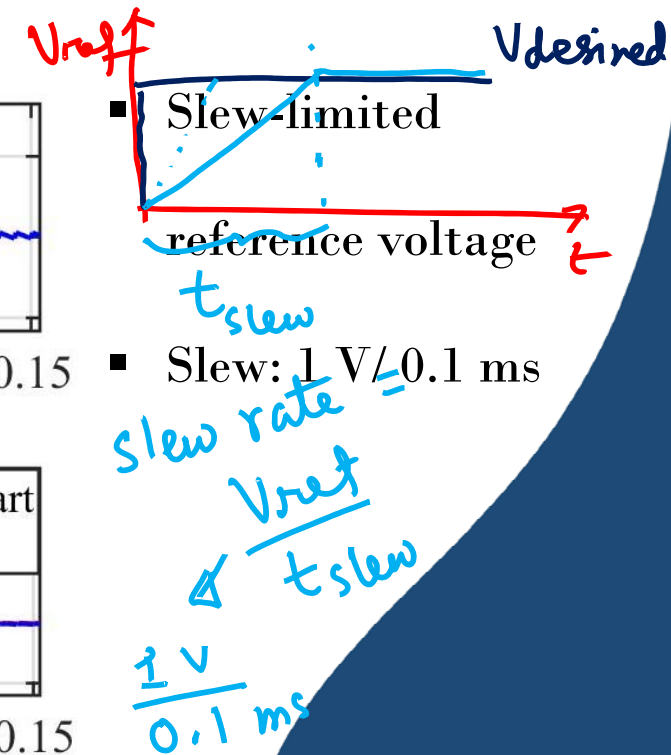
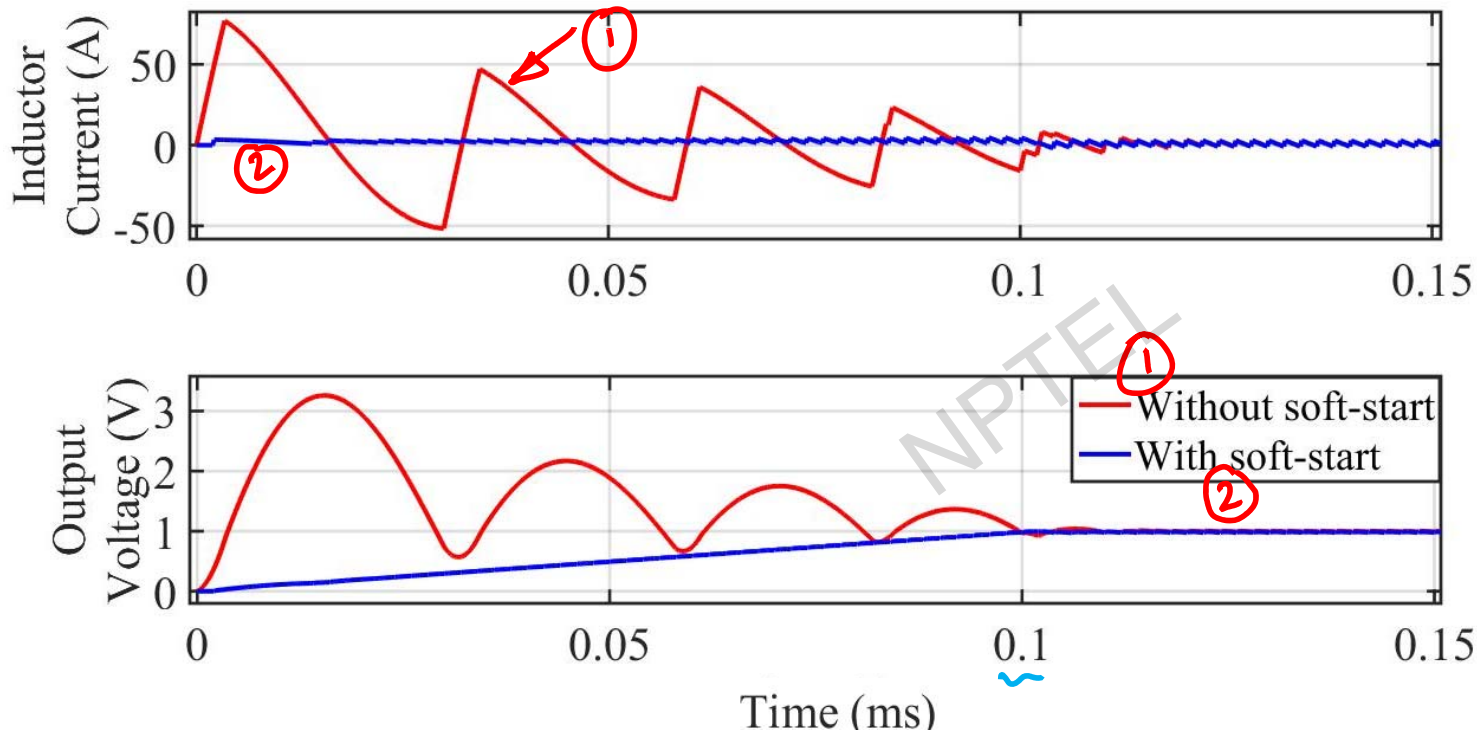


$V_{in}=12$; $R=1$; $V_m=10$; $K_p=30$; $K_i=20000$; $K_d=0.04$

PID Controller – Functionality

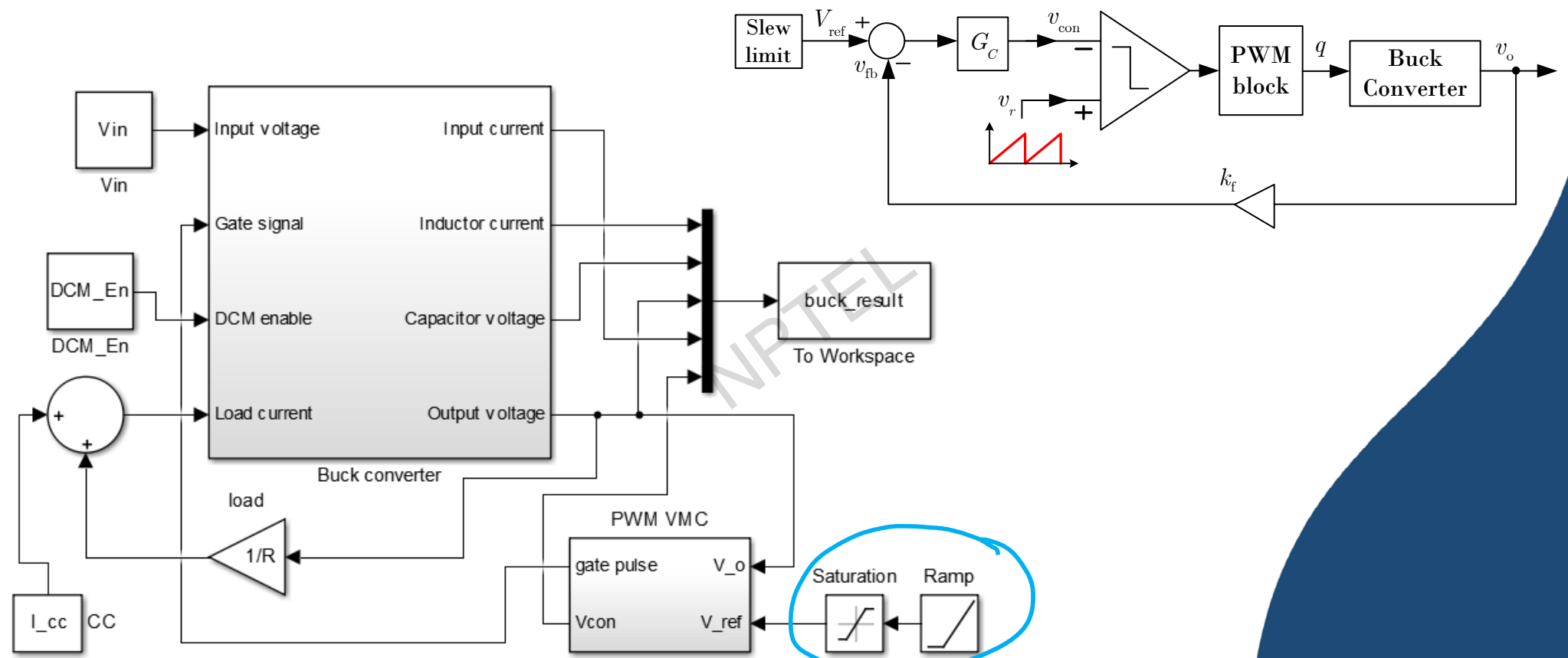
PID Gain	Percentage Overshoot	Settling Time	Steady-state Error
Increasing K_P	Increases ✓	Minimal impact	Decreases
Increasing K_I	Increases ✓	Increases ✓	Zero steady-state error ✓
Increasing K_D	Decreases ✓	Decreases ✓	<u>No impact</u>

Simulating using a Soft-Start Logic in VMC

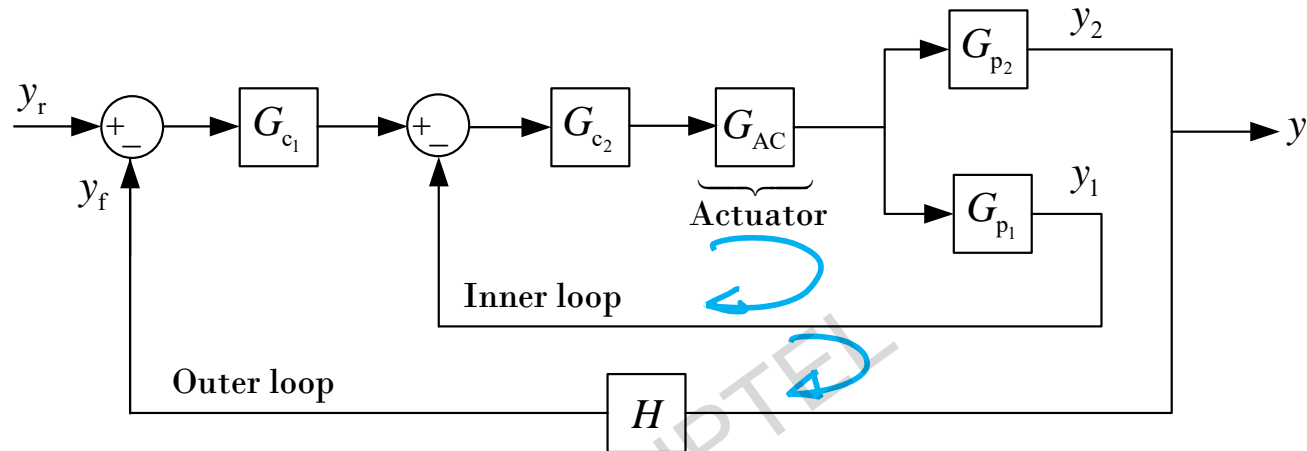


$V_{in}=12$; $R=1$; $V_m=10$; $K_p=30$; $K_i=20000$; $K_d=0.04$

MATLAB with Soft-Start in VMC



Basic Two Loop Output Feedback



Two loop control

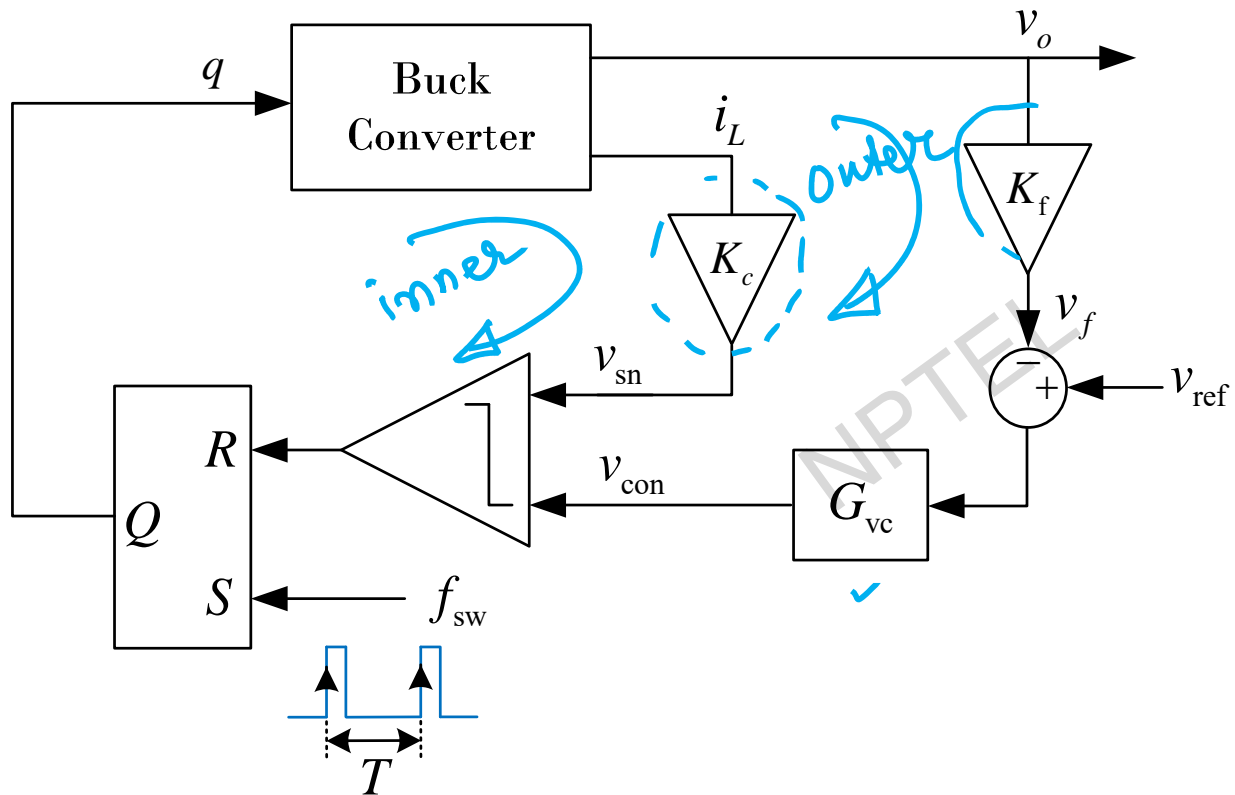
Master / slave control

Cascade control

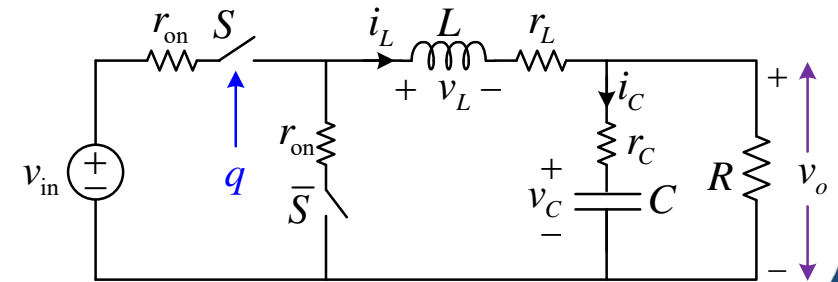
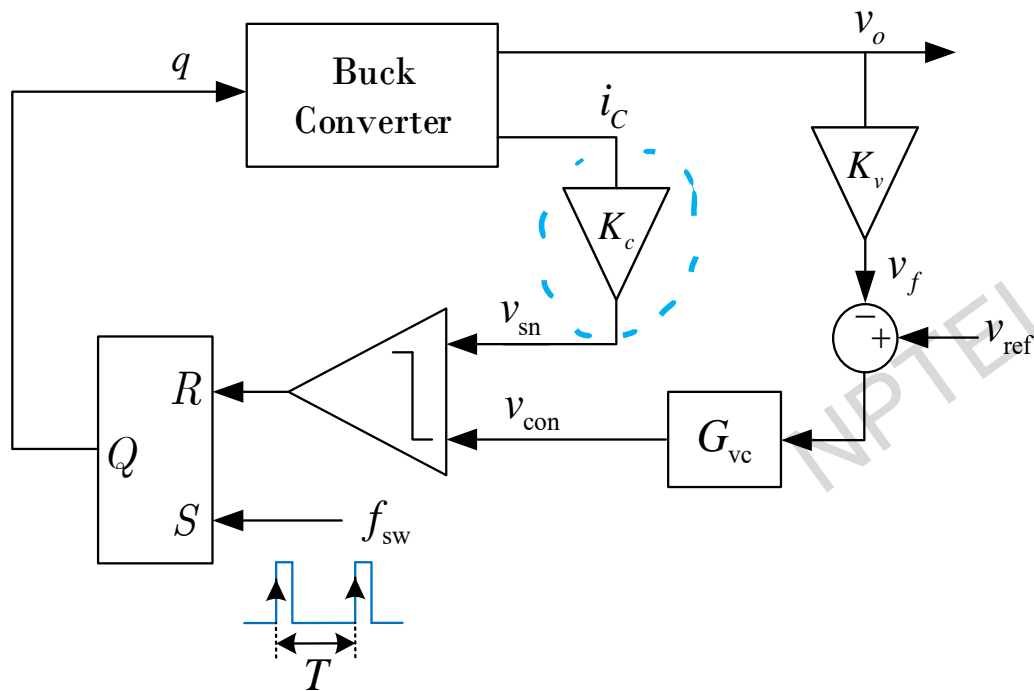
Two Loop Control in SMPC

- Outer loop → generally (output) voltage loop
- Inner loop:
 - Inductor current
 - Capacitor current
 - Derivative of output voltage
 - Ripple output voltage

Current Mode Control



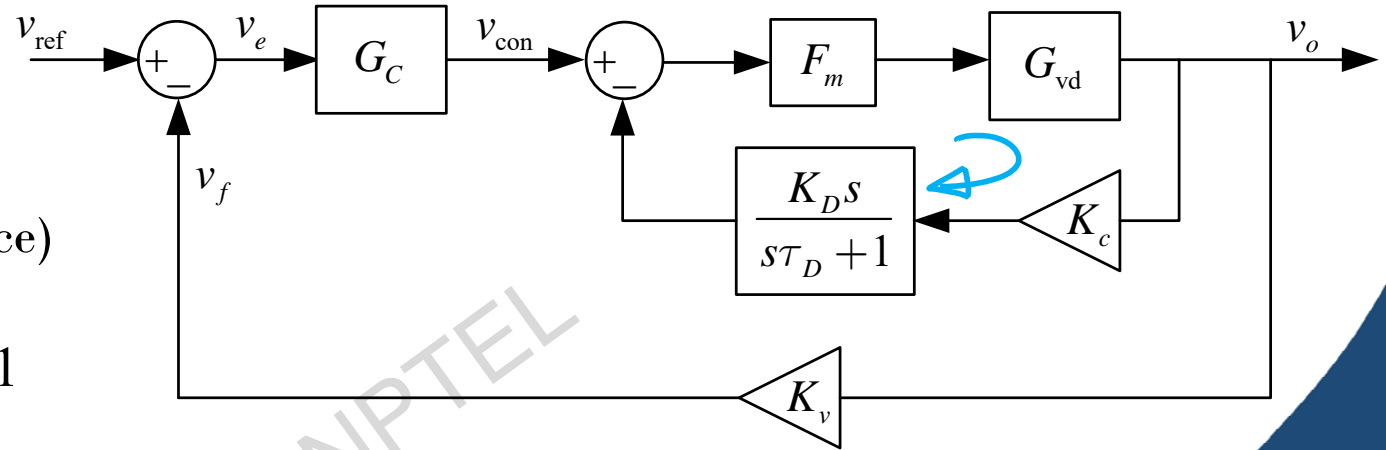
Capacitor current based Two Loop Control



Two loop Control using Voltage Derivative inner loop

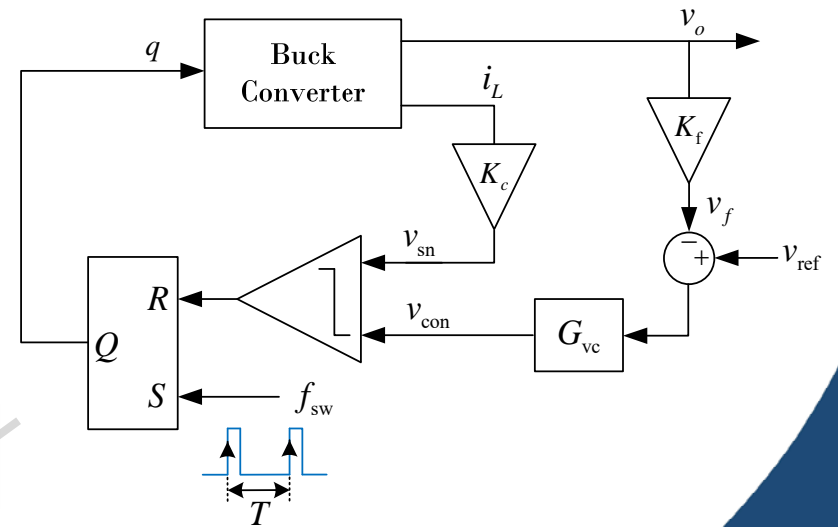
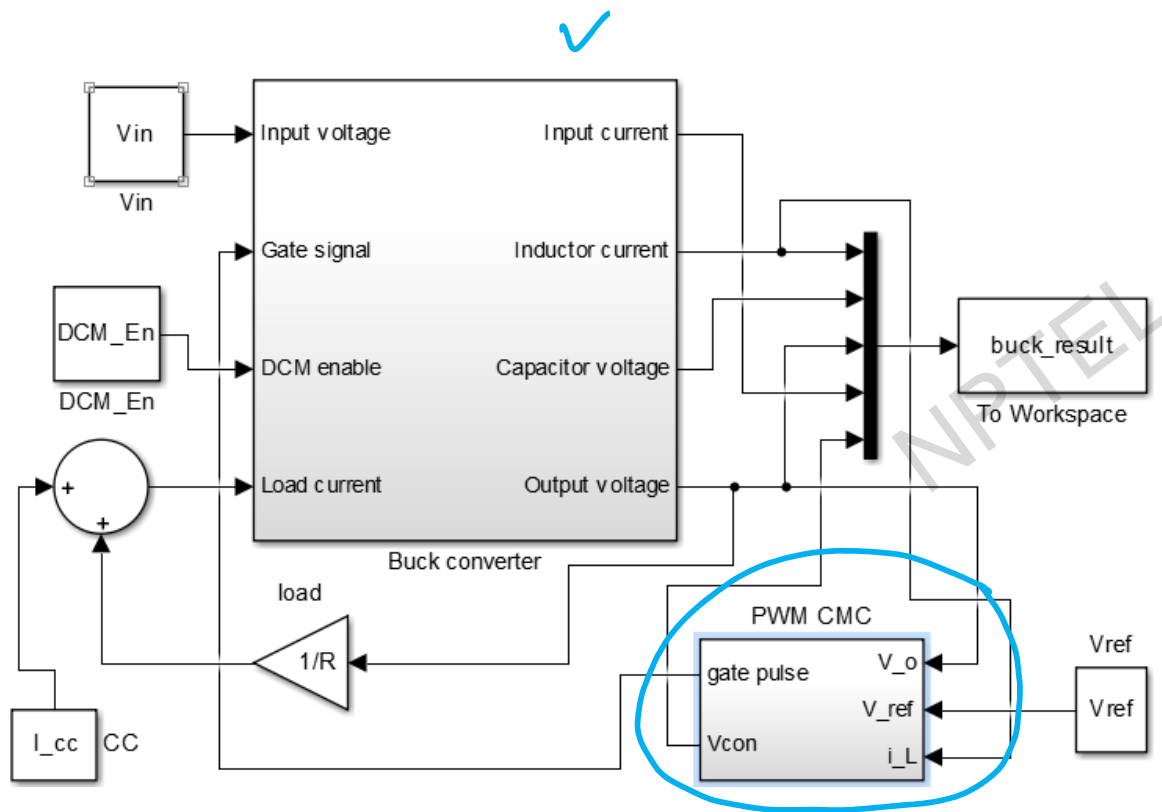
→ $K_D = C$
(Output Capacitance)

$$\tau_D = \frac{T}{50} \text{ (say), } K_c = 1$$

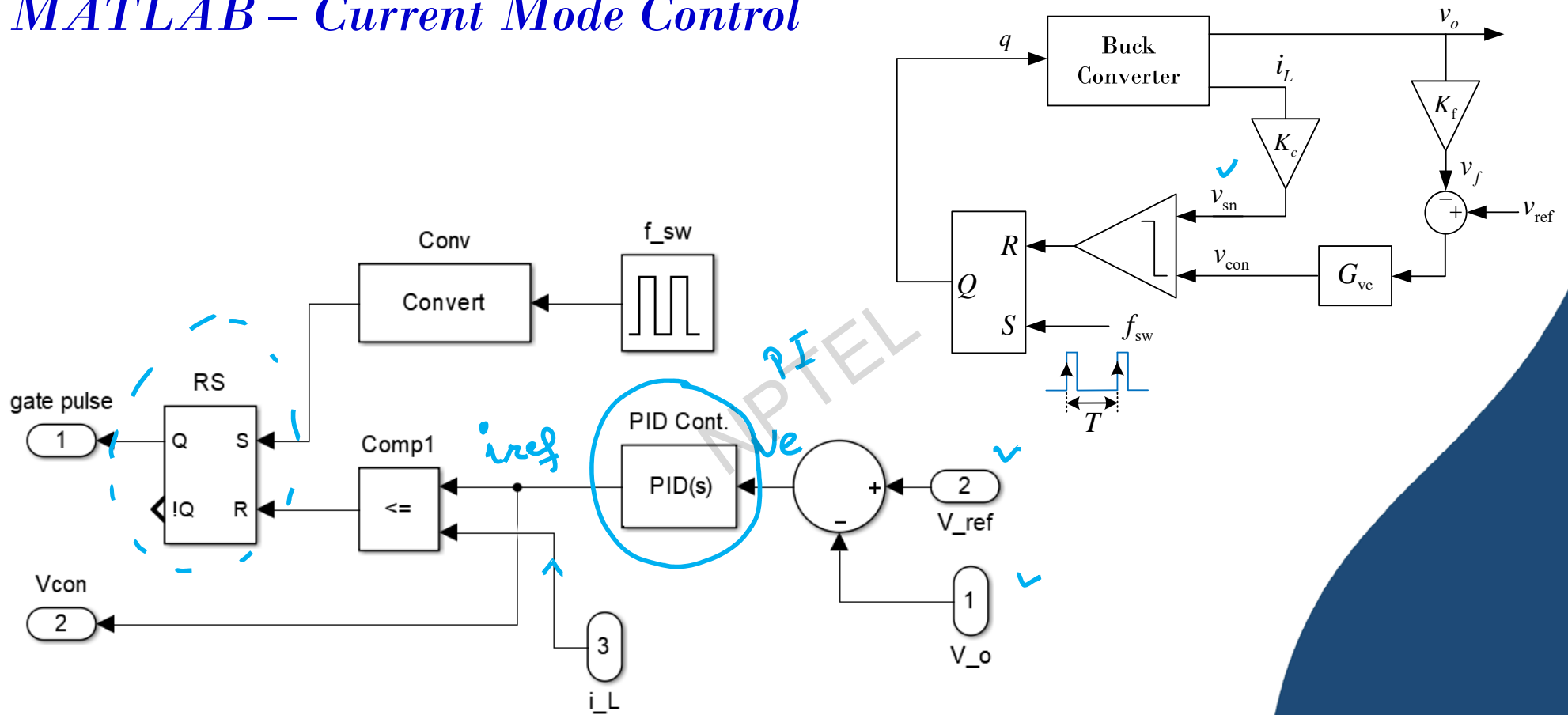


→ Use same voltage controller parameters as capacitor current and compare responses

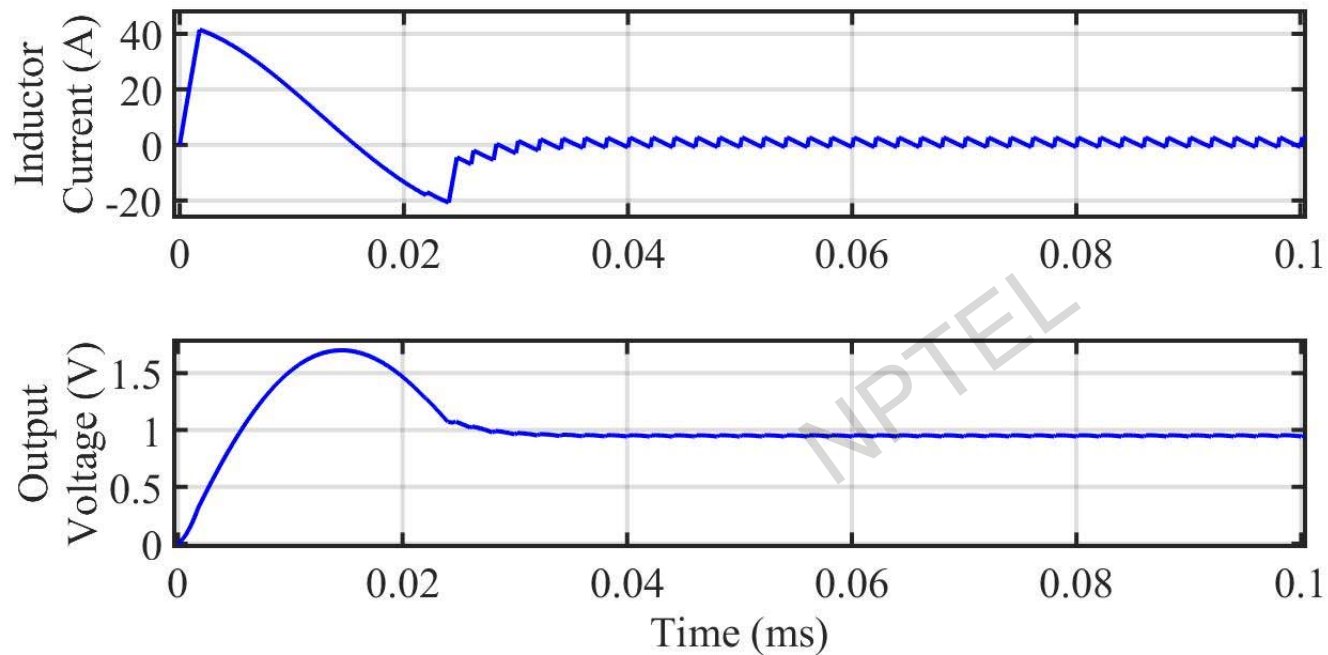
MATLAB – Current Mode Control



MATLAB – Current Mode Control



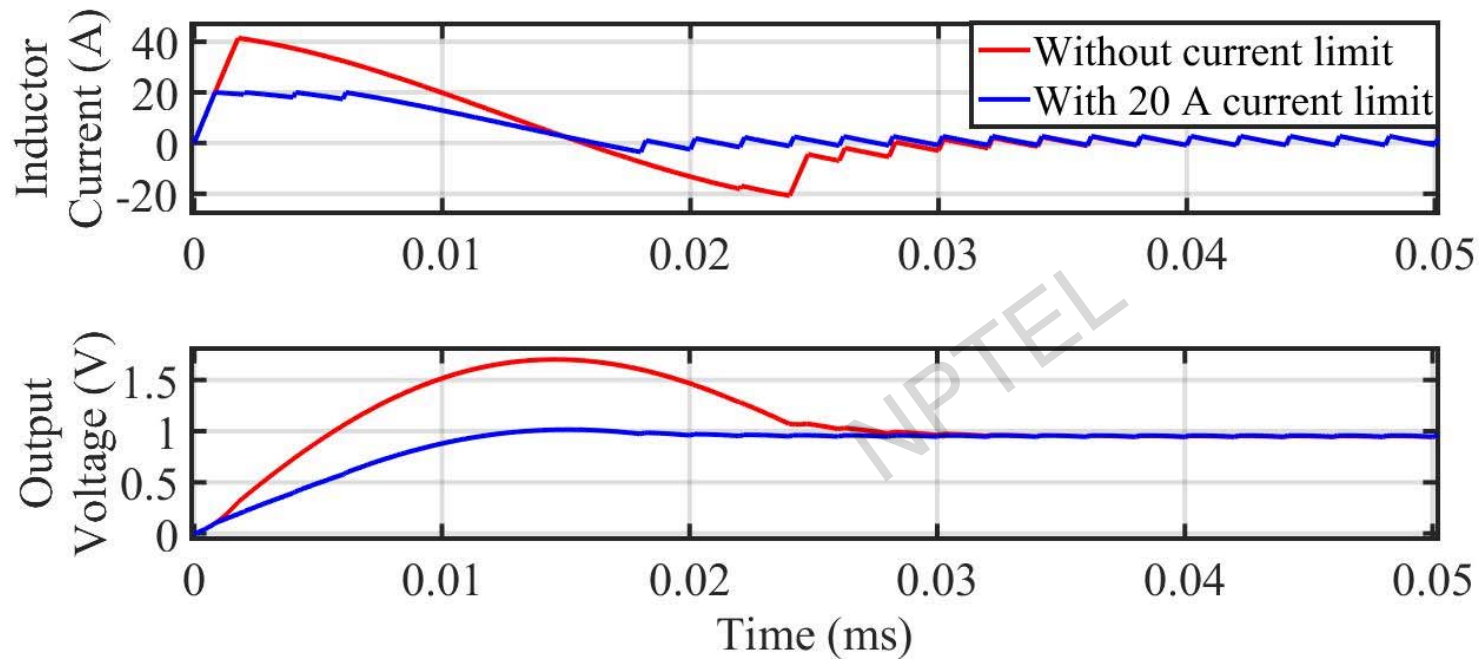
Simulating a Start-up Case Study under CMC



$$G_{vc}(s) = K_p + \frac{K_I}{s}$$

Vin=12; R=1; K_p=60; K_i=20000

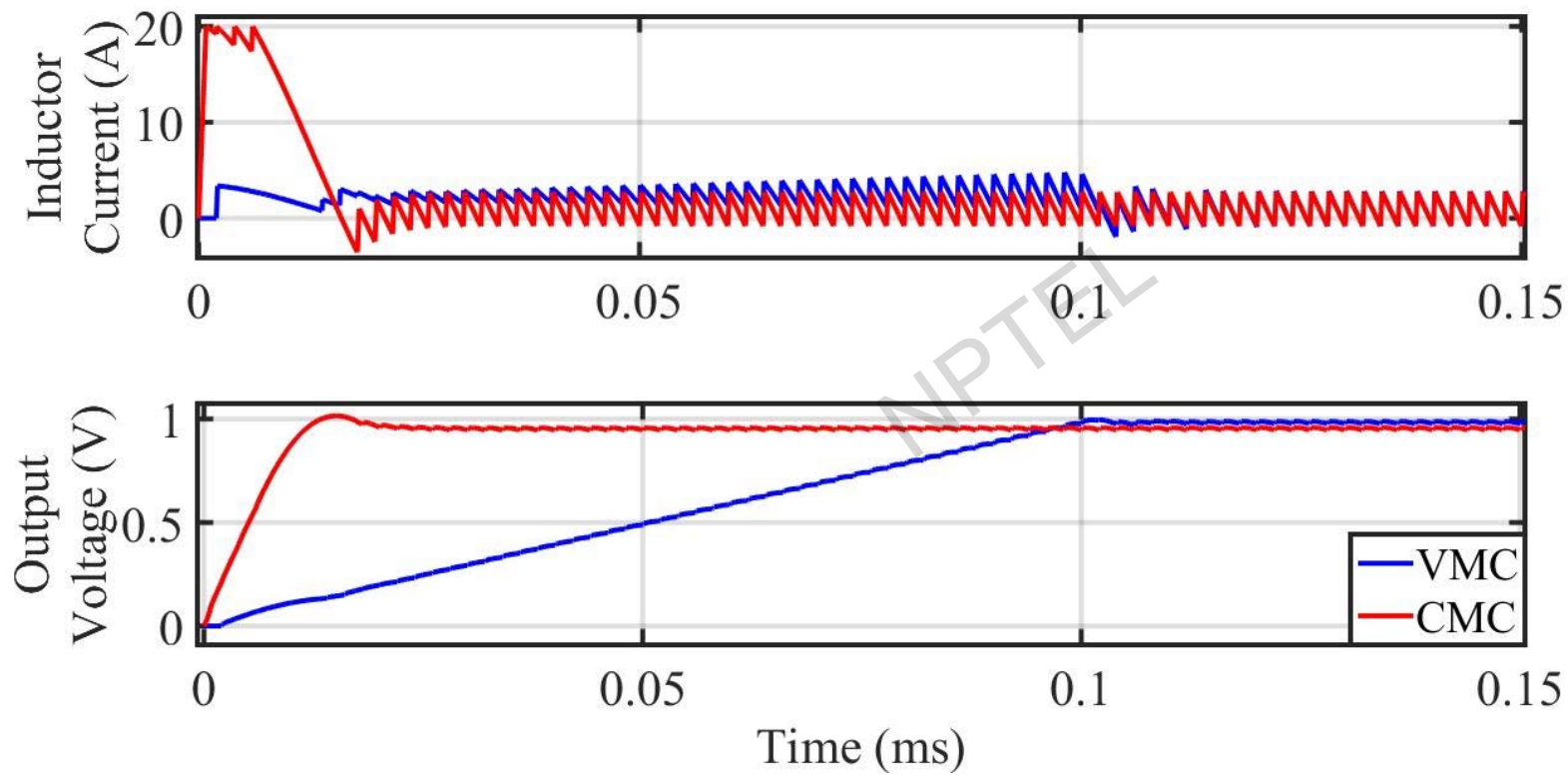
Simulating a Start-up with Current Limit under CMC



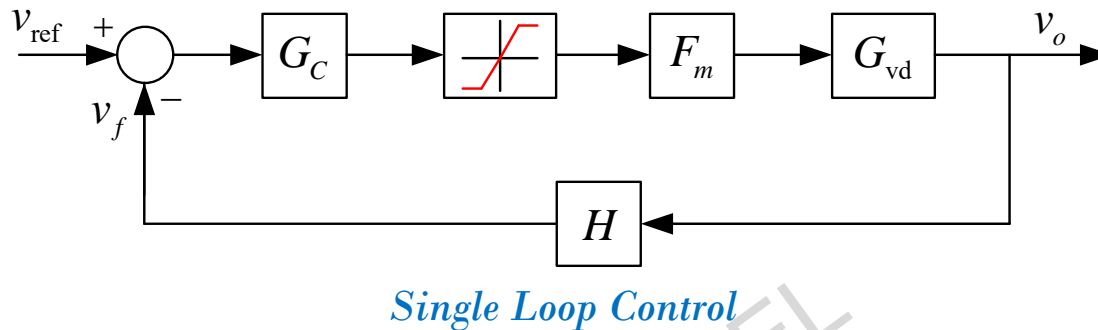
$$G_{vc}(s) = K_p + \frac{K_I}{s}$$

$$V_{in}=12; R=1; K_p=60; K_i=20000$$

Strat-up Logic Comparison – VMC vs. CMC



Limitations of Single Loop VMC



- No control over current !!!
- Compensation sensitive to operating conditions ✓
- Fault protection and start-up logics separately needed
- Difficult to optimize transient and start-up performance

Advantages of Two-Loop CMC

- Possibility of reduced-order system dynamics using time-scale separation
- Simplified controller design with improved robustness
- Higher bandwidth can be achieved without compromising phase margin
- But, sensor requirement increases in current based implementation ✓
- Existence of sub-harmonic instability over wide duty ratio range ✓

Summary

- Fixed-frequency single loop control – discussed
- Fixed-frequency two loop control methods – discussed
- MATLAB based implementation – demonstrated
- Advantages/limitations of feedback control methods – discussed



**THANK
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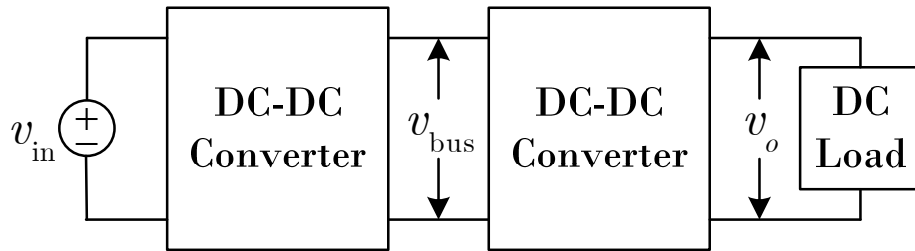
Module 03: Fixed Frequency Control Methods

Lecture 16: Feedback Control of Cascaded SMPCs

Concepts Covered

- Cascaded converter – intermediate bus architecture
- Concept of constant power load
- Instability and limit cycle oscillation
- Feedback control for active damping

Cascaded Converters and Applications



Examples

▪ LED driving

$$\begin{aligned} v_{in} &= 12 \text{ V} \\ v_{bus} &\in [30, 48] \text{ V} \\ v_o &= 12 \text{ V} \end{aligned} \quad \left. \vphantom{\begin{aligned} v_{in} &= 12 \text{ V} \\ v_{bus} &\in [30, 48] \text{ V} \\ v_o &= 12 \text{ V} \end{aligned}} \right\} \text{Head lamp load}$$

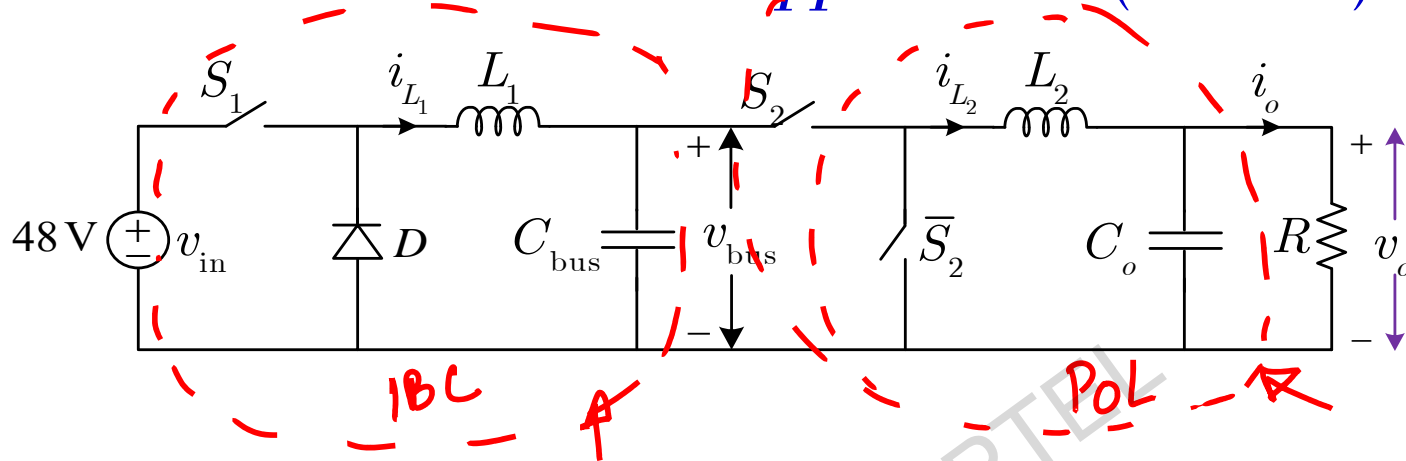
▪ Data center

$$\begin{aligned} v_{in} &= 48 \text{ V} \\ v_{bus} &\in [6, 18] \text{ V} \\ v_o &= 1 \text{ V} \end{aligned} \quad \left. \vphantom{\begin{aligned} v_{in} &= 48 \text{ V} \\ v_{bus} &\in [6, 18] \text{ V} \\ v_o &= 1 \text{ V} \end{aligned}} \right\} \text{Processor load}$$

Cascaded Converters and Applications (contd...)

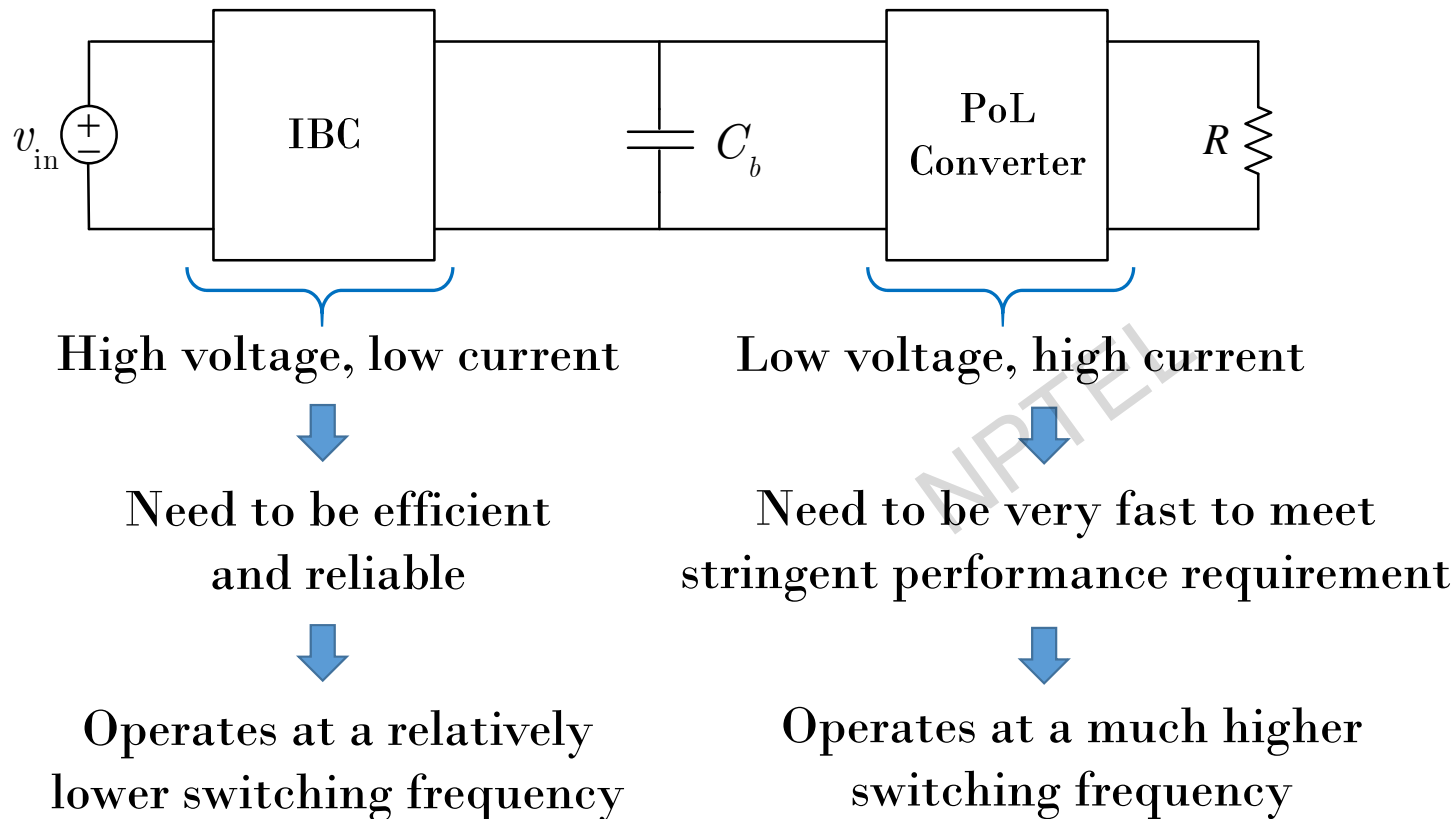
- Consider the data center example
(intermediate bus architecture)
- Two cascaded buck converters
 - Input side buck → known as intermediate bus converter (IBC)
 - Output side buck → known as point of load (PoL) converter

Cascaded Converters and Applications (contd...)

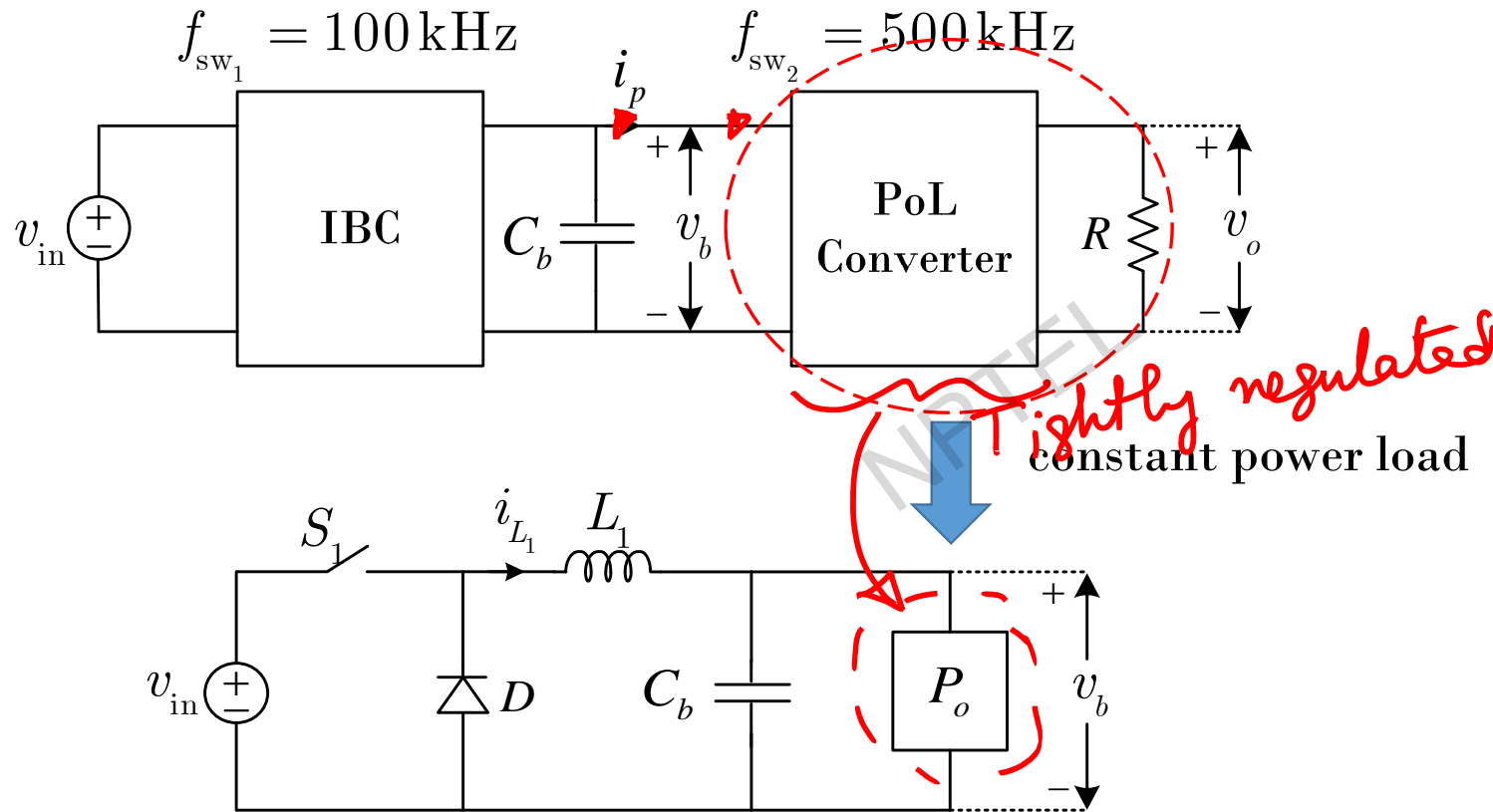


- Use earlier simulation models of a conventional buck converter and a synchronous buck converter
- Configure the above files to show a cascaded converter

Dynamics of Cascaded Converter



Constant Power Load



Simulation Case Study

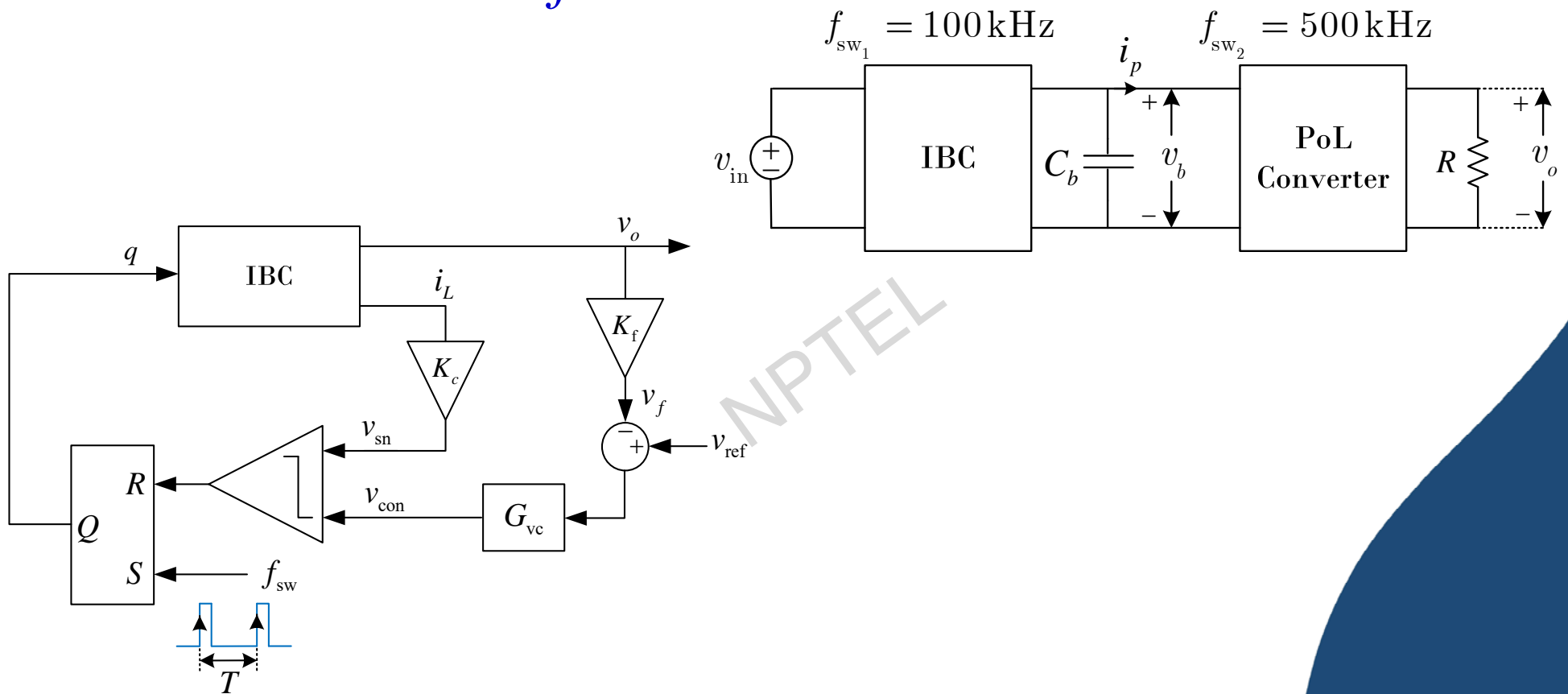
■ Case 1:

- Use two separate converters (IBC and PoL converter)
- Operate IBC in open loop at $f_{sw_1} = 100\text{ kHz}$
- Operate PoL converter under CMC at $f_{sw_2} = 500\text{ kHz}$

■ Case 2:

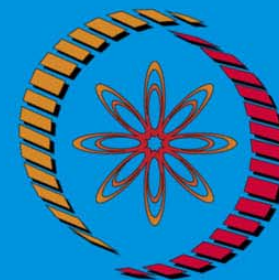
- Keep the same IBC configuration
- Replace PoL converter using a CPL where $P_o = v_o i_o$

Current Mode Control of IBC



Summary

- Cascaded dc-dc converters – Plug and play MATLAB model
- Origin of constant power load
- Nature of damping and existence of limit cycle oscillations
- Active damping using current mode control



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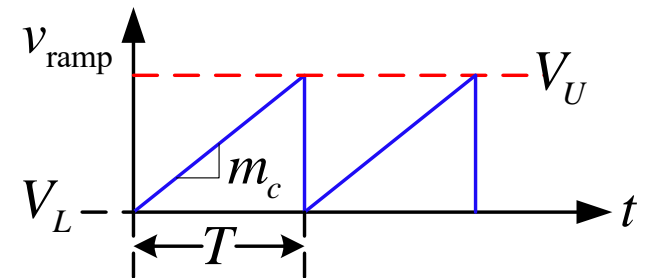
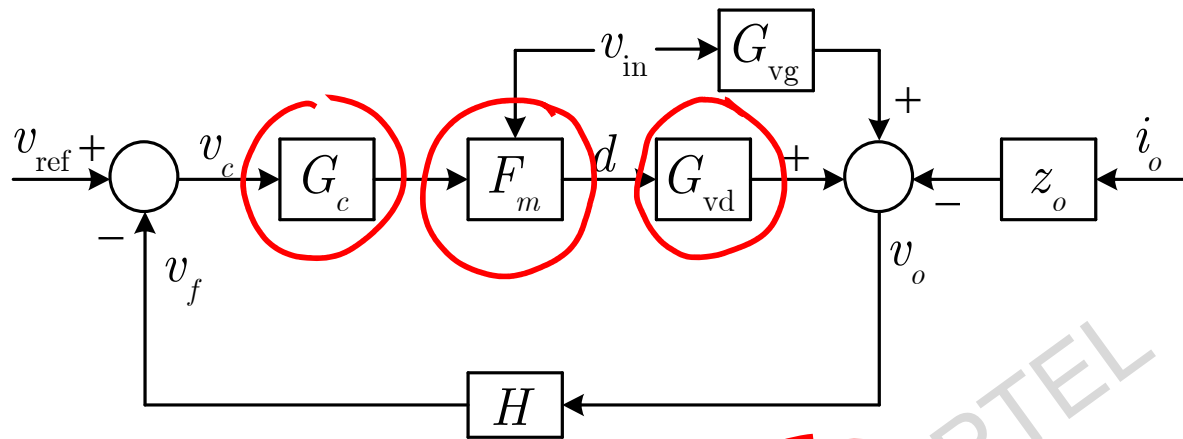
Module 03: Fixed Frequency Control Methods

Lecture 17: Combined feedback/feedforward control

Concepts Covered

- Input voltage feedforward in VMC
- Load current feedforward in CMC
- Droop control and applications

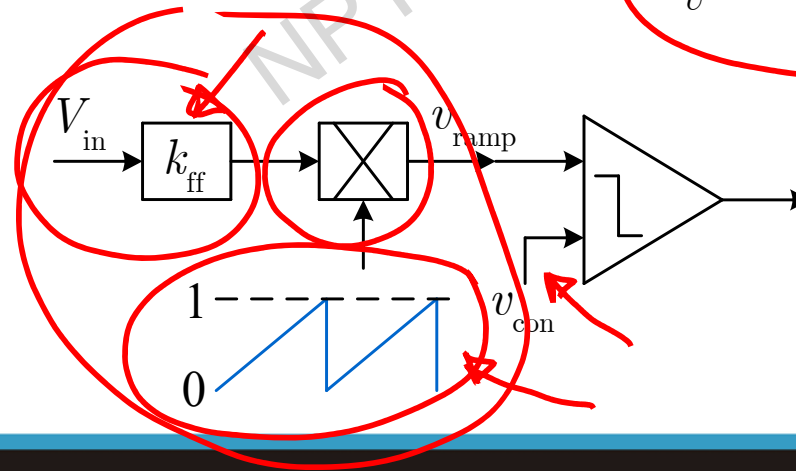
Input Voltage Feedforward in VMC



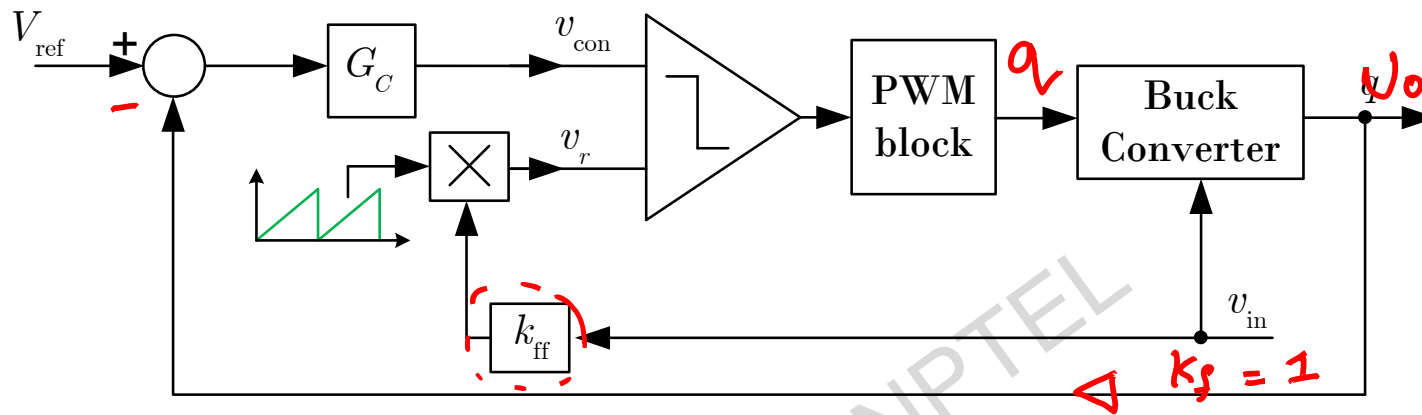
$$V_U = k_{\text{ff}} V_{\text{in}}$$

$$F_m = \left(\frac{1}{m_c T} \right)$$

$$m_c = \frac{V_U - V_L}{T}$$



Input Voltage Feedforward in VMC



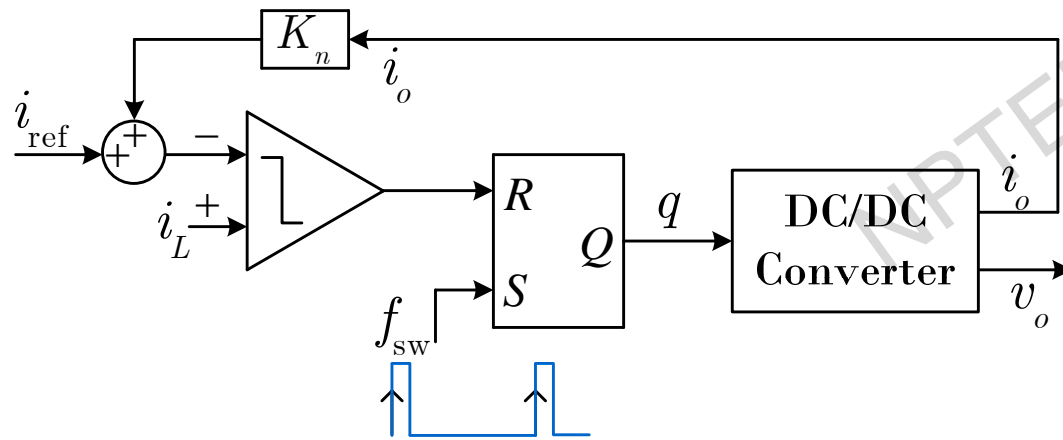
- Simulate Line Transient Response with and without feedforward

Simulate DC-DC converter

- Without feedforward
 - With feedforward
- } Under VMC
- Show that CMC offers inherent input voltage feedforward
by virtue of using inductor current

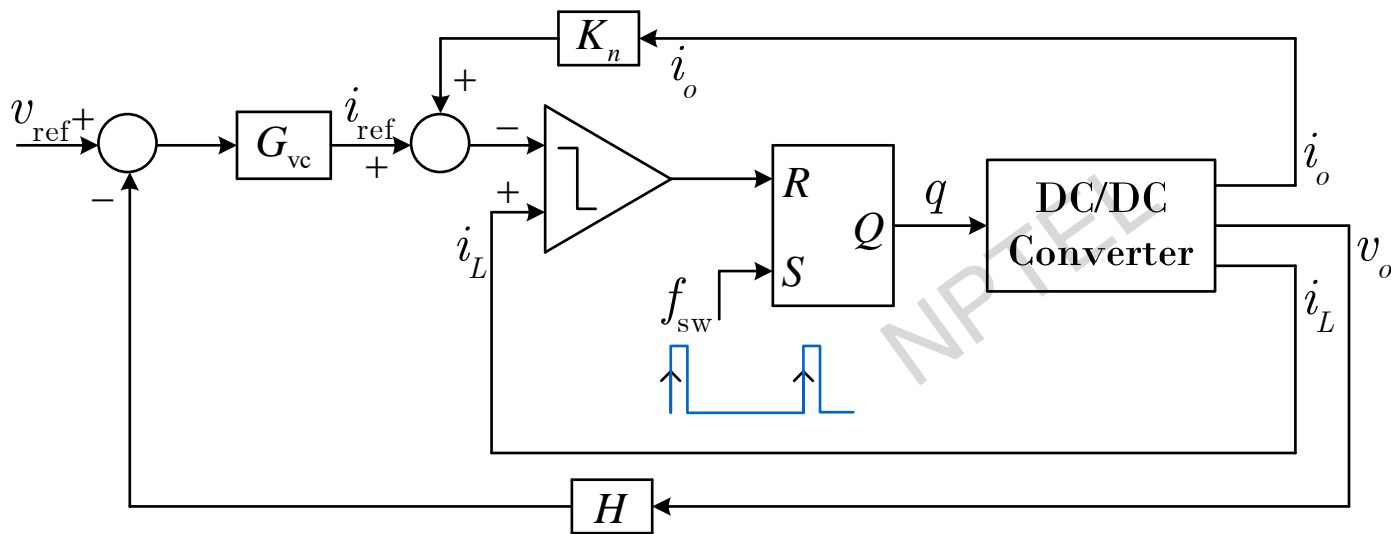
Load Current Feedforward in CMC

Open outer-loop

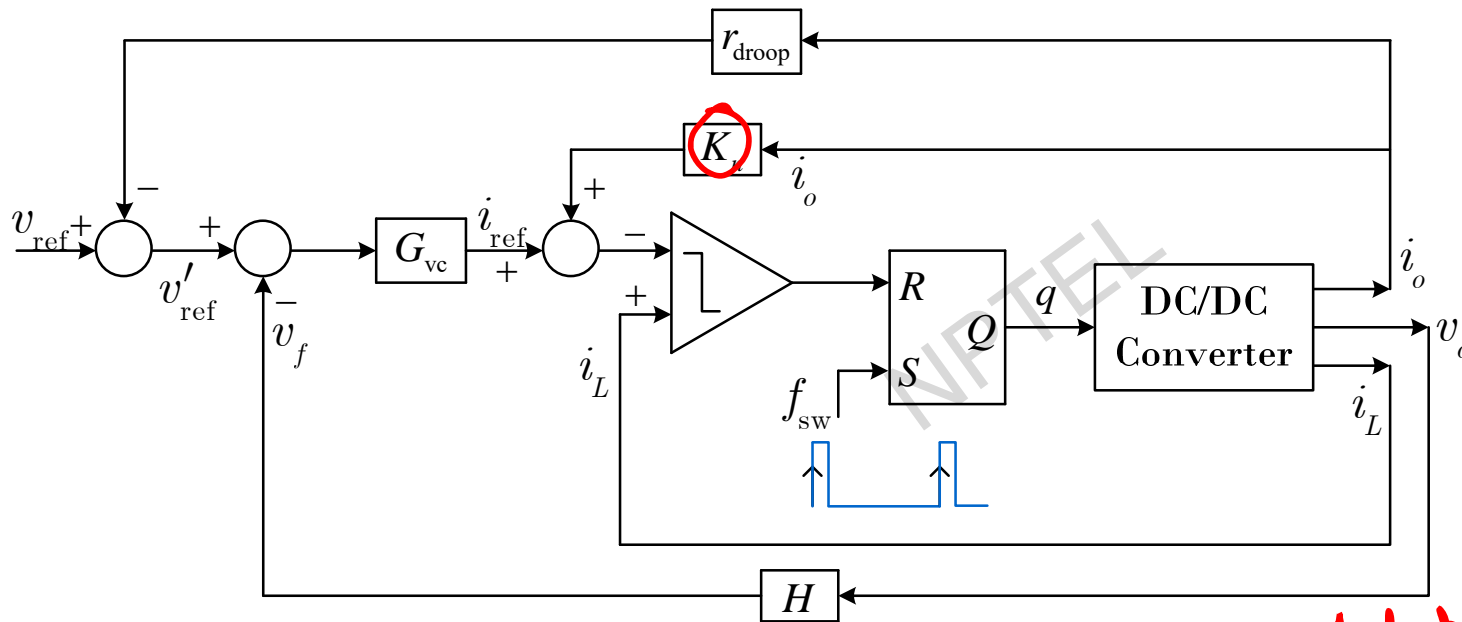


Load Current Feedforward in CMC

Step 1



Step 2



$$k_n = 1 \text{ buck}$$

$$k_n = \frac{V_{mg}}{V_{in}} \text{ boost}$$

AVP \rightarrow Adaptive voltage positioning

Droop Control and Applications

- Adaptive voltage positioning in VRM application
- Nearly resistive output impedance
- DC microgrid applications
- Energy optimization in IBA

*Cut down transient
effect
Reduces current overshoot
undershoot*

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Summary

- Combined feedback and feedforward control offers excellent disturbance rejection and fast transient performance
- Suitable circuits needed either to sense or estimate load current
- More design aspects to be discussed later



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CONTROL AND TUNING METHODS IN SMPCs

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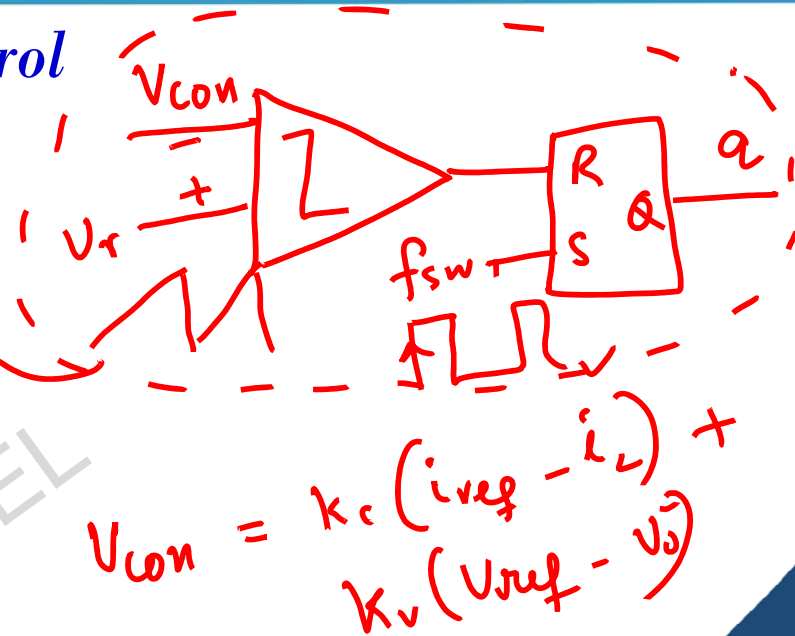
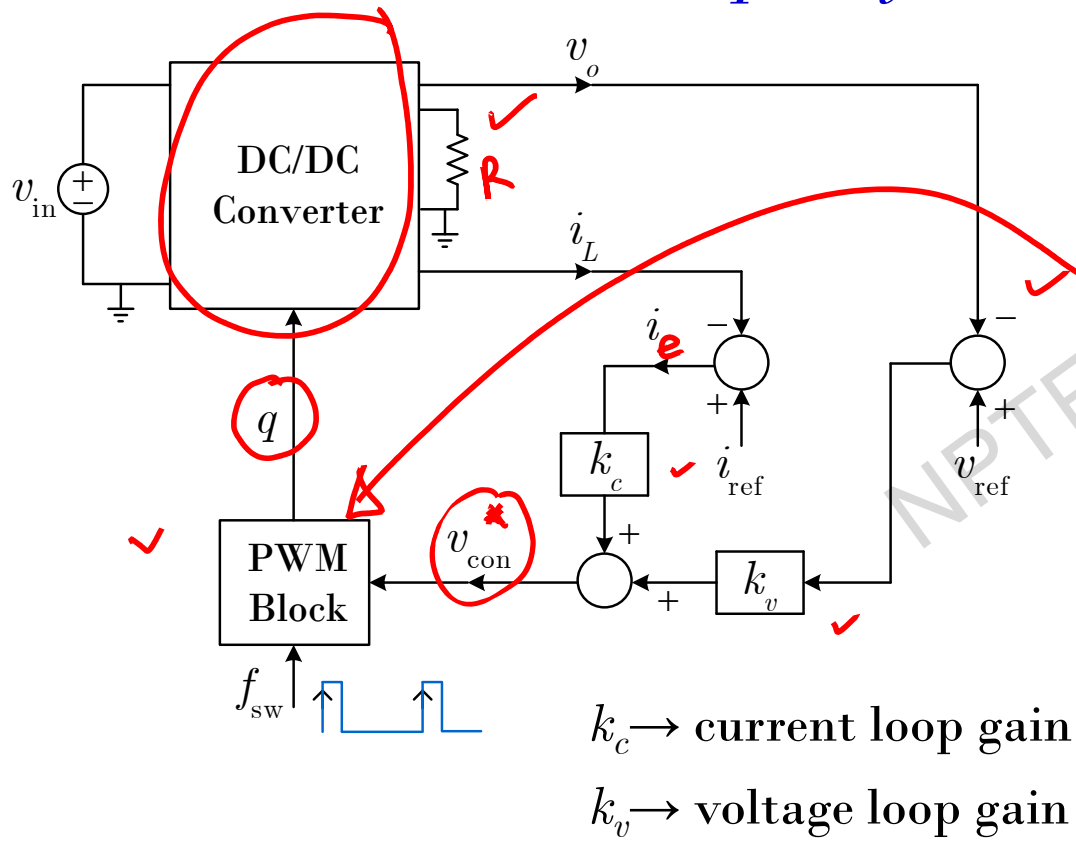
Module 03: Fixed Frequency Control Methods

Lecture 18: State feedback control

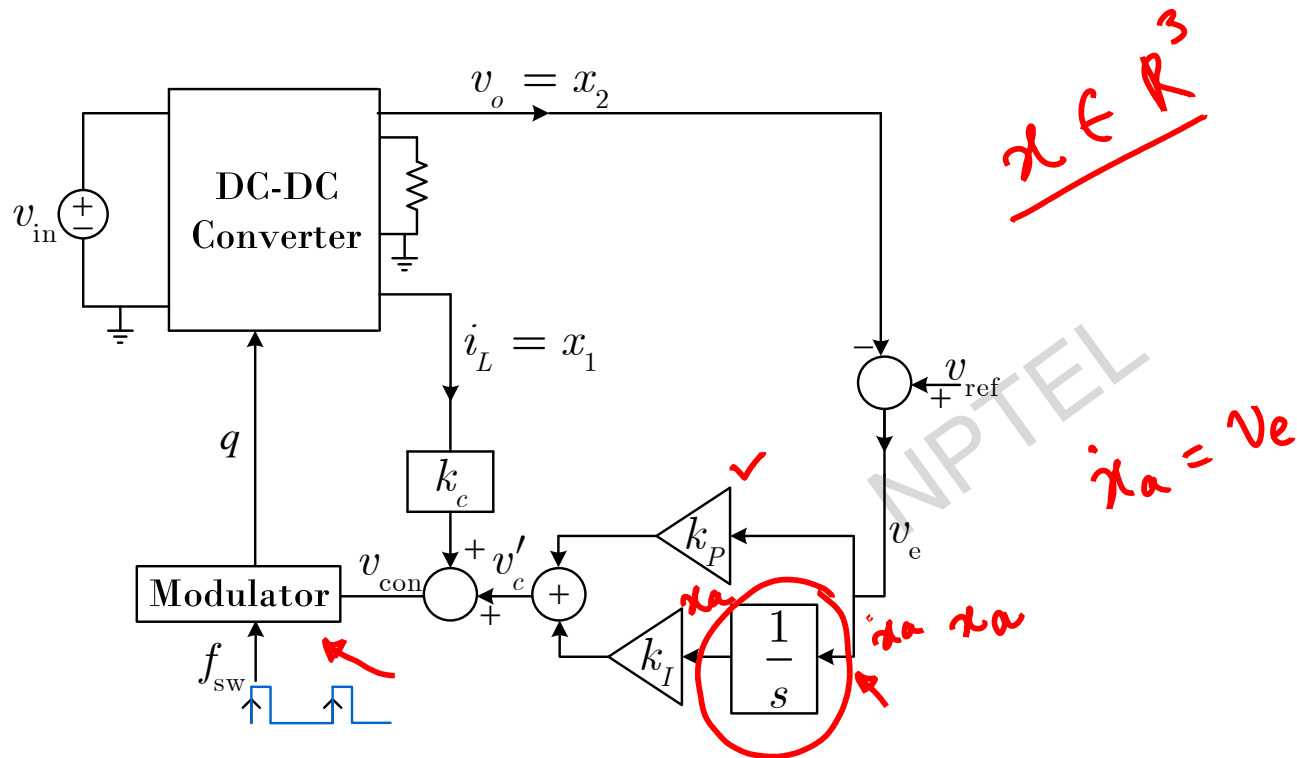
Concepts Covered

- Implementation of state feedback PWM control
- Linking CMC and state feedback control
- Alternative form of state feedback
- Multivariable state feedback control in IBA
- Observer based state feedback control

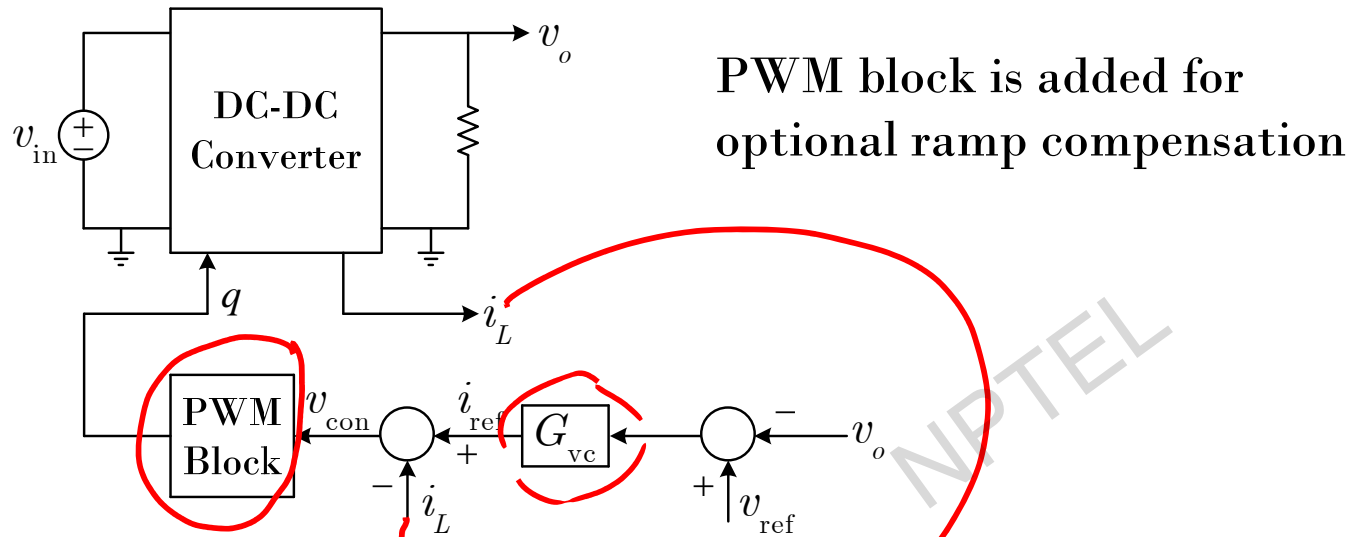
State Feedback Fixed Frequency Control



Augmented State Feedback Control



Current Mode Control (CMC) Implementation



For a PI voltage controller

$$G_{vc} = \underline{k_{vp}} + \frac{k_{vi}}{s}, \quad i_{ref} = \underline{k_{vp}}(v_{ref} - v_o) + \underline{k_{vi}} \int (v_{ref} - v_o) dt$$

Analogy between state feedback control and CMC

State feedback control

$$\underline{v_{con}} = k_v (v_{ref} - v_o) + k_c (\overset{x}{i_{ref}} - i_L)$$

Set

$$k_v = k_P; \quad k_c = 1$$

$$\overset{x}{i_{ref}} = k_I \int (v_{ref} - v_o) dt$$

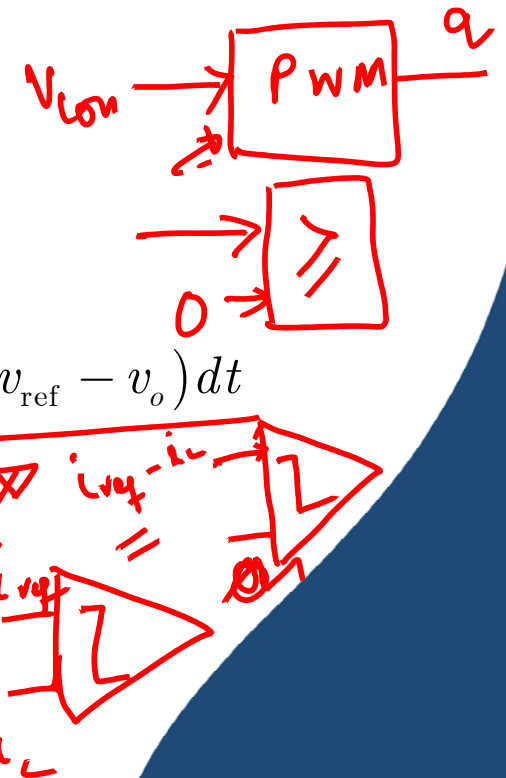
CMC

$$\underline{v_{con}} = \overset{x}{i_{ref}} - \underline{i_L}$$

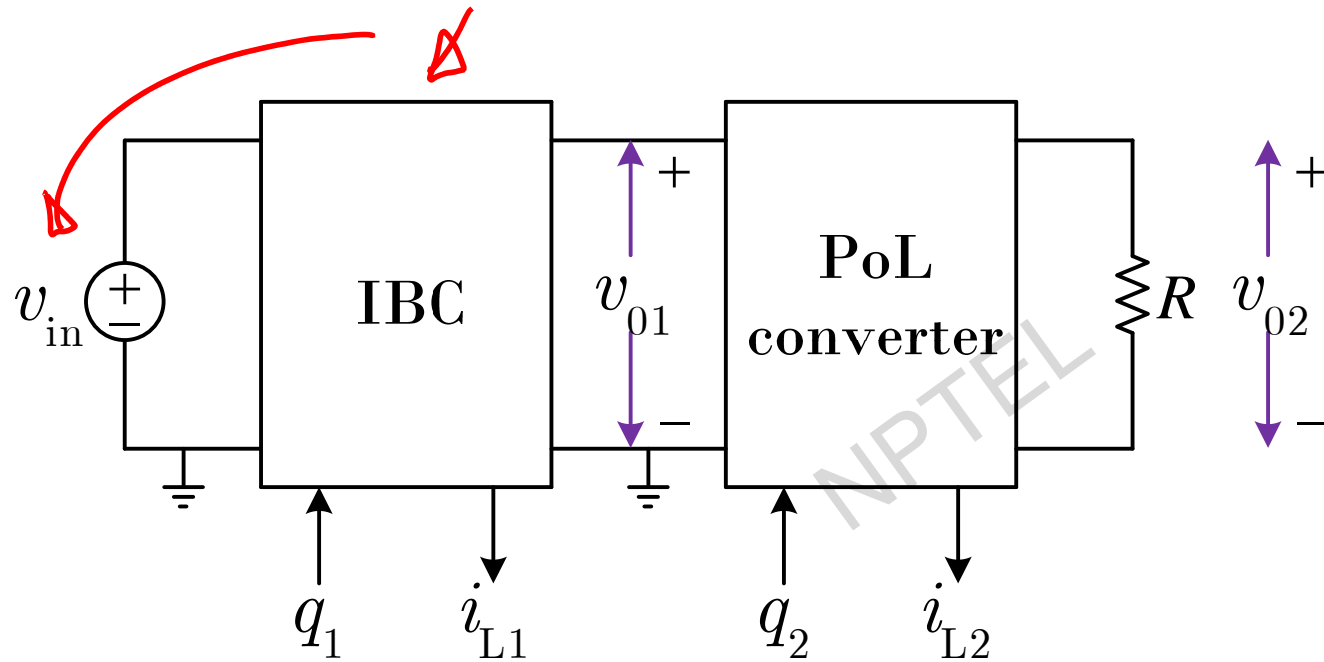
$$\underline{i_{ref}} = k_{vp} (v_{ref} - v_o) + \underbrace{k_{vi}}_{\text{circled}} \int (v_{ref} - v_o) dt$$

$$k_{vp} = k_P$$

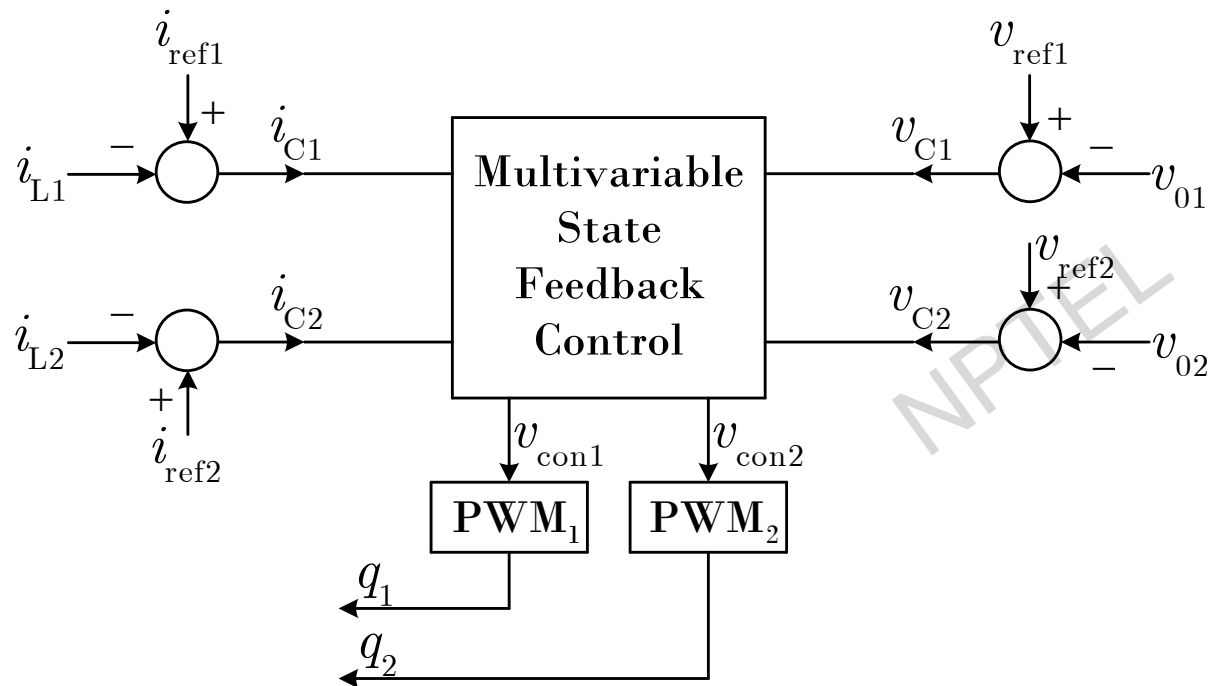
$$k_{vi} = k_I$$



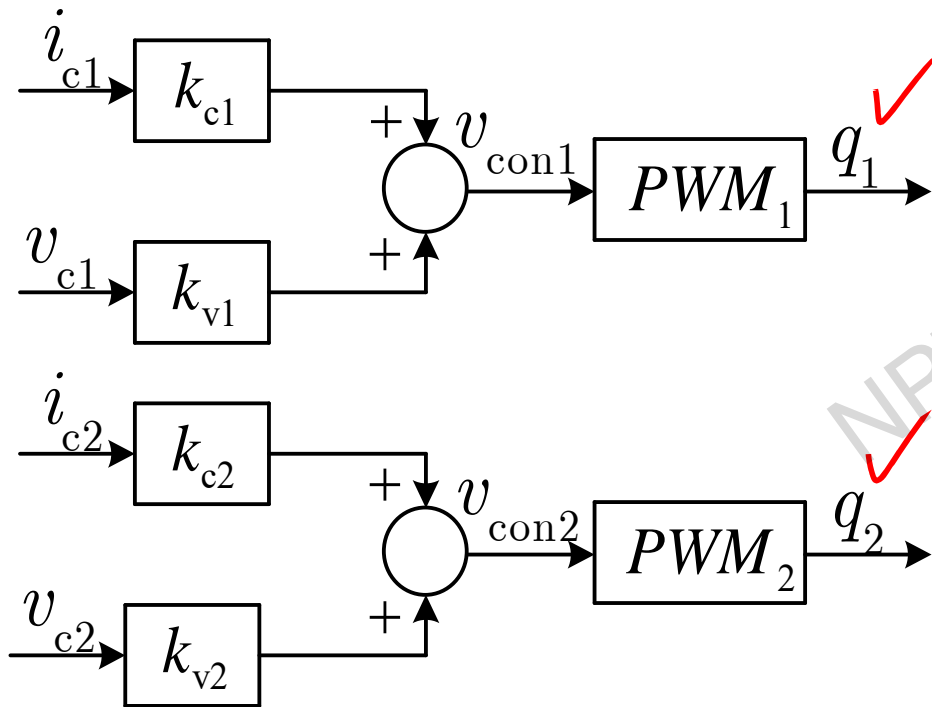
Multivariable State Feedback Control



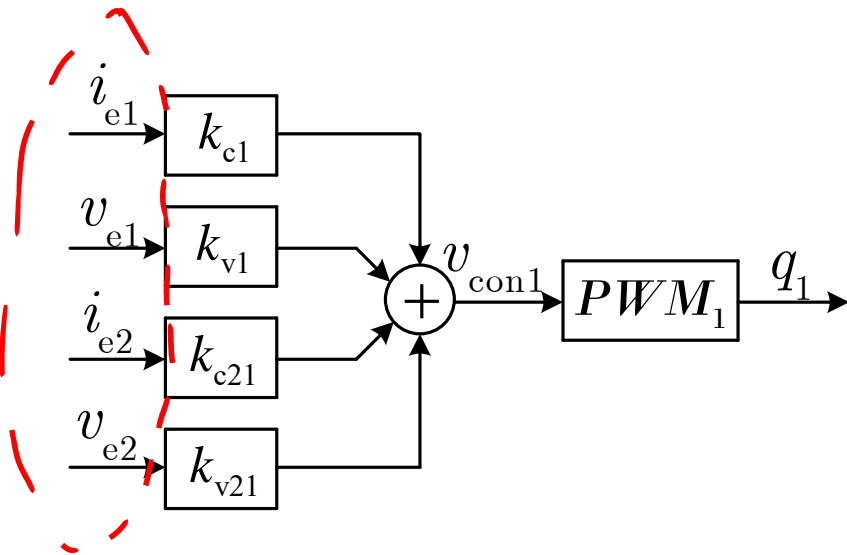
Multivariable State Feedback Control



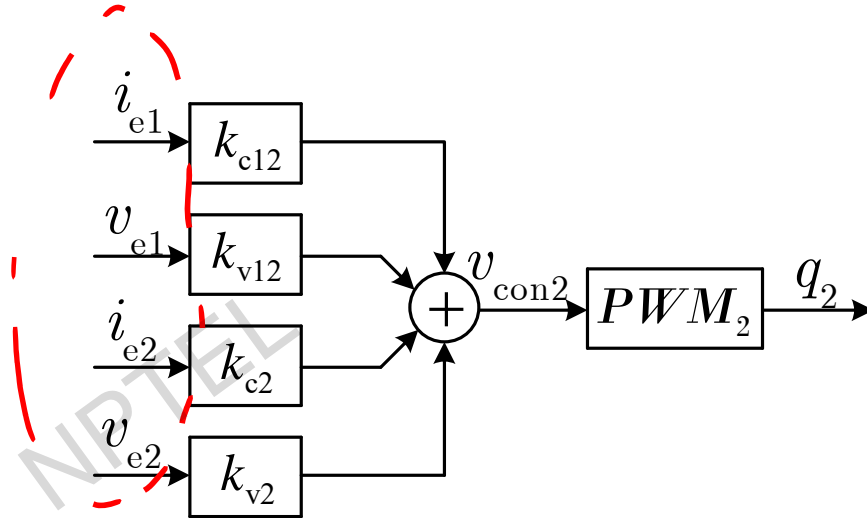
Two Single Degree of Freedom Control



Multivariable Control

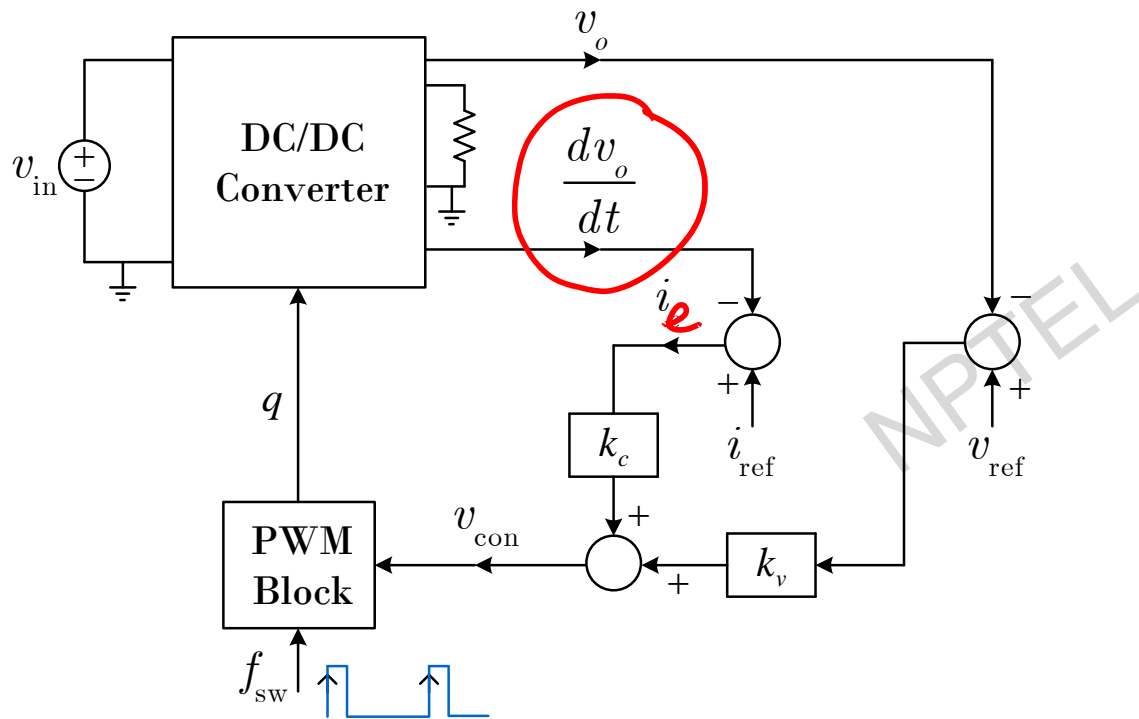


$\left. \begin{matrix} k_{c21} \\ k_{v21} \end{matrix} \right\}$ cross terms

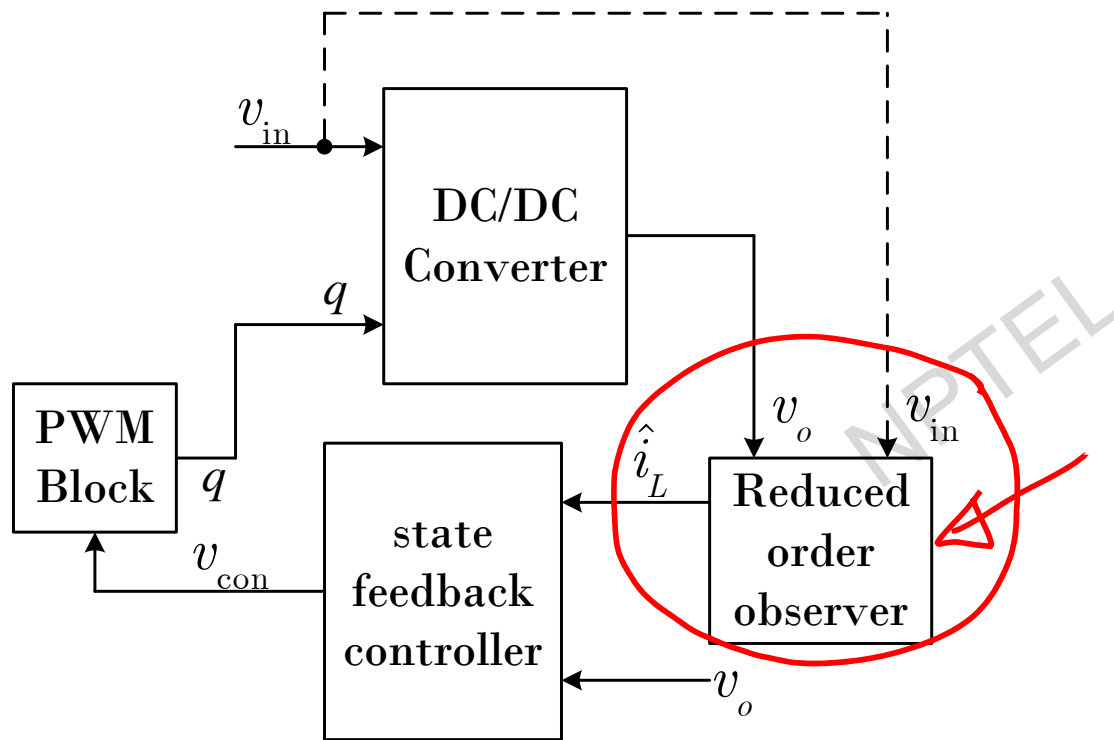


$\left. \begin{matrix} k_{c12} \\ k_{v12} \end{matrix} \right\}$ cross terms

Alternative Form of State Feedback Control



Observer Based State Feedback Control



Summary

- Introduction to state feedback control
- Linking state feedback control with CMC
- State feedback control in cascaded converters
- Multivariable state feedback control
- Alternative state feedback control structures



**THANK
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