Heuristic Analysis

To come up with a heuristic for evaluation function, I tried to consider the parameters which can lead to more winning for the computer player if game is continued to the end.

As "sample_player.py" is suggesting, some of the parametres which may be important are:

1-Number of available moves for the computer player, the greater the better.

2-Number of available moves for the opponent, the smaller the better.

3-Distance from the center of game board, the smaller the better.

4-Another parameter I thought can show if the computer player is in good state, is how many of the next moves is in common between computer player and the opponent. The parameter is named "intersect num" and the smaller the better.

```
-custom_score: 2 * own_moves - opp_moves
```

This is similar to improved score but gives more weight to the states which computer player had more moves.

```
-custom_score_2: 5 * own_moves - 10 * opp_moves - 3 * intersect_num - 2 * radius
```

For this score, I tried to give positive and negative scores to the above parameters and tried different coefficients to get higher result than AB Improved player.

```
-custom_score_2: (0.1 + own_moves * own_moves ) / ((0.1 + opp_moves) * (radius +0.1) * (intersect_num + .1) )
```

For this score, I used the above parameters, but instead of adding and subtracting them, I used multiplication and division to calculate value for each state.

Using the above custom scores I ran the tournament 10 times which the result table are shown below the report. The average win rate based on the tables are:

```
-Average win rate for AB_Custom: 67.1%
-Average win rate for AB_Custom_2: 70.7%
-Average win rate for AB_Custom_3: 69%

-Average win rate for AB_Custom against MM_Improved: 64%
-Average win rate for AB_Custom against AB_Improved: 49%

-Average win rate for AB_Custom_2 against AB_Improved: 54%
-Average win rate for AB_Custom_2 against AB_Improved: 54%
-Average win rate for AB_Custom_3 against MM_Improved: 55%
-Average win rate for AB_Custom_3 against AB_Improved: 55%
-Average win rate for AB_Custom_3 against AB_Improved: 55%
```

Based on the above average values and the tables below, although AB_Custom_3 is close to AB_Custom_2 too but I choose AB_Custom_2 for the following reasons:

1- It has the best average performance among the 3

2- It wins in 96% of the games against other players with the win rate greater than 50%, showing stability in winning.

3— Although it is more complex than AB_Improved, but it is still fairly simple and can go deep enough to have better performance than AB_Improved in 54% of the time. 4— It considers various parameters from computer player moves, opponent moves and their intersection, and also the radius, each of which have positive or negative effect on the state of the game and tries to evaluate each state considering all of those parameters.

Match #	Opponent		roved	_	ustom	AB_Cus	_	AB_Cus	_
		Won			Lost	Won		Won	Lost
1	Random	10	0	8	2	10	0	10	0
2	MM_Open	5	5	8	2	6	4	6	4
3	MM_Center	8	2	10	0	10	0	9	1
4	MM_Improved	7	3	5	5	8	2	7	3
5	AB_0pen	3	7	7	3	8	2	5	5
6	AB_Center	4	6	5	5	4	6	8	2
7	AB_Improved	4	6	5	5	6	4	6	4
	Win Rate:	58	. 6%	68	.6%	74.	3%	72.	. 9%
Match #	Opponent	ΔR Tmr	oroved	AR Cı	ustom	AR Cus	stom_2	AB_Cus	stom 3
naccii π	орропсис		Lost	Won			Lost	Won	. —
1	Random	7	L031	10	2030	9	1	10	2031
2	MM_Open	5	5	7	3	5	5	5	5
3	MM_Center	9	3	9	3	7	3	8	2
4	MM_Improved	5	5	7	1	6	4	6	4
5	AB_Open	5	, 5 5	6	3 4	7	3	4	6
6	AB_open	5	5	6	1 1 1 4	6	4	5	5
7	AB_Improved	6	1 4	5	l 5	6	4	6	1 4
	Win Rate:	60	. 0%	71	.4%	65.	7%	62.	. 9%
Match #	Opponent	AB_Imp			ustom	AB_Cus		AB_Cus	_
		Won	Lost	Won	Lost	Won	Lost	Won	Lost
1	Random	10	0	9	1	9	1	8	2
2	MM_Open	4	6	9	1	9	1	8	2
3	MM_Center	6	4	8	2	8	2	8	2
4	MM_Improved	6	4	6	4	8	2	6	4
5	AB_0pen	6	4	4	6	7	3	5	5
6	AB_Center	4	6	3	7	7	3	5	5
7	AB_Improved	6	4	4	6	5	5	7	3
	Win Rate:	60.0%		61.4%		75.7%		67.1%	
Match #	Opponent		roved Lost		ustom Lost		stom_2 Lost	AB_Cus Won	stom_3 Lost

4									
1	Random	9	1	10	0	10	0	10	0
2	MM_Open	7	j 3	6	j 4	7	j 3	9	j 1
3	MM_Center	6	j 4	8	j 2	7	j 3	7	j 3
4	MM_Improved	7	3	5	j 5	6	j 4	8	j 2
5	AB_0pen	3	7	7	3	6	i 4	6	j 4
6	AB_Center	3	, 7	3	7	6	4	6	4
7	AB_Improved	6	4	4	6	5	5	3	7
	 Win Rate:	 58.	 .6%	 61	 . 4%	 67	 . 1%	 70	 ∙0%
Matala #		AB_Improved							
Match #	Opponent	Won AB_Imp	roved Lost	Won	ustom Lost		stom_2 Lost	AB_Cus	stom_3 Lost
1	Random	9	1	9	1	9	1	10	j 0
2	MM_Open	6	4	5	, <u> </u>	6	i 4	6	4
3	MM_Center	7	3	9		9	i i	8	j .
4	MM_Improved	7	3	6	4	9	1 1	5	5
5	AB_Open	4	, 3 6	4	4	5	1	3	, 3 7
6	AB_Center	5	5	4	6 6	5	5 5	6	<i> </i> 4
7	AB_Improved	6	4	5	5	4	6	7	3
	Win Rate:	62	.9%	60	.0%	67	1%	64	. 3%
Matc	h # Opponer	n+ ΔF	3_Impro	ved	AB_Cust	-om ΔI	3 Custo	m_2 AI	R Custi
Hatt	# Opponer	Won	Lost	Won	Lost	Won	Lost	Won	Lost
1	Random	10	0	9	1	10	2032	9	1
2	MM_Open	5	0	7	1	6	0	8	1
			3						
3	MM_Center	7		8	2	10	0	8	2
4	MM_Improved	8	2	6	4	6	4	8	2
5	AB_0pen	5	5	7	3	5	5	7	3
6	AB_Center	5	5	5	5	6	4	7	3
7	AB_Improved	6	4	6	4	8	2	6	4
	Win Rate:	65 . 7%		68.6%					
	WIII Nate.	65	. /%	68	. 6%	72	.9%	75	. 7%
Match #	Opponent	AB_Imp		68 AB_Cu:		72 AB_Cus		75 AB_Cus	
Match #			roved	AB_Cu	stom	AB_Cus	tom_2	AB_Cus	tom_3
Match #		AB_Imp	roved		stom	AB_Cus			tom_3
	Opponent Random	AB_Imp	roved Lost 1	AB_Cu: Won	stom Lost 1	AB_Cust Won 8	tom_2 Lost 2	AB_Cus [.] Won 10	tom_3 Lost 0
1 2	Opponent Random MM_Open	AB_Imp Won 9 7	roved Lost 1 3	AB_Cus Won 9 7	stom Lost 1 3	AB_Cus ⁻ Won 8 8	tom_2 Lost 2 2	AB_Cus [.] Won 10 8	tom_3 Lost 0 2
1 2 3	Opponent Random MM_Open MM_Center	AB_Imp Won 9 7 7	roved Lost 1 3	AB_Cus Won 9 7 8	stom Lost 1 3 2	AB_Cus ⁻ Won 8 8 9	tom_2 Lost 2 2 1	AB_Cus ⁻ Won 10 8 9	tom_3 Lost 0 2 1
1 2 3 4	Opponent Random MM_Open MM_Center MM_Improved	AB_Imp Won 9 7 7 6	roved Lost 1 3 3	AB_Cu: Won 9 7 8 7	stom Lost 1 3 2	AB_Cus ⁻¹ Won 8 8 9 7	tom_2 Lost 2 2 1	AB_Cus ⁻ Won 10 8 9 6	tom_3 Lost 0 2 1
1 2 3 4 5	Opponent Random MM_Open MM_Center MM_Improved AB_Open	AB_Imp Won 9 7 7 6 5	roved Lost 1 3 3 4	AB_Cu: Won 9 7 8 7 6	stom Lost 1 3 2 3	AB_Cus ⁻ Won 8 8 9 7 7	tom_2 Lost 2 2 1 3	AB_Cus ⁻ Won 10 8 9 6	tom_3 Lost 0 2 1 4
1 2 3 4 5	Opponent Random MM_Open MM_Center MM_Improved AB_Open AB_Center	AB_Imp Won 9 7 7 6 5	roved Lost 1 3 3 4 5	AB_Cu: Won 9 7 8 7 6 6	stom Lost 1 3 2 3 4	AB_Cus ⁻ Won 8 8 9 7 7	tom_2 Lost 2 2 1 3 3	AB_Cus ⁻ Won 10 8 9 6 5	tom_3 Lost 0 2 1 4 5
1 2 3 4 5	Opponent Random MM_Open MM_Center MM_Improved AB_Open AB_Center AB_Improved	AB_Imp Won 9 7 7 6 5 4 7	roved Lost 1 3 3 4 5 6	AB_Cu: Won 9 7 8 7 6 6	stom Lost 1 3 2 3 4 4	AB_Cus ⁻¹ Won 8 8 9 7 7 7 5	tom_2 Lost 2 2 1 3 3 3	AB_Cus ⁻ Won 10 8 9 6 5 6	tom_3 Lost 0 2 1 4 5 4
1 2 3 4 5	Opponent Random MM_Open MM_Center MM_Improved AB_Open AB_Center	AB_Imp Won 9 7 7 6 5 4 7	roved Lost 1 3 3 4 5	AB_Cu: Won 9 7 8 7 6 6	stom Lost 1 3 2 3 4	AB_Cus ⁻¹ Won 8 8 9 7 7 7 5	tom_2 Lost 2 2 1 3 3	AB_Cus ⁻ Won 10 8 9 6 5 6	tom_3 Lost 0 2 1 4 5
1 2 3 4 5	Opponent Random MM_Open MM_Center MM_Improved AB_Open AB_Center AB_Improved	AB_Imp Won 9 7 7 6 5 4 7 	roved Lost 1 3 3 4 5 6	AB_Cus Won 9 7 8 7 6 6 5 ———————————————————————————————	stom Lost 1 3 2 3 4 4	AB_Cust Won 8 8 9 7 7 7 5 	tom_2 Lost 2 2 1 3 3 3	AB_Cus ⁻ Won 10 8 9 6 5 6 8	tom_3 Lost 0 2 1 4 5 4
1 2 3 4 5 6 7	Opponent Random MM_Open MM_Center MM_Improved AB_Open AB_Center AB_Improved Win Rate: Opponent	AB_Imp Won 9 7 7 6 5 4 7 	roved Lost 1 3 3 4 5 6 3	AB_Cus Won 9 7 8 7 6 6 5 	stom Lost 1 3 2 3 4 5 5 6%	AB_Cus- Won 8 9 7 7 7 5 72 AB_Cus- Won	tom_2 Lost 2 2 1 3 3 3 5	AB_Cus- Won 10 8 9 6 5 6 8 74 AB_Cus-	tom_3 Lost 0 2 1 4 5 4 2 3% stom_3 Lost
1 2 3 4 5 6 7	Opponent Random MM_Open MM_Center MM_Improved AB_Open AB_Center AB_Improved Win Rate: Opponent Random	AB_Imp Won 9 7 7 6 5 4 7 	roved Lost 1 3 3 4 5 6 3 3 3%	AB_Cus Won 9 7 8 7 6 6 5 	stom Lost 1 3 2 3 4 5 5 6%	AB_Cus- Won 8 9 7 7 7 5 72 AB_Cus	tom_2 Lost 2 2 1 3 3 5 5 5 5 stom_2 Lost 1	AB_Cus- Won 10 8 9 6 5 6 8 74 AB_Cus	tom_3 Lost 0 2 1 4 5 4 2 3% stom_3 Lost 0
1 2 3 4 5 6 7 	Opponent Random MM_Open MM_Center MM_Improved AB_Open AB_Center AB_Improved Win Rate: Opponent Random MM_Open	AB_Imp Won 9 7 7 6 5 4 7 	roved Lost 1 3 3 4 5 6 3 3 3 croved Lost 2	AB_Cus Won 9 7 8 7 6 6 5 	stom Lost 3 2 3 4 5 5 6%	AB_Cus- Won 8 9 7 7 7 5 72 AB_Cus- Won 9 7	tom_2 Lost 2 2 1 3 3 59% stom_2 Lost 1	AB_Cus- Won 10 8 9 6 5 6 8 74 AB_Cus-	tom_3 Lost 0 2 1 4 5 4 2 3% stom_3 Lost 0 3
1 2 3 4 5 6 7 	Opponent Random MM_Open MM_Center MM_Improved AB_Open AB_Center AB_Improved Win Rate: Opponent Random MM_Open MM_Center	AB_Imp Won 9 7 7 6 5 4 7 64 AB_Imp Won 8 8	roved Lost 1 3 3 4 5 6 3 3 3 croved Lost 2 2	AB_Cus Won 9 7 8 7 6 6 5 	stom Lost 3 2 3 4 5 5 6%	AB_Cus- Won 8 9 7 7 7 5 72 AB_Cus- Won 9 7 9	tom_2 Lost 2 2 1 3 3 5 9% stom_2 Lost 1 3 1	AB_Cus- Won 10 8 9 6 5 6 8 74 AB_Cus- Won 10 7 7	tom_3 Lost 0 2 1 4 5 4 2 3% stom_3 Lost 0 3
1 2 3 4 5 6 7 	Opponent Random MM_Open MM_Center MM_Improved AB_Open AB_Center AB_Improved Win Rate: Opponent Random MM_Open MM_Center MM_Improved	AB_Imp Won 9 7 6 5 4 7 	roved Lost 3 3 4 5 6 3 3 2 Lost 2 2 3 4	AB_Cus Won 9 7 8 7 6 6 5 	stom Lost 3 2 3 4 5 5 6% Lost 1 3 1	AB_Cus- Won 8 9 7 7 5 72 AB_Cus Won 9 7 9 7	tom_2 Lost 2 2 3 3 5 9% stom_2 Lost 1 3 3	AB_Cus- Won 10 8 9 6 5 6 8 74 AB_Cus- Won 10 7 7 6	tom_3 Lost 0 2 1 4 5 4 2 3% stom_3 Lost 0 3 3 4
1 2 3 4 5 6 7 	Opponent Random MM_Open MM_Center MM_Improved AB_Open AB_Center AB_Improved Win Rate: Opponent Random MM_Open MM_Center	AB_Imp Won 9 7 7 6 5 4 7 64 AB_Imp Won 8 8	roved Lost 1 3 3 4 5 6 3 3 3 croved Lost 2 2	AB_Cus Won 9 7 8 7 6 6 5 	stom Lost 3 2 3 4 5 5 6%	AB_Cus- Won 8 9 7 7 7 5 72 AB_Cus- Won 9 7 9	tom_2 Lost 2 2 1 3 3 5 9% stom_2 Lost 1 3 1	AB_Cus- Won 10 8 9 6 5 6 8 74 AB_Cus- Won 10 7 7	tom_3 Lost 0 2 1 4 5 4 2 3% stom_3 Lost 0 3

Win Rate:		62.	62.9%		64.3%		70.0%		65.7%	
Match #	Opponent	AB_Improved		AB_Custom		AB_Custom_2		AB_Custom_3		
		Won	Lost	Won	Lost	Won	Lost	Won	Lost	
1	Random	9	1	9	1	10	0	7	j 3	
2	MM_Open	6	4	8	2	8	2	6	j 4	
3	MM_Center	8	2	9	1	8	2	9	j 1	
4	MM Improved	5	5	7	j 3	6	j 4	7	j 3	
5	AB_Open	7	3	6	4	7	3	7	3	
6	AB_Center	6	4	7	j 3	6	4	7	j 3	
7	AB_Improved	4	6	6	4	3	7	3	7	
	Win Rate:	64.3%		74.3%		68.6%		65.7%		
Match #	Opponent	AB_Improved		AB_Custom		AB_Custom_2		AB_Custom_3		
		Won	Lost	Won	Lost	Won	Lost	Won	Lost	
1	Random	9	1	9	1	9	1	9	1	
2	MM_Open	7	3	7	j 3	8	2	8	j 2	
3	MM_Center	8	2	10	j 0	10	j 0	9	j 1	
4	MM_Improved	6	4	8	2	6	4	6	j 4	
5	AB_Open	5	5	6	j 4	5	5	6	j 4	
6	AB_Center	5	5	5	5	7	3	6	4	
7	AB_Improved	6	4	6	4	6	4	6	4	
	Win Rate:	 65.7%		 72 . 9%		 72 . 9%		 71.4%		