Regression to the mean modeling

Mean pain rating of 7.2 at 0.8 correlation

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Generate 2x2 covariance matrix

Generate a covariance matrix using an SD of 1.2, 1.7, and 2.2, and correlation of 0.8.

```
cor \leftarrow matrix(c(1, 0.8, 0.8, 1), ncol = 2)
std_1 \leftarrow c(1.2, 1.2)
std_2 \leftarrow c(1.7, 1.7)
std_3 \leftarrow c(2.2, 2.2)
cov_1 <- cor2cov(cor.mat = cor,</pre>
                   sd = std 1
cov_1
          [,1] [,2]
## [1,] 1.440 1.152
## [2,] 1.152 1.440
cov_2 <- cor2cov(cor.mat = cor,</pre>
                   sd = std_2
cov_2
##
          [,1] [,2]
## [1,] 2.890 2.312
## [2,] 2.312 2.890
cov_3 <- cor2cov(cor.mat = cor,</pre>
                   sd = std_3
cov_3
##
          [,1] [,2]
## [1,] 4.840 3.872
## [2,] 3.872 4.840
```

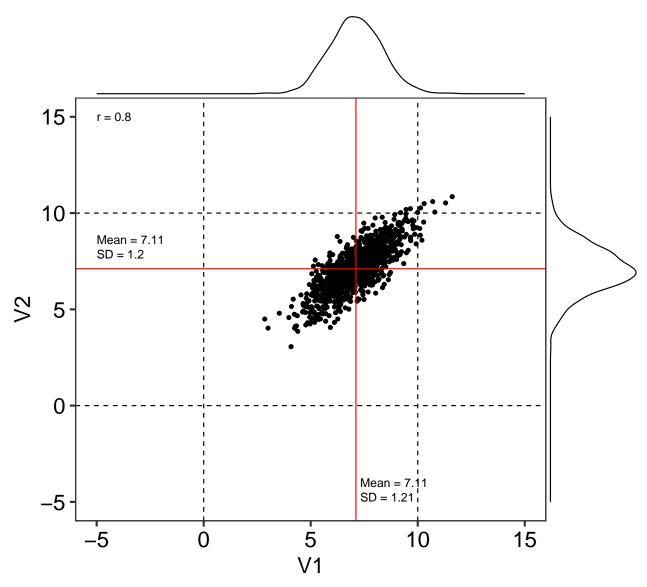
Mean = 7.2, SD = 1.2, Cor = 0.8

Generate and summarise data

Base data

```
geom_vline(xintercept = 10, linetype = 2) +
annotate(geom = 'text', x = -5, y = 15, hjust = 0,
         label = str_glue("r = {round(cor(seven_1.base$V1, seven_1.base$V2), 2)}")) +
annotate(geom = 'text', x = -5, y = mean(seven_1.base$V2) + 1.5, hjust = 0,
         label = str_glue("Mean = {round(mean(seven_1.base$V2), 2)}")) +
annotate(geom = 'text', x = -5, y = mean(seven_1.base$V2) + 0.75, hjust = 0,
         label = str_glue("SD = {round(sd(seven_1.base$V2),2)}")) +
annotate(geom = 'text', x = mean(seven_1.base$V1) + 0.2, y = -4, hjust = 0,
         label = str_glue("Mean = {round(mean(seven_1.base$V1), 2)}")) +
annotate(geom = 'text', x = mean(seven_1.base$V1) + 0.2, y = -4.75, hjust = 0,
         label = str_glue("SD = {round(sd(seven_1.base$V1), 2)}")) +
labs(title = 'Unconstained',
     caption = 'Parameters: Mean = 7.2, SD = 1.2, Cor = 0.8') +
scale_y_continuous(limits = c(-5, 15)) +
scale_x_continuous(limits = c(-5, 15)) +
theme(panel.grid = element_blank(),
      plot.subtitle = element_text(size = 16)))
```

Unconstained



Parameters: Mean = 7.2, SD = 1.2, Cor = 0.8

```
# Linear regression
summary(lm(V2 ~ V1, data = seven_1.base))
##
## Call:
## lm(formula = V2 ~ V1, data = seven_1.base)
## Residuals:
               1Q Median
                               ЗQ
                                      Max
## -2.1052 -0.4681 0.0142 0.4799 2.3636
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.50474
                          0.13720
                                   10.97 <2e-16 ***
```

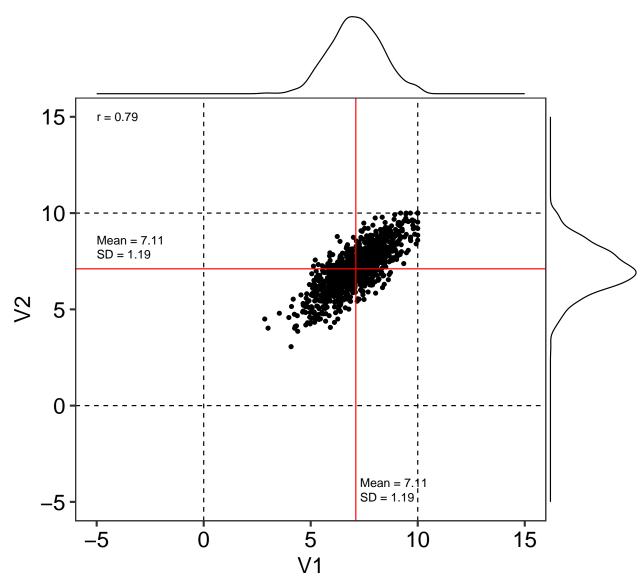
```
## V1
                0.78780
                           0.01901
                                   41.43 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.7271 on 998 degrees of freedom
## Multiple R-squared: 0.6323, Adjusted R-squared: 0.632
## F-statistic: 1716 on 1 and 998 DF, p-value: < 2.2e-16
Constrain values to 0-10 range
# Process data
seven_1 <- seven_1.base %>%
   mutate(V1 = case_when(
              V1 < 1 \sim 1,
              V1 > 10 \sim 10,
              TRUE ~ V1)) %>%
   mutate(V2 = case_when(
               V2 < 0 ~ 0,
              V2 > 10 \sim 10,
              TRUE ~ V2)) %>%
   mutate(group = 'No threshold')
# Plot processed data
ggMarginal(ggplot(data = seven_1) +
               aes(x = V1, y = V2) +
               geom_point() +
               geom hline(yintercept = mean(seven 1$V2), colour = 'red') +
               geom_vline(xintercept = mean(seven_1$V1), colour = 'red') +
               geom_hline(yintercept = 0, linetype = 2) +
               geom_hline(yintercept = 10, linetype = 2) +
               geom_vline(xintercept = 0, linetype = 2) +
               geom_vline(xintercept = 10, linetype = 2) +
               annotate(geom = 'text', x = -5, y = 15, hjust = 0,
                        label = str_glue("r = {round(cor(seven_1$V1, seven_1$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven_1$V2) + 1.5, hjust = 0,
                        label = str_glue("Mean = {round(mean(seven_1$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven_1$V2) + 0.75, hjust = 0,
                        label = str_glue("SD = {round(sd(seven_1$V2),2)}")) +
               annotate(geom = 'text', x = mean(seven_1$V1) + 0.2, y = -4, hjust = 0,
                        label = str_glue("Mean = {round(mean(seven_1$V1), 2)}")) +
               annotate(geom = 'text', x = mean(seven_1$V1) + 0.2, y = -4.75, hjust = 0,
                        label = str_glue("SD = {round(sd(seven_1$V1), 2)}")) +
```

caption = 'Parameters: Mean = 7.2, SD = 1.2, Cor = 0.8') +

labs(title = 'Constrained (0-10 range)',

scale_y_continuous(limits = c(-5, 15)) +
scale x continuous(limits = c(-5, 15)))

Constrained (0-10 range)



Parameters: Mean = 7.2, SD = 1.2, Cor = 0.8

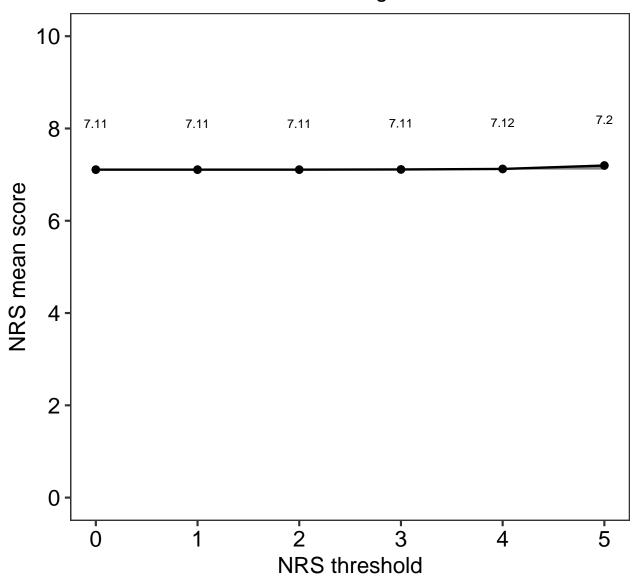
```
# Linear regression
summary(lm(V2 ~ V1, data = seven_1))
##
## Call:
## lm(formula = V2 ~ V1, data = seven_1)
## Residuals:
                 1Q
                     Median
## -2.10435 -0.47078 0.01293 0.48223
                                       2.36387
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                          0.13872
                                    10.77
                                            <2e-16 ***
## (Intercept) 1.49420
```

```
## V1      0.78944     0.01925     41.02     <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.7264 on 998 degrees of freedom
## Multiple R-squared: 0.6277, Adjusted R-squared: 0.6273
## F-statistic: 1682 on 1 and 998 DF, p-value: < 2.2e-16</pre>
```

Model mean of V1 with increasing V1 thresholds from 0 to 5

```
# Extract visit 1 data
seven_1V1 <- seven_1$V1
# Generate a vector of threshold values to iterate over
cutoff <- 0:5
# Generate a vector of V1 means at each V1 threshold
seven_1V1.shift <- sapply(cutoff, function(x){mean(seven_1V1[seven_1V1 > x])})
# Calculate deviation
(seven_1V1.df <- data.frame(cutoff = cutoff,</pre>
                          mean = seven 1V1.shift) %>%
        mutate(deviation = mean - mean(seven_1V1)))
    cutoff
##
               mean
                     deviation
## 1
       0 7.107816 0.000000000
         1 7.107816 0.000000000
## 2
## 3
         2 7.107816 0.000000000
## 4
         3 7.112076 0.004260057
## 5
         4 7.122936 0.015120053
## 6
         5 7.197557 0.089741175
# Plot data
ggplot(data = seven_1V1.df) +
   aes(x = cutoff, y = mean, ymin = mean(seven_1V1), ymax = mean) +
    geom_ribbon(alpha = 0.6) +
   geom_point(size = 3) +
   geom line(size = 1) +
   geom_text(aes(label = round(mean, 2)), nudge_y = 1) +
    scale_y_continuous(limits = c(0, 10),
                       breaks = c(0, 2, 4, 6, 8, 10)) +
   labs(title = 'Shift in V1 mean with increasing V1 NRS threshold value',
         caption = 'Parameters: Mean = 7.2, SD = 1.2, Cor = 0.8',
         x = 'NRS threshold',
         y = 'NRS mean score')
```

Shift in V1 mean with increasing V1 NRS threshold value



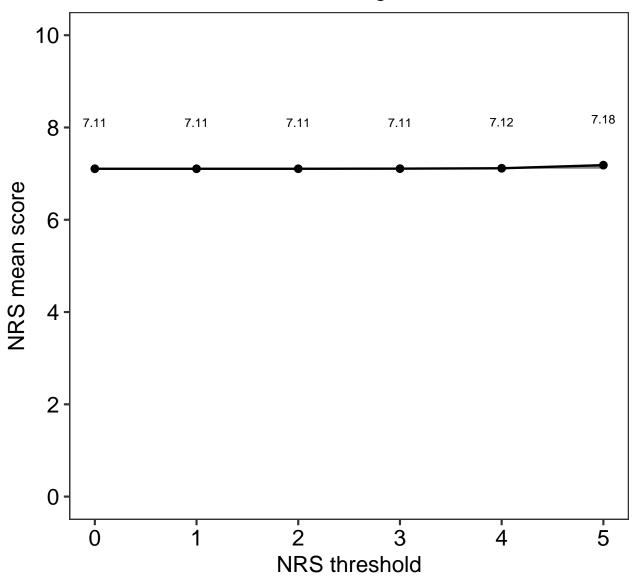
Parameters: Mean = 7.2, SD = 1.2, Cor = 0.8

Model mean of V2 with increasing V1 thresholds from 0 to 5

mean(.))

```
# Calculate deviation
(seven_1V2.df <- data.frame(cutoff = cutoff,</pre>
                           mean = seven_1V2.shift) %>%
       mutate(deviation = mean - mean(seven_1V2)))
##
    cutoff
               mean deviation
## 1
         0 7.105379 0.000000000
## 2
         1 7.105379 0.000000000
## 3
         2 7.105379 0.000000000
         3 7.107990 0.002610279
## 4
## 5
         4 7.115950 0.010570767
## 6
         5 7.183916 0.078536769
# Plot data
ggplot(data = seven_1V2.df) +
    aes(x = cutoff, y = mean, ymin = mean(seven_1V2), ymax = mean) +
    geom_ribbon(alpha = 0.6) +
    geom_point(size = 3) +
    geom_line(size = 1) +
    geom_text(aes(label = round(mean, 2)), nudge_y = 1) +
    scale_y_continuous(limits = c(0, 10),
                       breaks = c(0, 2, 4, 6, 8, 10)) +
    labs(title = 'Shift in V2 mean with increasing V1 NRS threshold value',
         caption = 'Parameters: Mean = 7.2, SD = 1.2, Cor = 0.8',
         x = 'NRS threshold',
         y = 'NRS mean score')
```

Shift in V2 mean with increasing V1 NRS threshold value



Parameters: Mean = 7.2, SD = 1.2, Cor = 0.8

Placebo response

```
R = 2000,
traditional = FALSE,
bca = TRUE)

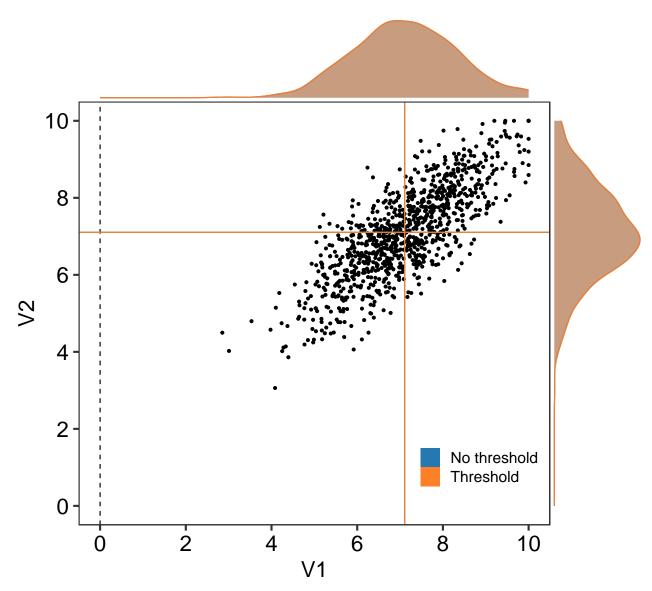
diff_1.0$.id <- 0

kable(diff_1.0)</pre>
```

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
0	1000	0.00244	0.95	-0.0473	0.0491

```
ggMarginal(placebo_1.0[, 1:3] %>%
               bind_rows(seven_1) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_1,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_1.0,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_1$V1),
                          colour = pal[1]) +
               geom_vline(xintercept = mean(placebo_1.0$V1),
                          colour = pal[2]) +
               geom_vline(xintercept = 0, linetype = 2) +
               geom_hline(yintercept = mean(seven_1$V2),
                          colour = pal[1]) +
               geom_hline(yintercept = mean(placebo_1.0$V2),
                          colour = pal[2]) +
               scale_y_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'A: Baseline pain threshold = 0',
                    caption = 'Parameters: Mean = 7.2, SD = 1.2, Cor = 0.8') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15)),
           groupColour = TRUE,
           groupFill = TRUE)
```

A: Baseline pain threshold = 0



Parameters: Mean = 7.2, SD = 1.2, Cor = 0.8

```
bca = TRUE)
```

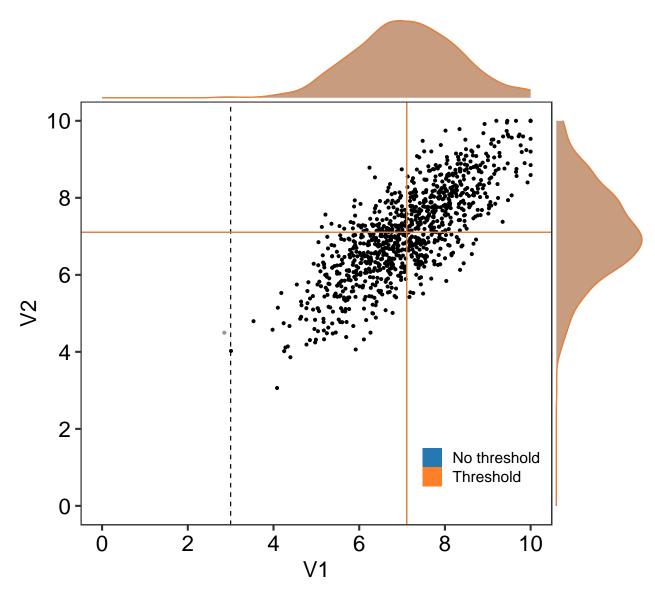
```
diff 1.3$.id <- 3
```

kable(diff_1.3)

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
3	999	0.00409	0.95	-0.0415	0.0483

```
ggMarginal(placebo_1.3[, 1:3] %>%
               bind_rows(seven_1) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_1,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_1.3,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_1$V1),
                          colour = pal[1]) +
               geom_vline(xintercept = mean(placebo_1.3$V1),
                          colour = pal[2]) +
               geom_vline(xintercept = 3, linetype = 2) +
               geom_hline(yintercept = mean(seven_1$V2),
                          colour = pal[1]) +
               geom_hline(yintercept = mean(placebo_1.3$V2),
                          colour = pal[2]) +
               scale_y_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale colour manual(values = pal) +
               labs(title = 'B: Baseline pain threshold = 3',
                    caption = 'Parameters: Mean = 7.2, SD = 1.2, Cor = 0.8') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15)),
           groupColour = TRUE,
           groupFill = TRUE)
```

B: Baseline pain threshold = 3



Parameters: Mean = 7.2, SD = 1.2, Cor = 0.8

```
# Process that data
placebo_1.4 <- seven_1 %>%
    filter(V1 >= 4) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

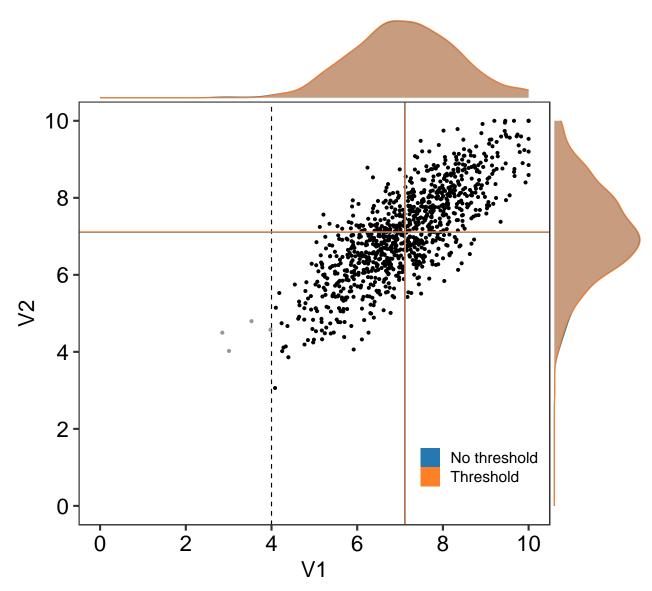
# Calculate the mean (95%CI) difference between V1 and V2
diff_1.4 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_1.4,
R = 2000,
traditional = FALSE,
bca = TRUE)

diff_1.4$.id <- 4
kable(diff_1.4)</pre>
```

```
ggMarginal(placebo_1.4[, 1:3] %>%
               bind_rows(seven_1) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_1,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_1.4,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_1$V1),
                          colour = pal[1]) +
               geom_vline(xintercept = mean(placebo_1.4$V1),
                          colour = pal[2]) +
               geom_vline(xintercept = 4, linetype = 2) +
               geom_hline(yintercept = mean(seven_1$V2),
                          colour = pal[1]) +
               geom_hline(yintercept = mean(placebo_1.4$V2),
                          colour = pal[2]) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'C: Baseline pain threshold = 4',
                    caption = 'Parameters: Mean = 7.2, SD = 1.2, Cor = 0.8') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15)),
           groupColour = TRUE,
           groupFill = TRUE)
```

C: Baseline pain threshold = 4



Parameters: Mean = 7.2, SD = 1.2, Cor = 0.8

```
# Process that data
placebo_1.5 <- seven_1 %>%
    filter(V1 >= 5) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

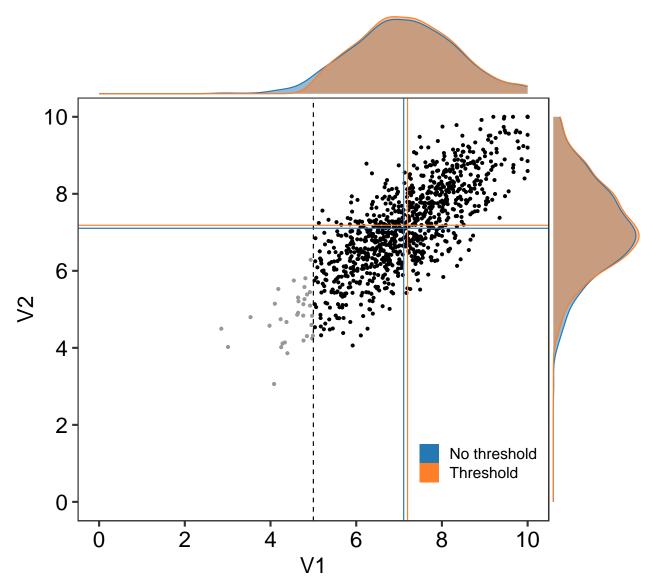
# Calculate the mean (95%CI) difference between V1 and V2
diff_1.5 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_1.5,
R = 2000,
traditional = FALSE,
bca = TRUE)

diff_1.5$.id <- 5
kable(diff_1.5)</pre>
```

```
ggMarginal(placebo_1.5[, 1:3] %>%
               bind_rows(seven_1) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_1,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_1.5,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_1$V1),
                          colour = pal[1]) +
               geom_vline(xintercept = mean(placebo_1.5$V1),
                          colour = pal[2]) +
               geom_vline(xintercept = 5, linetype = 2) +
               geom_hline(yintercept = mean(seven_1$V2),
                          colour = pal[1]) +
               geom_hline(yintercept = mean(placebo_1.5$V2),
                          colour = pal[2]) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'D: Baseline pain threshold = 5',
                    caption = 'Parameters: Mean = 7.2, SD = 1.2, Cor = 0.8') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15)),
           groupColour = TRUE,
           groupFill = TRUE)
```

D: Baseline pain threshold = 5



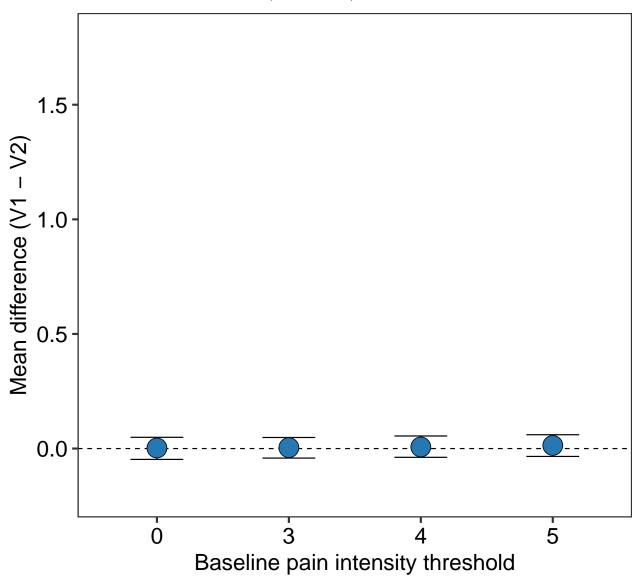
Parameters: Mean = 7.2, SD = 1.2, Cor = 0.8

Difference plot

```
# Bind diff_*.* dataframes
diff_all_1 <- diff_1.0 %>%
  bind_rows(diff_1.3, diff_1.4, diff_1.5)

pp_1 <- diff_all_1 %>%
  mutate(Threshold = factor(.id)) %>%
  ggplot(data = .) +
  aes(x = Threshold,
    y = Mean,
    ymin = Bca.lower,
    ymax = Bca.upper) +
```

Parameters: Mean = 7.2, SD = 1.2, Cor = 0.8



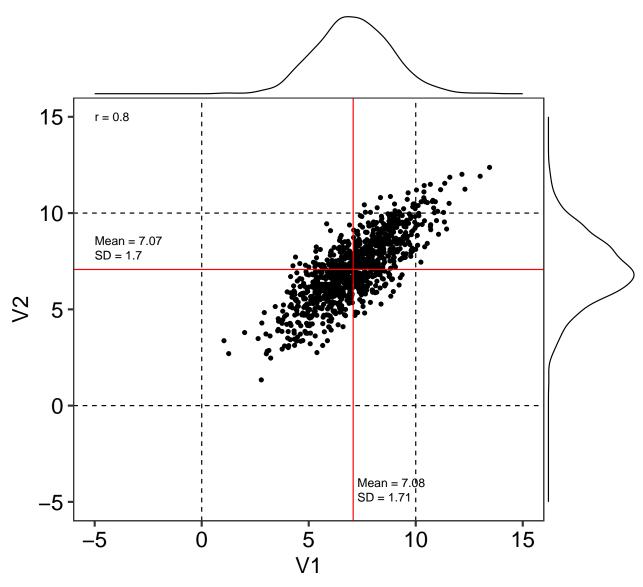
Mean = 7.2, SD = 1.7, Cor = 0.8

Generate and summarise data

Base data

```
# Set the random seed for reproducibility
set.seed(2019)
# Generate the data
seven 2.base \leftarrow as.data.frame(mvrnorm(n = 1000, mu = c(7.2, 7.2), Sigma = cov 2))
# Plot base data
ggMarginal(ggplot(data = seven_2.base) +
               aes(x = V1, y = V2) +
               geom_point() +
               geom_hline(yintercept = mean(seven_2.base$V2), colour = 'red') +
               geom_vline(xintercept = mean(seven_2.base$V1), colour = 'red') +
               geom_hline(yintercept = 0, linetype = 2) +
               geom_hline(yintercept = 10, linetype = 2) +
               geom_vline(xintercept = 0, linetype = 2) +
               geom_vline(xintercept = 10, linetype = 2) +
               annotate(geom = 'text', x = -5, y = 15, hjust = 0,
                        label = str_glue("r = {round(cor(seven_2.base$V1, seven_2.base$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven_2.base$V2) + 1.5, hjust = 0,
                        label = str_glue("Mean = {round(mean(seven_2.base$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven_2.base$V2) + 0.75, hjust = 0,
                        label = str glue("SD = {round(sd(seven 2.base$V2),2)}")) +
               annotate(geom = 'text', x = mean(seven_2.base$V1) + 0.2, y = -4, hjust = 0,
                        label = str_glue("Mean = {round(mean(seven_2.base$V1), 2)}")) +
               annotate(geom = 'text', x = mean(seven_2.base$V1) + 0.2, y = -4.75, hjust = 0,
                        label = str_glue("SD = {round(sd(seven_2.base$V1), 2)}")) +
               labs(title = 'Unconstrained',
                    caption = 'Parameters: Mean = 7.2, SD = 1.7, Cor = 0.8') +
               scale_y_continuous(limits = c(-5, 15)) +
               scale_x_continuous(limits = c(-5, 15)))
```

Unconstrained

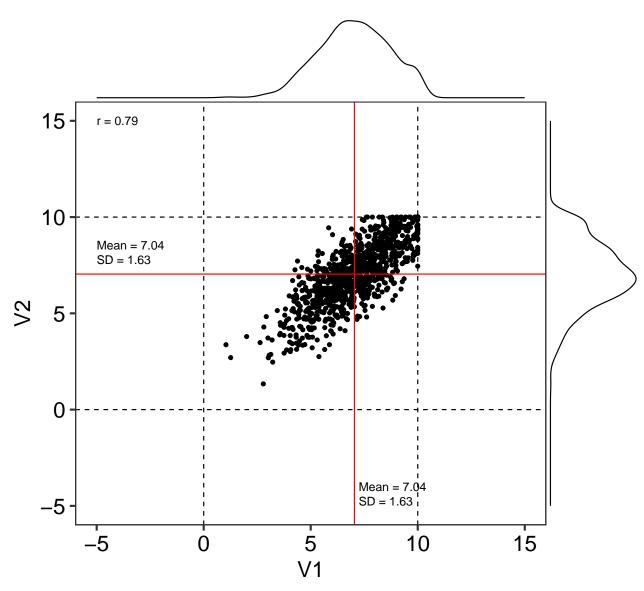


Parameters: Mean = 7.2, SD = 1.7, Cor = 0.8

```
## V1
                0.78780
                           0.01901
                                   41.43
                                           <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.03 on 998 degrees of freedom
## Multiple R-squared: 0.6323, Adjusted R-squared: 0.632
## F-statistic: 1716 on 1 and 998 DF, p-value: < 2.2e-16
Constrain values to 0-10 range
# Process data
seven 2 <- seven 2.base %>%
   mutate(V1 = case_when(
              V1 < 1 \sim 1,
              V1 > 10 \sim 10,
              TRUE ~ V1)) %>%
   mutate(V2 = case_when(
               V2 < 0 ~ 0,
              V2 > 10 \sim 10,
              TRUE ~ V2)) %>%
   mutate(group = 'No threshold')
# Plot processed data
ggMarginal(ggplot(data = seven_2) +
               aes(x = V1, y = V2) +
               geom_point() +
               geom hline(yintercept = mean(seven 2$V2), colour = 'red') +
               geom_vline(xintercept = mean(seven_2$V1), colour = 'red') +
               geom_hline(yintercept = 0, linetype = 2) +
               geom_hline(yintercept = 10, linetype = 2) +
               geom_vline(xintercept = 0, linetype = 2) +
               geom_vline(xintercept = 10, linetype = 2) +
               annotate(geom = 'text', x = -5, y = 15, hjust = 0,
                        label = str_glue("r = {round(cor(seven_2$V1, seven_2$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven_2$V2) + 1.5, hjust = 0,
                        label = str_glue("Mean = {round(mean(seven_2$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven_2$V2) + 0.75, hjust = 0,
                        label = str_glue("SD = {round(sd(seven_2$V2),2)}")) +
               annotate(geom = 'text', x = mean(seven_2$V1) + 0.2, y = -4, hjust = 0,
                        label = str_glue("Mean = {round(mean(seven_2$V1), 2)}")) +
               annotate(geom = 'text', x = mean(seven_2$V1) + 0.2, y = -4.75, hjust = 0,
                        label = str_glue("SD = {round(sd(seven_2$V1), 2)}")) +
               labs(title ='Constrained (0-10 range)',
                    caption = 'Parameters: Mean = 7.2, SD = 1.7, Cor = 0.8') +
               scale_y_continuous(limits = c(-5, 15)) +
```

scale x continuous(limits = c(-5, 15)))

Constrained (0-10 range)



Parameters: Mean = 7.2, SD = 1.7, Cor = 0.8

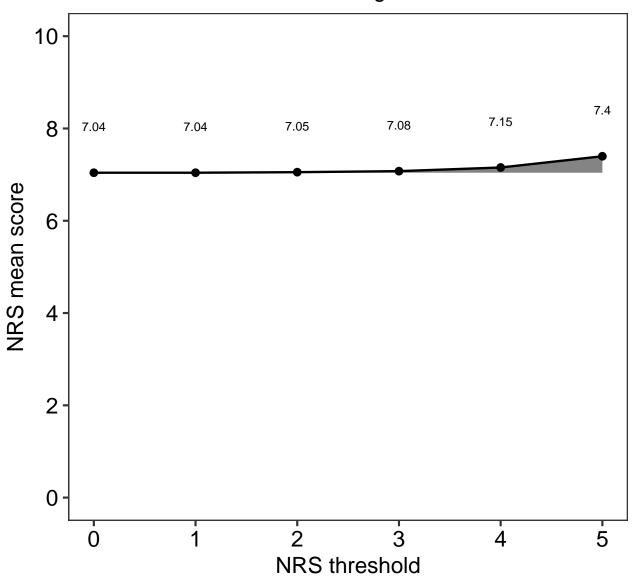
```
# Linear regression
summary(lm(V2 ~ V1, data = seven_2))
##
## Call:
## lm(formula = V2 ~ V1, data = seven_2)
## Residuals:
                1Q Median
                               ЗQ
                                      Max
## -2.9836 -0.6454 0.0445 0.6543 3.3480
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                                    10.66 <2e-16 ***
## (Intercept) 1.50661
                          0.14130
```

```
## V1      0.78590     0.01955     40.20     <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.01 on 998 degrees of freedom
## Multiple R-squared: 0.6182, Adjusted R-squared: 0.6178
## F-statistic: 1616 on 1 and 998 DF, p-value: < 2.2e-16</pre>
```

Model mean of V1 with increasing V1 thresholds from 0 to 5

```
# Extract visit 1 data
seven_2V1 <- seven_2$V1
# Generate a vector of threshold values to iterate over
cutoff <- 0:5
# Generate a vector of V1 means at each V1 threshold
seven_2V1.shift <- sapply(cutoff, function(x){mean(seven_2V1[seven_2V1 > x])})
# Calculate deviation
(seven_2V1.df <- data.frame(cutoff = cutoff,</pre>
                           mean = seven 2V1.shift) %>%
        mutate(deviation = mean - mean(seven_2V1)))
    cutoff
##
               mean deviation
## 1
      0 7.041127 0.00000000
         1 7.041127 0.00000000
## 2
## 3
         2 7.052931 0.01180407
## 4
         3 7.075191 0.03406380
## 5
         4 7.154426 0.11329881
## 6
         5 7.397882 0.35675418
# Plot data
ggplot(data = seven_2V1.df) +
   aes(x = cutoff, y = mean, ymin = mean(seven_2V1), ymax = mean) +
    geom_ribbon(alpha = 0.6) +
   geom_point(size = 3) +
   geom line(size = 1) +
   geom_text(aes(label = round(mean, 2)), nudge_y = 1) +
    scale_y_continuous(limits = c(0, 10),
                       breaks = c(0, 2, 4, 6, 8, 10)) +
   labs(title = 'Shift in V1 mean with increasing V1 NRS threshold value',
         caption = 'Parameters: Mean = 7.2, SD = 1.7, Cor = 0.8',
         x = 'NRS threshold',
         y = 'NRS mean score')
```

Shift in V1 mean with increasing V1 NRS threshold value



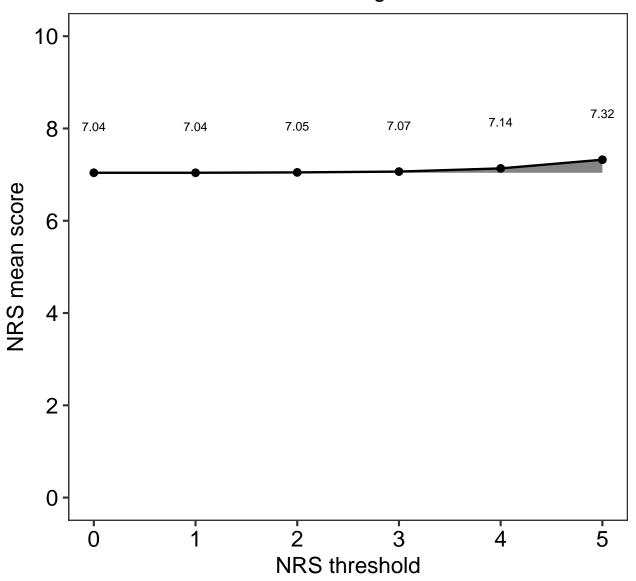
Parameters: Mean = 7.2, SD = 1.7, Cor = 0.8

Model mean of V2 with increasing V1 thresholds from 0 to 5

mean(.))

```
# Calculate deviation
(seven_2V2.df <- data.frame(cutoff = cutoff,</pre>
                           mean = seven_2V2.shift) %>%
       mutate(deviation = mean - mean(seven_2V2)))
##
     cutoff
               mean deviation
## 1
         0 7.040208 0.000000000
## 2
         1 7.040208 0.000000000
## 3
         2 7.048232 0.008024196
         3 7.065861 0.025653116
## 4
## 5
         4 7.135019 0.094810924
## 6
         5 7.323100 0.282892282
# Plot data
ggplot(data = seven_2V2.df) +
    aes(x = cutoff, y = mean, ymin = mean(seven_2V2), ymax = mean) +
    geom_ribbon(alpha = 0.6) +
    geom_point(size = 3) +
    geom_line(size = 1) +
    geom_text(aes(label = round(mean, 2)), nudge_y = 1) +
    scale_y_continuous(limits = c(0, 10),
                       breaks = c(0, 2, 4, 6, 8, 10)) +
    labs(title = 'Shift in V2 mean with increasing V1 NRS threshold value',
         caption = 'Parameters: Mean = 7.2, SD = 1.7, Cor = 0.8',
         x = 'NRS threshold',
         y = 'NRS mean score')
```

Shift in V2 mean with increasing V1 NRS threshold value



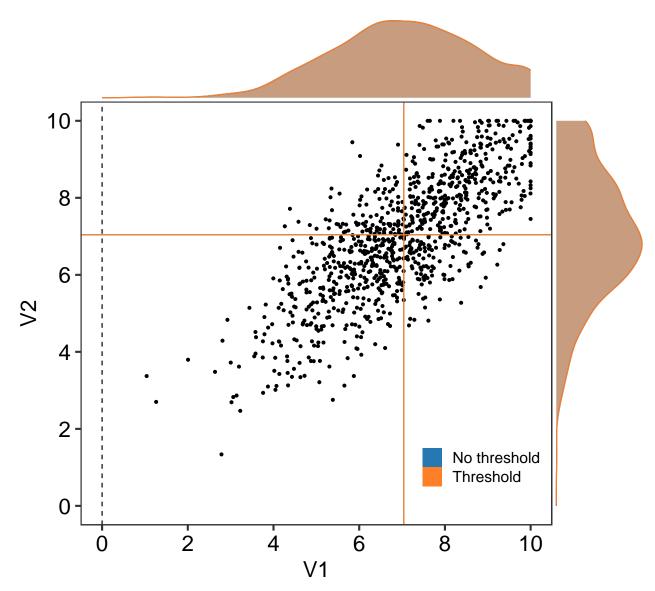
Parameters: Mean = 7.2, SD = 1.7, Cor = 0.8

Placebo response

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
0	1000	0.00092	0.95	-0.0677	0.0657

```
ggMarginal(placebo_2.0[, 1:3] %>%
               bind_rows(seven_2) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_2,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_2.0,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_2$V1),
                          colour = pal[1]) +
               geom_vline(xintercept = mean(placebo_2.0$V1),
                          colour = pal[2]) +
               geom_vline(xintercept = 0, linetype = 2) +
               geom_hline(yintercept = mean(seven_2$V2),
                          colour = pal[1]) +
               geom_hline(yintercept = mean(placebo_2.0$V2),
                          colour = pal[2]) +
               scale_y_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'A: Baseline pain threshold = 0',
                    caption = 'Parameters: Mean = 7.2, SD = 1.7, Cor = 0.8') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15)),
           groupColour = TRUE,
           groupFill = TRUE)
```

A: Baseline pain threshold = 0



Parameters: Mean = 7.2, SD = 1.7, Cor = 0.8

```
# Process data
placebo_2.3 <- seven_2 %>%
    filter(V1 >= 3) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_2.3 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_2.3,
    R = 2000,
    traditional = FALSE,
    bca = TRUE)

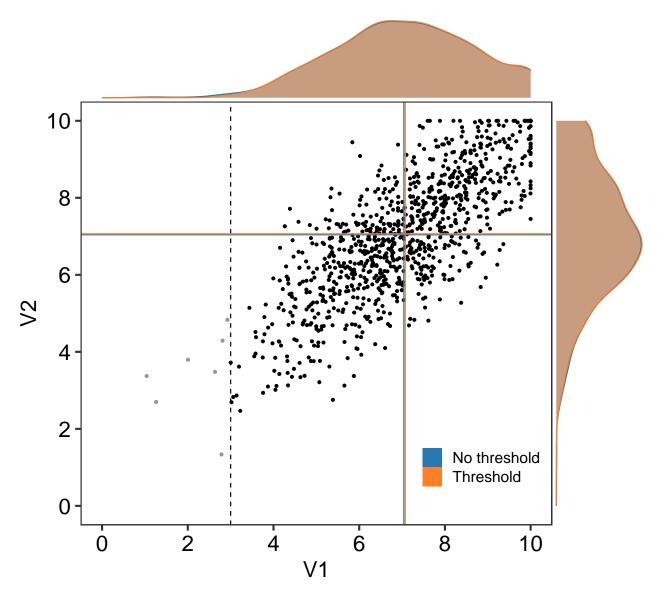
diff_2.3$.id <- 3
kable(diff_2.3)</pre>
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 3
 993
 0.00933
 0.95
 -0.061
 0.0722

```
ggMarginal(placebo_2.3[, 1:3] %>%
               bind_rows(seven_2) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_2,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_2.3,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_2$V1),
                          colour = pal[1]) +
               geom_vline(xintercept = mean(placebo_2.3$V1),
                          colour = pal[2]) +
               geom_vline(xintercept = 3, linetype = 2) +
               geom_hline(yintercept = mean(seven_2$V2),
                          colour = pal[1]) +
               geom_hline(yintercept = mean(placebo_2.3$V2),
                          colour = pal[2]) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'B: Baseline pain threshold = 3',
                    caption = 'Parameters: Mean = 7.2, SD = 1.7, Cor = 0.8') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15)),
           groupColour = TRUE,
           groupFill = TRUE)
```

B: Baseline pain threshold = 3



Parameters: Mean = 7.2, SD = 1.7, Cor = 0.8

```
# Process that data
placebo_2.4 <- seven_2 %>%
    filter(V1 >= 4) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_2.4 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_2.4,
R = 2000,
traditional = FALSE,
bca = TRUE)

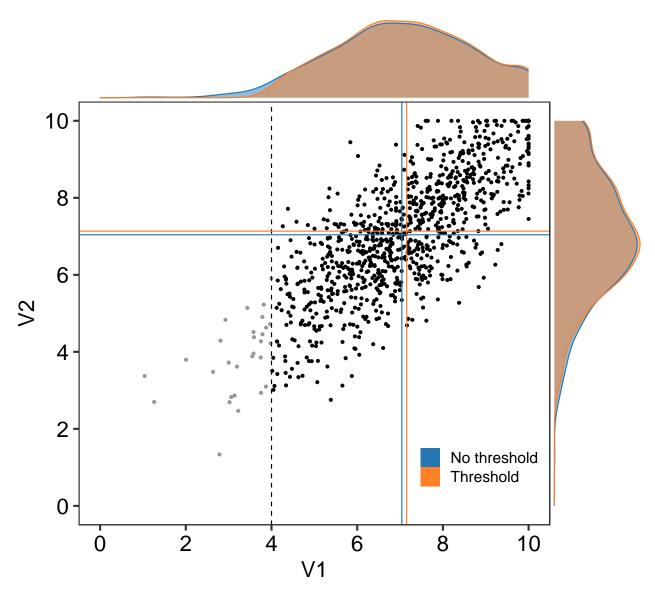
diff_2.4$.id <- 4
kable(diff_2.4)</pre>
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 4
 971
 0.0194
 0.95
 -0.0494
 0.0869

```
ggMarginal(placebo_2.4[, 1:3] %>%
               bind_rows(seven_2) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_2,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_2.4,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_2$V1),
                          colour = pal[1]) +
               geom_vline(xintercept = mean(placebo_2.4$V1),
                          colour = pal[2]) +
               geom_vline(xintercept = 4, linetype = 2) +
               geom_hline(yintercept = mean(seven_2$V2),
                          colour = pal[1]) +
               geom_hline(yintercept = mean(placebo_2.4$V2),
                          colour = pal[2]) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'C: Baseline pain threshold = 4',
                    caption = 'Parameters: Mean = 7.2, SD = 1.7, Cor = 0.8') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15)),
           groupColour = TRUE,
           groupFill = TRUE)
```

C: Baseline pain threshold = 4



Parameters: Mean = 7.2, SD = 1.7, Cor = 0.8

```
# Process that data
placebo_2.5 <- seven_2 %>%
    filter(V1 >= 5) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_2.5 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_2.5,
R = 2000,
traditional = FALSE,
bca = TRUE)

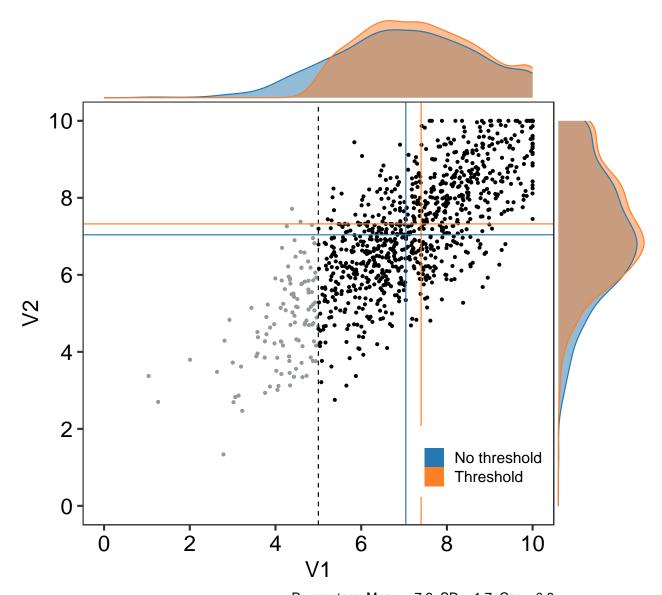
diff_2.5$.id <- 5
kable(diff_2.5)</pre>
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 5
 888
 0.0748
 0.95
 0.00655
 0.143

```
ggMarginal(placebo_2.5[, 1:3] %>%
               bind_rows(seven_2) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_2,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_2.5,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_2$V1),
                          colour = pal[1]) +
               geom_vline(xintercept = mean(placebo_2.5$V1),
                          colour = pal[2]) +
               geom_vline(xintercept = 5, linetype = 2) +
               geom_hline(yintercept = mean(seven_2$V2),
                          colour = pal[1]) +
               geom_hline(yintercept = mean(placebo_2.5$V2),
                          colour = pal[2]) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'D: Baseline pain threshold = 5',
                    caption = 'Parameters: Mean = 7.2, SD = 1.7, Cor = 0.8') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15)),
           groupColour = TRUE,
           groupFill = TRUE)
```

D: Baseline pain threshold = 5



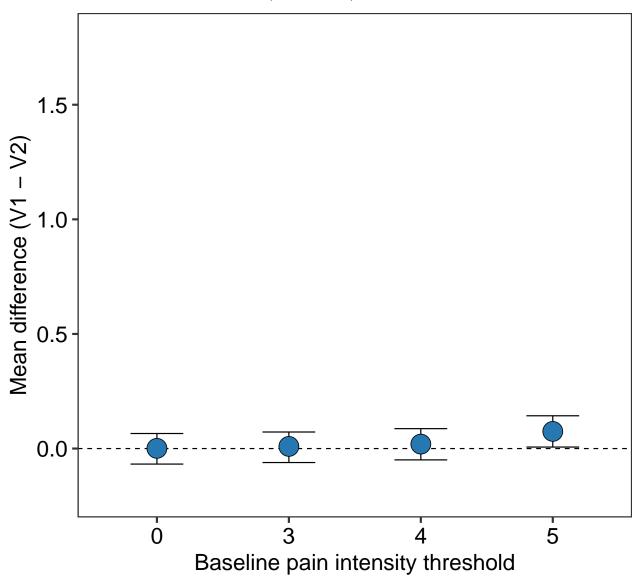
Parameters: Mean = 7.2, SD = 1.7, Cor = 0.8

Difference plot

```
# Bind diff_*.* dataframes
diff_all_2 <- diff_2.0 %>%
  bind_rows(diff_2.3, diff_2.4, diff_2.5)

pp_2 <- diff_all_2 %>%
  mutate(Threshold = factor(.id)) %>%
  ggplot(data = .) +
  aes(x = Threshold,
    y = Mean,
    ymin = Bca.lower,
    ymax = Bca.upper) +
```

Parameters: Mean = 7.2, SD = 1.7, Cor = 0.8



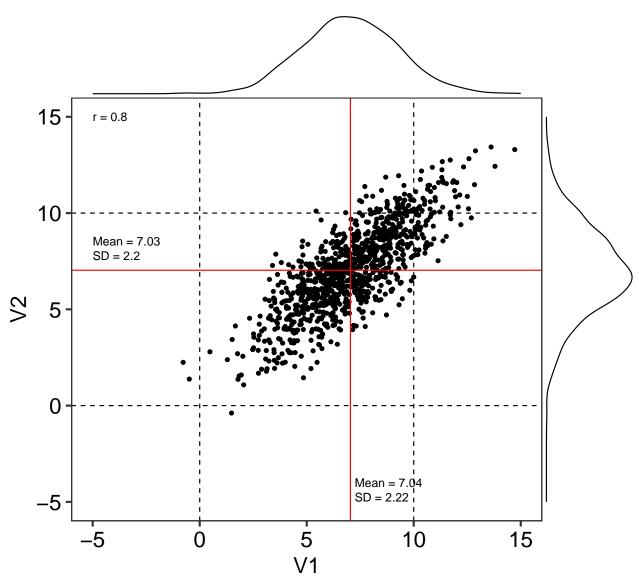
Mean = 7.2, SD = 2.2, Cor = 0.8

Generate and summarise data

Base data

```
# Set the random seed for reproducibility
set.seed(2019)
# Generate the data
seven 3.base \leftarrow as.data.frame(mvrnorm(n = 1000, mu = c(7.2, 7.2), Sigma = cov 3))
# Plot base data
ggMarginal(ggplot(data = seven_3.base) +
               aes(x = V1, y = V2) +
               geom_point() +
               geom_hline(yintercept = mean(seven_3.base$V2), colour = 'red') +
               geom_vline(xintercept = mean(seven_3.base$V1), colour = 'red') +
               geom_hline(yintercept = 0, linetype = 2) +
               geom_hline(yintercept = 10, linetype = 2) +
               geom_vline(xintercept = 0, linetype = 2) +
               geom_vline(xintercept = 10, linetype = 2) +
               annotate(geom = 'text', x = -5, y = 15, hjust = 0,
                        label = str_glue("r = {round(cor(seven_3.base$V1, seven_3.base$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven_3.base$V2) + 1.5, hjust = 0,
                        label = str_glue("Mean = {round(mean(seven_3.base$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven_3.base$V2) + 0.75, hjust = 0,
                        label = str glue("SD = {round(sd(seven 3.base$V2),2)}")) +
               annotate(geom = 'text', x = mean(seven_3.base$V1) + 0.2, y = -4, hjust = 0,
                        label = str_glue("Mean = {round(mean(seven_3.base$V1), 2)}")) +
               annotate(geom = 'text', x = mean(seven_3.base$V1) + 0.2, y = -4.75, hjust = 0,
                        label = str_glue("SD = {round(sd(seven_3.base$V1), 2)}")) +
               labs(title = 'Unconstrained',
                    caption = 'Parameters: Mean = 7.2, SD = 2.2, Cor = 0.8') +
               scale_y_continuous(limits = c(-5, 15)) +
               scale_x_continuous(limits = c(-5, 15)))
## Warning: Removed 1 rows containing missing values (geom_point).
## Warning: Removed 1 rows containing missing values (geom point).
```

Unconstrained

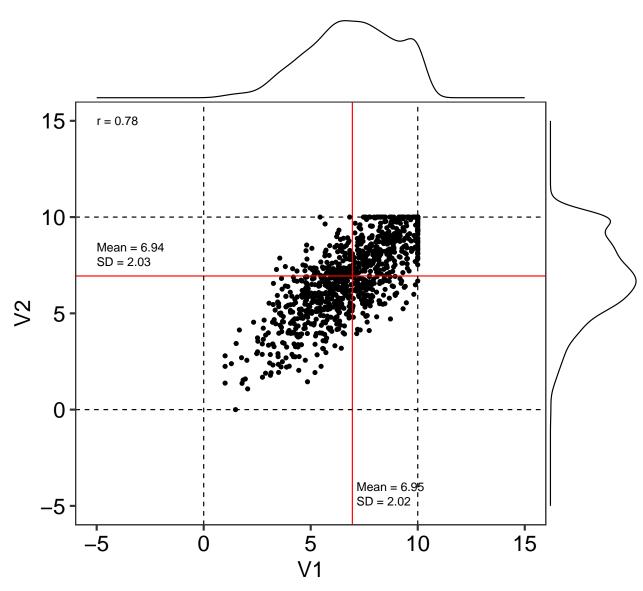


Parameters: Mean = 7.2, SD = 2.2, Cor = 0.8

```
## V1
                0.78780
                           0.01901
                                   41.43 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.333 on 998 degrees of freedom
## Multiple R-squared: 0.6323, Adjusted R-squared: 0.632
## F-statistic: 1716 on 1 and 998 DF, p-value: < 2.2e-16
Constrain values to 0-10 range
# Process data
seven_3 <- seven_3.base %>%
   mutate(V1 = case_when(
              V1 < 1 \sim 1,
              V1 > 10 \sim 10,
              TRUE ~ V1)) %>%
   mutate(V2 = case_when(
               V2 < 0 ~ 0,
              V2 > 10 \sim 10,
              TRUE ~ V2)) %>%
   mutate(group = 'No threshold')
# Plot processed data
ggMarginal(ggplot(data = seven_3) +
               aes(x = V1, y = V2) +
               geom_point() +
               geom hline(yintercept = mean(seven 3$V2), colour = 'red') +
               geom_vline(xintercept = mean(seven_3$V1), colour = 'red') +
               geom_hline(yintercept = 0, linetype = 2) +
               geom_hline(yintercept = 10, linetype = 2) +
               geom_vline(xintercept = 0, linetype = 2) +
               geom_vline(xintercept = 10, linetype = 2) +
               annotate(geom = 'text', x = -5, y = 15, hjust = 0,
                        label = str_glue("r = {round(cor(seven_3$V1, seven_3$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven_3$V2) + 1.5, hjust = 0,
                        label = str_glue("Mean = {round(mean(seven_3$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(seven_3$V2) + 0.75, hjust = 0,
                        label = str_glue("SD = {round(sd(seven_3$V2),2)}")) +
               annotate(geom = 'text', x = mean(seven_3$V1) + 0.2, y = -4, hjust = 0,
                        label = str_glue("Mean = {round(mean(seven_3$V1), 2)}")) +
               annotate(geom = 'text', x = mean(seven_3$V1) + 0.2, y = -4.75, hjust = 0,
                        label = str_glue("SD = {round(sd(seven_3$V1), 2)}")) +
               labs(title = 'Constrained (0-10 range)',
                    caption = 'Parameters: Mean = 7.2, SD = 2.2, Cor = 0.8') +
```

scale_y_continuous(limits = c(-5, 15)) +
scale x continuous(limits = c(-5, 15)))

Constrained (0-10 range)



Parameters: Mean = 7.2, SD = 2.2, Cor = 0.8

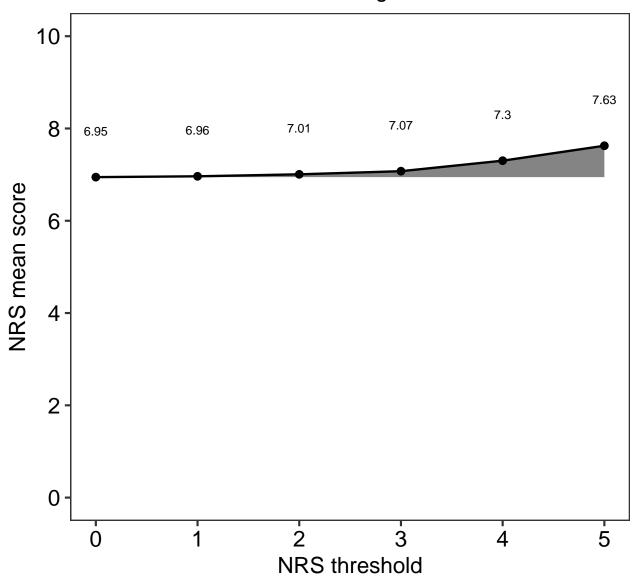
```
# Linear regression
summary(lm(V2 ~ V1, data = seven_3))
##
## Call:
## lm(formula = V2 ~ V1, data = seven_3)
## Residuals:
                1Q Median
                                ЗQ
                                       Max
## -3.8496 -0.8122 0.0994 0.7941
                                  4.2410
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.48862
                                     10.35
                                            <2e-16 ***
                           0.14385
```

```
## V1      0.78511     0.01989     39.47     <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.267 on 998 degrees of freedom
## Multiple R-squared: 0.6095, Adjusted R-squared: 0.6091
## F-statistic: 1558 on 1 and 998 DF, p-value: < 2.2e-16</pre>
```

Model mean of V1 with increasing V1 thresholds from 0 to 5

```
# Extract visit 1 data
seven_3V1 <- seven_3$V1
# Generate a vector of threshold values to iterate over
cutoff <- 0:5
# Generate a vector of V1 means at each V1 threshold
seven_3V1.shift <- sapply(cutoff, function(x){mean(seven_3V1[seven_3V1 > x])})
# Calculate deviation
(seven_3V1.df <- data.frame(cutoff = cutoff,</pre>
                           mean = seven 3V1.shift) %>%
        mutate(deviation = mean - mean(seven_3V1)))
    cutoff
##
               mean deviation
## 1
      0 6.945539 0.00000000
## 2
         1 6.963429 0.01789029
## 3
         2 7.006297 0.06075826
## 4
         3 7.074325 0.12878537
## 5
         4 7.301871 0.35633221
## 6
         5 7.625753 0.68021434
# Plot data
ggplot(data = seven_3V1.df) +
   aes(x = cutoff, y = mean, ymin = mean(seven_3V1), ymax = mean) +
    geom_ribbon(alpha = 0.6) +
   geom_point(size = 3) +
   geom line(size = 1) +
   geom_text(aes(label = round(mean, 2)), nudge_y = 1) +
    scale_y_continuous(limits = c(0, 10),
                       breaks = c(0, 2, 4, 6, 8, 10)) +
   labs(title = 'Shift in V1 mean with increasing V1 NRS threshold value',
         caption = 'Parameters: Mean = 7.2, SD = 2.2, Cor = 0.8',
         x = 'NRS threshold',
         y = 'NRS mean score')
```

Shift in V1 mean with increasing V1 NRS threshold value



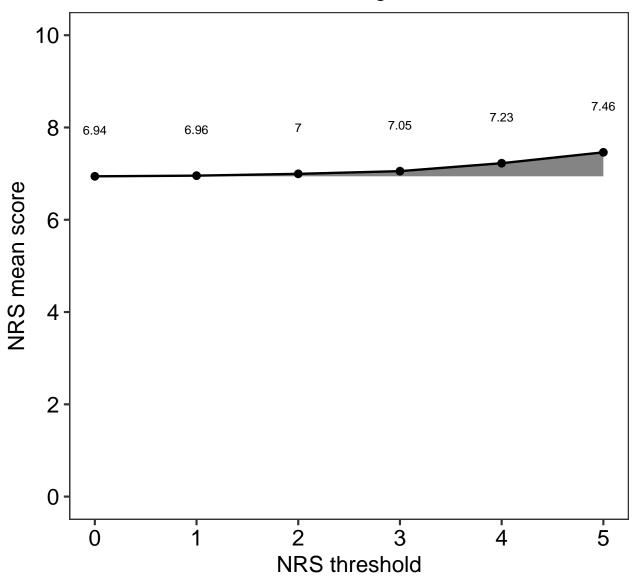
Parameters: Mean = 7.2, SD = 2.2, Cor = 0.8

Model mean of V2 with increasing V1 thresholds from 0 to 5

mean(.))

```
# Calculate deviation
(seven_3V2.df <- data.frame(cutoff = cutoff,</pre>
                           mean = seven_3V2.shift) %>%
       mutate(deviation = mean - mean(seven_3V2)))
##
     cutoff
              mean deviation
## 1
         0 6.941653 0.00000000
## 2
         1 6.956104 0.01445148
## 3
         2 6.995030 0.05337779
         3 7.053862 0.11220905
## 4
## 5
         4 7.225689 0.28403612
## 6
         5 7.461585 0.51993259
# Plot data
ggplot(data = seven_3V2.df) +
    aes(x = cutoff, y = mean, ymin = mean(seven_3V2), ymax = mean) +
    geom_ribbon(alpha = 0.6) +
    geom_point(size = 3) +
    geom_line(size = 1) +
    geom_text(aes(label = round(mean, 2)), nudge_y = 1) +
    scale_y_continuous(limits = c(0, 10),
                       breaks = c(0, 2, 4, 6, 8, 10)) +
    labs(title = 'Shift in V2 mean with increasing V1 NRS threshold value',
         caption = 'Parameters: Mean = 7.2, SD = 2.2, Cor = 0.8',
         x = 'NRS threshold',
         y = 'NRS mean score')
```

Shift in V2 mean with increasing V1 NRS threshold value



Parameters: Mean = 7.2, SD = 2.2, Cor = 0.8

Placebo response

```
R = 2000,
traditional = FALSE,
bca = TRUE)

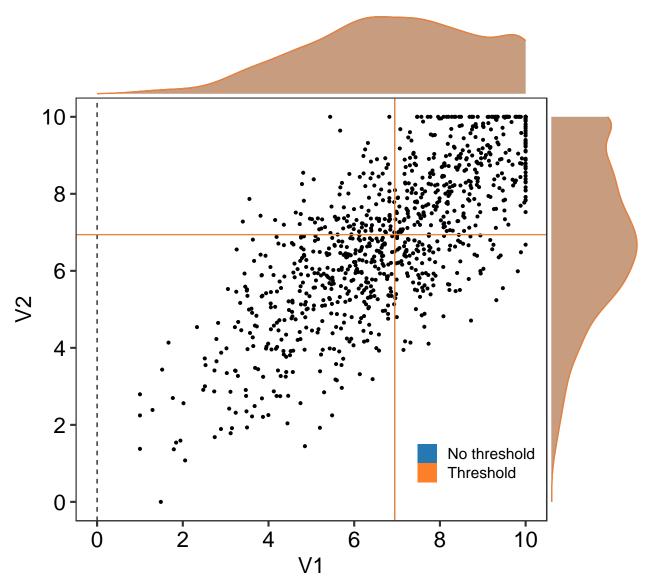
diff_3.0$.id <- 0

kable(diff_3.0)</pre>
```

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
0	1000	0.00389	0.95	-0.0805	0.0846

```
ggMarginal(placebo_3.0[, 1:3] %>%
               bind_rows(seven_3) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_3,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_3.0,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_3$V1),
                          colour = pal[1]) +
               geom_vline(xintercept = mean(placebo_3.0$V1),
                          colour = pal[2]) +
               geom_vline(xintercept = 0, linetype = 2) +
               geom_hline(yintercept = mean(seven_3$V2),
                          colour = pal[1]) +
               geom_hline(yintercept = mean(placebo_3.0$V2),
                          colour = pal[2]) +
               scale_y_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'A: Baseline pain threshold = 0',
                    caption = 'Parameters: Mean = 7.2, SD = 2.2, Cor = 0.8') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15)),
           groupColour = TRUE,
           groupFill = TRUE)
```

A: Baseline pain threshold = 0



Parameters: Mean = 7.2, SD = 2.2, Cor = 0.8

```
# Process data
placebo_3.3 <- seven_3 %>%
    filter(V1 >= 3) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_3.3 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_3.3,
R = 2000,
traditional = FALSE,
bca = TRUE)

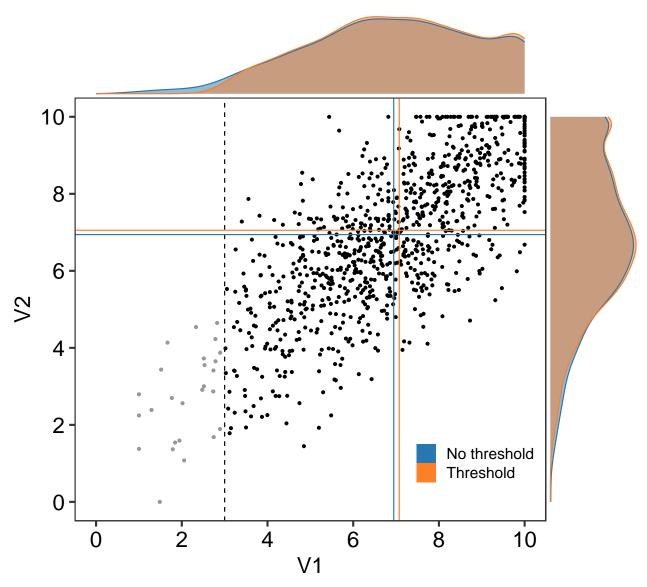
diff_3.3$.id <- 3
kable(diff_3.3)</pre>
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 3
 974
 0.0205
 0.95
 -0.0719
 0.106

```
ggMarginal(placebo_3.3[, 1:3] %>%
               bind_rows(seven_3) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_3,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_3.3,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_3$V1),
                          colour = pal[1]) +
               geom_vline(xintercept = mean(placebo_3.3$V1),
                          colour = pal[2]) +
               geom_vline(xintercept = 3, linetype = 2) +
               geom_hline(yintercept = mean(seven_3$V2),
                          colour = pal[1]) +
               geom_hline(yintercept = mean(placebo_3.3$V2),
                          colour = pal[2]) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'B: Baseline pain threshold = 3',
                    caption = 'Parameters: Mean = 7.2, SD = 2.2, Cor = 0.8') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15)),
           groupColour = TRUE,
           groupFill = TRUE)
```

B: Baseline pain threshold = 3



Parameters: Mean = 7.2, SD = 2.2, Cor = 0.8

```
# Process that data
placebo_3.4 <- seven_3 %>%
    filter(V1 >= 4) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_3.4 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_3.4,
R = 2000,
traditional = FALSE,
bca = TRUE)

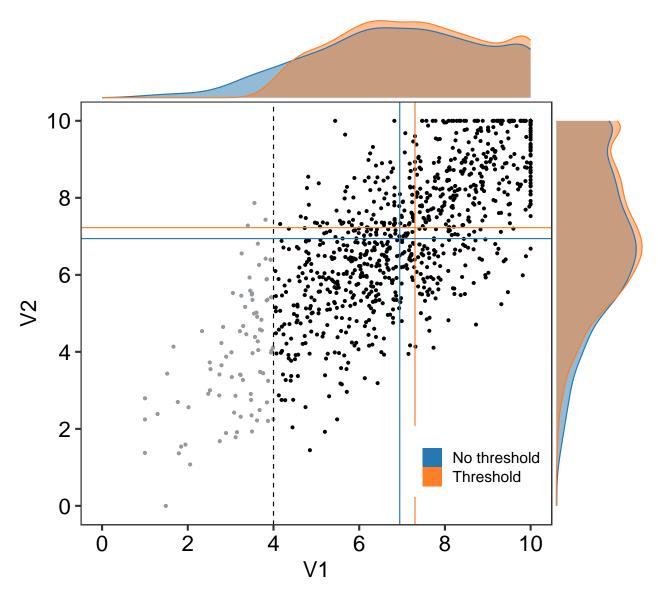
diff_3.4$.id <- 4
kable(diff_3.4)</pre>
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 4
 915
 0.0762
 0.95
 -0.00664
 0.166

```
ggMarginal(placebo_3.4[, 1:3] %>%
               bind_rows(seven_3) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_3,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_3.4,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_3$V1),
                          colour = pal[1]) +
               geom_vline(xintercept = mean(placebo_3.4$V1),
                          colour = pal[2]) +
               geom_vline(xintercept = 4, linetype = 2) +
               geom_hline(yintercept = mean(seven_3$V2),
                          colour = pal[1]) +
               geom_hline(yintercept = mean(placebo_3.4$V2),
                          colour = pal[2]) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'C: Baseline pain threshold = 4',
                    caption = 'Parameters: Mean = 7.2, SD = 2.2, Cor = 0.8') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15)),
           groupColour = TRUE,
           groupFill = TRUE)
```

C: Baseline pain threshold = 4



Parameters: Mean = 7.2, SD = 2.2, Cor = 0.8

```
# Process that data
placebo_3.5 <- seven_3 %>%
    filter(V1 >= 5) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_3.5 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_3.5,
R = 2000,
traditional = FALSE,
bca = TRUE)

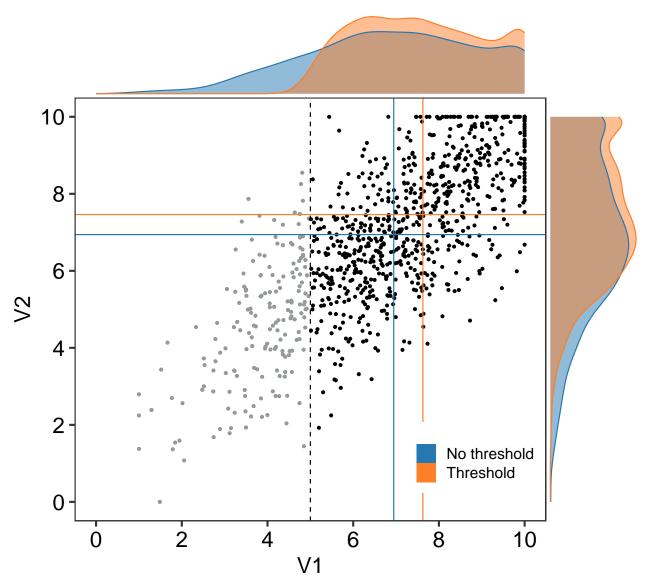
diff_3.5$.id <- 5
kable(diff_3.5)</pre>
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 5
 819
 0.164
 0.95
 0.0739
 0.256

```
ggMarginal(placebo_3.5[, 1:3] %>%
               bind_rows(seven_3) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = seven_3,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_3.5,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(seven_3$V1),
                          colour = pal[1]) +
               geom_vline(xintercept = mean(placebo_3.5$V1),
                          colour = pal[2]) +
               geom_vline(xintercept = 5, linetype = 2) +
               geom_hline(yintercept = mean(seven_3$V2),
                          colour = pal[1]) +
               geom_hline(yintercept = mean(placebo_3.5$V2),
                          colour = pal[2]) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'D: Baseline pain threshold = 5',
                    caption = 'Parameters: Mean = 7.2, SD = 2.2, Cor = 0.8') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15)),
           groupColour = TRUE,
           groupFill = TRUE)
```

D: Baseline pain threshold = 5



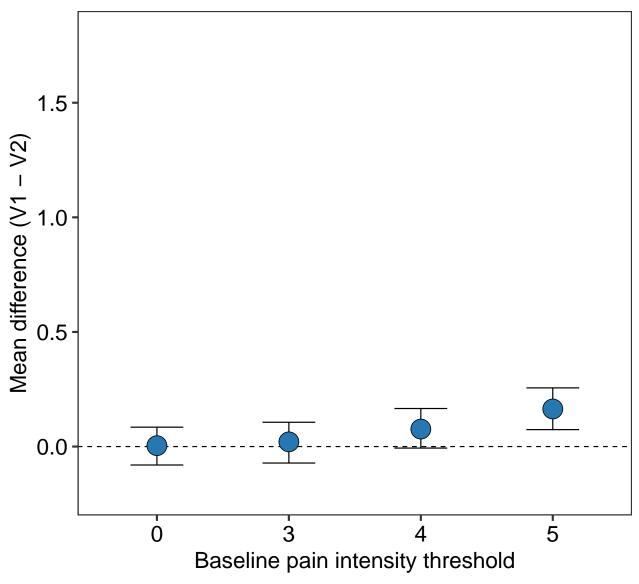
Parameters: Mean = 7.2, SD = 2.2, Cor = 0.8

Difference plot

```
# Bind diff_*.* dataframes
diff_all_3 <- diff_3.0 %>%
  bind_rows(diff_3.3, diff_3.4, diff_3.5)

pp_3 <- diff_all_3 %>%
  mutate(Threshold = factor(.id)) %>%
  ggplot(data = .) +
  aes(x = Threshold,
    y = Mean,
    ymin = Bca.lower,
    ymax = Bca.upper) +
```

Parameters: Mean = 7.2, SD = 2.2, Cor = 0.8



Publication plot

```
pp_4 <- pp_1 + pp_2 + pp_3
ggsave('figures/7.2_0.8.png', pp_4, width = 17, height = 7)</pre>
```

Session information

[61] stats4_3.6.0

```
sessionInfo()
## R version 3.6.0 (2019-04-26)
## Platform: x86_64-apple-darwin15.6.0 (64-bit)
## Running under: macOS Mojave 10.14.6
##
## Matrix products: default
          /Library/Frameworks/R.framework/Versions/3.6/Resources/lib/libRblas.0.dylib
## LAPACK: /Library/Frameworks/R.framework/Versions/3.6/Resources/lib/libRlapack.dylib
## locale:
## [1] en_US.UTF-8/en_US.UTF-8/en_US.UTF-8/C/en_US.UTF-8/en_US.UTF-8
## attached base packages:
## [1] stats
                 graphics grDevices utils
                                               datasets methods
                                                                   base
##
## other attached packages:
## [1] patchwork_0.0.1 knitr_1.24
                                          MBESS_4.6.0
                                                           ggExtra_0.8
## [5] rcompanion_2.2.2 MASS_7.3-51.4
                                          magrittr_1.5
                                                           forcats_0.4.0
## [9] stringr_1.4.0
                         dplyr_0.8.3
                                          purrr_0.3.2
                                                           readr_1.3.1
## [13] tidyr_0.8.3.9000 tibble_2.1.3
                                          ggplot2_3.2.0
                                                           tidyverse_1.2.1
##
## loaded via a namespace (and not attached):
## [1] nlme 3.1-141
                           matrixStats 0.54.0 lubridate 1.7.4
## [4] httr_1.4.1
                           tools_3.6.0
                                              backports_1.1.4
## [7] R6_2.4.0
                           nortest_1.0-4
                                              lazyeval_0.2.2
## [10] colorspace_1.4-1
                           withr_2.1.2.9000
                                              tidyselect_0.2.5
## [13] compiler_3.6.0
                           cli_1.1.0
                                              rvest_0.3.4
## [16] expm_0.999-4
                           xml2_1.2.2
                                              sandwich_2.5-1
## [19] labeling_0.3
                           scales_1.0.0
                                              lmtest_0.9-37
## [22] mvtnorm_1.0-11
                           multcompView_0.1-7 digest_0.6.20
## [25] foreign_0.8-72
                           rmarkdown_1.14
                                              pkgconfig_2.0.2
## [28] htmltools_0.3.6
                           manipulate_1.0.1
                                              highr_0.8
## [31] rlang_0.4.0
                           readxl_1.3.1
                                              rstudioapi_0.10
## [34] shiny_1.3.2
                           generics_0.0.2
                                              zoo_1.8-6
## [37] jsonlite_1.6
                           modeltools_0.2-22 Matrix_1.2-17
## [40] Rcpp_1.0.2
                           DescTools_0.99.28
                                              munsell_0.5.0
## [43] stringi_1.4.3
                           multcomp_1.4-10
                                              yaml 2.2.0
## [46] plyr_1.8.4
                           grid 3.6.0
                                              parallel 3.6.0
## [49] promises_1.0.1
                           crayon_1.3.4
                                              miniUI_0.1.1.1
## [52] lattice_0.20-38
                           haven_2.1.1
                                              splines_3.6.0
## [55] hms_0.5.0
                           zeallot_0.1.0
                                              pillar_1.4.2
## [58] EMT_1.1
                           boot_1.3-23
                                              codetools_0.2-16
```

evaluate_0.14

glue_1.3.1

##	[64]	modelr_0.1.5	vctrs_0.2.0	httpuv_1.5.1
##	[67]	cellranger_1.1.0	gtable_0.3.0	assertthat_0.2.1
##	[70]	xfun_0.8	mime_0.7	coin_1.3-0
##	[73]	libcoin_1.0-4	xtable_1.8-4	broom_0.5.2
##	[76]	later 0.8.0	survival 2.44-1.1	TH.data 1.0-10