

Predicting Climate Regime Change in Chaotic Convection

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The Lorenz system

History

Chaos

Thermosyphon

The forecasting problem

Data assimilation

Results

Thermosyphon

Conclusions

Inception

Developed in the '60s by Edward N. Lorenz (1917–2008) to show the National Weather Service that linear methods are inadequate for the problem of short-term weather prediction. It is the simplest realistic model of convection.



First example of *deterministic chaos*:

“When the present determines the future, but the approximate present does not approximately determine the future.”

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- ▶ sensitive dependence on initial conditions (ICs)
- ▶ small deviations grow exponentially with time
- ▶ aperiodic
- ▶ nonlinear
- ▶ ... but deterministic!

⇒ It is difficult to forecast chaotic behavior even with knowledge of the governing equations.

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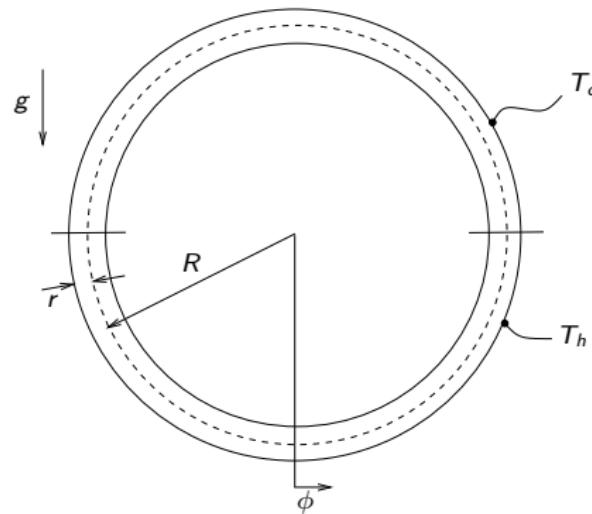
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A physical analog

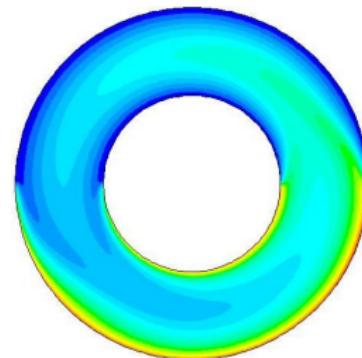
Lorenz derived his equations for fluid held between a lower, hot plate and an upper, cold plate (Rayleigh-Bénard). For certain parameters, his solution describes the dynamics of a *thermosyphon*.



Experiment and simulation



- ▶ Experimental apparatus under construction
- ▶ 8 sites for temperature measurements
- ▶ Heating/cooling jackets



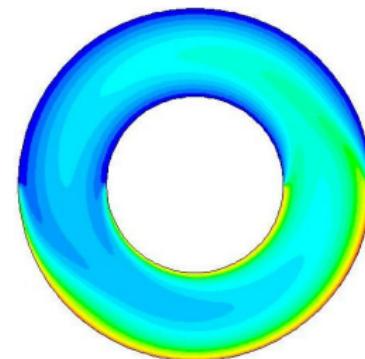
- ▶ Temperature profile for steady rotating fluid
- ▶ $\mathcal{O}(10^4)$ discretization of Navier-Stokes equations
- ▶ FLUENT: a computational fluid dynamics package

Image credit: Ridouane

Experiment and simulation

The plan:

FLUENT simulations
represent the thermosyphon
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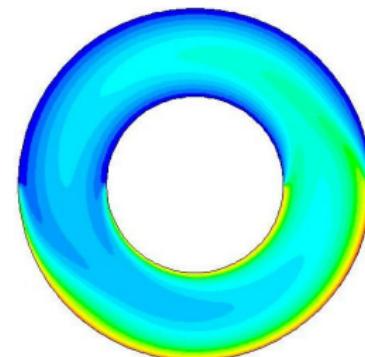
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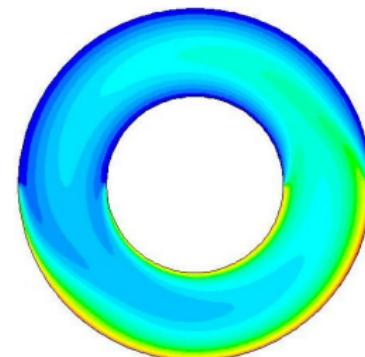
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This is what we call the
imperfect model forecasting
scenario.



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└ The Lorenz system

 └ Thermosyphon

Regime changes in action

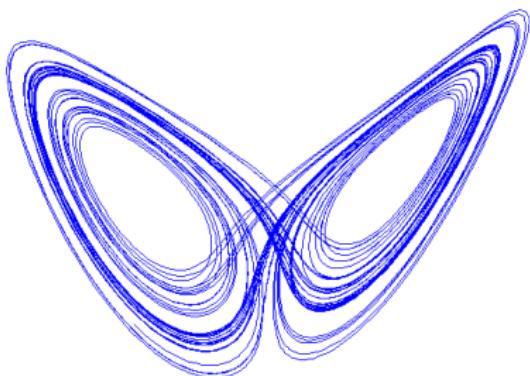
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Credit: El Hassan Ridouane

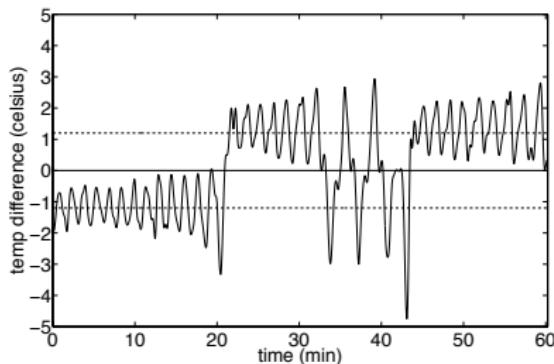
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Lorenz's chaotic attractor



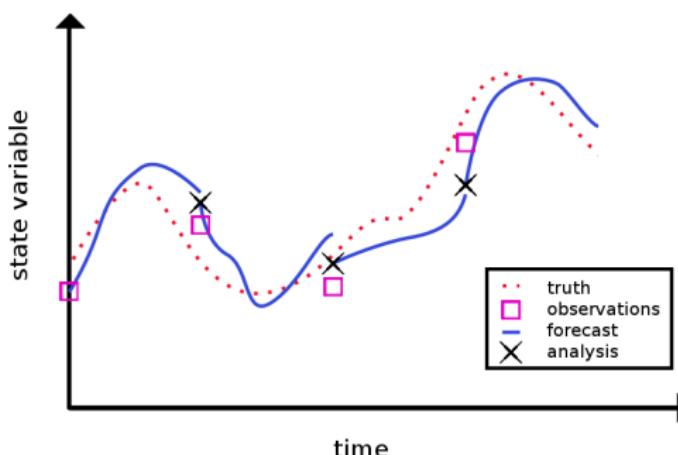
The system's attractor, which is
the shape it traces out in
state space



Timeseries for $\Delta T_{3-9} =$
horizontal temperature
difference across the loop

The initial value problem

When observing a real system, we can never perfectly know its state. *Data assimilation* (DA) estimates this using forecasts and observations.



DA Algorithms

The optimal combination of background forecasts and observations depends on (estimated) background and observational error.

- ▶ 3D-Var: Constant background error. In operational use.
- ▶ Extended Kalman Filter: Update background error with linear model. Numerically prohibitive for large models.
- ▶ Ensemble Kalman Filter: Use an *ensemble* of states to represent the current state. Ensemble spread used to estimate background error. Numerically efficient in large models.

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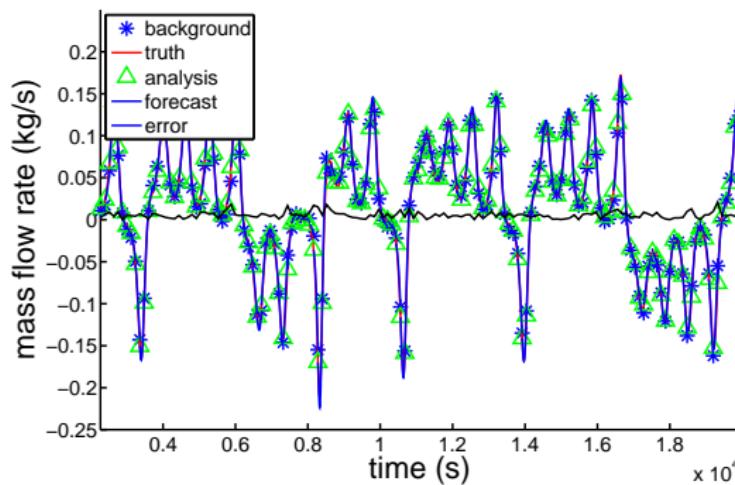
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DA results for EM forecasting FLUENT (imperfect model) 120s assimilation window



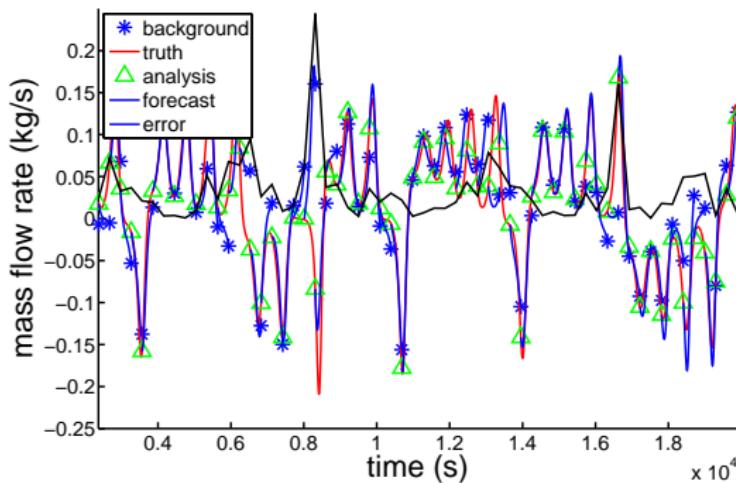
Observational noise is 1% climatological mean ($\sqrt{\langle q^2 \rangle}$)

Error relative to climatological mean in observation space

Forecasting succeeds

DA results for EM forecasting FLUENT (imperfect model)

300s assimilation window



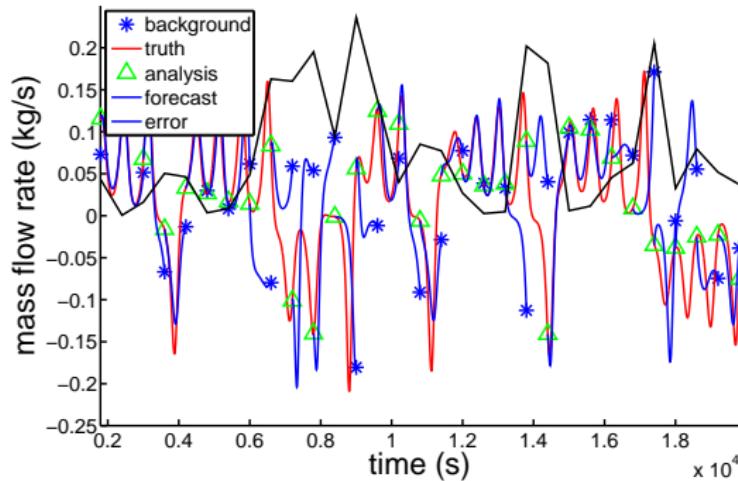
Observational noise is 1% climatological mean ($\sqrt{\langle q^2 \rangle}$)

Error relative to climatological mean in observation space

Forecasting (more or less) succeeds

DA results for EM forecasting FLUENT (imperfect model)

600s assimilation window

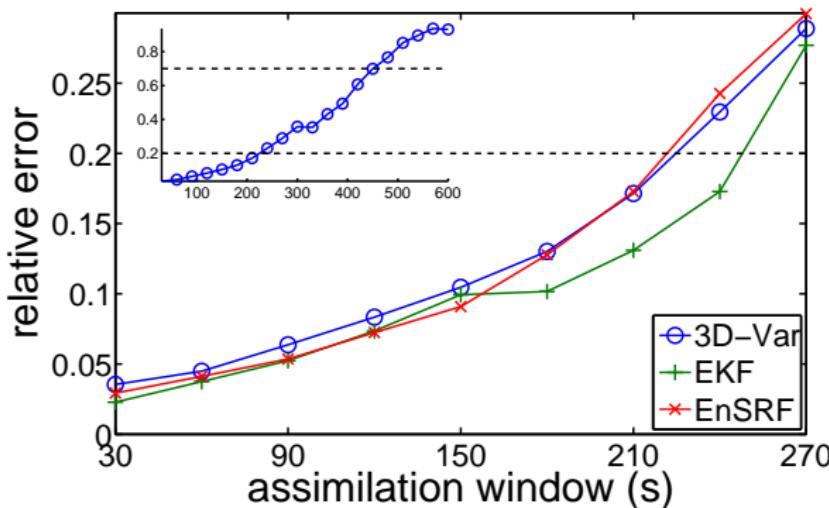
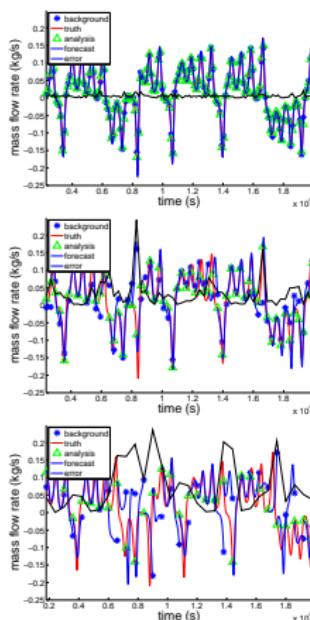


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Error relative to climatological mean in observation space

Forecasting **fails!**

DA results: accuracy degrades for longer windows



Error relative to climatological mean
 Dashed lines for “perfect” and “useless” forecasts

Wrapping up

- ▶ DA is an effective way of coupling a low-dimensional, approximate model to a realistic physical simulation of the thermosyphon
- ▶ A combination of techniques should be able to quantitatively predict regime changes and duration (soon)
- ▶ Application to laboratory thermosyphon
- ▶ Part of a larger effort to improve predictive power of global weather and climate models ...

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Global weather model simulations

(LoadingMovie)

Credit: Nick Allgaier... check out his talk in the Jost room at 3:15

Acknowledgments

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Thanks also to El Hassan Ridouane, for FLUENT pictures and much help, Floyd Vilmont, who is building the thermosyphon, Darren Hitt, for discussions and fluid dynamics expertise, and Nick Allgaier, who got the GFS up-and-running without going insane (cheers!).