# Regression to the mean modeling

Mean pain rating of 7.2 at 0.2 correlation

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### Generate 2x2 covariance matrix

Generate a covariance matrix using an SD of 1.2, 1.7, and 2.2, and correlation of 0.2.

```
cor \leftarrow matrix(c(1, 0.2, 0.2, 1), ncol = 2)
std_1 \leftarrow c(1.2, 1.2)
std_2 \leftarrow c(1.7, 1.7)
std_3 \leftarrow c(2.2, 2.2)
cov_1 <- cor2cov(cor.mat = cor,</pre>
                   sd = std 1
cov_1
          [,1] [,2]
## [1,] 1.440 0.288
## [2,] 0.288 1.440
cov_2 <- cor2cov(cor.mat = cor,</pre>
                   sd = std_2
cov_2
##
          [,1] [,2]
## [1,] 2.890 0.578
## [2,] 0.578 2.890
cov_3 <- cor2cov(cor.mat = cor,</pre>
                   sd = std_3
cov_3
##
          [,1] [,2]
## [1,] 4.840 0.968
## [2,] 0.968 4.840
```

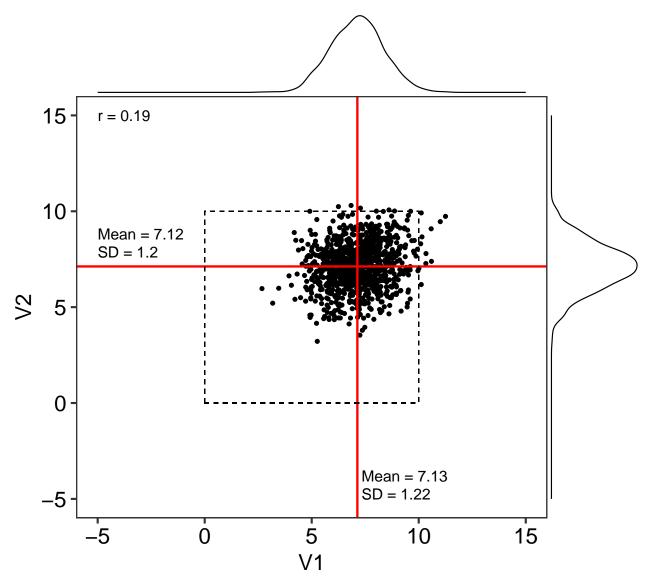
### Mean = 7.2, SD = 1.2, Cor = 0.2

### Generate and summarise data

#### Base data

```
xmin = 0, xmax = 10,
          colour = '#000000',
          alpha = 0,
          linetype = 2) +
annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5,
         label = str_glue("r = {round(cor(seven_1.base$V1, seven_1.base$V2), 2)}")) +
annotate(geom = 'text', x = -5, y = mean(seven_1.base$V2) + 1.7,
         hjust = 0, size = 5,
         label = str_glue("Mean = {round(mean(seven_1.base$V2), 2)}")) +
annotate(geom = 'text', x = -5, y = mean(seven_1.base$V2) + 0.75,
         hjust = 0, size = 5,
         label = str_glue("SD = {round(sd(seven_1.base$V2),2)}")) +
annotate(geom = 'text', x = mean(seven_1.base$V1) + 0.2, <math>y = -3.8,
         hjust = 0, size = 5,
         label = str_glue("Mean = {round(mean(seven_1.base$V1), 2)}")) +
annotate(geom = 'text', x = mean(seven_1.base$V1) + 0.2, <math>y = -4.75,
         hjust = 0, size = 5,
         label = str_glue("SD = {round(sd(seven_1.base$V1), 2)}")) +
labs(title = 'A: Unconstained',
     caption = 'Parameters: Mean = 7.2, SD = 1.2, Cor = 0.2') +
scale_y_continuous(limits = c(-5, 15)) +
scale_x_continuous(limits = c(-5, 15)) +
theme(plot.caption = element_text(size = 14)))
```

## A: Unconstained



Parameters: Mean = 7.2, SD = 1.2, Cor = 0.2

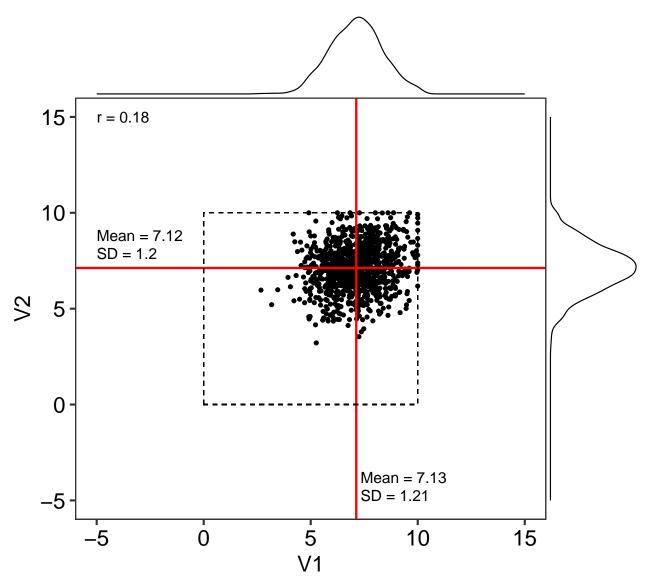
```
# Linear regression
summary(lm(V2 ~ V1, data = seven_1.base))
##
## Call:
## lm(formula = V2 ~ V1, data = seven_1.base)
## Residuals:
##
      Min
               1Q Median
                               ЗQ
                                      Max
## -3.6055 -0.7584 0.0394 0.8105 3.2859
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 5.80733
                          0.22159 26.207 < 2e-16 ***
```

```
## V1
               0.18442
                          0.03063 6.021 2.43e-09 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.179 on 998 degrees of freedom
## Multiple R-squared: 0.03506,
                                  Adjusted R-squared: 0.03409
## F-statistic: 36.26 on 1 and 998 DF, p-value: 2.427e-09
Constrain values to 0-10 range
```

```
# Process data
seven_1 <- seven_1.base %>%
   mutate(V1 = case_when(
               V1 < 1 ~ 1,
               V1 > 10 \sim 10,
               TRUE ~ V1)) %>%
   mutate(V2 = case_when(
               V2 < 0 ~ 0,
               V2 > 10 \sim 10,
               TRUE ~ V2)) %>%
   mutate(group = 'No threshold')
# Plot processed data
ggMarginal(ggplot(data = seven_1) +
               aes(x = V1, y = V2) +
               geom_point() +
               geom hline(yintercept = mean(seven 1$V2),
                          colour = 'red', size = 1) +
               geom_vline(xintercept = mean(seven_1$V1),
                          colour = 'red', size = 1) +
               geom_rect(ymin = 0, ymax = 10,
                         xmin = 0, xmax = 10,
                         colour = '#000000',
                         alpha = 0,
                         linetype = 2) +
               annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5,
                        label = str_glue("r = {round(cor(seven_1$V1, seven_1$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven_1$V2) + 1.7,
                        hjust = 0, size = 5,
                        label = str_glue("Mean = {round(mean(seven_1$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven_1$V2) + 0.75,
                        hjust = 0, size = 5,
                        label = str_glue("SD = {round(sd(seven_1$V2),2)}")) +
               annotate(geom = 'text', x = mean(seven_1$V1) + 0.2, y = -3.8,
                        hjust = 0, size = 5,
                        label = str glue("Mean = {round(mean(seven 1$V1), 2)}")) +
               annotate(geom = 'text', x = mean(seven_1$V1) + 0.2, y = -4.75,
                        hjust = 0, size = 5,
                        label = str_glue("SD = {round(sd(seven_1$V1), 2)}")) +
               labs(title = 'B: Constrained (0-10 range)',
                    caption = 'Parameters: Mean = 7.2, SD = 1.2, Cor = 0.2') +
               scale_y_continuous(limits = c(-5, 15)) +
               scale_x_continuous(limits = c(-5, 15)) +
```

```
theme(plot.caption = element_text(size = 14)))
```

## B: Constrained (0-10 range)



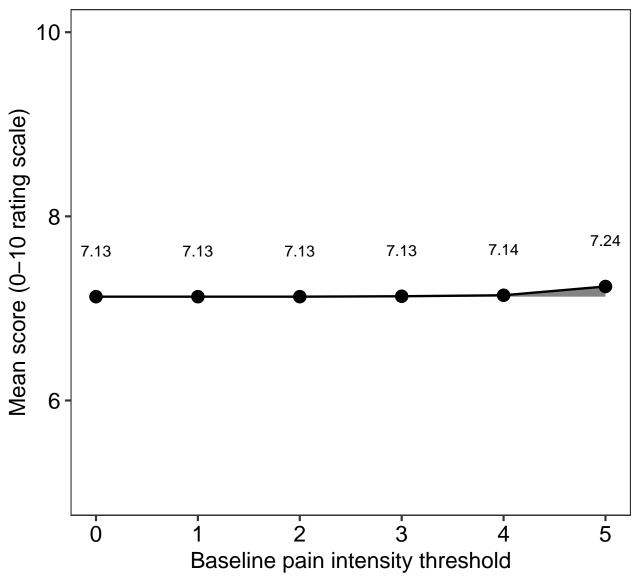
Parameters: Mean = 7.2, SD = 1.2, Cor = 0.2

```
## (Intercept) 5.81766    0.22342    26.04 < 2e-16 ***
## V1     0.18298    0.03091    5.92 4.42e-09 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.178 on 998 degrees of freedom
## Multiple R-squared: 0.03393,    Adjusted R-squared: 0.03296
## F-statistic: 35.05 on 1 and 998 DF,  p-value: 4.418e-09</pre>
```

### Model mean of V1 with increasing V1 thresholds from 0 to 5

```
# Extract visit 1 data
seven_1V1 <- seven_1$V1
# Generate a vector of threshold values to iterate over
cutoff <- 0:5
# Generate a vector of V1 means at each V1 threshold
seven_1V1.shift <- sapply(cutoff, function(x){mean(seven_1V1[seven_1V1 > x])})
# Calculate deviation
(seven_1V1.df <- data.frame(cutoff = cutoff,</pre>
                          mean = seven_1V1.shift) %>%
        mutate(deviation = mean - mean(seven 1V1)))
##
    cutoff
                mean
                       deviation
         0 7.127445 0.000000000
## 1
## 2
         1 7.127445 0.000000000
## 3
         2 7.127445 0.000000000
## 4
         3 7.131900 0.004455853
## 5
         4 7.142766 0.015321102
## 6
         5 7.238151 0.110706771
# Plot data
ggplot(data = seven_1V1.df) +
    aes(x = cutoff, y = mean, ymin = mean(seven_1V1), ymax = mean) +
   geom ribbon(alpha = 0.6) +
   geom point(size = 5) +
   geom_line(size = 1) +
    geom_text(aes(label = round(mean, 2)),
              nudge_y = 0.5, size = 5) +
   scale_y_continuous(limits = c(5, 10),
                       breaks = c(0, 2, 4, 6, 8, 10)) +
   labs(title = 'A: Shift in V1 mean with increasing V1 threshold value',
         caption = 'Parameters: Mean = 7.2, SD = 1.2, Cor = 0.2',
         x = 'Baseline pain intensity threshold',
         y = 'Mean score (0-10 rating scale)') +
   theme(plot.caption = element_text(size = 14))
```

## A: Shift in V1 mean with increasing V1 threshold value



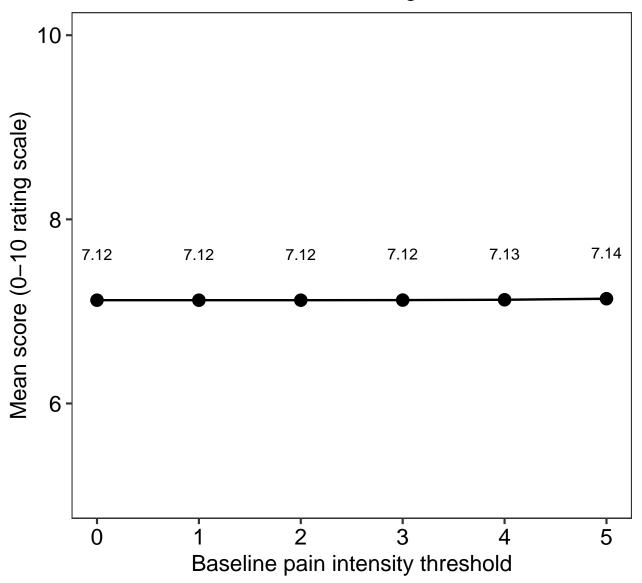
Parameters: Mean = 7.2, SD = 1.2, Cor = 0.2

### Model mean of V2 with increasing V1 thresholds from 0 to 5

#### mean(.))

```
# Calculate deviation
(seven_1V2.df <- data.frame(cutoff = cutoff,</pre>
                           mean = seven_1V2.shift) %>%
       mutate(deviation = mean - mean(seven_1V2)))
##
    cutoff
              mean deviation
## 1
         0 7.121818 0.000000000
## 2
         1 7.121818 0.000000000
## 3
         2 7.121818 0.000000000
## 4
         3 7.122974 0.001155543
## 5
         4 7.126532 0.004713580
## 6
         5 7.138074 0.016255995
# Plot data
ggplot(data = seven_1V2.df) +
   aes(x = cutoff, y = mean, ymin = mean(seven_1V2), ymax = mean) +
   geom_ribbon(alpha = 0.6) +
   geom_point(size = 5) +
   geom_line(size = 1) +
   geom_text(aes(label = round(mean, 2)),
              nudge_y = 0.5, size = 5) +
   scale_y_continuous(limits = c(5, 10),
                       breaks = c(0, 2, 4, 6, 8, 10)) +
   labs(title = 'B: Shift in V2 mean with increasing V1 threshold value',
         caption = 'Parameters: Mean = 7.2, SD = 1.2, Cor = 0.2',
         x = 'Baseline pain intensity threshold',
         y = 'Mean score (0-10 rating scale)') +
   theme(plot.caption = element_text(size = 14))
```

## B: Shift in V2 mean with increasing V1 threshold value



Parameters: Mean = 7.2, SD = 1.2, Cor = 0.2

### Placebo response

```
R = 2000,
traditional = FALSE,
bca = TRUE)
```

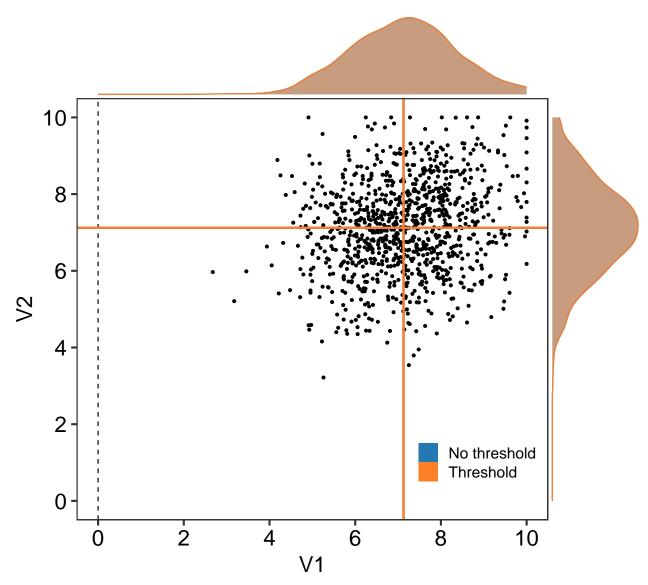
#### kable(diff\_1.0)

diff 1.0\$.id <- 0

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
0	1000	0.00563	0.95	-0.0936	0.101

```
ggMarginal(placebo_1.0[, 1:3] %>%
               bind_rows(seven_1) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_1,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_1.0,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_1$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_1.0$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 0, linetype = 2) +
               geom_hline(yintercept = mean(seven_1$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_1.0$V2),
                          colour = pal[2], size = 1) +
               scale_y_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale colour manual(values = pal) +
               labs(title = 'A: Baseline pain threshold = 0',
                    caption = 'Parameters: Mean = 7.2, SD = 1.2, Cor = 0.2') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

## A: Baseline pain threshold = 0



Parameters: Mean = 7.2, SD = 1.2, Cor = 0.2

```
bca = TRUE)
```

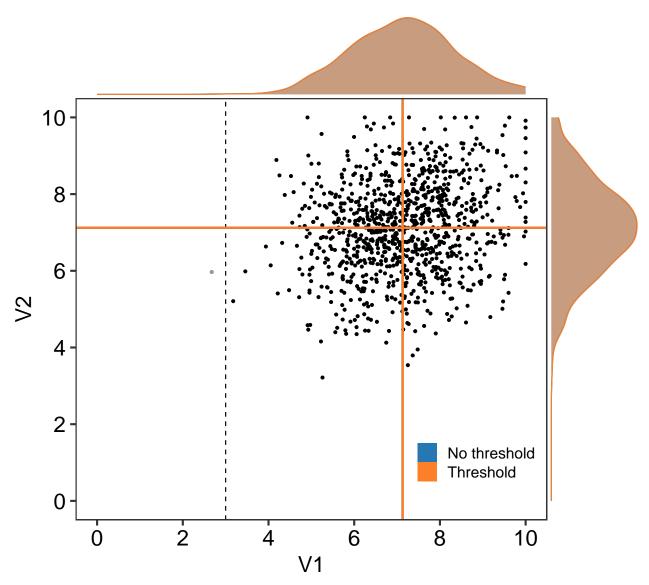
```
diff 1.3$.id <- 3
```

#### kable(diff\_1.3)

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
3	999	0.00893	0.95	-0.0835	0.0974

```
ggMarginal(placebo_1.3[, 1:3] %>%
               bind_rows(seven_1) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_1,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_1.3,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_1$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_1.3$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 3, linetype = 2) +
               geom_hline(yintercept = mean(seven_1$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_1.3$V2),
                          colour = pal[2], size = 1) +
               scale_y_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale colour manual(values = pal) +
               labs(title = 'B: Baseline pain threshold = 3',
                    caption = 'Parameters: Mean = 7.2, SD = 1.2, Cor = 0.2') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

## B: Baseline pain threshold = 3



Parameters: Mean = 7.2, SD = 1.2, Cor = 0.2

```
# Process that data
placebo_1.4 <- seven_1 %>%
    filter(V1 >= 4) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_1.4 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_1.4,
    R = 2000,
    traditional = FALSE,
    bca = TRUE)

diff_1.4$.id <- 4

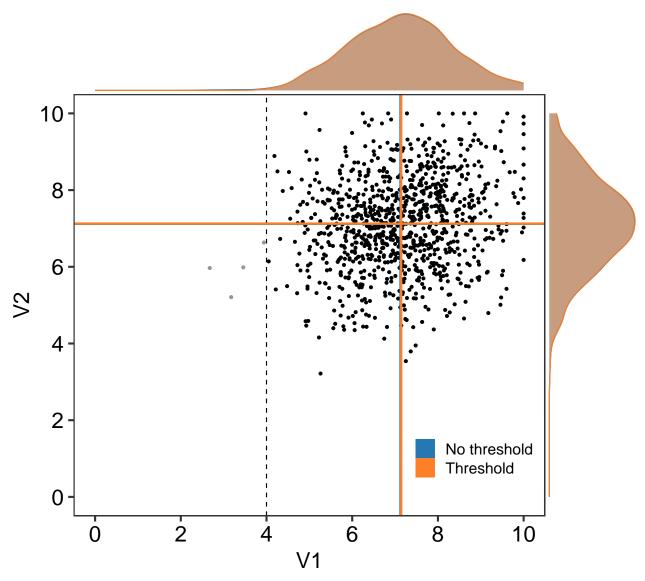
kable(diff_1.4)</pre>
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 4
 996
 0.0162
 0.95
 -0.0768
 0.113

```
ggMarginal(placebo_1.4[, 1:3] %>%
               bind_rows(seven_1) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_1,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_1.4,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_1$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_1.4$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 4, linetype = 2) +
               geom_hline(yintercept = mean(seven_1$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_1.4$V2),
                          colour = pal[2], size = 1) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'C: Baseline pain threshold = 4',
                    caption = 'Parameters: Mean = 7.2, SD = 1.2, Cor = 0.2') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

## C: Baseline pain threshold = 4



Parameters: Mean = 7.2, SD = 1.2, Cor = 0.2

```
# Process that data
placebo_1.5 <- seven_1 %>%
    filter(V1 >= 5) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_1.5 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_1.5,
R = 2000,
traditional = FALSE,
bca = TRUE)

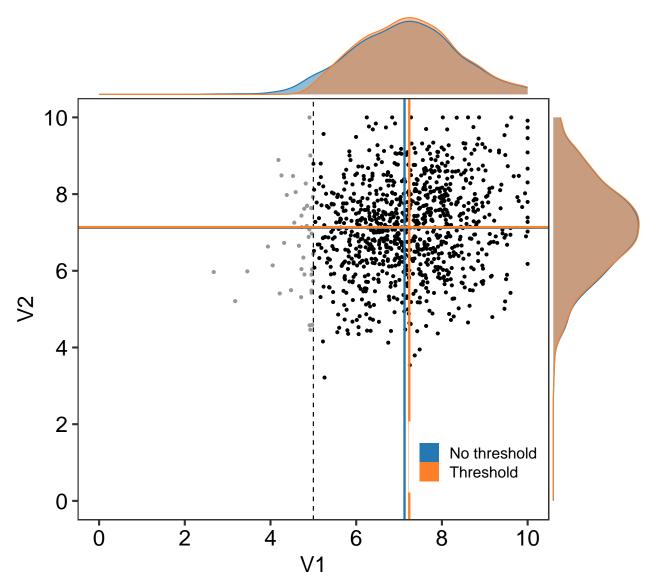
diff_1.5$.id <- 5
kable(diff_1.5)</pre>
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 5
 958
 0.1
 0.95
 0.00696
 0.192

```
ggMarginal(placebo_1.5[, 1:3] %>%
               bind_rows(seven_1) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_1,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_1.5,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_1$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_1.5$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 5, linetype = 2) +
               geom_hline(yintercept = mean(seven_1$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_1.5$V2),
                          colour = pal[2], size = 1) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'D: Baseline pain threshold = 5',
                    caption = 'Parameters: Mean = 7.2, SD = 1.2, Cor = 0.2') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

## D: Baseline pain threshold = 5



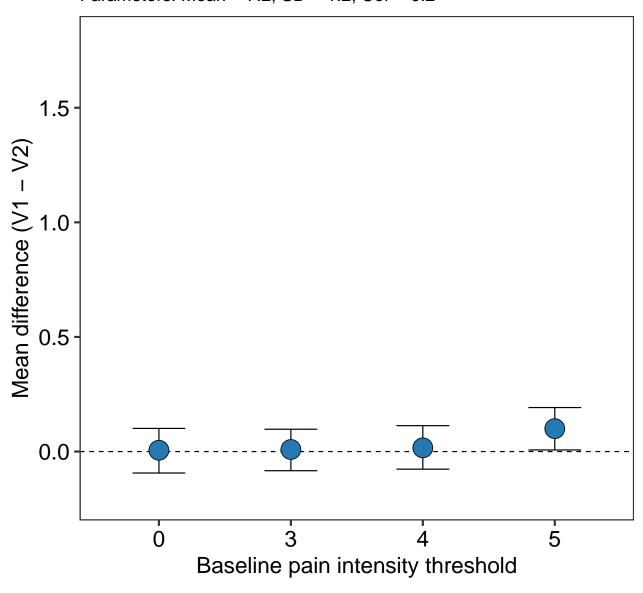
Parameters: Mean = 7.2, SD = 1.2, Cor = 0.2

### Difference plot

```
# Bind diff_*.* dataframes
diff_all_1 <- diff_1.0 %>%
  bind_rows(diff_1.3, diff_1.4, diff_1.5)

pp_1 <- diff_all_1 %>%
  mutate(Threshold = factor(.id)) %>%
  ggplot(data = .) +
  aes(x = Threshold,
    y = Mean,
    ymin = Bca.lower,
    ymax = Bca.upper) +
```

Parameters: Mean = 7.2, SD = 1.2, Cor = 0.2



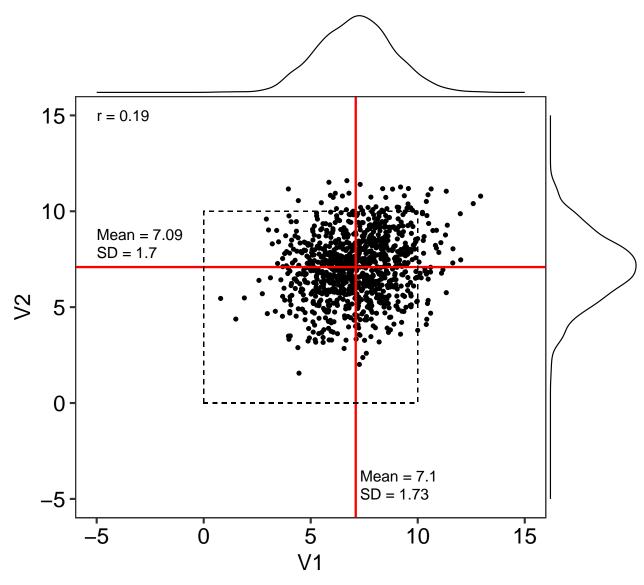
### Mean = 7.2, SD = 1.7, Cor = 0.2

#### Generate and summarise data

#### Base data

```
# Set the random seed for reproducibility
set.seed(2019)
# Generate the data
seven 2.base \leftarrow as.data.frame(mvrnorm(n = 1000, mu = c(7.2, 7.2), Sigma = cov 2))
# Plot base data
ggMarginal(ggplot(data = seven_2.base) +
               aes(x = V1, y = V2) +
               geom_point() +
               geom_hline(yintercept = mean(seven_2.base$V2),
                          colour = 'red', size = 1) +
               geom_vline(xintercept = mean(seven_2.base$V1),
                          colour = 'red', size = 1) +
               geom_rect(ymin = 0, ymax = 10,
                         xmin = 0, xmax = 10,
                         colour = '#000000',
                         alpha = 0,
                         linetype = 2) +
               annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5,
                        label = str_glue("r = {round(cor(seven_2.base$V1, seven_2.base$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven 2.base$V2) + 1.7,
                        hjust = 0, size = 5,
                        label = str_glue("Mean = {round(mean(seven_2.base$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven_2.base$V2) + 0.75,
                        hjust = 0, size = 5,
                        label = str_glue("SD = {round(sd(seven_2.base$V2),2)}")) +
               annotate(geom = 'text', x = mean(seven_2.base$V1) + 0.2, y = -3.8,
                        hjust = 0, size = 5,
                        label = str_glue("Mean = {round(mean(seven_2.base$V1), 2)}")) +
               annotate(geom = 'text', x = mean(seven_2.base$V1) + 0.2, <math>y = -4.75,
                        hjust = 0, size = 5,
                        label = str_glue("SD = {round(sd(seven_2.base$V1), 2)}")) +
               labs(title = 'A: Unconstrained',
                    caption = 'Parameters: Mean = 7.2, SD = 1.7, Cor = 0.2') +
               scale_y_continuous(limits = c(-5, 15)) +
               scale_x_continuous(limits = c(-5, 15)) +
               theme(plot.caption = element_text(size = 14)))
```

## A: Unconstrained



Parameters: Mean = 7.2, SD = 1.7, Cor = 0.2

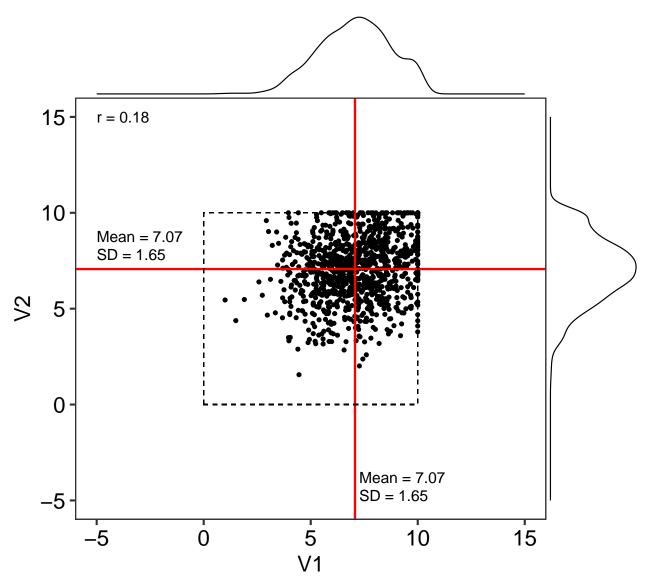
```
# Linear regression
summary(lm(V2 ~ V1, data = seven_2.base))
##
## Call:
## lm(formula = V2 ~ V1, data = seven_2.base)
## Residuals:
##
      Min
               1Q Median
                               ЗQ
                                      Max
## -5.1078 -1.0744 0.0558 1.1482 4.6550
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 5.78032
                          0.22389 25.818 < 2e-16 ***
```

```
## V1
                0.18442
                           0.03063 6.021 2.43e-09 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.67 on 998 degrees of freedom
                                   Adjusted R-squared: 0.03409
## Multiple R-squared: 0.03506,
## F-statistic: 36.26 on 1 and 998 DF, p-value: 2.427e-09
Constrain values to 0-10 range
# Process data
seven_2 <- seven_2.base %>%
   mutate(V1 = case_when(
              V1 < 1 \sim 1,
              V1 > 10 \sim 10,
              TRUE ~ V1)) %>%
   mutate(V2 = case_when(
               V2 < 0 ~ 0,
              V2 > 10 \sim 10,
              TRUE ~ V2)) %>%
   mutate(group = 'No threshold')
# Plot processed data
ggMarginal(ggplot(data = seven_2) +
               aes(x = V1, y = V2) +
               geom_point() +
               geom hline(yintercept = mean(seven 2$V2),
                          colour = 'red', size = 1) +
               geom_vline(xintercept = mean(seven_2$V1),
                          colour = 'red', size = 1) +
               geom_rect(ymin = 0, ymax = 10,
                         xmin = 0, xmax = 10,
                         colour = '#000000',
                         alpha = 0,
                         linetype = 2) +
               annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5,
                        label = str_glue("r = {round(cor(seven_2$V1, seven_2$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven_2$V2) + 1.7,
                        hjust = 0, size = 5,
                        label = str_glue("Mean = {round(mean(seven_2$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven_2$V2) + 0.75,
                        hjust = 0, size = 5,
                        label = str_glue("SD = {round(sd(seven_2$V2),2)}")) +
               annotate(geom = 'text', x = mean(seven_2$V1) + 0.2, y = -3.8,
                        hjust = 0, size = 5,
                        label = str glue("Mean = {round(mean(seven 2$V1), 2)}")) +
               annotate(geom = 'text', x = mean(seven_2$V1) + 0.2, y = -4.75,
                        hjust = 0, size = 5,
                        label = str_glue("SD = {round(sd(seven_2$V1), 2)}")) +
               labs(title = 'B: Constrained (0-10 range)',
                    caption = 'Parameters: Mean = 7.2, SD = 1.7, Cor = 0.2') +
```

scale\_y\_continuous(limits = c(-5, 15)) + scale\_x\_continuous(limits = c(-5, 15)) +

```
theme(plot.caption = element_text(size = 14)))
```

## B: Constrained (0-10 range)



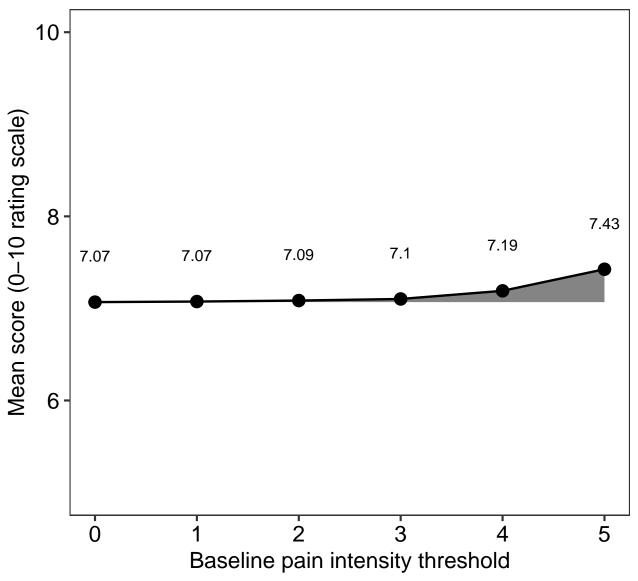
Parameters: Mean = 7.2, SD = 1.7, Cor = 0.2

```
## (Intercept) 5.80974    0.22597    25.711    < 2e-16 ***
## V1          0.17762    0.03113    5.705    1.53e-08 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.623 on 998 degrees of freedom
## Multiple R-squared: 0.03159,    Adjusted R-squared: 0.03062
## F-statistic: 32.55 on 1 and 998 DF,   p-value: 1.53e-08</pre>
```

### Model mean of V1 with increasing V1 thresholds from 0 to 5

```
# Extract visit 1 data
seven_2V1 <- seven_2$V1
# Generate a vector of threshold values to iterate over
cutoff <- 0:5
# Generate a vector of V1 means at each V1 threshold
seven_2V1.shift <- sapply(cutoff, function(x){mean(seven_2V1[seven_2V1 > x])})
# Calculate deviation
(seven 2V1.df <- data.frame(cutoff = cutoff,
                           mean = seven_2V1.shift) %>%
        mutate(deviation = mean - mean(seven 2V1)))
##
    cutoff
                mean
                       deviation
         0 7.068450 0.000000000
## 1
## 2
          1 7.074524 0.006074524
## 3
         2 7.085306 0.016856165
## 4
         3 7.102548 0.034098098
## 5
         4 7.190929 0.122478927
## 6
         5 7.425577 0.357127016
# Plot data
ggplot(data = seven_2V1.df) +
   aes(x = cutoff, y = mean, ymin = mean(seven_2V1), ymax = mean) +
   geom ribbon(alpha = 0.6) +
   geom point(size = 5) +
   geom_line(size = 1) +
    geom_text(aes(label = round(mean, 2)),
              nudge_y = 0.5, size = 5) +
   scale_y_continuous(limits = c(5, 10),
                       breaks = c(0, 2, 4, 6, 8, 10)) +
   labs(title = 'A: Shift in V1 mean with increasing V1 threshold value',
         caption = 'Parameters: Mean = 7.2, SD = 1.7, Cor = 0.2',
         x = 'Baseline pain intensity threshold',
         y = 'Mean score (0-10 rating scale)') +
   theme(plot.caption = element_text(size = 14))
```

## A: Shift in V1 mean with increasing V1 threshold value



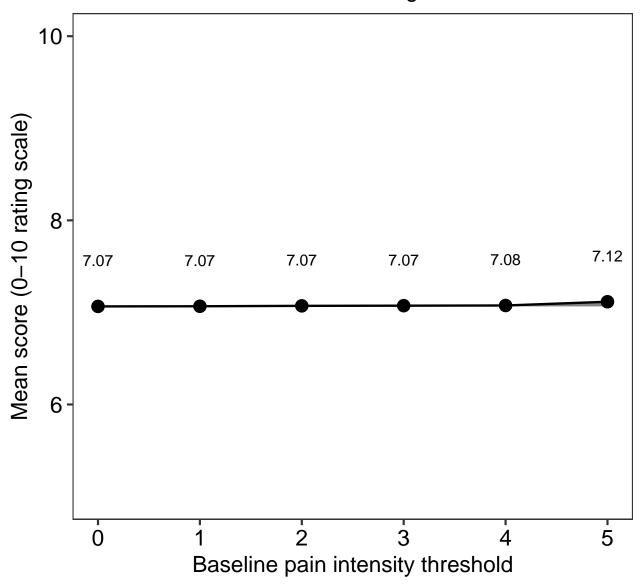
Parameters: Mean = 7.2, SD = 1.7, Cor = 0.2

### Model mean of V2 with increasing V1 thresholds from 0 to 5

#### mean(.))

```
# Calculate deviation
(seven_2V2.df <- data.frame(cutoff = cutoff,</pre>
                           mean = seven_2V2.shift) %>%
       mutate(deviation = mean - mean(seven_2V2)))
##
    cutoff
               mean deviation
## 1
         0 7.065253 0.000000000
## 2
         1 7.066866 0.001613006
## 3
         2 7.071156 0.005902915
         3 7.073102 0.007848565
## 4
## 5
         4 7.075173 0.009920094
## 6
         5 7.115842 0.050588164
# Plot data
ggplot(data = seven_2V2.df) +
   aes(x = cutoff, y = mean, ymin = mean(seven_2V2), ymax = mean) +
   geom_ribbon(alpha = 0.6) +
   geom_point(size = 5) +
   geom_line(size = 1) +
   geom_text(aes(label = round(mean, 2)),
              nudge_y = 0.5, size = 5) +
   scale_y_continuous(limits = c(5, 10),
                       breaks = c(0, 2, 4, 6, 8, 10)) +
   labs(title = 'B: Shift in V2 mean with increasing V1 threshold value',
         caption = 'Parameters: Mean = 7.2, SD = 1.7, Cor = 0.2',
         x = 'Baseline pain intensity threshold',
         y = 'Mean score (0-10 rating scale)') +
   theme(plot.caption = element_text(size = 14))
```

## B: Shift in V2 mean with increasing V1 threshold value



Parameters: Mean = 7.2, SD = 1.7, Cor = 0.2

### Placebo response

```
R = 2000,
traditional = FALSE,
bca = TRUE)
```

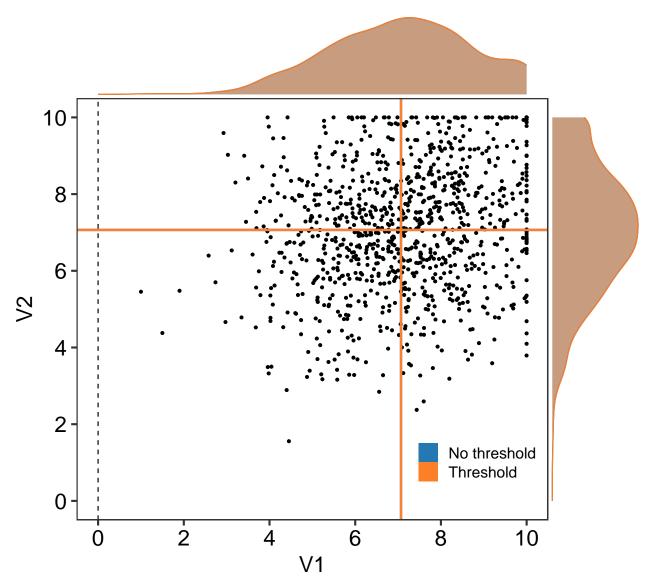
## diff\_2.0\$.id <- 0

#### kable(diff 2.0)

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
0	1000	0.0032	0.95	-0.133	0.134

```
ggMarginal(placebo_2.0[, 1:3] %>%
               bind_rows(seven_2) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_2,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_2.0,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_2$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_2.0$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 0, linetype = 2) +
               geom_hline(yintercept = mean(seven_2$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_2.0$V2),
                          colour = pal[2], size = 1) +
               scale_y_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale colour manual(values = pal) +
               labs(title = 'A: Baseline pain threshold = 0',
                    caption = 'Parameters: Mean = 7.2, SD = 1.7, Cor = 0.2') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

## A: Baseline pain threshold = 0



Parameters: Mean = 7.2, SD = 1.7, Cor = 0.2

```
# Process data
placebo_2.3 <- seven_2 %>%
    filter(V1 >= 3) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_2.3 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_2.3,
R = 2000,
traditional = FALSE,
bca = TRUE)

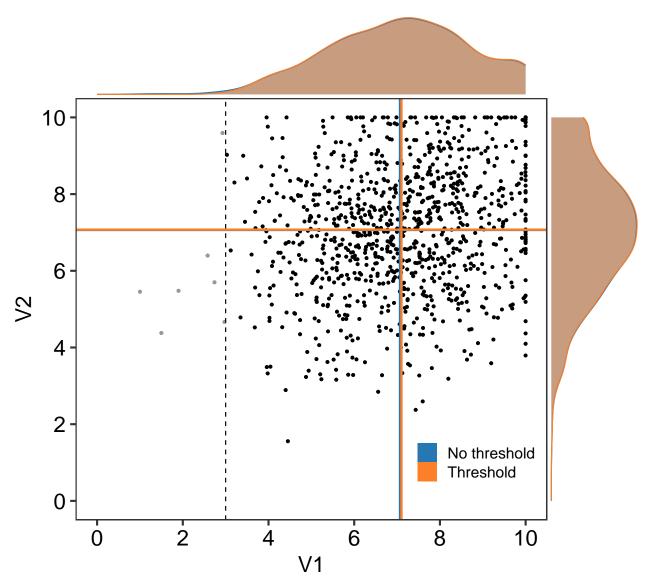
diff_2.3$.id <- 3
kable(diff_2.3)</pre>
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 3
 993
 0.0294
 0.95
 -0.101
 0.158

```
ggMarginal(placebo_2.3[, 1:3] %>%
               bind_rows(seven_2) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_2,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_2.3,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_2$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_2.3$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 3, linetype = 2) +
               geom_hline(yintercept = mean(seven_2$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_2.3$V2),
                          colour = pal[2], size = 1) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'B: Baseline pain threshold = 3',
                    caption = 'Parameters: Mean = 7.2, SD = 1.7, Cor = 0.2') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

## B: Baseline pain threshold = 3



Parameters: Mean = 7.2, SD = 1.7, Cor = 0.2

```
# Process that data
placebo_2.4 <- seven_2 %>%
    filter(V1 >= 4) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_2.4 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_2.4,
R = 2000,
traditional = FALSE,
bca = TRUE)

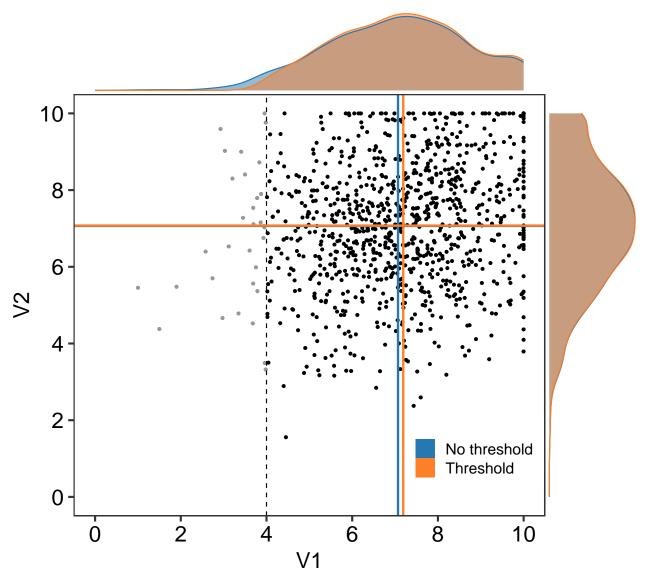
diff_2.4$.id <- 4
kable(diff_2.4)</pre>
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 4
 968
 0.116
 0.95
 -0.00764
 0.257

```
ggMarginal(placebo_2.4[, 1:3] %>%
               bind_rows(seven_2) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_2,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_2.4,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_2$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_2.4$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 4, linetype = 2) +
               geom_hline(yintercept = mean(seven_2$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_2.4$V2),
                          colour = pal[2], size = 1) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'C: Baseline pain threshold = 4',
                    caption = 'Parameters: Mean = 7.2, SD = 1.7, Cor = 0.2') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

## C: Baseline pain threshold = 4



Parameters: Mean = 7.2, SD = 1.7, Cor = 0.2

```
# Process that data
placebo_2.5 <- seven_2 %>%
    filter(V1 >= 5) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_2.5 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_2.5,
R = 2000,
traditional = FALSE,
bca = TRUE)

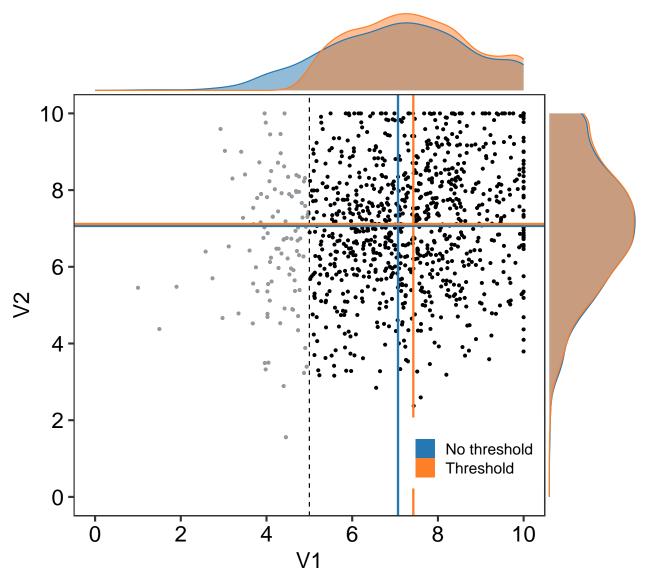
diff_2.5$.id <- 5</pre>
kable(diff_2.5)
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 5
 890
 0.31
 0.95
 0.189
 0.438

```
ggMarginal(placebo_2.5[, 1:3] %>%
               bind_rows(seven_2) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_2,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_2.5,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_2$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_2.5$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 5, linetype = 2) +
               geom_hline(yintercept = mean(seven_2$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_2.5$V2),
                          colour = pal[2], size = 1) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'D: Baseline pain threshold = 5',
                    caption = 'Parameters: Mean = 7.2, SD = 1.7, Cor = 0.2') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

## D: Baseline pain threshold = 5



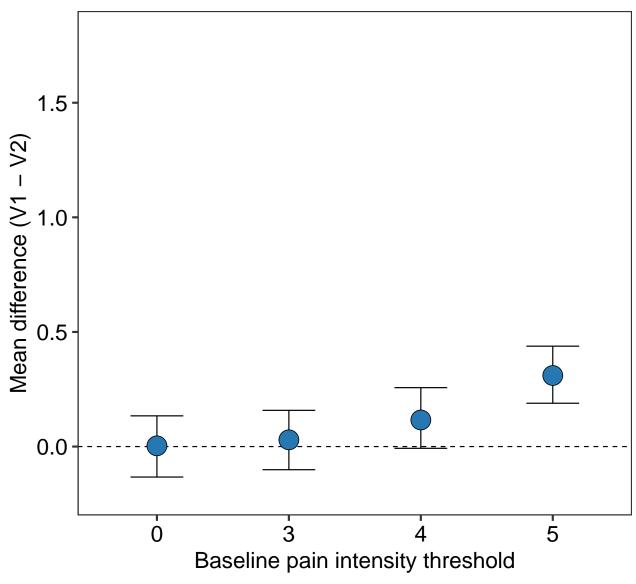
Parameters: Mean = 7.2, SD = 1.7, Cor = 0.2

### Difference plot

```
# Bind diff_*.* dataframes
diff_all_2 <- diff_2.0 %>%
  bind_rows(diff_2.3, diff_2.4, diff_2.5)

pp_2 <- diff_all_2 %>%
  mutate(Threshold = factor(.id)) %>%
  ggplot(data = .) +
  aes(x = Threshold,
    y = Mean,
    ymin = Bca.lower,
    ymax = Bca.upper) +
```

Parameters: Mean = 7.2, SD = 1.7, Cor = 0.2



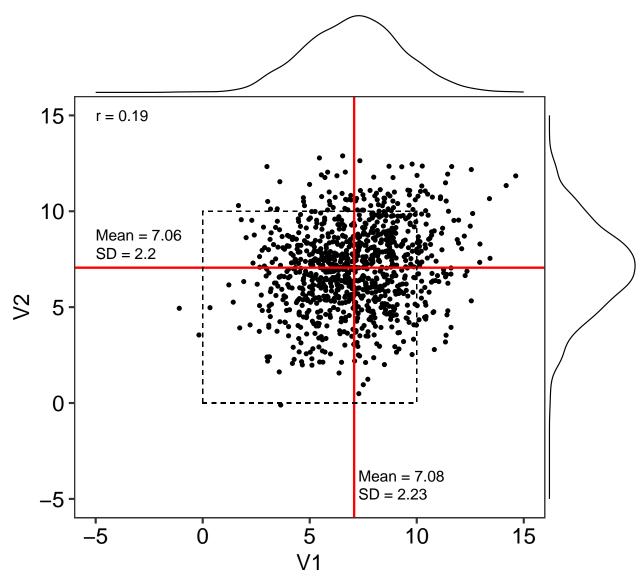
# Mean = 7.2, SD = 2.2, Cor = 0.2

#### Generate and summarise data

#### Base data

```
# Set the random seed for reproducibility
set.seed(2019)
# Generate the data
seven 3.base \leftarrow as.data.frame(mvrnorm(n = 1000, mu = c(7.2, 7.2), Sigma = cov 3))
# Plot base data
ggMarginal(ggplot(data = seven_3.base) +
               aes(x = V1, y = V2) +
               geom_point() +
               geom_hline(yintercept = mean(seven_3.base$V2),
                          colour = 'red', size = 1) +
               geom_vline(xintercept = mean(seven_3.base$V1),
                          colour = 'red', size = 1) +
               geom_rect(ymin = 0, ymax = 10,
                         xmin = 0, xmax = 10,
                         colour = '#000000',
                         alpha = 0,
                         linetype = 2) +
               annotate(geom = 'text', x = -5, y = 15,
                        hjust = 0, size = 5,
                        label = str glue("r = {round(cor(seven 3.base$V1, seven 3.base$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven_3.base$V2) + 1.7,
                        hjust = 0, size = 5,
                        label = str_glue("Mean = {round(mean(seven_3.base$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven_3.base$V2) + 0.75,
                        hjust = 0, size = 5,
                        label = str_glue("SD = {round(sd(seven_3.base$V2),2)}")) +
               annotate(geom = 'text', x = mean(seven_3.base$V1) + 0.2, <math>y = -3.8,
                        hjust = 0, size = 5,
                        label = str_glue("Mean = {round(mean(seven_3.base$V1), 2)}")) +
               annotate(geom = 'text', x = mean(seven_3.base$V1) + 0.2, <math>y = -4.75,
                        hjust = 0, size = 5,
                        label = str_glue("SD = {round(sd(seven_3.base$V1), 2)}")) +
               labs(title = 'A: Unconstrained',
                    caption = 'Parameters: Mean = 7.2, SD = 2.2, Cor = 0.2') +
               scale_y_continuous(limits = c(-5, 15)) +
               scale_x_continuous(limits = c(-5, 15)) +
               theme(plot.caption = element_text(size = 14)))
```

# A: Unconstrained



Parameters: Mean = 7.2, SD = 2.2, Cor = 0.2

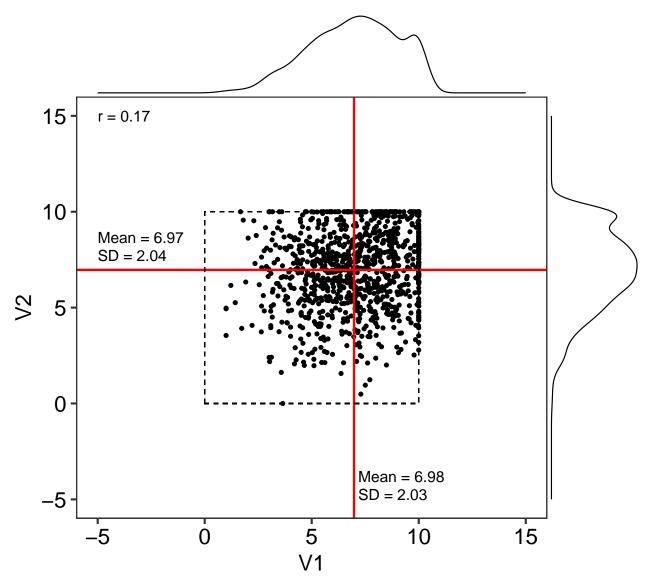
```
# Linear regression
summary(lm(V2 ~ V1, data = seven_3.base))
##
## Call:
## lm(formula = V2 ~ V1, data = seven_3.base)
## Residuals:
##
       Min
                1Q Median
                               ЗQ
                                      Max
## -6.6101 -1.3905 0.0722 1.4859 6.0241
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 5.75330
                          0.22723 25.320 < 2e-16 ***
```

```
## V1
               0.18442
                          0.03063 6.021 2.43e-09 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.162 on 998 degrees of freedom
## Multiple R-squared: 0.03506,
                                   Adjusted R-squared: 0.03409
## F-statistic: 36.26 on 1 and 998 DF, p-value: 2.427e-09
Constrain values to 0-10 range
# Process data
seven_3 <- seven_3.base %>%
   mutate(V1 = case_when(
              V1 < 1 ~ 1,
              V1 > 10 \sim 10,
              TRUE ~ V1)) %>%
   mutate(V2 = case_when(
              V2 < 0 ~ 0,
              V2 > 10 \sim 10,
```

```
TRUE ~ V2)) %>%
   mutate(group = 'No threshold')
# Plot processed data
ggMarginal(ggplot(data = seven_3) +
               aes(x = V1, y = V2) +
               geom_point() +
               geom hline(yintercept = mean(seven 3$V2),
                          colour = 'red', size = 1) +
               geom_vline(xintercept = mean(seven_3$V1),
                          colour = 'red', size = 1) +
               geom_rect(ymin = 0, ymax = 10,
                         xmin = 0, xmax = 10,
                         colour = '#000000',
                         alpha = 0,
                         linetype = 2) +
               annotate(geom = 'text', x = -5, y = 15,
                        hjust = 0, size = 5,
                        label = str_glue("r = {round(cor(seven_3$V1, seven_3$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven_3$V2) + 1.7,
                        hjust = 0, size = 5,
                        label = str_glue("Mean = {round(mean(seven_3$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven_3$V2) + 0.75,
                        hjust = 0, size = 5,
                        label = str glue("SD = {round(sd(seven 3$V2),2)}")) +
               annotate(geom = 'text', x = mean(seven_3$V1) + 0.2, y = -3.8,
                        hjust = 0, size = 5,
                        label = str_glue("Mean = {round(mean(seven_3$V1), 2)}")) +
               annotate(geom = 'text', x = mean(seven_3$V1) + 0.2, y = -4.75,
                        hjust = 0, size = 5,
                        label = str_glue("SD = {round(sd(seven_3$V1), 2)}")) +
               labs(title = 'B: Constrained (0-10 range)',
                    caption = 'Parameters: Mean = 7.2, SD = 2.2, Cor = 0.2') +
               scale_y_continuous(limits = c(-5, 15)) +
```

```
scale_x_continuous(limits = c(-5, 15)) +
theme(plot.caption = element_text(size = 14)))
```

# B: Constrained (0–10 range)



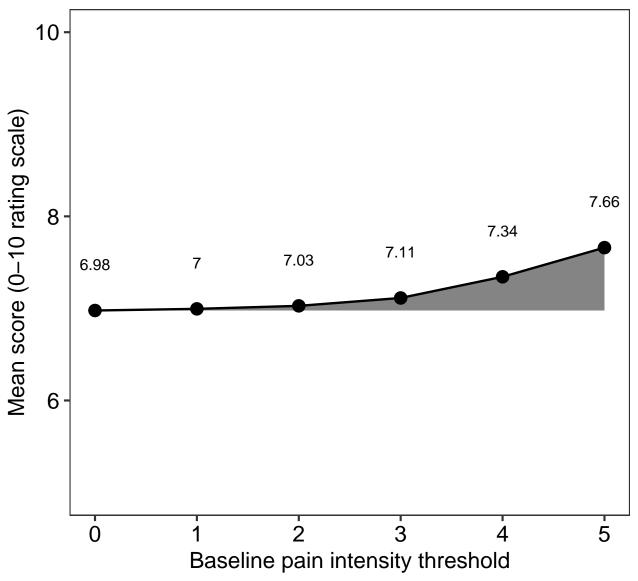
Parameters: Mean = 7.2, SD = 2.2, Cor = 0.2

```
# Linear regression
summary(lm(V2 ~ V1, data = seven_3))
##
## Call:
## lm(formula = V2 ~ V1, data = seven_3)
##
## Residuals:
## Min    1Q Median    3Q Max
## -6.5358 -1.3077    0.1519    1.5704    3.9376
##
## Coefficients:
```

### Model mean of V1 with increasing V1 thresholds from 0 to 5

```
# Extract visit 1 data
seven_3V1 <- seven_3$V1
# Generate a vector of threshold values to iterate over
cutoff <- 0:5
# Generate a vector of V1 means at each V1 threshold
seven 3V1.shift <- sapply(cutoff, function(x){mean(seven 3V1[seven 3V1 > x])})
# Calculate deviation
(seven_3V1.df <- data.frame(cutoff = cutoff,</pre>
                           mean = seven 3V1.shift) %>%
        mutate(deviation = mean - mean(seven 3V1)))
               mean deviation
     cutoff
## 1
        0 6.977233 0.00000000
## 2
         1 6.995219 0.01798566
## 3
         2 7.027714 0.05048026
## 4
         3 7.113306 0.13607222
## 5
         4 7.343401 0.36616808
         5 7.660189 0.68295586
## 6
# Plot data
ggplot(data = seven_3V1.df) +
   aes(x = cutoff, y = mean, ymin = mean(seven_3V1), ymax = mean) +
   geom ribbon(alpha = 0.6) +
   geom_point(size = 5) +
    geom line(size = 1) +
   geom_text(aes(label = round(mean, 2)),
              nudge y = 0.5, size = 5) +
    scale_y_continuous(limits = c(5, 10),
                       breaks = c(0, 2, 4, 6, 8, 10)) +
   labs(title = 'A: Shift in V1 mean with increasing V1 threshold value',
         caption = 'Parameters: Mean = 7.2, SD = 2.2, Cor = 0.2',
         x = 'Baseline pain intensity threshold',
         y = 'Mean score (0-10 rating scale)') +
    theme(plot.caption = element_text(size = 14))
```

# A: Shift in V1 mean with increasing V1 threshold value



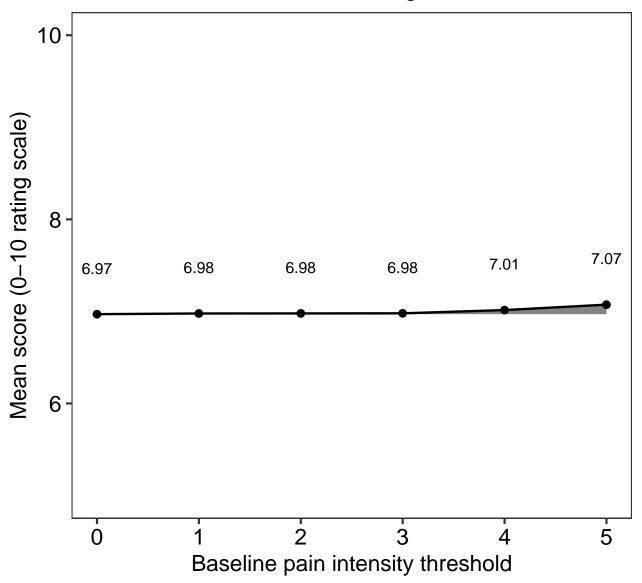
Parameters: Mean = 7.2, SD = 2.2, Cor = 0.2

## Model mean of V2 with increasing V1 thresholds from 0 to 5

#### mean(.))

```
# Calculate deviation
(seven_3V2.df <- data.frame(cutoff = cutoff,</pre>
                           mean = seven_3V2.shift) %>%
       mutate(deviation = mean - mean(seven_3V2)))
##
    cutoff
               mean deviation
## 1
         0 6.969986 0.000000000
## 2
         1 6.977457 0.007471655
## 3
         2 6.978098 0.008112313
## 4
         3 6.979226 0.009240947
## 5
         4 7.014595 0.044609353
## 6
         5 7.073418 0.103432683
# Plot data
ggplot(data = seven_3V2.df) +
   aes(x = cutoff, y = mean, ymin = mean(seven_3V2), ymax = mean) +
   geom_ribbon(alpha = 0.6) +
   geom_point(size = 3) +
   geom_line(size = 1) +
   geom_text(aes(label = round(mean, 2)),
              nudge_y = 0.5, size = 5) +
   scale_y_continuous(limits = c(5, 10),
                       breaks = c(0, 2, 4, 6, 8, 10)) +
   labs(title = 'B: Shift in V2 mean with increasing V1 threshold value',
         caption = 'Parameters: Mean = 7.2, SD = 2.2, Cor = 0.2',
         x = 'Baseline pain intensity threshold',
         y = 'Mean score (0-10 rating scale)') +
   theme(plot.caption = element_text(size = 14))
```

# B: Shift in V2 mean with increasing V1 threshold value



Parameters: Mean = 7.2, SD = 2.2, Cor = 0.2

### Placebo response

```
R = 2000,
traditional = FALSE,
bca = TRUE)
```

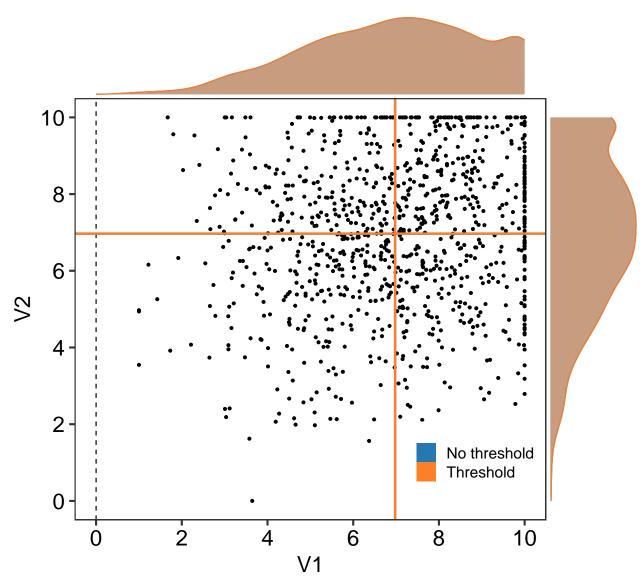
### $diff_3.0$ %.id <- 0

#### kable(diff 3.0)

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
0	1000	0.00725	0.95	-0.161	0.166

```
ggMarginal(placebo_3.0[, 1:3] %>%
               bind_rows(seven_3) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_3,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_3.0,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_3$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_3.0$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 0, linetype = 2) +
               geom_hline(yintercept = mean(seven_3$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_3.0$V2),
                          colour = pal[2], size = 1) +
               scale_y_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale colour manual(values = pal) +
               labs(title = 'A: Baseline pain threshold = 0',
                    caption = 'Parameters: Mean = 7.2, SD = 2.2, Cor = 0.2') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

# A: Baseline pain threshold = 0



Parameters: Mean = 7.2, SD = 2.2, Cor = 0.2

```
# Process data
placebo_3.3 <- seven_3 %>%
    filter(V1 >= 3) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_3.3 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_3.3,
R = 2000,
traditional = FALSE,
bca = TRUE)

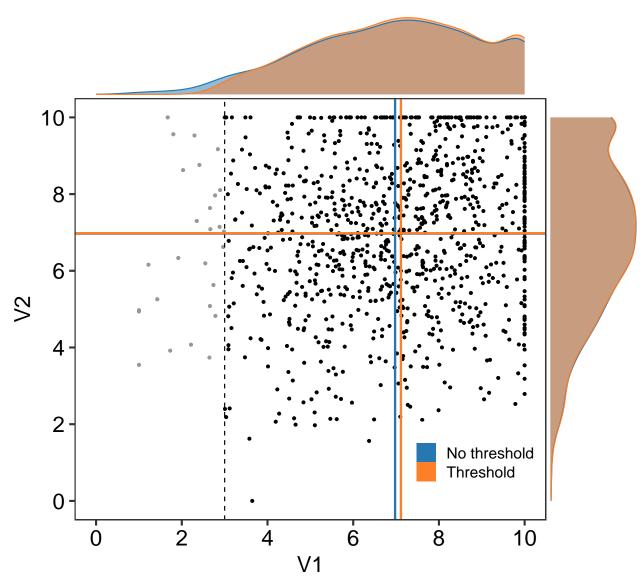
diff_3.3$.id <- 3
kable(diff_3.3)</pre>
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 3
 972
 0.134
 0.95
 -0.0215
 0.289

```
ggMarginal(placebo_3.3[, 1:3] %>%
               bind_rows(seven_3) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_3,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_3.3,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_3$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_3.3$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 3, linetype = 2) +
               geom_hline(yintercept = mean(seven_3$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_3.3$V2),
                          colour = pal[2], size = 1) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'B: Baseline pain threshold = 3',
                    caption = 'Parameters: Mean = 7.2, SD = 2.2, Cor = 0.2') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

# B: Baseline pain threshold = 3



Parameters: Mean = 7.2, SD = 2.2, Cor = 0.2

```
# Process that data
placebo_3.4 <- seven_3 %>%
    filter(V1 >= 4) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_3.4 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_3.4,
R = 2000,
traditional = FALSE,
bca = TRUE)

diff_3.4$.id <- 4

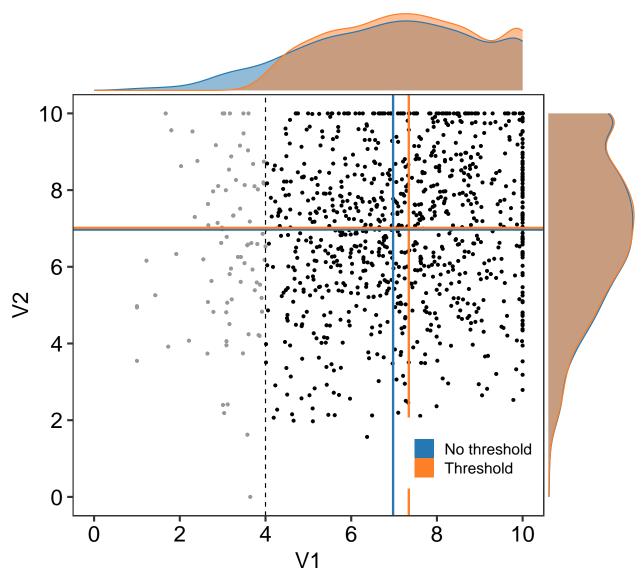
kable(diff_3.4)</pre>
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 4
 914
 0.329
 0.95
 0.159
 0.492

```
ggMarginal(placebo_3.4[, 1:3] %>%
               bind_rows(seven_3) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_3,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_3.4,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_3$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_3.4$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 4, linetype = 2) +
               geom_hline(yintercept = mean(seven_3$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_3.4$V2),
                          colour = pal[2], size = 1) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'C: Baseline pain threshold = 4',
                    caption = 'Parameters: Mean = 7.2, SD = 2.2, Cor = 0.2') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

# C: Baseline pain threshold = 4



Parameters: Mean = 7.2, SD = 2.2, Cor = 0.2

```
# Process that data
placebo_3.5 <- seven_3 %>%
    filter(V1 >= 5) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

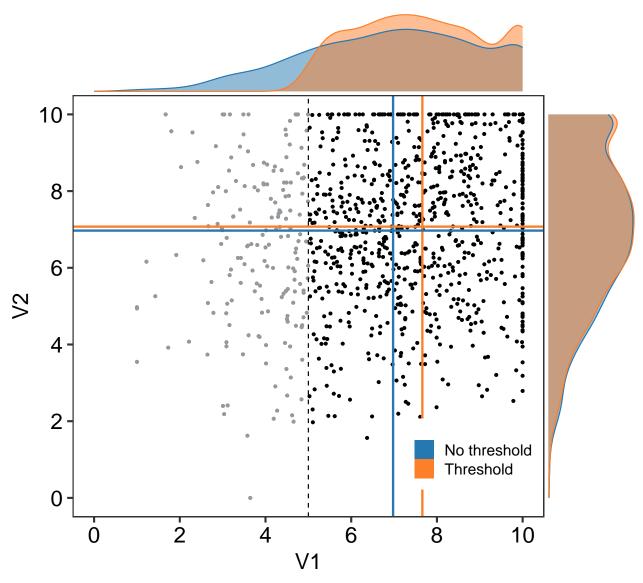
# Calculate the mean (95%CI) difference between V1 and V2
diff_3.5 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_3.5,
R = 2000,
traditional = FALSE,
bca = TRUE)

diff_3.5$.id <- 5
kable(diff_3.5)</pre>
```

```
ggMarginal(placebo_3.5[, 1:3] %>%
               bind_rows(seven_3) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_3,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_3.5,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_3$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_3.5$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 5, linetype = 2) +
               geom_hline(yintercept = mean(seven_3$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_3.5$V2),
                          colour = pal[2], size = 1) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'D: Baseline pain threshold = 5',
                    caption = 'Parameters: Mean = 7.2, SD = 2.2, Cor = 0.2') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

# D: Baseline pain threshold = 5



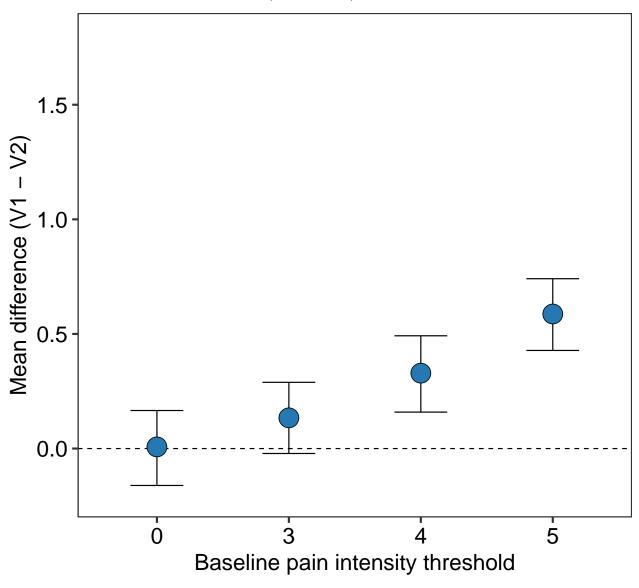
Parameters: Mean = 7.2, SD = 2.2, Cor = 0.2

# Difference plot

```
# Bind diff_*.* dataframes
diff_all_3 <- diff_3.0 %>%
  bind_rows(diff_3.3, diff_3.4, diff_3.5)

pp_3 <- diff_all_3 %>%
  mutate(Threshold = factor(.id)) %>%
  ggplot(data = .) +
  aes(x = Threshold,
    y = Mean,
    ymin = Bca.lower,
    ymax = Bca.upper) +
```

Parameters: Mean = 7.2, SD = 2.2, Cor = 0.2



# Publication plot

```
pp_4 <- pp_1 + pp_2 + pp_3
ggsave('figures/7.2_0.2.png', pp_4, width = 17, height = 7)</pre>
```

### Session information

## [61] stats4\_3.6.0

```
sessionInfo()
## R version 3.6.0 (2019-04-26)
## Platform: x86_64-apple-darwin15.6.0 (64-bit)
## Running under: macOS Mojave 10.14.6
##
## Matrix products: default
          /Library/Frameworks/R.framework/Versions/3.6/Resources/lib/libRblas.0.dylib
## LAPACK: /Library/Frameworks/R.framework/Versions/3.6/Resources/lib/libRlapack.dylib
## locale:
## [1] en_US.UTF-8/en_US.UTF-8/en_US.UTF-8/C/en_US.UTF-8/en_US.UTF-8
## attached base packages:
## [1] stats
                 graphics grDevices utils
                                               datasets methods
                                                                   base
##
## other attached packages:
## [1] patchwork_0.0.1 knitr_1.24
                                          MBESS_4.6.0
                                                           ggExtra_0.8
## [5] rcompanion_2.2.2 MASS_7.3-51.4
                                          magrittr_1.5
                                                           forcats_0.4.0
## [9] stringr_1.4.0
                         dplyr_0.8.3
                                          purrr_0.3.2
                                                           readr_1.3.1
## [13] tidyr_0.8.3.9000 tibble_2.1.3
                                          ggplot2_3.2.0
                                                           tidyverse_1.2.1
##
## loaded via a namespace (and not attached):
## [1] nlme 3.1-141
                           matrixStats 0.54.0 lubridate 1.7.4
## [4] httr_1.4.1
                           tools_3.6.0
                                              backports_1.1.4
## [7] R6_2.4.0
                           nortest_1.0-4
                                              lazyeval_0.2.2
## [10] colorspace_1.4-1
                           withr_2.1.2.9000
                                              tidyselect_0.2.5
## [13] compiler_3.6.0
                           cli_1.1.0
                                              rvest_0.3.4
## [16] expm_0.999-4
                           xml2_1.2.2
                                              sandwich_2.5-1
## [19] labeling_0.3
                           scales_1.0.0
                                              lmtest_0.9-37
## [22] mvtnorm_1.0-11
                           multcompView_0.1-7 digest_0.6.20
## [25] foreign_0.8-72
                           rmarkdown_1.14
                                              pkgconfig_2.0.2
## [28] htmltools_0.3.6
                           manipulate_1.0.1
                                              highr_0.8
## [31] rlang_0.4.0
                           readxl_1.3.1
                                              rstudioapi_0.10
## [34] shiny_1.3.2
                           generics_0.0.2
                                              zoo_1.8-6
## [37] jsonlite_1.6
                           modeltools_0.2-22 Matrix_1.2-17
## [40] Rcpp_1.0.2
                           DescTools_0.99.28
                                              munsell_0.5.0
## [43] stringi_1.4.3
                           multcomp_1.4-10
                                              yaml 2.2.0
## [46] plyr_1.8.4
                           grid 3.6.0
                                              parallel 3.6.0
## [49] promises_1.0.1
                           crayon_1.3.4
                                              miniUI_0.1.1.1
## [52] lattice_0.20-38
                           haven_2.1.1
                                              splines_3.6.0
## [55] hms_0.5.0
                           zeallot_0.1.0
                                              pillar_1.4.2
## [58] EMT_1.1
                           boot_1.3-23
                                              codetools_0.2-16
```

evaluate\_0.14

glue\_1.3.1

##	[64]	modelr_0.1.5	vctrs_0.2.0	httpuv_1.5.1
##	[67]	cellranger_1.1.0	gtable_0.3.0	assertthat_0.2.1
##	[70]	xfun_0.8	mime_0.7	coin_1.3-0
##	[73]	libcoin_1.0-4	xtable_1.8-4	broom_0.5.2
##	[76]	later 0.8.0	survival 2.44-1.1	TH.data 1.0-10