## Supplement 1

Flattening of the relationship between successive pain intensity ratings

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### 1 Introduction

The use of pain intensity cut-offs for study inclusion in clinical trial (typically a lower cut-off of 4/10 on an 11-point numerical pain rating scale) has two consequences. Firstly, the cut-off artificially raises the baseline mean pain score of the sample above that of the mean score of the population from which the sample was drawn. Secondly, unless the correlation between two sequential measurements is 1, there should be a "flattening" of the relationship between the first and subsequent measurements. This "flattening" means that the cut-off has a disproportionate effect on the mean baseline pain intensity compared to subsequent measurements.

This script demonstrates the "flattening" of the relationship between two sequential pain measurements in a hypothetical placebo group in a clinical trial for the management of neuropathic pain, in the absence of any cut-off. For both the baseline and subsequent measurement (V1 and V2, respectively), the mean pain

intensity was set at 6.2 (SD 1.7); typical baseline center and spread values for placebo groups in placebocontrolled trials for the management of neuropathic pain when there is no cut-off inclusion criterion (see Supplement 2). By using the same mean (SD) pain intensity for both measurements I have assumed that the pain is, on average, stable over the time period between the two measurements.

For the purposes of this simulation, I examined the relationship between the two measurements (V1 and V2) over a range of correlation values, namely: r = 1.0, 0.8, 0.5, and 0.2.

Also, I constructed the models under two conditions: constrained and unconstrained pain intensity ratings. For the unconstrained models I took the raw values obtained through sampling from a bivariate normal distribution. Thereafter, values were filtered (constrained) such that the minimum V1 value was 1 and the minimum V2 value was 0 on an 11-point NRS, and the maximum V1 and V2 values were 10 on an 11-point NRS. The minimum value of V1 was set to 1 because volunteers eligible to enter a placebo-controlled clinical trial can be expected to have at least some pain. In comparison, V2 values were unconstrained and could take any value from 0 to 10 because pain intensity may take values across the full range of the scale on follow-up. Maximum pain rating were limited to values of 10, the upper limit of the rating scale.

For reproducibility, I set the random seed to "2019" for all random sampling procedures.

Note: Because of random sampling the mean (SD) of the samples differ slightly from the population mean (SD).

### 2 Generate 2x2 covariance matrices

Generate covariance matrices using an SD of 1.7 and correlation of r = 1.0, 0.8, 0.5, and 0.2.

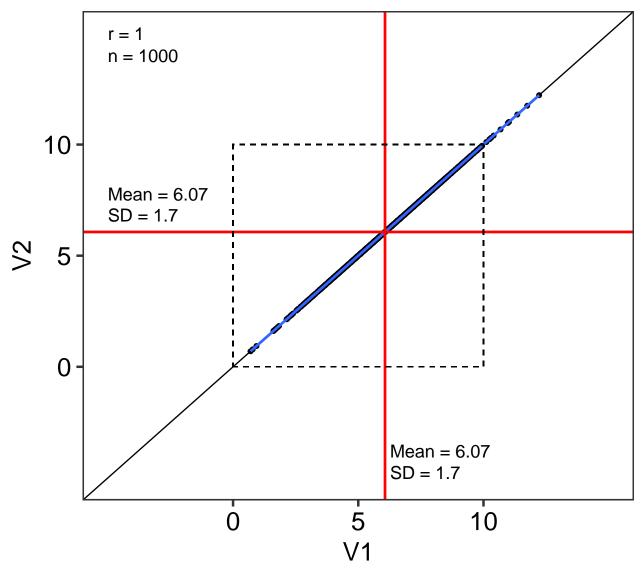
```
# Generate 2*2 correlation matrices
cor_10 \leftarrow matrix(c(1, 1, 1, 1), ncol = 2)
cor_08 \leftarrow matrix(c(1, 0.8, 0.8, 1), ncol = 2)
cor_05 \leftarrow matrix(c(1, 0.5, 0.5, 1), ncol = 2)
cor_02 \leftarrow matrix(c(1, 0.2, 0.2, 1), ncol = 2)
# Set the standard deviation
std <- c(1.7, 1.7)
# Generate 2*2 covariance matrices using the correlation matrices and SD
cov_10 <- cor2cov(cor.mat = cor_10,</pre>
                    sd = std)
cov_10
##
         [,1] [,2]
## [1,] 2.89 2.89
## [2,] 2.89 2.89
cov_08 <- cor2cov(cor.mat = cor_08,</pre>
                    sd = std)
cov_08
##
          [,1] [,2]
## [1,] 2.890 2.312
## [2,] 2.312 2.890
cov_05 \leftarrow cor2cov(cor.mat = cor_05,
                    sd = std)
cov_05
```

### 3 Correlation: r = 1.0

#### 3.1 Unconstrained data

```
# Set the random seed for reproducibility
set.seed(2019)
# Generate the data (1000 pairs from a bivariate normal distribution)
cor_10.base \leftarrow as.data.frame(mvrnorm(n = 1000, mu = c(6.2, 6.2), Sigma = cov_10))
# Plot unconstrained data
ggplot(data = cor_10.base) +
   aes(x = V1, y = V2) +
    geom_point() +
    geom_abline(slope = 1, intercept = 0) +
    geom_smooth(method = 'lm',
                se = FALSE) +
   geom hline(yintercept = mean(cor 10.base$V2),
               colour = 'red', size = 1) +
   geom_vline(xintercept = mean(cor_10.base$V1),
               colour = 'red', size = 1) +
    geom_rect(ymin = 0, ymax = 10,
              xmin = 0, xmax = 10,
              colour = '#000000',
              alpha = 0,
              linetype = 2) +
    annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5,
             label = str_glue("r = {round(cor(cor_10.base$V1,
                              cor 10.base$V2), 2)}")) +
    annotate(geom = 'text', x = -5, y = 14, hjust = 0, size = 5,
             label = str_glue("n = {round(nrow(cor_10.base))}")) +
    annotate(geom = 'text', x = -5, y = mean(cor_10.base$V2) + 1.7,
             hjust = 0, size = 5,
             label = str_glue("Mean = {round(mean(cor_10.base$V2), 2)}")) +
    annotate(geom = 'text', x = -5, y = mean(cor 10.base$V2) + 0.75,
             hjust = 0, size = 5,
             label = str_glue("SD = {round(sd(cor_10.base$V2),2)}")) +
   annotate(geom = 'text', x = mean(cor_10.base$V1) + 0.2, y = -3.8,
             hjust = 0, size = 5,
```

## A: Unconstained



Population parameters: Mean = 6.2, SD = 1.7, r = 1.0

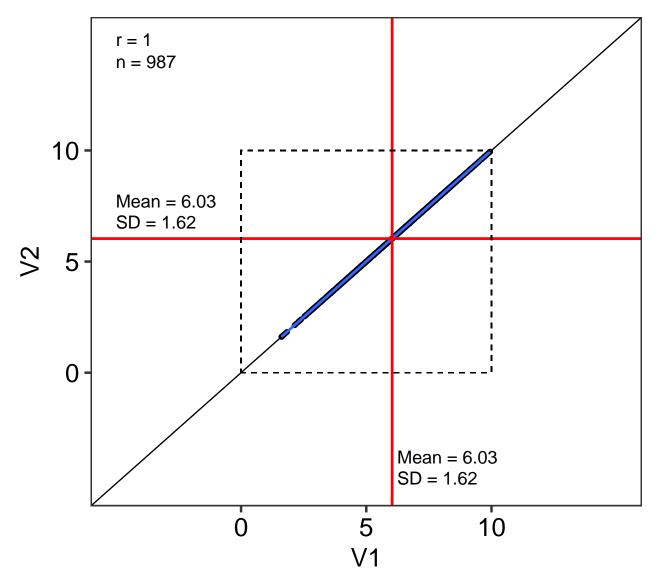
```
# Linear regression
summary(lm(V2 ~ V1, data = cor_10.base))
## Warning in summary.lm(lm(V2 ~ V1, data = cor_10.base)): essentially perfect fit:
## summary may be unreliable
##
## Call:
## lm(formula = V2 ~ V1, data = cor_10.base)
## Residuals:
##
         Min
                     1Q
                            Median
                                           3Q
## -5.232e-14 3.000e-18 4.900e-17 9.800e-17 1.548e-15
##
## Coefficients:
                Estimate Std. Error
                                       t value Pr(>|t|)
## (Intercept) -5.393e-15 1.945e-16 -2.773e+01 <2e-16 ***
               1.000e+00 3.087e-17 3.240e+16 <2e-16 ***
## V1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.662e-15 on 998 degrees of freedom
                           1, Adjusted R-squared:
## Multiple R-squared:
## F-statistic: 1.05e+33 on 1 and 998 DF, p-value: < 2.2e-16
Confint(lm(V2 ~ V1, data = cor_10.base))
## Warning in summary.lm(object, ...): essentially perfect fit: summary may be
## unreliable
                                   2.5 %
                                                 97.5 %
                  Estimate
## (Intercept) -5.39264e-15 -5.774318e-15 -5.010962e-15
## V1
               1.00000e+00 1.000000e+00 1.000000e+00
```

### 3.2 Constrained data

```
# Constrain data
cor_10.constrained <- cor_10.base %>%
   filter(V1 >= 1 & V1 <= 10) %>%
   filter(V2 >= 0 & V2 <= 10) %>%
   mutate(group = 'No threshold')
# Plot constrained data
ggplot(data = cor_10.constrained) +
    aes(x = V1, y = V2) +
    geom_point() +
    geom_abline(slope = 1, intercept = 0) +
    geom_smooth(method = 'lm',
                se = FALSE) +
    geom_hline(yintercept = mean(cor_10.constrained$V2),
               colour = 'red', size = 1) +
    geom vline(xintercept = mean(cor 10.constrained$V1),
               colour = 'red', size = 1) +
    geom_rect(ymin = 0, ymax = 10,
```

```
xmin = 0, xmax = 10,
          colour = '#000000',
          alpha = 0,
          linetype = 2) +
annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5,
         label = str_glue("r = {round(cor(cor_10.constrained$V1,
                                     cor_10.constrained$V2), 2)}")) +
annotate(geom = 'text', x = -5, y = 14, hjust = 0, size = 5,
         label = str_glue("n = {round(nrow(cor_10.constrained))}")) +
annotate(geom = 'text', x = -5, y = mean(cor_10.constrained$V2) + 1.7,
         hjust = 0, size = 5,
         label = str_glue("Mean = {round(mean(cor_10.constrained$V2), 2)}")) +
annotate(geom = 'text', x = -5, y = mean(cor_10.constrained$V2) + 0.75,
         hjust = 0, size = 5,
         label = str_glue("SD = {round(sd(cor_10.constrained$V2),2)}")) +
annotate(geom = 'text', x = mean(cor_10.constrained$V1) + 0.2, y = -3.8,
         hjust = 0, size = 5,
         label = str_glue("Mean = {round(mean(cor_10.constrained$V1), 2)}")) +
annotate(geom = 'text', x = mean(cor_10.constrained$V1) + 0.2, y = -4.75,
         hjust = 0, size = 5,
         label = str_glue("SD = {round(sd(cor_10.constrained$V1), 2)}")) +
labs(title = 'B: Constrained',
     caption = 'Population parameters: Mean = 6.2, SD = 1.7, r = 1.0') +
scale_y_continuous(limits = c(-5, 15),
                   breaks = c(0, 5, 10)) +
scale_x_continuous(limits = c(-5, 15),
                  breaks = c(0, 5, 10) +
theme(plot.caption = element_text(size = 14))
```

# **B**: Constrained



Population parameters: Mean = 6.2, SD = 1.7, r = 1.0

```
# Linear regression
summary(lm(V2 ~ V1, data = cor_10.constrained))
## Warning in summary.lm(lm(V2 ~ V1, data = cor_10.constrained)): essentially
## perfect fit: summary may be unreliable
##
## Call:
## lm(formula = V2 ~ V1, data = cor_10.constrained)
##
## Residuals:
                             Median
         Min
                      1Q
                                            ЗQ
                                                      Max
## -4.814e-14 3.000e-18 4.800e-17 9.500e-17 1.553e-15
##
## Coefficients:
```

```
Estimate Std. Error
                                      t value Pr(>|t|)
## (Intercept) -5.428e-15 1.895e-16 -2.865e+01 <2e-16 ***
## V1
              1.000e+00 3.033e-17 3.297e+16
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.54e-15 on 985 degrees of freedom
## Multiple R-squared:
                           1, Adjusted R-squared:
## F-statistic: 1.087e+33 on 1 and 985 DF, p-value: < 2.2e-16
Confint(lm(V2 ~ V1, data = cor_10.constrained))
## Warning in summary.lm(object, ...): essentially perfect fit: summary may be
## unreliable
                   Estimate
                                    2.5 %
                                                97.5 %
## (Intercept) -5.428038e-15 -5.799812e-15 -5.056264e-15
               1.000000e+00 1.000000e+00 1.000000e+00
```

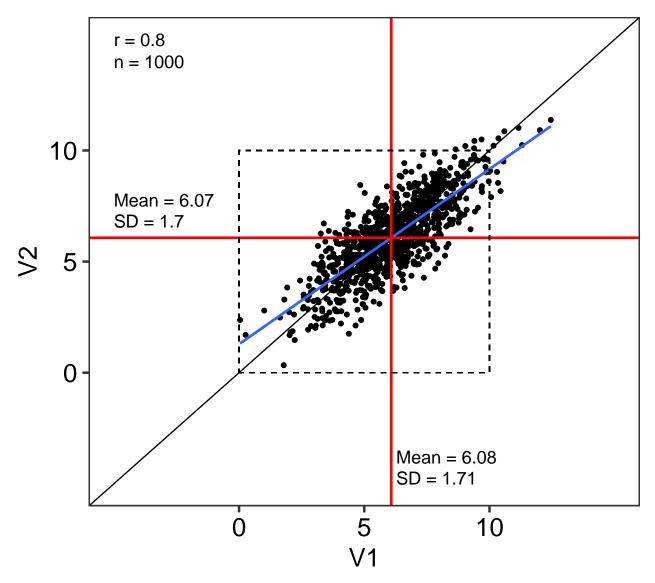
### 4 Correlation: r = 0.8

#### 4.1 Unconstrained data

```
# Set the random seed for reproducibility
set.seed(2019)
# Generate the data (1000 pairs from a bivariate normal distribution)
cor_08.base \leftarrow as.data.frame(mvrnorm(n = 1000, mu = c(6.2, 6.2), Sigma = cov_08))
# Plot unconstrained data
ggplot(data = cor_08.base) +
   aes(x = V1, y = V2) +
   geom_point() +
   geom_abline(slope = 1, intercept = 0) +
    geom_smooth(method = 'lm',
                se = FALSE) +
    geom_hline(yintercept = mean(cor_08.base$V2),
               colour = 'red', size = 1) +
    geom_vline(xintercept = mean(cor_08.base$V1),
               colour = 'red', size = 1) +
    geom_rect(ymin = 0, ymax = 10,
              xmin = 0, xmax = 10,
              colour = '#000000',
              alpha = 0,
              linetype = 2) +
    annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5,
             label = str_glue("r = {round(cor(cor_08.base$V1,
                              cor_08.base$V2), 2)}")) +
    annotate(geom = 'text', x = -5, y = 14, hjust = 0, size = 5,
             label = str_glue("n = {round(nrow(cor_08.base))}")) +
    annotate(geom = 'text', x = -5, y = mean(cor_08.base$V2) + 1.7,
```

```
hjust = 0, size = 5,
         label = str_glue("Mean = {round(mean(cor_08.base$V2), 2)}")) +
annotate(geom = 'text', x = -5, y = mean(cor_08.base$V2) + 0.75,
        hjust = 0, size = 5,
         label = str_glue("SD = {round(sd(cor_08.base$V2),2)}")) +
annotate(geom = 'text', x = mean(cor_08.base$V1) + 0.2, y = -3.8,
         hjust = 0, size = 5,
         label = str_glue("Mean = {round(mean(cor_08.base$V1), 2)}")) +
annotate(geom = 'text', x = mean(cor_08.base$V1) + 0.2, y = -4.75,
        hjust = 0, size = 5,
        label = str_glue("SD = {round(sd(cor_08.base$V1), 2)}")) +
labs(title = 'A: Unconstained',
     caption = 'Population parameters: Mean = 6.2, SD = 1.7, r = 0.8') +
scale_y_continuous(limits = c(-5, 15),
                   breaks = c(0, 5, 10)) +
scale_x_continuous(limits = c(-5, 15),
                   breaks = c(0, 5, 10)) +
theme(plot.caption = element_text(size = 14))
```

# A: Unconstained

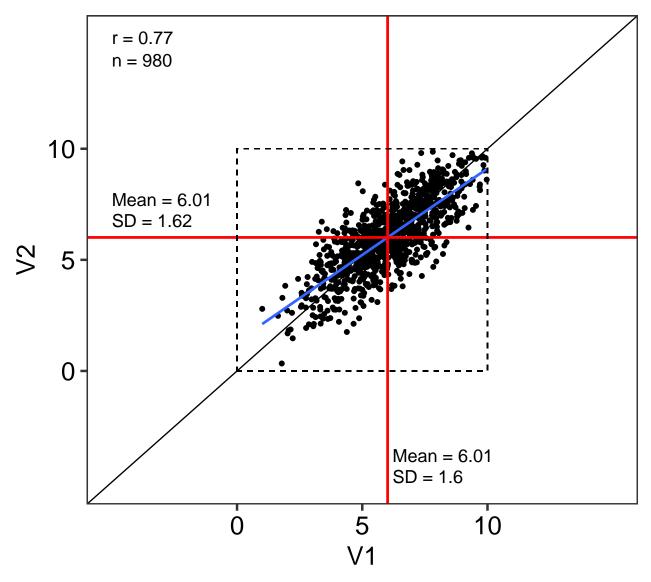


Population parameters: Mean = 6.2, SD = 1.7, r = 0.8

#### 4.2 Constrained data

```
# Constrain data
cor_08.constrained <- cor_08.base %>%
   filter(V1 >= 1 & V1 <= 10) %>%
   filter(V2 >= 0 & V2 <= 10) %>%
   mutate(group = 'No threshold')
# Plot constrained data
ggplot(data = cor_08.constrained) +
    aes(x = V1, y = V2) +
    geom_point() +
   geom_abline(slope = 1, intercept = 0) +
    geom_smooth(method = 'lm',
                se = FALSE) +
    geom_hline(yintercept = mean(cor_08.constrained$V2),
              colour = 'red', size = 1) +
    geom vline(xintercept = mean(cor 08.constrained$V1),
              colour = 'red', size = 1) +
    geom_rect(ymin = 0, ymax = 10,
              xmin = 0, xmax = 10,
              colour = '#000000',
              alpha = 0,
              linetype = 2) +
    annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5,
             label = str_glue("r = {round(cor(cor_08.constrained$V1,
                             cor_08.constrained$V2), 2)}")) +
    annotate(geom = 'text', x = -5, y = 14, hjust = 0, size = 5,
             label = str_glue("n = {round(nrow(cor_08.constrained))}")) +
    annotate(geom = 'text', x = -5, y = mean(cor_08.constrained$V2) + 1.7,
             hjust = 0, size = 5,
             label = str_glue("Mean = {round(mean(cor_08.constrained$V2), 2)}")) +
    annotate(geom = 'text', x = -5, y = mean(cor_08.constrained$V2) + 0.75,
             hjust = 0, size = 5,
             label = str glue("SD = {round(sd(cor 08.constrained$V2),2)}")) +
    annotate(geom = 'text', x = mean(cor_08.constrained$V1) + 0.2, y = -3.8,
             hjust = 0, size = 5,
             label = str_glue("Mean = {round(mean(cor_08.constrained$V1), 2)}")) +
    annotate(geom = 'text', x = mean(cor_08.constrained$V1) + 0.2, y = -4.75,
```

## **B**: Constrained



Population parameters: Mean = 6.2, SD = 1.7, r = 0.8

```
# Linear regression
summary(lm(V2 ~ V1, data = cor_08.constrained))
```

```
##
## Call:
## lm(formula = V2 ~ V1, data = cor_08.constrained)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -2.9875 -0.6579 0.0259 0.6839 3.3476
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.33056
                          0.12744
                                    10.44
                                            <2e-16 ***
                          0.02048
                                    37.98
               0.77811
                                            <2e-16 ***
## V1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.028 on 978 degrees of freedom
## Multiple R-squared: 0.596, Adjusted R-squared: 0.5956
## F-statistic: 1443 on 1 and 978 DF, p-value: < 2.2e-16
Confint(lm(V2 ~ V1, data = cor_08.constrained))
                           2.5 %
##
               Estimate
                                    97.5 %
## (Intercept) 1.3305625 1.080473 1.5806523
              0.7781086 0.737910 0.8183071
```

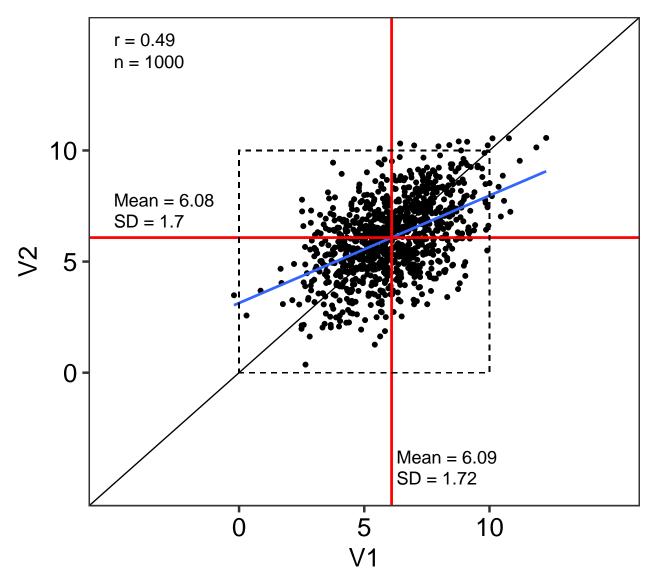
### 5 Correlation: r = 0.5

#### 5.1 Unconstrained data

```
# Set the random seed for reproducibility
set.seed(2019)
# Generate the data (1000 pairs from a bivariate normal distribution)
cor_05.base \leftarrow as.data.frame(mvrnorm(n = 1000, mu = c(6.2, 6.2), Sigma = cov_05))
# Plot unconstrained data
ggplot(data = cor_05.base) +
    aes(x = V1, y = V2) +
    geom_point() +
    geom_abline(slope = 1, intercept = 0) +
    geom_smooth(method = 'lm',
                se = FALSE) +
    geom_hline(yintercept = mean(cor_05.base$V2),
               colour = 'red', size = 1) +
    geom_vline(xintercept = mean(cor_05.base$V1),
               colour = 'red', size = 1) +
    geom_rect(ymin = 0, ymax = 10,
              xmin = 0, xmax = 10,
              colour = '#000000',
              alpha = 0,
              linetype = 2) +
```

```
annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5,
         label = str_glue("r = {round(cor(cor_05.base$V1,
                          cor_05.base$V2), 2)}")) +
annotate(geom = 'text', x = -5, y = 14, hjust = 0, size = 5,
         label = str_glue("n = {round(nrow(cor_05.base))}")) +
annotate(geom = 'text', x = -5, y = mean(cor_05.base$V2) + 1.7,
         hjust = 0, size = 5,
         label = str_glue("Mean = {round(mean(cor_05.base$V2), 2)}")) +
annotate(geom = 'text', x = -5, y = mean(cor_05.base$V2) + 0.75,
         hjust = 0, size = 5,
         label = str_glue("SD = {round(sd(cor_05.base$V2),2)}")) +
annotate(geom = 'text', x = mean(cor_05.base$V1) + 0.2, y = -3.8,
         hjust = 0, size = 5,
         label = str_glue("Mean = {round(mean(cor_05.base$V1), 2)}")) +
annotate(geom = 'text', x = mean(cor_05.base$V1) + 0.2, y = -4.75,
         hjust = 0, size = 5,
         label = str_glue("SD = {round(sd(cor_05.base$V1), 2)}")) +
labs(title = 'A: Unconstained',
     caption = 'Population parameters: Mean = 6.2, SD = 1.7, r = 0.5') +
scale_y_continuous(limits = c(-5, 15),
                   breaks = c(0, 5, 10)) +
scale_x_continuous(limits = c(-5, 15),
                  breaks = c(0, 5, 10) +
theme(plot.caption = element_text(size = 14))
```

# A: Unconstained

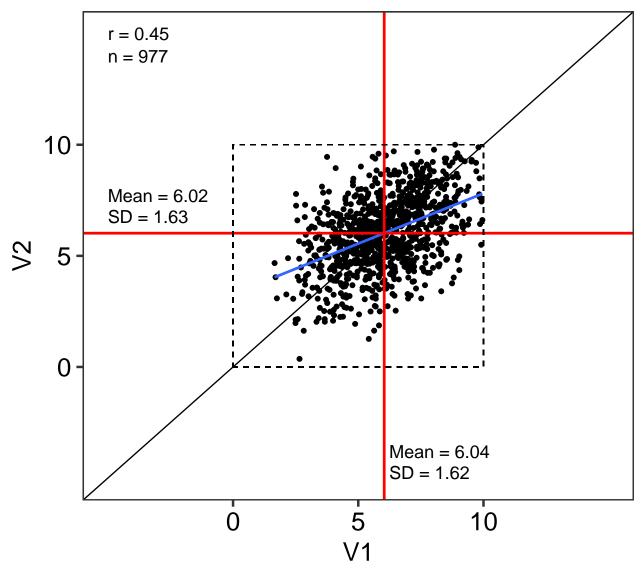


Population parameters: Mean = 6.2, SD = 1.7, r = 0.5

#### 5.2 Constrained data

```
# Constrain data
cor_05.constrained <- cor_05.base %>%
   filter(V1 >= 1 & V1 <= 10) %>%
   filter(V2 >= 0 & V2 <= 10) %>%
   mutate(group = 'No threshold')
# Plot constrained data
ggplot(data = cor_05.constrained) +
    aes(x = V1, y = V2) +
    geom_point() +
   geom_abline(slope = 1, intercept = 0) +
    geom_smooth(method = 'lm',
                se = FALSE) +
    geom_hline(yintercept = mean(cor_05.constrained$V2),
              colour = 'red', size = 1) +
    geom vline(xintercept = mean(cor 05.constrained$V1),
              colour = 'red', size = 1) +
    geom_rect(ymin = 0, ymax = 10,
              xmin = 0, xmax = 10,
              colour = '#000000',
              alpha = 0,
              linetype = 2) +
    annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5,
             label = str_glue("r = {round(cor(cor_05.constrained$V1,
                             cor_05.constrained$V2), 2)}")) +
    annotate(geom = 'text', x = -5, y = 14, hjust = 0, size = 5,
             label = str_glue("n = {round(nrow(cor_05.constrained))}")) +
    annotate(geom = 'text', x = -5, y = mean(cor_05.constrained$V2) + 1.7,
             hjust = 0, size = 5,
             label = str_glue("Mean = {round(mean(cor_05.constrained$V2), 2)}")) +
    annotate(geom = 'text', x = -5, y = mean(cor_05.constrained$V2) + 0.75,
             hjust = 0, size = 5,
             label = str glue("SD = {round(sd(cor 05.constrained$V2),2)}")) +
    annotate(geom = 'text', x = mean(cor_05.constrained$V1) + 0.2, y = -3.8,
             hjust = 0, size = 5,
             label = str_glue("Mean = {round(mean(cor_05.constrained$V1), 2)}")) +
    annotate(geom = 'text', x = mean(cor_05.constrained$V1) + 0.2, y = -4.75,
```

## **B**: Constrained



Population parameters: Mean = 6.2, SD = 1.7, r = 0.5

```
# Linear regression
summary(lm(V2 ~ V1, data = cor_05.constrained))
```

```
##
## Call:
## lm(formula = V2 ~ V1, data = cor_05.constrained)
## Residuals:
##
                               3Q
      Min
               1Q Median
                                      Max
## -4.4780 -0.9659 0.0715 1.0044 4.4663
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                3.2874
                           0.1806
                                    18.21
                                            <2e-16 ***
                           0.0289
                0.4526
                                    15.66
                                            <2e-16 ***
## V1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.458 on 975 degrees of freedom
## Multiple R-squared: 0.201, Adjusted R-squared: 0.2002
## F-statistic: 245.3 on 1 and 975 DF, p-value: < 2.2e-16
Confint(lm(V2 ~ V1, data = cor_05.constrained))
                            2.5 %
##
               Estimate
                                     97.5 %
## (Intercept) 3.2873685 2.9330333 3.6417037
## V1
              0.4526108 0.3958984 0.5093231
```

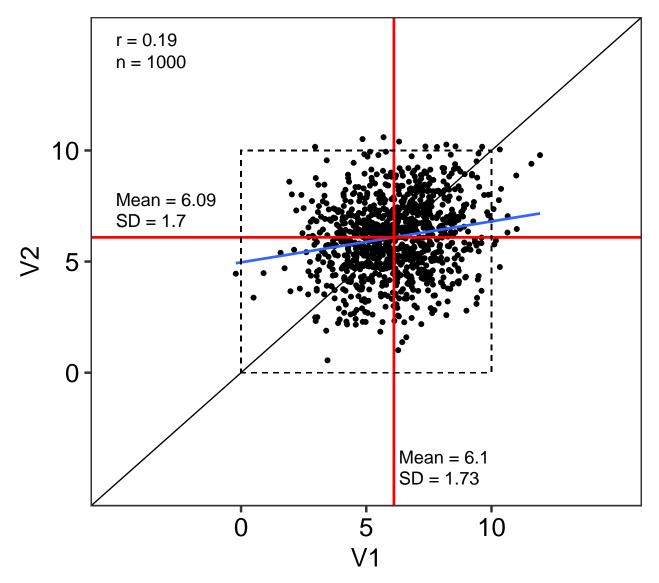
### 6 Correlation: r = 0.2

#### 6.1 Unconstrained data

```
# Set the random seed for reproducibility
set.seed(2019)
# Generate the data
cor_02.base \leftarrow as.data.frame(mvrnorm(n = 1000, mu = c(6.2, 6.2), Sigma = cov_02))
# Plot unconstrained data
ggplot(data = cor_02.base) +
    aes(x = V1, y = V2) +
    geom_point() +
    geom_abline(slope = 1, intercept = 0) +
    geom_smooth(method = 'lm',
                se = FALSE) +
    geom_hline(yintercept = mean(cor_02.base$V2),
               colour = 'red', size = 1) +
    geom_vline(xintercept = mean(cor_02.base$V1),
               colour = 'red', size = 1) +
    geom_rect(ymin = 0, ymax = 10,
              xmin = 0, xmax = 10,
              colour = '#000000',
              alpha = 0,
              linetype = 2) +
```

```
annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5,
         label = str_glue("r = {round(cor(cor_02.base$V1,
                          cor_02.base$V2), 2)}")) +
annotate(geom = 'text', x = -5, y = 14, hjust = 0, size = 5,
         label = str_glue("n = {round(nrow(cor_02.base))}")) +
annotate(geom = 'text', x = -5, y = mean(cor_02.base$V2) + 1.7,
         hjust = 0, size = 5,
         label = str_glue("Mean = {round(mean(cor_02.base$V2), 2)}")) +
annotate(geom = 'text', x = -5, y = mean(cor_02.base$V2) + 0.75,
         hjust = 0, size = 5,
         label = str_glue("SD = {round(sd(cor_02.base$V2),2)}")) +
annotate(geom = 'text', x = mean(cor_02.base$V1) + 0.2, y = -3.8,
         hjust = 0, size = 5,
         label = str_glue("Mean = {round(mean(cor_02.base$V1), 2)}")) +
annotate(geom = 'text', x = mean(cor_02.base\$V1) + 0.2, y = -4.75,
         hjust = 0, size = 5,
         label = str_glue("SD = {round(sd(cor_02.base$V1), 2)}")) +
labs(title = 'A: Unconstained',
     caption = 'Population parameters: Mean = 6.2, SD = 1.7, r = 0.2') +
scale_y_continuous(limits = c(-5, 15),
                   breaks = c(0, 5, 10)) +
scale_x_continuous(limits = c(-5, 15),
                  breaks = c(0, 5, 10) +
theme(plot.caption = element_text(size = 14))
```

# A: Unconstained

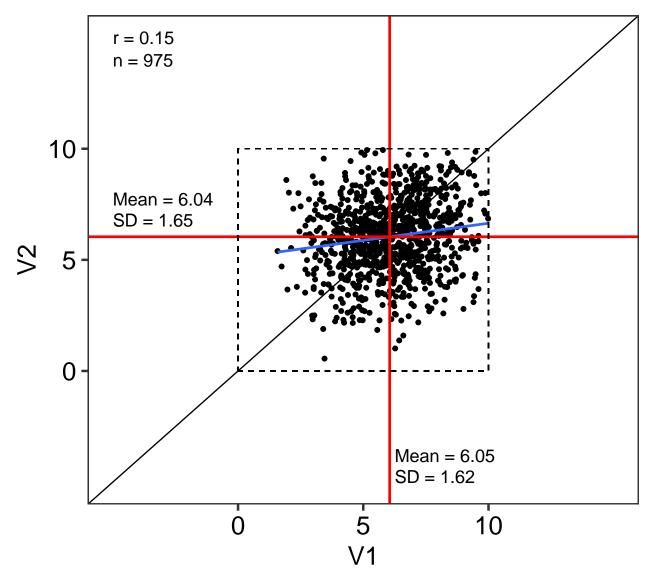


Population parameters: Mean = 6.2, SD = 1.7, r = 0.2

#### 6.2 Constrained data

```
# Constrain data
cor_02.constrained <- cor_02.base %>%
   filter(V1 >= 1 & V1 <= 10) %>%
   filter(V2 >= 0 & V2 <= 10) %>%
   mutate(group = 'No threshold')
# Plot constrained data
ggplot(data = cor_02.constrained) +
    aes(x = V1, y = V2) +
    geom_point() +
   geom_abline(slope = 1, intercept = 0) +
    geom_smooth(method = 'lm',
                se = FALSE) +
    geom_hline(yintercept = mean(cor_02.constrained$V2),
              colour = 'red', size = 1) +
    geom vline(xintercept = mean(cor 02.constrained$V1),
              colour = 'red', size = 1) +
    geom_rect(ymin = 0, ymax = 10,
              xmin = 0, xmax = 10,
              colour = '#000000',
              alpha = 0,
              linetype = 2) +
    annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5,
             label = str_glue("r = {round(cor(cor_02.constrained$V1,
                             cor_02.constrained$V2), 2)}")) +
    annotate(geom = 'text', x = -5, y = 14, hjust = 0, size = 5,
             label = str_glue("n = {round(nrow(cor_02.constrained))}")) +
    annotate(geom = 'text', x = -5, y = mean(cor_02.constrained$V2) + 1.7,
             hjust = 0, size = 5,
             label = str_glue("Mean = {round(mean(cor_02.constrained$V2), 2)}")) +
    annotate(geom = 'text', x = -5, y = mean(cor_02.constrained$V2) + 0.75,
             hjust = 0, size = 5,
             label = str glue("SD = {round(sd(cor 02.constrained$V2),2)}")) +
    annotate(geom = 'text', x = mean(cor_02.constrained$V1) + 0.2, y = -3.8,
             hjust = 0, size = 5,
             label = str_glue("Mean = {round(mean(cor_02.constrained$V1), 2)}")) +
    annotate(geom = 'text', x = mean(cor_02.constrained$V1) + 0.2, y = -4.75,
```

## **B**: Constrained



Population parameters: Mean = 6.2, SD = 1.7, r = 0.2

```
# Linear regression
summary(lm(V2 ~ V1, data = cor_02.constrained))
```

```
##
## Call:
## lm(formula = V2 ~ V1, data = cor_02.constrained)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -5.0812 -1.0431 0.0732 1.1351 4.0403
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 5.10485
                          0.20205 25.265 < 2e-16 ***
               0.15424
                          0.03224
                                   4.784 1.98e-06 ***
## V1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.632 on 973 degrees of freedom
## Multiple R-squared: 0.02298,
                                   Adjusted R-squared: 0.02198
## F-statistic: 22.89 on 1 and 973 DF, p-value: 1.983e-06
Confint(lm(V2 ~ V1, data = cor_02.constrained))
##
                             2.5 %
                                      97.5 %
               Estimate
## (Intercept) 5.1048528 4.70834309 5.5013625
## V1
              0.1542393 0.09097187 0.2175067
```

### 7 Publication plots

The output of the code is plotted to a 'PNG' graphics file.

```
\# r = 1.0
plot_1 <- ggplot(data = cor_10.constrained) +</pre>
    aes(x = V1, y = V2) +
    geom_point() +
    geom_abline(slope = 1, intercept = 0) +
    geom_smooth(method = 'lm',
                se = FALSE,
                size = 1.5) +
    geom_hline(yintercept = mean(cor_10.constrained$V2),
               colour = 'red') +
    geom_vline(xintercept = mean(cor_10.constrained$V1),
               colour = 'red') +
    geom_rect(ymin = 0, ymax = 10,
              xmin = 0, xmax = 10,
              colour = '#000000',
              alpha = 0,
              linetype = 2) +
    annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 6,
             label = str_glue("r* = {round(cor(cor_10.constrained$V1,
                                          cor_10.constrained$V2), 2)}")) +
    annotate(geom = 'text', x = -5, y = 13.7, hjust = 0, size = 6,
             label = str_glue("n* = {round(nrow(cor_10.constrained))}")) +
    annotate(geom = 'text', x = -5, y = mean(cor_10.constrained$V2) + 1.7,
```

```
hjust = 0, size = 4,
             label = str_glue("Mean = {round(mean(cor_10.constrained$V2), 2)}")) +
    annotate(geom = 'text', x = -5, y = mean(cor_10.constrained$V2) + 0.75,
             hjust = 0, size = 4,
             label = str_glue("SD = {round(sd(cor_10.constrained$V2),2)}")) +
    annotate(geom = 'text', x = mean(cor_10.constrained$V1) + 0.2, y = -3.8,
             hjust = 0, size = 4,
             label = str_glue("Mean = {round(mean(cor_10.constrained$V1), 2)}")) +
    annotate(geom = 'text', x = mean(cor_10.constrained$V1) + 0.2, y = -4.75,
             hjust = 0, size = 4,
             label = str_glue("SD = {round(sd(cor_10.constrained$V1), 2)}")) +
    labs(subtitle = 'Population parameters: Mean = 6.2, SD = 1.7, r = 1.0') +
    scale_y_continuous(limits = c(-5, 15),
                       breaks = c(0, 5, 10)) +
    scale_x_continuous(limits = c(-5, 15),
                       breaks = c(0, 5, 10) +
   theme_bw(base_size = 18) +
    theme(axis.text = element_text(colour = '#000000'),
          axis.title.x = element_blank(),
          panel.grid = element_blank(),
         plot.subtitle = element_text(size = 14))
\# r = 0.8
plot_2 <- ggplot(data = cor_08.constrained) +</pre>
    aes(x = V1, y = V2) +
    geom_point() +
    geom abline(slope = 1, intercept = 0) +
    geom_smooth(method = 'lm',
                se = FALSE,
                size = 1.5) +
    geom hline(yintercept = mean(cor 08.constrained$V2),
               colour = 'red') +
    geom_vline(xintercept = mean(cor_08.constrained$V1),
               colour = 'red') +
    geom_rect(ymin = 0, ymax = 10,
              xmin = 0, xmax = 10,
              colour = '#000000',
              alpha = 0,
              linetype = 2) +
    annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 6,
             label = str_glue("r* = {round(cor(cor_08.constrained$V1,
                              cor_08.constrained$V2), 2)}")) +
    annotate(geom = 'text', x = -5, y = 13.7, hjust = 0, size = 6,
             label = str glue("n* = {round(nrow(cor 08.constrained))}")) +
    annotate(geom = 'text', x = -5, y = mean(cor_08.constrained$V2) + 1.7,
             hjust = 0, size = 4,
             label = str_glue("Mean = {round(mean(cor_08.constrained$V2), 2)}")) +
    annotate(geom = 'text', x = -5, y = mean(cor_08.constrained$V2) + 0.75,
             hjust = 0, size = 4,
             label = str_glue("SD = {round(sd(cor_08.constrained$V2),2)}")) +
    annotate(geom = 'text', x = mean(cor_08.constrained$V1) + 0.2, y = -3.8,
             hjust = 0, size = 4,
             label = str_glue("Mean = {round(mean(cor_08.constrained$V1), 2)}")) +
```

```
annotate(geom = 'text', x = mean(cor_08.constrained$V1) + 0.2, y = -4.75,
             hjust = 0, size = 4,
             label = str_glue("SD = {round(sd(cor_08.constrained$V1), 2)}")) +
    labs(subtitle = 'Population parameters: Mean = 6.2, SD = 1.7, r = 0.8') +
    scale_y_continuous(limits = c(-5, 15),
                       breaks = c(0, 5, 10)) +
    scale_x_continuous(limits = c(-5, 15),
                      breaks = c(0, 5, 10) +
   theme_bw(base_size = 18) +
    theme(axis.text = element_text(colour = '#000000'),
          axis.title = element_blank(),
          panel.grid = element_blank(),
         plot.subtitle = element_text(size = 14))
\# r = 0.5
plot_3 <- ggplot(data = cor_05.constrained) +</pre>
    aes(x = V1, y = V2) +
    geom_point() +
    geom_abline(slope = 1, intercept = 0) +
    geom_smooth(method = 'lm',
                se = FALSE,
                size = 1.5) +
    geom_hline(yintercept = mean(cor_05.constrained$V2),
               colour = 'red') +
    geom_vline(xintercept = mean(cor_05.constrained$V1),
               colour = 'red') +
    geom_rect(ymin = 0, ymax = 10,
              xmin = 0, xmax = 10,
              colour = '#000000',
              alpha = 0,
              linetype = 2) +
    annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 6,
             label = str_glue("r* = {round(cor(cor_05.constrained$V1,
                              cor_05.constrained$V2), 2)}")) +
    annotate(geom = 'text', x = -5, y = 13.7, hjust = 0, size = 6,
             label = str_glue("n* = {round(nrow(cor_05.constrained))}")) +
    annotate(geom = 'text', x = -5, y = mean(cor_05.constrained$V2) + 1.7,
             hjust = 0, size = 4,
             label = str_glue("Mean = {round(mean(cor_05.constrained$V2), 2)}")) +
    annotate(geom = 'text', x = -5, y = mean(cor_05.constrained$V2) + 0.75,
             hjust = 0, size = 4,
             label = str_glue("SD = {round(sd(cor_05.constrained$V2),2)}")) +
    annotate(geom = 'text', x = mean(cor_05.constrained$V1) + 0.2, y = -3.8,
             hjust = 0, size = 4,
             label = str_glue("Mean = {round(mean(cor_05.constrained$V1), 2)}")) +
    annotate(geom = 'text', x = mean(cor_05.constrained$V1) + 0.2, y = -4.75,
             hjust = 0, size = 4,
             label = str_glue("SD = {round(sd(cor_05.constrained$V1), 2)}")) +
   labs(subtitle = 'Population parameters: Mean = 6.2, SD = 1.7, r = 0.5') +
    scale_y_continuous(limits = c(-5, 15),
                       breaks = c(0, 5, 10)) +
    scale_x_continuous(limits = c(-5, 15),
                       breaks = c(0, 5, 10) +
```

```
theme_bw(base_size = 18) +
    theme(axis.text = element text(colour = '#000000'),
          panel.grid = element_blank(),
          plot.subtitle = element_text(size = 14))
\# r = 0.2
plot_4 <- ggplot(data = cor_02.constrained) +</pre>
    aes(x = V1, y = V2) +
    geom_point() +
    geom_abline(slope = 1, intercept = 0) +
    geom_smooth(method = 'lm',
                se = FALSE,
                size = 1.5) +
    geom_hline(yintercept = mean(cor_02.constrained$V2),
               colour = 'red') +
    geom_vline(xintercept = mean(cor_02.constrained$V1),
               colour = 'red') +
    geom_rect(ymin = 0, ymax = 10,
              xmin = 0, xmax = 10,
              colour = '#000000',
              alpha = 0,
              linetype = 2) +
    annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 6,
             label = str_glue("r* = {round(cor(cor_02.constrained$V1,
                             cor 02.constrained$V2), 2)}")) +
    annotate(geom = 'text', x = -5, y = 13.7, hjust = 0, size = 6,
             label = str_glue("n* = {round(nrow(cor_02.constrained))}")) +
    annotate(geom = 'text', x = -5, y = mean(cor_02.constrained$V2) + 1.7,
             hjust = 0, size = 4,
             label = str_glue("Mean = {round(mean(cor_02.constrained$V2), 2)}")) +
    annotate(geom = 'text', x = -5, y = mean(cor_02.constrained$V2) + 0.75,
             hjust = 0, size = 4,
             label = str_glue("SD = {round(sd(cor_02.constrained$V2),2)}")) +
    annotate(geom = 'text', x = mean(cor_02.constrained\$V1) + 0.2, y = -3.8,
             hjust = 0, size = 4,
             label = str_glue("Mean = {round(mean(cor_02.constrained$V1), 2)}")) +
    annotate(geom = 'text', x = mean(cor_02.constrained$V1) + 0.2, y = -4.75,
             hjust = 0, size = 4,
             label = str_glue("SD = {round(sd(cor_02.constrained$V1), 2)}")) +
    labs(subtitle = 'Population parameters: Mean = 6.2, SD = 1.7, r = 0.2') +
    scale_y_continuous(limits = c(-5, 15),
                       breaks = c(0, 5, 10)) +
    scale x continuous(limits = c(-5, 15),
                       breaks = c(0, 5, 10)) +
   theme_bw(base_size = 18) +
    theme(axis.text = element_text(colour = '#000000'),
          axis.title.y = element_blank(),
          panel.grid = element_blank(),
          plot.subtitle = element_text(size = 14))
# Patchwork
patch <- plot_1 + plot_2 + plot_3 + plot_4 +
  plot_layout(ncol = 2) + plot_annotation(tag_levels = 'A')
```

#### 8 Session information

## [53] openxlsx 4.1.5

## [57] abind\_1.4-5

```
sessionInfo()
## R version 4.0.2 (2020-06-22)
## Platform: x86 64-apple-darwin17.0 (64-bit)
## Running under: macOS Catalina 10.15.5
##
## Matrix products: default
          /Library/Frameworks/R.framework/Versions/4.0/Resources/lib/libRblas.dylib
## BLAS:
## LAPACK: /Library/Frameworks/R.framework/Versions/4.0/Resources/lib/libRlapack.dylib
##
## locale:
## [1] en_US.UTF-8/en_US.UTF-8/en_US.UTF-8/C/en_US.UTF-8/en_US.UTF-8
## attached base packages:
## [1] stats
                graphics grDevices utils
                                               datasets methods
                                                                   base
##
## other attached packages:
## [1] patchwork_1.0.1 car_3.0-9
                                        carData_3.0-4
                                                        MBESS 4.8.0
## [5] MASS_7.3-52
                        magrittr_1.5
                                        forcats_0.5.0
                                                        stringr_1.4.0
## [9] dplyr 1.0.2
                        purrr 0.3.4
                                        readr 1.3.1
                                                        tidyr 1.1.1
## [13] tibble_3.0.3
                        ggplot2_3.3.2
                                        tidyverse_1.3.0
## loaded via a namespace (and not attached):
## [1] Rcpp_1.0.5
                          lattice_0.20-41
                                            lubridate_1.7.9
                                                              assertthat_0.2.1
## [5] digest_0.6.25
                          R6_2.4.1
                                            cellranger_1.1.0 backports_1.1.9
## [9] reprex_0.3.0
                          evaluate_0.14
                                            httr_1.4.2
                                                              pillar_1.4.6
## [13] rlang_0.4.7
                          curl_4.3
                                            readxl_1.3.1
                                                              rstudioapi_0.11
## [17] data.table_1.13.0 blob_1.2.1
                                            Matrix_1.2-18
                                                              rmarkdown_2.3
## [21] splines_4.0.2
                          foreign_0.8-80
                                            munsell_0.5.0
                                                              broom_0.7.0
## [25] compiler_4.0.2
                          modelr_0.1.8
                                            xfun_0.16
                                                              pkgconfig_2.0.3
## [29] mgcv_1.8-32
                          htmltools_0.5.0
                                            tidyselect_1.1.0 rio_0.5.16
## [33] fansi_0.4.1
                                                              withr_2.2.0
                          crayon_1.3.4
                                            dbplyr_1.4.4
## [37] grid 4.0.2
                          nlme 3.1-149
                                            jsonlite 1.7.0
                                                              gtable 0.3.0
## [41] lifecycle_0.2.0
                          DBI_1.1.0
                                            scales_1.1.1
                                                              zip_2.1.0
## [45] cli 2.0.2
                          stringi_1.4.6
                                            farver_2.0.3
                                                              fs_1.5.0
## [49] xml2_1.3.2
                          ellipsis_0.3.1
                                            generics_0.0.2
                                                              vctrs_0.3.4
```

glue 1.4.2

hms 0.5.3

colorspace\_1.4-1 rvest\_0.3.6

tools 4.0.2

yaml\_2.2.1

## [61] knitr\_1.29 haven\_2.3.1