Regression to the mean modeling

Mean pain rating of 5.2 at 0.5 correlation

Peter Kamerman

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Generate 2x2 covariance matrix

Generate a covariance matrix using an SD of 1.2, 1.7, and 2.2, and correlation of 0.5.

```
cor \leftarrow matrix(c(1, 0.5, 0.5, 1), ncol = 2)
std_1 \leftarrow c(1.2, 1.2)
std_2 \leftarrow c(1.7, 1.7)
std_3 \leftarrow c(2.2, 2.2)
cov_1 <- cor2cov(cor.mat = cor,</pre>
                   sd = std 1
cov_1
         [,1] [,2]
## [1,] 1.44 0.72
## [2,] 0.72 1.44
cov_2 <- cor2cov(cor.mat = cor,</pre>
                   sd = std_2
cov_2
##
          [,1] [,2]
## [1,] 2.890 1.445
## [2,] 1.445 2.890
cov_3 <- cor2cov(cor.mat = cor,</pre>
                   sd = std_3
cov_3
##
         [,1] [,2]
## [1,] 4.84 2.42
## [2,] 2.42 4.84
```

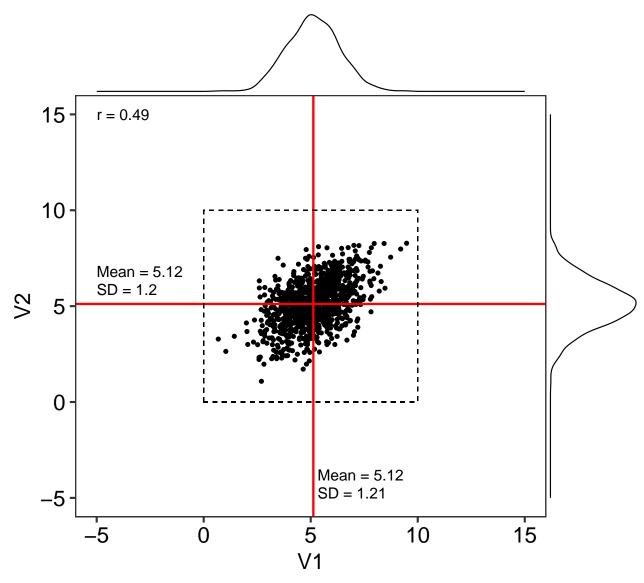
Mean = 5.2, SD = 1.2, Cor = 0.5

Generate and summarise data

Base data

```
xmin = 0, xmax = 10,
          colour = '#000000',
          alpha = 0,
          linetype = 2) +
annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5,
         label = str_glue("r = {round(cor(five_1.base$V1, five_1.base$V2), 2)}")) +
annotate(geom = 'text', x = -5, y = mean(five_1.base$V2) + 1.7,
         hjust = 0, size = 5,
         label = str_glue("Mean = {round(mean(five_1.base$V2), 2)}")) +
annotate(geom = 'text', x = -5, y = mean(five_1.base$V2) + 0.75,
         hjust = 0, size = 5,
         label = str_glue("SD = {round(sd(five_1.base$V2),2)}")) +
annotate(geom = 'text', x = mean(five_1.base$V1) + 0.2, y = -3.8,
         hjust = 0, size = 5,
         label = str_glue("Mean = {round(mean(five_1.base$V1), 2)}")) +
annotate(geom = 'text', x = mean(five_1.base$V1) + 0.2, <math>y = -4.75,
         hjust = 0, size = 5,
         label = str_glue("SD = {round(sd(five_1.base$V1), 2)}")) +
labs(title = 'A: Unconstained',
     caption = 'Parameters: Mean = 5.2, SD = 1.2, Cor = 0.5') +
scale_y_continuous(limits = c(-5, 15)) +
scale_x_continuous(limits = c(-5, 15)) +
theme(plot.caption = element_text(size = 14)))
```

A: Unconstained



Parameters: Mean = 5.2, SD = 1.2, Cor = 0.5

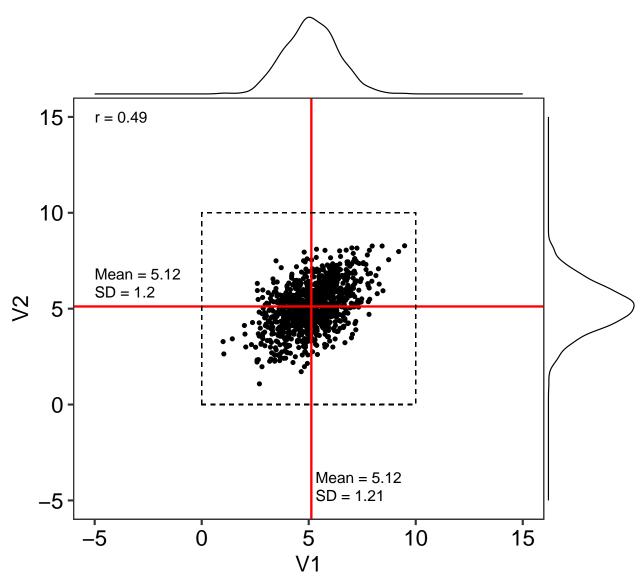
```
# Linear regression
summary(lm(V2 ~ V1, data = five_1.base))
##
## Call:
## lm(formula = V2 ~ V1, data = five_1.base)
## Residuals:
##
       Min
                1Q Median
                                ЗQ
                                       Max
## -3.1716 -0.6956 0.0432 0.6975 3.1783
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 2.63846
                           0.14332
                                     18.41
                                             <2e-16 ***
```

five 1 <- five 1.base %>% mutate(V1 = case_when(V1 < 1 ~ 1, $V1 > 10 \sim 10$, TRUE ~ V1)) %>% mutate(V2 = case_when(V2 < 0 ~ 0, $V2 > 10 \sim 10$, TRUE ~ V2)) %>% mutate(group = 'No threshold') # Plot processed data ggMarginal(ggplot(data = five_1) + aes(x = V1, y = V2) +geom_point() + geom hline(vintercept = mean(five 1\$V2), colour = 'red', size = 1) + geom_vline(xintercept = mean(five_1\$V1), colour = 'red', size = 1) + geom_rect(ymin = 0, ymax = 10, xmin = 0, xmax = 10,colour = '#000000', alpha = 0, linetype = 2) +annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5, label = str_glue("r = {round(cor(five_1\$V1, five_1\$V2), 2)}")) + annotate(geom = 'text', x = -5, $y = mean(five_1$V2) + 1.7$, hjust = 0, size = 5, label = str_glue("Mean = {round(mean(five_1\$V2), 2)}")) + annotate(geom = 'text', x = -5, $y = mean(five_1$V2) + 0.75$, hjust = 0, size = 5, label = str_glue("SD = {round(sd(five_1\$V2),2)}")) + annotate(geom = 'text', $x = mean(five_1$V1) + 0.2$, y = -3.8, hjust = 0, size = 5, label = str glue("Mean = {round(mean(five 1\$V1), 2)}")) + annotate(geom = 'text', $x = mean(five_1$V1) + 0.2$, y = -4.75, hjust = 0, size = 5, label = str_glue("SD = {round(sd(five_1\$V1), 2)}")) + labs(title = 'B: Constrained (0-10 range)', caption = 'Parameters: Mean = 5.2, SD = 1.2, Cor = 0.5') + $scale_y_continuous(limits = c(-5, 15)) +$

 $scale_x_continuous(limits = c(-5, 15)) +$

```
theme(plot.caption = element_text(size = 14)))
```

B: Constrained (0-10 range)



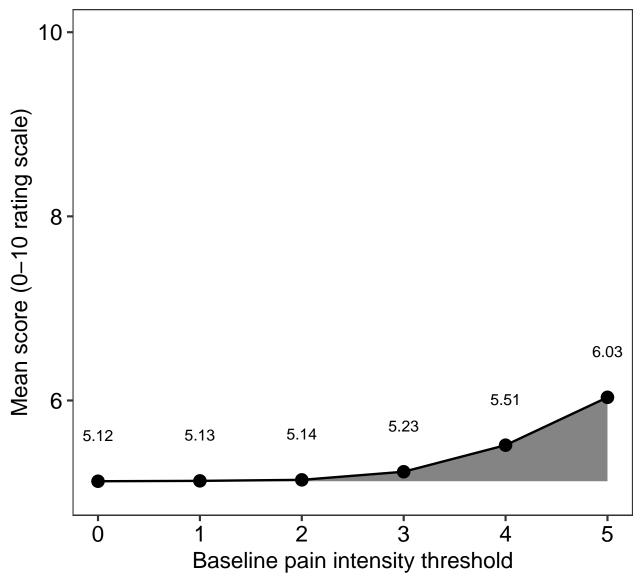
Parameters: Mean = 5.2, SD = 1.2, Cor = 0.5

```
## (Intercept) 2.63574   0.14345   18.37   <2e-16 ***
## V1      0.48397   0.02725   17.76   <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.045 on 998 degrees of freedom
## Multiple R-squared: 0.2402, Adjusted R-squared: 0.2394
## F-statistic: 315.4 on 1 and 998 DF, p-value: < 2.2e-16</pre>
```

Model mean of V1 with increasing V1 thresholds from 0 to 5

```
# Extract visit 1 data
five_1V1 <- five_1$V1
# Generate a vector of threshold values to iterate over
cutoff <- 0:5
# Generate a vector of V1 means at each V1 threshold
five_1V1.shift <- sapply(cutoff, function(x){mean(five_1V1[five_1V1 > x])})
# Calculate deviation
(five_1V1.df <- data.frame(cutoff = cutoff,</pre>
                          mean = five_1V1.shift) %>%
        mutate(deviation = mean - mean(five 1V1)))
##
    cutoff
                mean
                       deviation
         0 5.122791 0.000000000
## 1
## 2
          1 5.126918 0.004126918
## 3
         2 5.137883 0.015091815
## 4
         3 5.225994 0.103203603
## 5
         4 5.514581 0.391790095
## 6
          5 6.034325 0.911534105
# Plot data
ggplot(data = five_1V1.df) +
    aes(x = cutoff, y = mean, ymin = mean(five_1V1), ymax = mean) +
   geom ribbon(alpha = 0.6) +
   geom point(size = 5) +
   geom_line(size = 1) +
    geom_text(aes(label = round(mean, 2)),
              nudge_y = 0.5, size = 5) +
   scale_y_continuous(limits = c(5, 10),
                       breaks = c(0, 2, 4, 6, 8, 10)) +
   labs(title = 'A: Shift in V1 mean with increasing V1 threshold value',
         caption = 'Parameters: Mean = 5.2, SD = 1.2, Cor = 0.5',
         x = 'Baseline pain intensity threshold',
         y = 'Mean score (0-10 rating scale)') +
   theme(plot.caption = element_text(size = 14))
```

A: Shift in V1 mean with increasing V1 threshold value



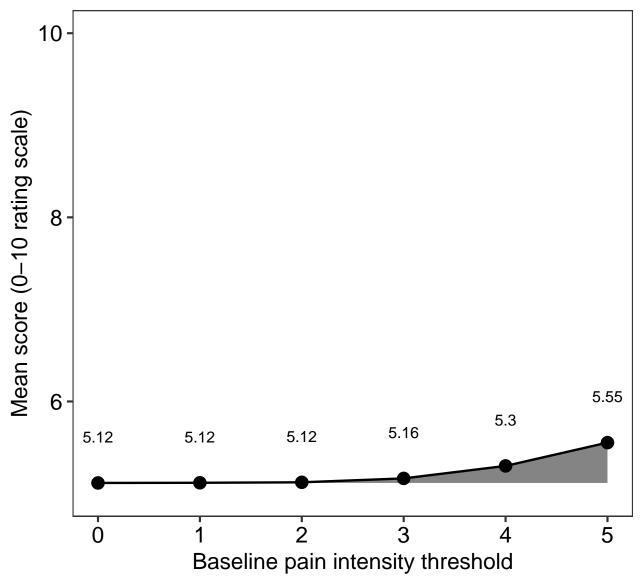
Parameters: Mean = 5.2, SD = 1.2, Cor = 0.5

Model mean of V2 with increasing V1 thresholds from 0 to 5

mean(.))

```
# Calculate deviation
(five_1V2.df <- data.frame(cutoff = cutoff,</pre>
                          mean = five_1V2.shift) %>%
       mutate(deviation = mean - mean(five_1V2)))
##
    cutoff
              mean deviation
## 1
         0 5.115030 0.000000000
## 2
         1 5.116863 0.001833823
## 3
         2 5.122042 0.007012834
         3 5.164573 0.049543750
## 4
## 5
         4 5.300008 0.184978478
## 6
         5 5.553082 0.438052453
# Plot data
ggplot(data = five_1V2.df) +
   aes(x = cutoff, y = mean, ymin = mean(five_1V2), ymax = mean) +
   geom_ribbon(alpha = 0.6) +
   geom_point(size = 5) +
   geom_line(size = 1) +
   geom_text(aes(label = round(mean, 2)),
              nudge_y = 0.5, size = 5) +
   scale_y_continuous(limits = c(5, 10),
                       breaks = c(0, 2, 4, 6, 8, 10)) +
   labs(title = 'B: Shift in V2 mean with increasing V1 threshold value',
        caption = 'Parameters: Mean = 5.2, SD = 1.2, Cor = 0.5',
        x = 'Baseline pain intensity threshold',
        y = 'Mean score (0-10 rating scale)') +
   theme(plot.caption = element_text(size = 14))
```

B: Shift in V2 mean with increasing V1 threshold value



Parameters: Mean = 5.2, SD = 1.2, Cor = 0.5

Placebo response

```
R = 2000,
traditional = FALSE,
bca = TRUE)

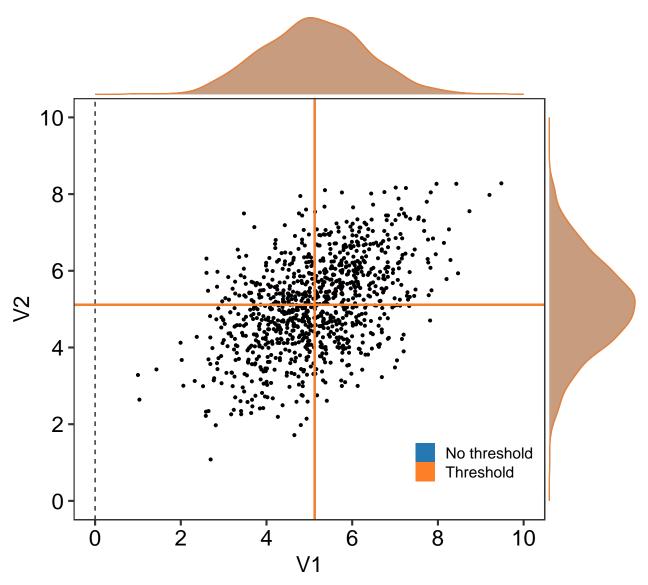
diff_1.0$.id <- 0

kable(diff 1.0)</pre>
```

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
0	1000	0.00776	0.95	-0.0706	0.0823

```
ggMarginal(placebo_1.0[, 1:3] %>%
               bind_rows(five_1) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = five_1,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_1.0,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(five_1$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_1.0$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 0, linetype = 2) +
               geom_hline(yintercept = mean(five_1$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_1.0$V2),
                          colour = pal[2], size = 1) +
               scale_y_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'A: Baseline pain threshold = 0',
                    caption = 'Parameters: Mean = 5.2, SD = 1.2, Cor = 0.5') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

A: Baseline pain threshold = 0



Parameters: Mean = 5.2, SD = 1.2, Cor = 0.5

```
bca = TRUE)
```

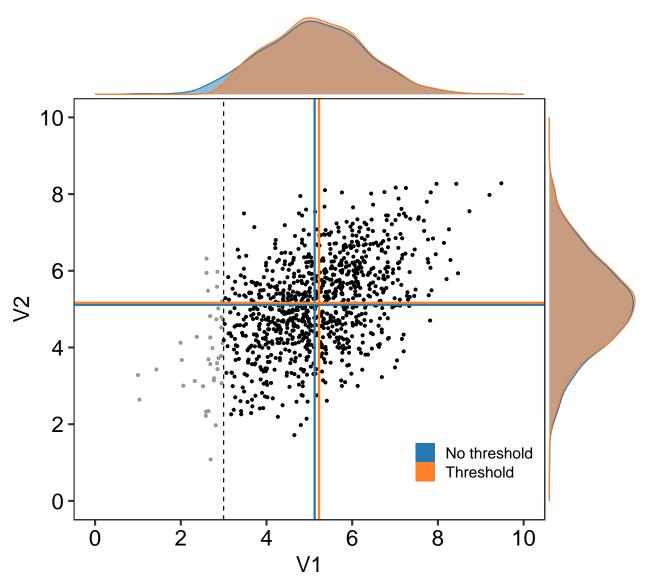
```
diff 1.3$.id <- 3
```

kable(diff_1.3)

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
3	961	0.0614	0.95	-0.0141	0.134

```
ggMarginal(placebo_1.3[, 1:3] %>%
               bind_rows(five_1) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = five_1,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_1.3,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(five_1$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_1.3$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 3, linetype = 2) +
               geom_hline(yintercept = mean(five_1$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_1.3$V2),
                          colour = pal[2], size = 1) +
               scale_y_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale colour manual(values = pal) +
               labs(title = 'B: Baseline pain threshold = 3',
                    caption = 'Parameters: Mean = 5.2, SD = 1.2, Cor = 0.5') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

B: Baseline pain threshold = 3



Parameters: Mean = 5.2, SD = 1.2, Cor = 0.5

```
# Process that data
placebo_1.4 <- five_1 %>%
    filter(V1 >= 4) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_1.4 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_1.4,
R = 2000,
traditional = FALSE,
bca = TRUE)

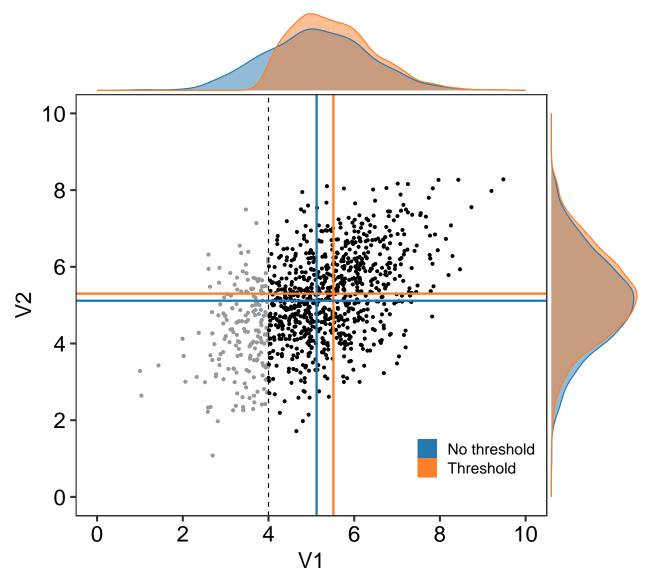
diff_1.4$.id <- 4
kable(diff_1.4)</pre>
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 4
 817
 0.215
 0.95
 0.136
 0.292

```
ggMarginal(placebo_1.4[, 1:3] %>%
               bind_rows(five_1) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = five_1,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_1.4,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(five_1$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_1.4$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 4, linetype = 2) +
               geom_hline(yintercept = mean(five_1$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_1.4$V2),
                          colour = pal[2], size = 1) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'C: Baseline pain threshold = 4',
                    caption = 'Parameters: Mean = 5.2, SD = 1.2, Cor = 0.5') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

C: Baseline pain threshold = 4



Parameters: Mean = 5.2, SD = 1.2, Cor = 0.5

```
# Process that data
placebo_1.5 <- five_1 %>%
    filter(V1 >= 5) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_1.5 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_1.5,
R = 2000,
traditional = FALSE,
bca = TRUE)

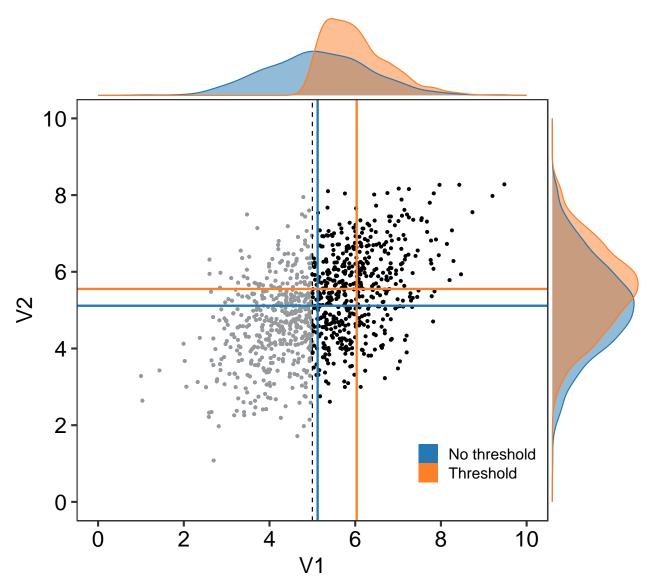
diff_1.5$.id <- 5
kable(diff_1.5)</pre>
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 5
 528
 0.481
 0.95
 0.385
 0.574

```
ggMarginal(placebo_1.5[, 1:3] %>%
               bind_rows(five_1) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = five_1,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_1.5,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(five_1$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_1.5$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 5, linetype = 2) +
               geom_hline(yintercept = mean(five_1$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_1.5$V2),
                          colour = pal[2], size = 1) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'D: Baseline pain threshold = 5',
                    caption = 'Parameters: Mean = 5.2, SD = 1.2, Cor = 0.5') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

D: Baseline pain threshold = 5



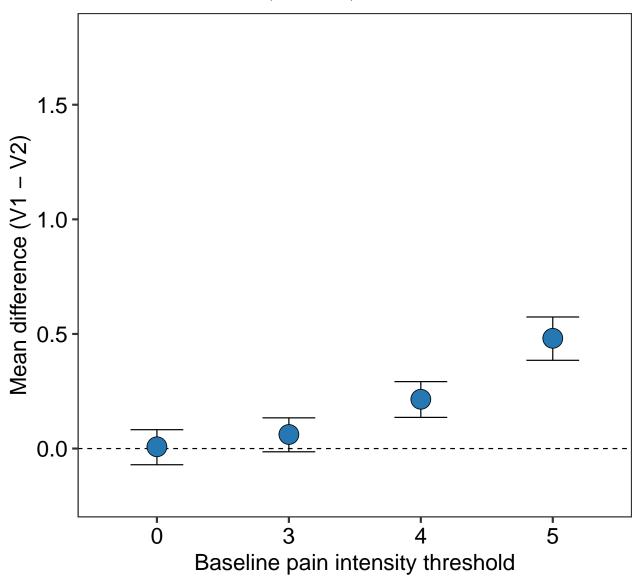
Parameters: Mean = 5.2, SD = 1.2, Cor = 0.5

Difference plot

```
# Bind diff_*.* dataframes
diff_all_1 <- diff_1.0 %>%
  bind_rows(diff_1.3, diff_1.4, diff_1.5)

pp_1 <- diff_all_1 %>%
  mutate(Threshold = factor(.id)) %>%
  ggplot(data = .) +
  aes(x = Threshold,
    y = Mean,
    ymin = Bca.lower,
    ymax = Bca.upper) +
```

Parameters: Mean = 5.2, SD = 1.2, Cor = 0.5



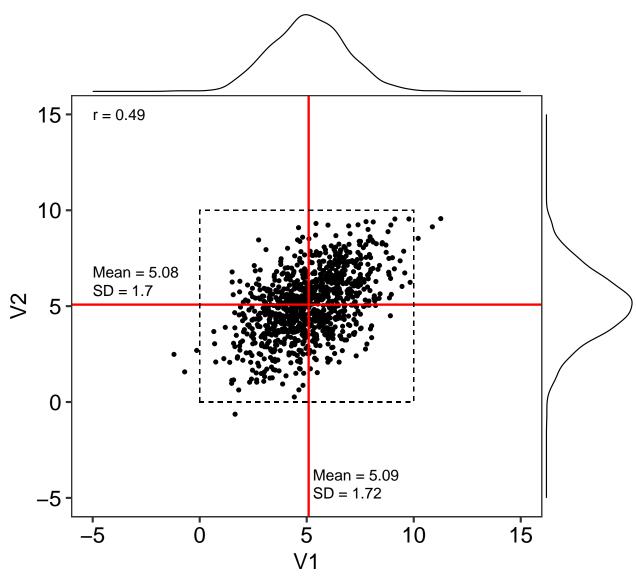
Mean = 5.2, SD = 1.7, Cor = 0.5

Generate and summarise data

Base data

```
# Set the random seed for reproducibility
set.seed(2019)
# Generate the data
five_2.base <- as.data.frame(mvrnorm(n = 1000, mu = c(5.2, 5.2), Sigma = cov_2))
# Plot base data
ggMarginal(ggplot(data = five_2.base) +
               aes(x = V1, y = V2) +
               geom_point() +
               geom_hline(yintercept = mean(five_2.base$V2),
                          colour = 'red', size = 1) +
               geom_vline(xintercept = mean(five_2.base$V1),
                          colour = 'red', size = 1) +
               geom_rect(ymin = 0, ymax = 10,
                         xmin = 0, xmax = 10,
                         colour = '#000000',
                         alpha = 0,
                         linetype = 2) +
               annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5,
                        label = str_glue("r = {round(cor(five_2.base$V1, five_2.base$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(five 2.base$V2) + 1.7,
                        hjust = 0, size = 5,
                        label = str_glue("Mean = {round(mean(five_2.base$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(five_2.base$V2) + 0.75,
                        hjust = 0, size = 5,
                        label = str_glue("SD = {round(sd(five_2.base$V2),2)}")) +
               annotate(geom = 'text', x = mean(five_2.base$V1) + 0.2, y = -3.8,
                        hjust = 0, size = 5,
                        label = str_glue("Mean = {round(mean(five_2.base$V1), 2)}")) +
               annotate(geom = 'text', x = mean(five_2.base$V1) + 0.2, <math>y = -4.75,
                        hjust = 0, size = 5,
                        label = str_glue("SD = {round(sd(five_2.base$V1), 2)}")) +
               labs(title = 'A: Unconstrained',
                    caption = 'Parameters: Mean = 5.2, SD = 1.7, Cor = 0.5') +
               scale_y_continuous(limits = c(-5, 15)) +
               scale_x_continuous(limits = c(-5, 15)) +
               theme(plot.caption = element_text(size = 14)))
```

A: Unconstrained



Parameters: Mean = 5.2, SD = 1.7, Cor = 0.5

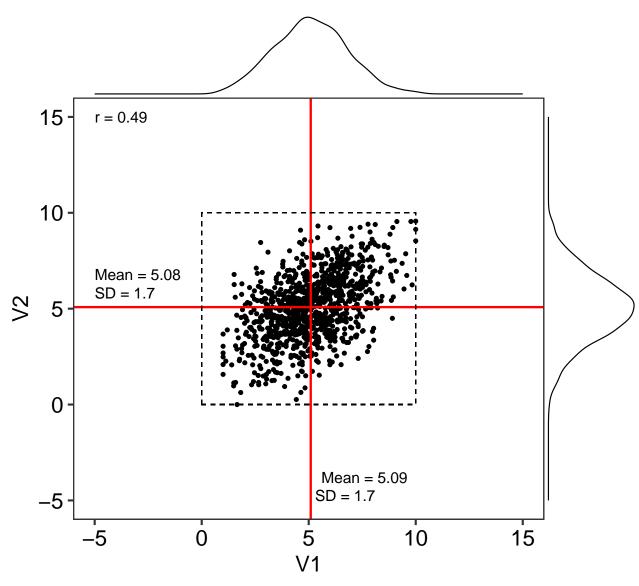
```
# Linear regression
summary(lm(V2 ~ V1, data = five_2.base))
##
## Call:
## lm(formula = V2 ~ V1, data = five_2.base)
## Residuals:
##
       Min
                1Q Median
                                ЗQ
                                       Max
## -4.4932 -0.9854 0.0613 0.9882 4.5026
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 2.61867
                          0.14628
                                    17.90
                                            <2e-16 ***
```

```
## V1
                0.48347
                           0.02723
                                   17.76 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.481 on 998 degrees of freedom
## Multiple R-squared: 0.2401, Adjusted R-squared: 0.2394
## F-statistic: 315.4 on 1 and 998 DF, p-value: < 2.2e-16
Constrain values to 0-10 range
# Process data
five 2 <- five 2.base %>%
   mutate(V1 = case_when(
              V1 < 1 \sim 1,
              V1 > 10 \sim 10,
              TRUE ~ V1)) %>%
   mutate(V2 = case_when(
               V2 < 0 \sim 0,
              V2 > 10 \sim 10,
              TRUE ~ V2)) %>%
   mutate(group = 'No threshold')
# Plot processed data
ggMarginal(ggplot(data = five_2) +
               aes(x = V1, y = V2) +
               geom_point() +
               geom hline(vintercept = mean(five 2$V2),
                          colour = 'red', size = 1) +
               geom_vline(xintercept = mean(five_2$V1),
                          colour = 'red', size = 1) +
               geom_rect(ymin = 0, ymax = 10,
                         xmin = 0, xmax = 10,
                         colour = '#000000',
                         alpha = 0,
                         linetype = 2) +
               annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5,
                        label = str_glue("r = {round(cor(five_2$V1, five_2$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(five_2$V2) + 1.7,
                        hjust = 0, size = 5,
                        label = str_glue("Mean = {round(mean(five_2$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(five_2$V2) + 0.75,
                        hjust = 0, size = 5,
                        label = str_glue("SD = {round(sd(five_2$V2),2)}")) +
               annotate(geom = 'text', x = mean(five_2$V1) + 0.5, y = -3.8,
                        hjust = 0, size = 5,
                        label = str glue("Mean = {round(mean(five 2$V1), 2)}")) +
               annotate(geom = 'text', x = mean(five_2$V1) + 0.2, y = -4.75,
                        hjust = 0, size = 5,
                        label = str_glue("SD = {round(sd(five_2$V1), 2)}")) +
               labs(title = 'B: Constrained (0-10 range)',
                    caption = 'Parameters: Mean = 5.2, SD = 1.7, Cor = 0.5') +
```

scale_y_continuous(limits = c(-5, 15)) + scale_x_continuous(limits = c(-5, 15)) +

```
theme(plot.caption = element_text(size = 14)))
```

B: Constrained (0-10 range)



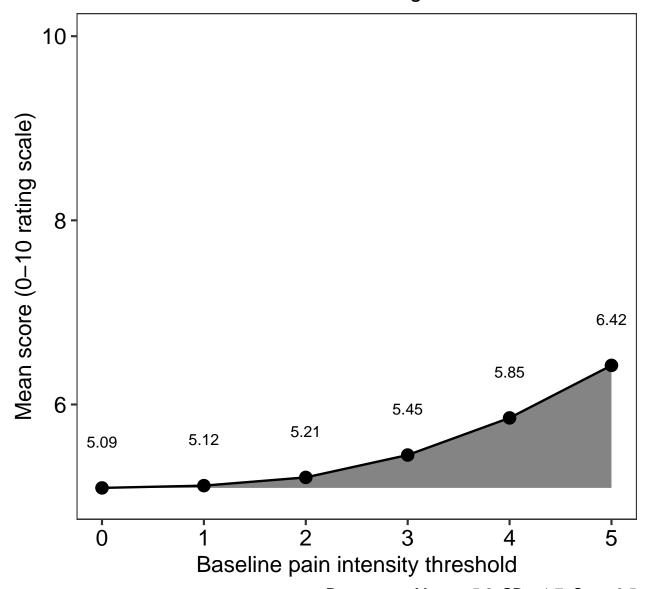
Parameters: Mean = 5.2, SD = 1.7, Cor = 0.5

```
## (Intercept) 2.59647   0.14830   17.51   <2e-16 ***
## V1         0.48762   0.02762   17.65   <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.481 on 998 degrees of freedom
## Multiple R-squared: 0.2379, Adjusted R-squared: 0.2372
## F-statistic: 311.6 on 1 and 998 DF, p-value: < 2.2e-16</pre>
```

Model mean of V1 with increasing V1 thresholds from 0 to 5

```
# Extract visit 1 data
five_2V1 <- five_2$V1
# Generate a vector of threshold values to iterate over
cutoff <- 0:5
# Generate a vector of V1 means at each V1 threshold
five_2V1.shift <- sapply(cutoff, function(x){mean(five_2V1[five_2V1 > x])})
# Calculate deviation
(five 2V1.df <- data.frame(cutoff = cutoff,
                           mean = five_2V1.shift) %>%
       mutate(deviation = mean - mean(five 2V1)))
##
    cutoff
               mean deviation
         0 5.093762 0.00000000
## 1
## 2
          1 5.118473 0.02471084
## 3
         2 5.207945 0.11418329
## 4
         3 5.450979 0.35721683
## 5
         4 5.854175 0.76041340
## 6
         5 6.424720 1.33095827
# Plot data
ggplot(data = five_2V1.df) +
    aes(x = cutoff, y = mean, ymin = mean(five_2V1), ymax = mean) +
   geom ribbon(alpha = 0.6) +
   geom point(size = 5) +
   geom_line(size = 1) +
    geom_text(aes(label = round(mean, 2)),
              nudge_y = 0.5, size = 5) +
   scale_y_continuous(limits = c(5, 10),
                       breaks = c(0, 2, 4, 6, 8, 10)) +
   labs(title = 'A: Shift in V1 mean with increasing V1 threshold value',
         caption = 'Parameters: Mean = 5.2, SD = 1.7, Cor = 0.5',
         x = 'Baseline pain intensity threshold',
         y = 'Mean score (0-10 rating scale)') +
   theme(plot.caption = element_text(size = 14))
```

A: Shift in V1 mean with increasing V1 threshold value



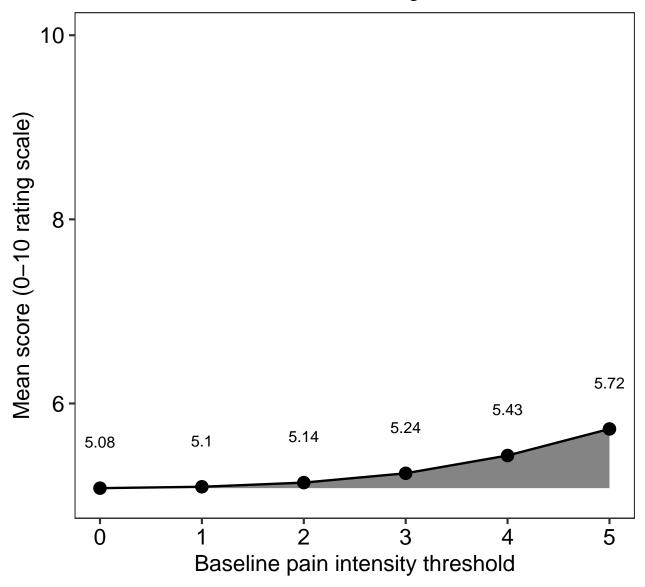
Parameters: Mean = 5.2, SD = 1.7, Cor = 0.5

Model mean of V2 with increasing V1 thresholds from 0 to 5

mean(.))

```
# Calculate deviation
(five_2V2.df <- data.frame(cutoff = cutoff,</pre>
                          mean = five_2V2.shift) %>%
       mutate(deviation = mean - mean(five_2V2)))
##
    cutoff
              mean deviation
## 1
         0 5.080261 0.00000000
## 2
         1 5.095284 0.01502254
## 3
         2 5.140449 0.06018785
## 4
         3 5.241791 0.16152985
## 5
         4 5.434797 0.35453608
## 6
         5 5.723440 0.64317914
# Plot data
ggplot(data = five_2V2.df) +
   aes(x = cutoff, y = mean, ymin = mean(five_2V2), ymax = mean) +
   geom_ribbon(alpha = 0.6) +
   geom_point(size = 5) +
   geom_line(size = 1) +
   geom_text(aes(label = round(mean, 2)),
              nudge_y = 0.5, size = 5) +
   scale_y_continuous(limits = c(5, 10),
                      breaks = c(0, 2, 4, 6, 8, 10)) +
   labs(title = 'B: Shift in V2 mean with increasing V1 threshold value',
        caption = 'Parameters: Mean = 5.2, SD = 1.7, Cor = 0.5',
        x = 'Baseline pain intensity threshold',
        y = 'Mean score (0-10 rating scale)') +
   theme(plot.caption = element_text(size = 14))
```

B: Shift in V2 mean with increasing V1 threshold value



Parameters: Mean = 5.2, SD = 1.7, Cor = 0.5

Placebo response

```
R = 2000,
traditional = FALSE,
bca = TRUE)
```

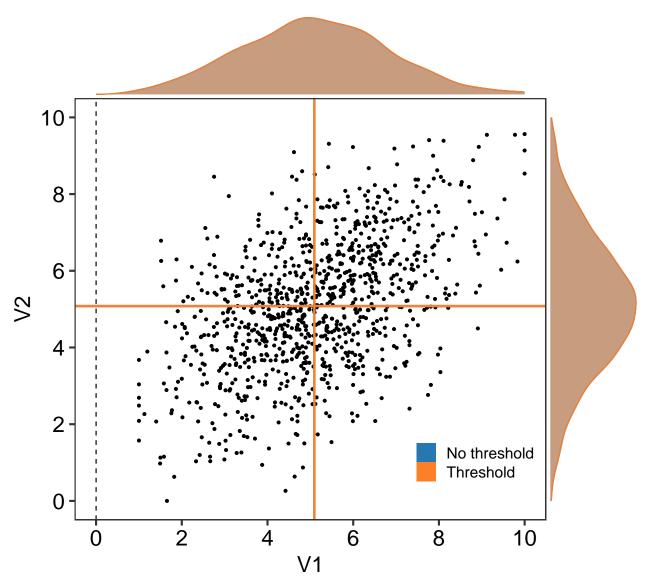
kable(diff 2.0)

diff 2.0\$.id <- 0

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
0	1000	0.0135	0.95	-0.0955	0.119

```
ggMarginal(placebo_2.0[, 1:3] %>%
               bind_rows(five_2) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = five_2,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_2.0,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(five_2$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_2.0$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 0, linetype = 2) +
               geom_hline(yintercept = mean(five_2$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_2.0$V2),
                          colour = pal[2], size = 1) +
               scale_y_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale colour manual(values = pal) +
               labs(title = 'A: Baseline pain threshold = 0',
                    caption = 'Parameters: Mean = 5.2, SD = 1.7, Cor = 0.5') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

A: Baseline pain threshold = 0



Parameters: Mean = 5.2, SD = 1.7, Cor = 0.5

```
# Process data
placebo_2.3 <- five_2 %>%
    filter(V1 >= 3) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_2.3 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_2.3,
R = 2000,
traditional = FALSE,
bca = TRUE)

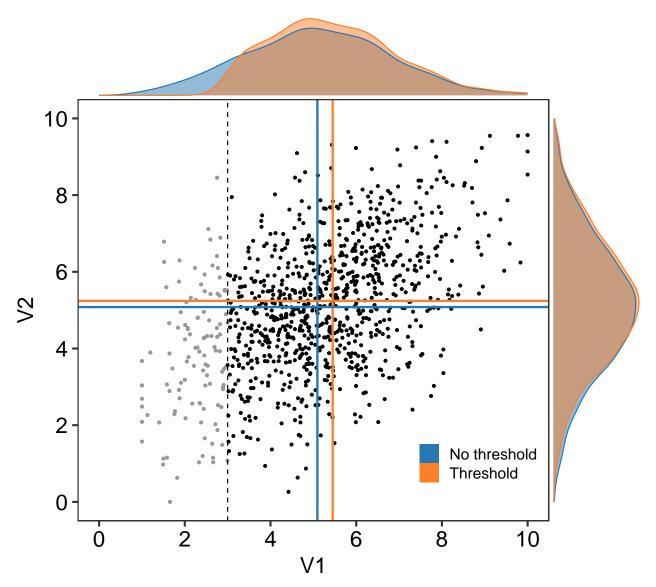
diff_2.3$.id <- 3
kable(diff_2.3)</pre>
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 3
 888
 0.209
 0.95
 0.107
 0.316

```
ggMarginal(placebo_2.3[, 1:3] %>%
               bind_rows(five_2) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = five_2,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_2.3,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(five_2$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_2.3$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 3, linetype = 2) +
               geom_hline(yintercept = mean(five_2$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_2.3$V2),
                          colour = pal[2], size = 1) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'B: Baseline pain threshold = 3',
                    caption = 'Parameters: Mean = 5.2, SD = 1.7, Cor = 0.5') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

B: Baseline pain threshold = 3



Parameters: Mean = 5.2, SD = 1.7, Cor = 0.5

```
# Process that data
placebo_2.4 <- five_2 %>%
    filter(V1 >= 4) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_2.4 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_2.4,
R = 2000,
traditional = FALSE,
bca = TRUE)

diff_2.4$.id <- 4

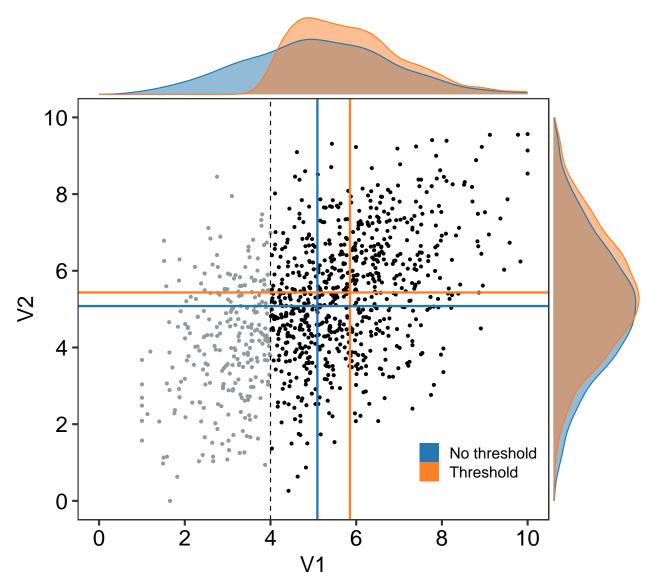
kable(diff_2.4)</pre>
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 4
 735
 0.419
 0.95
 0.307
 0.539

```
ggMarginal(placebo_2.4[, 1:3] %>%
               bind_rows(five_2) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = five_2,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_2.4,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(five_2$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_2.4$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 4, linetype = 2) +
               geom_hline(yintercept = mean(five_2$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_2.4$V2),
                          colour = pal[2], size = 1) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'C: Baseline pain threshold = 4',
                    caption = 'Parameters: Mean = 5.2, SD = 1.7, Cor = 0.5') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

C: Baseline pain threshold = 4



Parameters: Mean = 5.2, SD = 1.7, Cor = 0.5

```
# Process that data
placebo_2.5 <- five_2 %>%
    filter(V1 >= 5) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_2.5 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_2.5,
R = 2000,
traditional = FALSE,
bca = TRUE)

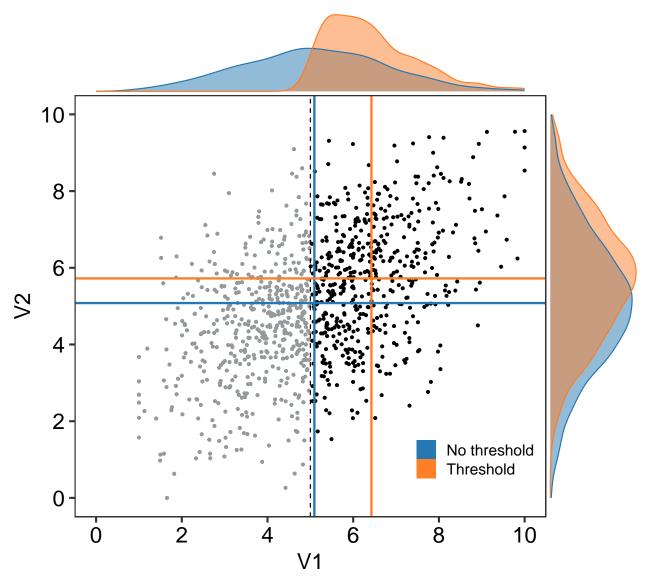
diff_2.5$.id <- 5
kable(diff_2.5)</pre>
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 5
 511
 0.701
 0.95
 0.571
 0.832

```
ggMarginal(placebo_2.5[, 1:3] %>%
               bind_rows(five_2) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = five_2,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_2.5,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(five_2$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_2.5$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 5, linetype = 2) +
               geom_hline(yintercept = mean(five_2$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_2.5$V2),
                          colour = pal[2], size = 1) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'D: Baseline pain threshold = 5',
                    caption = 'Parameters: Mean = 5.2, SD = 1.7, Cor = 0.5') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

D: Baseline pain threshold = 5



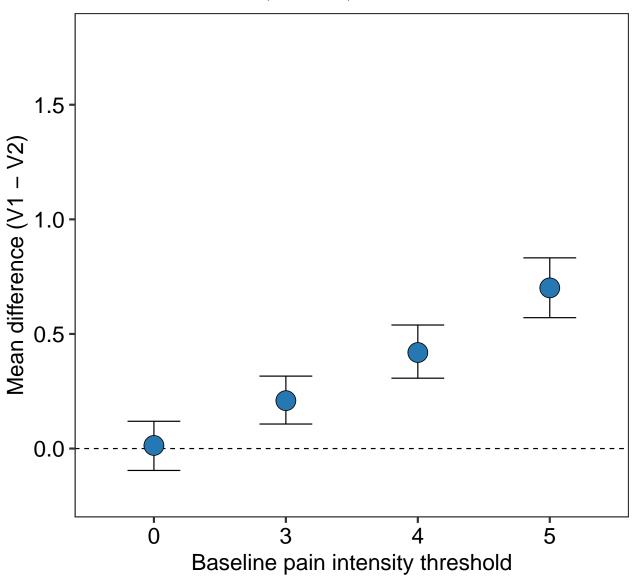
Parameters: Mean = 5.2, SD = 1.7, Cor = 0.5

Difference plot

```
# Bind diff_*.* dataframes
diff_all_2 <- diff_2.0 %>%
  bind_rows(diff_2.3, diff_2.4, diff_2.5)

pp_2 <- diff_all_2 %>%
  mutate(Threshold = factor(.id)) %>%
  ggplot(data = .) +
  aes(x = Threshold,
    y = Mean,
    ymin = Bca.lower,
    ymax = Bca.upper) +
```

Parameters: Mean = 5.2, SD = 1.7, Cor = 0.5



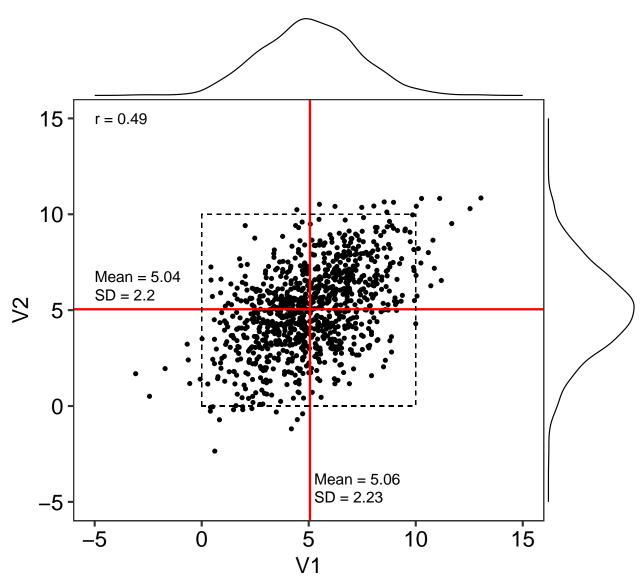
Mean = 5.2, SD = 2.2, Cor = 0.5

Generate and summarise data

Base data

```
# Set the random seed for reproducibility
set.seed(2019)
# Generate the data
five_3.base <- as.data.frame(mvrnorm(n = 1000, mu = c(5.2, 5.2), Sigma = cov_3))
# Plot base data
ggMarginal(ggplot(data = five_3.base) +
               aes(x = V1, y = V2) +
               geom_point() +
               geom_hline(yintercept = mean(five_3.base$V2),
                          colour = 'red', size = 1) +
               geom_vline(xintercept = mean(five_3.base$V1),
                          colour = 'red', size = 1) +
               geom_rect(ymin = 0, ymax = 10,
                         xmin = 0, xmax = 10,
                         colour = '#000000',
                         alpha = 0,
                         linetype = 2) +
               annotate(geom = 'text', x = -5, y = 15,
                        hjust = 0, size = 5,
                        label = str glue("r = {round(cor(five 3.base$V1, five 3.base$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(five_3.base$V2) + 1.7,
                        hjust = 0, size = 5,
                        label = str_glue("Mean = {round(mean(five_3.base$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(five_3.base$V2) + 0.75,
                        hjust = 0, size = 5,
                        label = str_glue("SD = {round(sd(five_3.base$V2),2)}")) +
               annotate(geom = 'text', x = mean(five_3.base$V1) + 0.2, <math>y = -3.8,
                        hjust = 0, size = 5,
                        label = str_glue("Mean = {round(mean(five_3.base$V1), 2)}")) +
               annotate(geom = 'text', x = mean(five_3.base$V1) + 0.2, <math>y = -4.75,
                        hjust = 0, size = 5,
                        label = str_glue("SD = {round(sd(five_3.base$V1), 2)}")) +
               labs(title = 'A: Unconstrained',
                    caption = 'Parameters: Mean = 5.2, SD = 2.2, Cor = 0.5') +
               scale_y_continuous(limits = c(-5, 15)) +
               scale_x_continuous(limits = c(-5, 15)) +
               theme(plot.caption = element_text(size = 14)))
```

A: Unconstrained



Parameters: Mean = 5.2, SD = 2.2, Cor = 0.5

```
# Linear regression
summary(lm(V2 ~ V1, data = five_3.base))
##
## Call:
## lm(formula = V2 ~ V1, data = five_3.base)
## Residuals:
##
       Min
                1Q Median
                                ЗQ
                                       Max
## -5.8147 -1.2753 0.0793 1.2788 5.8269
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 2.59889
                           0.15044
                                     17.27
                                             <2e-16 ***
```

```
## V1
                0.48347
                           0.02723
                                   17.76 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.916 on 998 degrees of freedom
## Multiple R-squared: 0.2401, Adjusted R-squared: 0.2394
## F-statistic: 315.4 on 1 and 998 DF, p-value: < 2.2e-16
Constrain values to 0-10 range
# Process data
five 3 \leftarrow five 3.base \%>\%
   mutate(V1 = case_when(
               V1 < 1 \sim 1,
               V1 > 10 \sim 10,
               TRUE ~ V1)) %>%
   mutate(V2 = case_when(
               V2 < 0 ~ 0,
               V2 > 10 \sim 10,
               TRUE ~ V2)) %>%
   mutate(group = 'No threshold')
# Plot processed data
ggMarginal(ggplot(data = five_3) +
               aes(x = V1, y = V2) +
               geom_point() +
               geom hline(vintercept = mean(five 3$V2),
                          colour = 'red', size = 1) +
               geom_vline(xintercept = mean(five_3$V1),
                          colour = 'red', size = 1) +
               geom_rect(ymin = 0, ymax = 10,
                         xmin = 0, xmax = 10,
                         colour = '#000000',
                         alpha = 0,
                         linetype = 2) +
               annotate(geom = 'text', x = -5, y = 15,
                        hjust = 0, size = 5,
                        label = str_glue("r = {round(cor(five_3$V1, five_3$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(five_3$V2) + 1.7,
                        hjust = 0, size = 5,
                        label = str_glue("Mean = {round(mean(five_3$V2), 2)}")) +
               annotate(geom = 'text', x = -5, y = mean(five_3$V2) + 0.75,
                        hjust = 0, size = 5,
                        label = str glue("SD = {round(sd(five 3$V2),2)}")) +
               annotate(geom = 'text', x = mean(five_3$V1) + 0.2, y = -3.8,
                        hjust = 0, size = 5,
                        label = str_glue("Mean = {round(mean(five_3$V1), 2)}")) +
```

annotate(geom = 'text', $x = mean(five_3$V1) + 0.2$, y = -4.75,

label = str_glue("SD = {round(sd(five_3\$V1), 2)}")) +

caption = 'Parameters: Mean = 5.2, SD = 2.2, Cor = 0.5') +

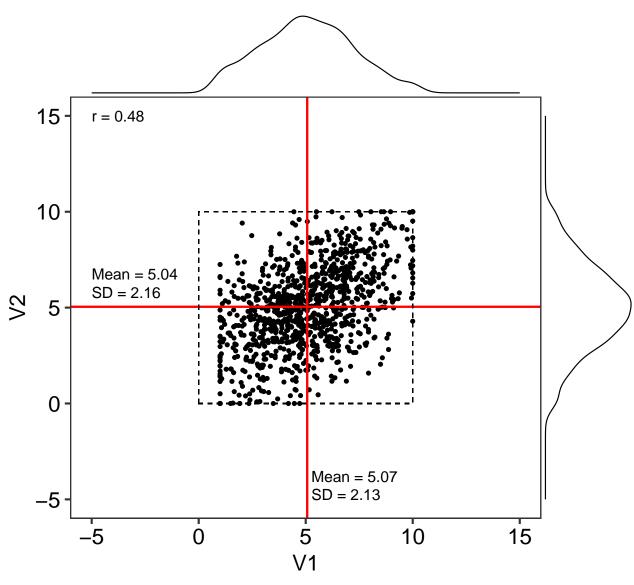
hjust = 0, size = 5,

labs(title = 'B: Constrained (0-10 range)',

 $scale_y_continuous(limits = c(-5, 15)) +$

```
scale_x_continuous(limits = c(-5, 15)) +
theme(plot.caption = element_text(size = 14)))
```

B: Constrained (0–10 range)



Parameters: Mean = 5.2, SD = 2.2, Cor = 0.5

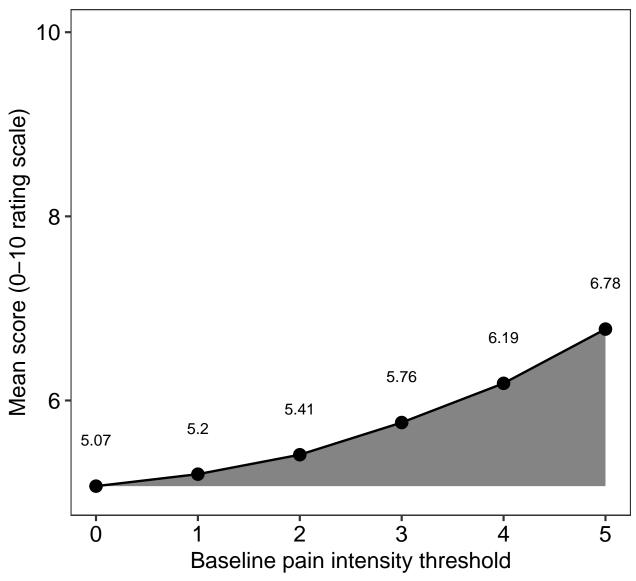
```
# Linear regression
summary(lm(V2 ~ V1, data = five_3))
##
## Call:
## lm(formula = V2 ~ V1, data = five_3)
##
## Residuals:
## Min    1Q Median    3Q Max
## -4.8718 -1.2985    0.0622    1.2906    5.8476
##
## Coefficients:
```

```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 2.56804   0.15476   16.59   <2e-16 ***
## V1         0.48846   0.02814   17.36   <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.898 on 998 degrees of freedom
## Multiple R-squared: 0.2319, Adjusted R-squared: 0.2311
## F-statistic: 301.3 on 1 and 998 DF, p-value: < 2.2e-16</pre>
```

Model mean of V1 with increasing V1 thresholds from 0 to 5

```
# Extract visit 1 data
five_3V1 <- five_3$V1
# Generate a vector of threshold values to iterate over
cutoff <- 0:5
# Generate a vector of V1 means at each V1 threshold
five 3V1.shift <- sapply(cutoff, function(x){mean(five 3V1[five 3V1 > x])})
# Calculate deviation
(five_3V1.df <- data.frame(cutoff = cutoff,</pre>
                           mean = five 3V1.shift) %>%
        mutate(deviation = mean - mean(five 3V1)))
     cutoff
                mean deviation
## 1
         0 5.069509 0.0000000
## 2
         1 5.199700 0.1301907
## 3
         2 5.410951 0.3414419
## 4
         3 5.760471 0.6909618
## 5
         4 6.186270 1.1167604
## 6
         5 6.775409 1.7058995
# Plot data
ggplot(data = five_3V1.df) +
   aes(x = cutoff, y = mean, ymin = mean(five_3V1), ymax = mean) +
    geom ribbon(alpha = 0.6) +
   geom_point(size = 5) +
    geom line(size = 1) +
   geom_text(aes(label = round(mean, 2)),
              nudge y = 0.5, size = 5) +
    scale_y_continuous(limits = c(5, 10),
                       breaks = c(0, 2, 4, 6, 8, 10)) +
   labs(title = 'A: Shift in V1 mean with increasing V1 threshold value',
         caption = 'Parameters: Mean = 5.2, SD = 2.2, Cor = 0.5',
         x = 'Baseline pain intensity threshold',
         y = 'Mean score (0-10 rating scale)') +
    theme(plot.caption = element_text(size = 14))
```

A: Shift in V1 mean with increasing V1 threshold value



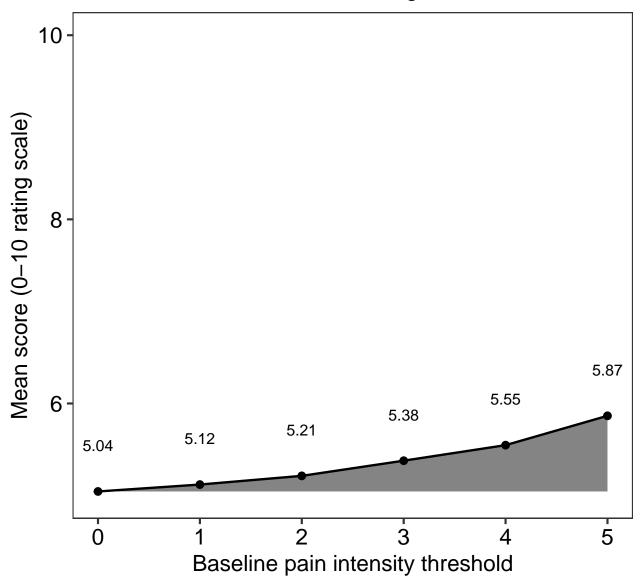
Parameters: Mean = 5.2, SD = 2.2, Cor = 0.5

Model mean of V2 with increasing V1 thresholds from 0 to 5

mean(.))

```
# Calculate deviation
(five_3V2.df <- data.frame(cutoff = cutoff,</pre>
                           mean = five_3V2.shift) %>%
       mutate(deviation = mean - mean(five_3V2)))
##
    cutoff
              mean deviation
## 1
         0 5.044282 0.00000000
## 2
         1 5.119444 0.07516135
## 3
         2 5.213786 0.16950321
## 4
         3 5.378531 0.33424872
## 5
         4 5.547313 0.50303028
## 6
         5 5.866011 0.82172822
# Plot data
ggplot(data = five_3V2.df) +
   aes(x = cutoff, y = mean, ymin = mean(five_3V2), ymax = mean) +
   geom_ribbon(alpha = 0.6) +
   geom_point(size = 3) +
   geom_line(size = 1) +
   geom_text(aes(label = round(mean, 2)),
              nudge_y = 0.5, size = 5) +
   scale_y_continuous(limits = c(5, 10),
                       breaks = c(0, 2, 4, 6, 8, 10)) +
   labs(title = 'B: Shift in V2 mean with increasing V1 threshold value',
         caption = 'Parameters: Mean = 5.2, SD = 2.2, Cor = 0.5',
         x = 'Baseline pain intensity threshold',
         y = 'Mean score (0-10 rating scale)') +
   theme(plot.caption = element_text(size = 14))
```

B: Shift in V2 mean with increasing V1 threshold value



Parameters: Mean = 5.2, SD = 2.2, Cor = 0.5

Placebo response

```
R = 2000,
traditional = FALSE,
bca = TRUE)
```

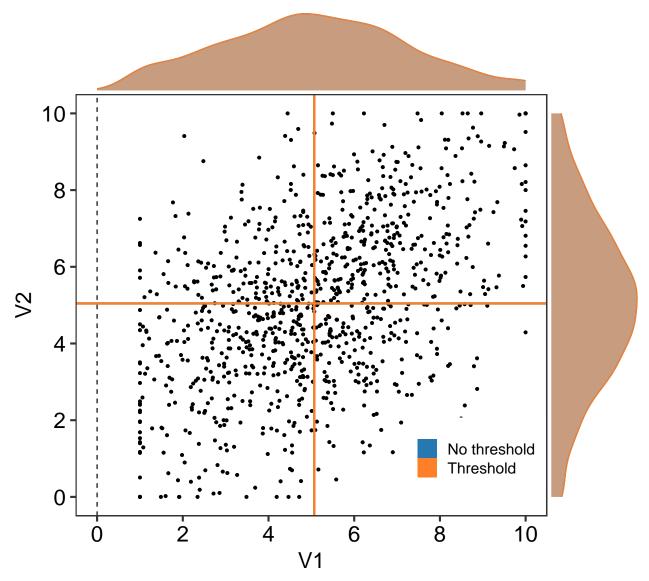
kable(diff 3.0)

diff 3.0\$.id <- 0

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
0	1000	0.0252	0.95	-0.112	0.159

```
ggMarginal(placebo_3.0[, 1:3] %>%
               bind_rows(five_3) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = five_3,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_3.0,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(five_3$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_3.0$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 0, linetype = 2) +
               geom_hline(yintercept = mean(five_3$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_3.0$V2),
                          colour = pal[2], size = 1) +
               scale_y_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale colour manual(values = pal) +
               labs(title = 'A: Baseline pain threshold = 0',
                    caption = 'Parameters: Mean = 5.2, SD = 2.2, Cor = 0.5') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

A: Baseline pain threshold = 0



Parameters: Mean = 5.2, SD = 2.2, Cor = 0.5

```
# Process data
placebo_3.3 <- five_3 %>%
    filter(V1 >= 3) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_3.3 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_3.3,
    R = 2000,
    traditional = FALSE,
    bca = TRUE)

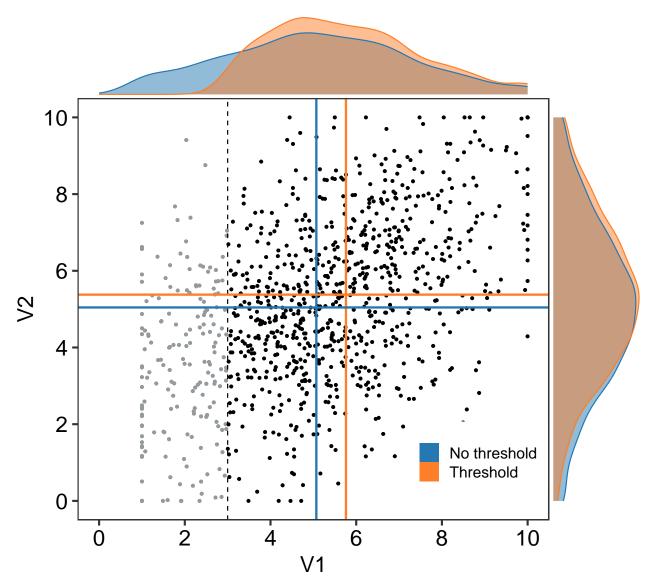
diff_3.3$.id <- 3
kable(diff_3.3)</pre>
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 3
 817
 0.382
 0.95
 0.243
 0.527

```
ggMarginal(placebo_3.3[, 1:3] %>%
               bind_rows(five_3) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = five_3,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_3.3,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(five_3$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_3.3$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 3, linetype = 2) +
               geom_hline(yintercept = mean(five_3$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_3.3$V2),
                          colour = pal[2], size = 1) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'B: Baseline pain threshold = 3',
                    caption = 'Parameters: Mean = 5.2, SD = 2.2, Cor = 0.5') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

B: Baseline pain threshold = 3



Parameters: Mean = 5.2, SD = 2.2, Cor = 0.5

```
# Process that data
placebo_3.4 <- five_3 %>%
    filter(V1 >= 4) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_3.4 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_3.4,
R = 2000,
traditional = FALSE,
bca = TRUE)
```

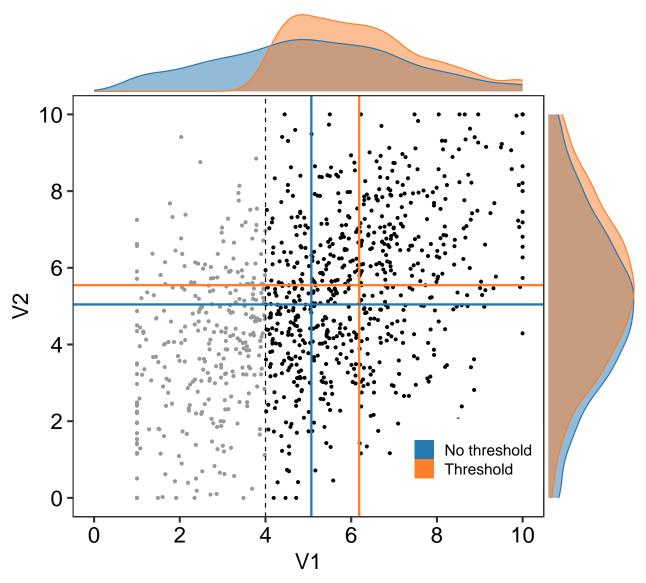
kable(diff_3.4)

diff 3.4\$.id <- 4

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
4	687	0.639	0.95	0.507	0.783

```
ggMarginal(placebo_3.4[, 1:3] %>%
               bind_rows(five_3) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = five_3,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_3.4,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(five_3$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_3.4$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 4, linetype = 2) +
               geom_hline(yintercept = mean(five_3$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_3.4$V2),
                          colour = pal[2], size = 1) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'C: Baseline pain threshold = 4',
                    caption = 'Parameters: Mean = 5.2, SD = 2.2, Cor = 0.5') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

C: Baseline pain threshold = 4



Parameters: Mean = 5.2, SD = 2.2, Cor = 0.5

```
# Process that data
placebo_3.5 <- five_3 %>%
    filter(V1 >= 5) %>%
    mutate(difference = V1 - V2) %>%
    mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
diff_3.5 <- groupwiseMean(difference ~ 1,</pre>
```

```
data = placebo_3.5,
R = 2000,
traditional = FALSE,
bca = TRUE)

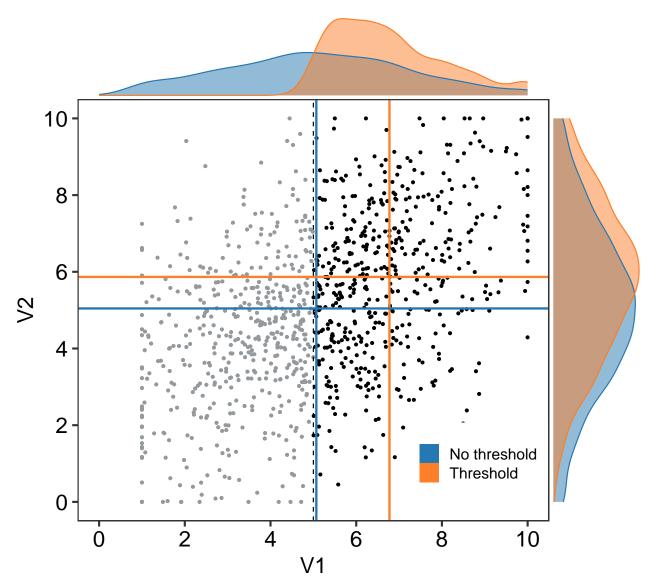
diff_3.5$.id <- 5
kable(diff_3.5)</pre>
```

 .id
 n
 Mean
 Conf.level
 Bca.lower
 Bca.upper

 5
 508
 0.909
 0.95
 0.731
 1.1

```
ggMarginal(placebo_3.5[, 1:3] %>%
               bind_rows(five_3) %>%
               mutate(group = factor(group,
                                     levels = c('No threshold', 'Threshold'),
                                     ordered = TRUE)) %>%
               ggplot(data = .) +
               aes(x = V1, y = V2) +
               geom_point(aes(colour = group, fill = group),
                          size = 1,
                          key_glyph = draw_key_rect) +
               geom_point(data = five_3,
                          colour = '#999999',
                          size = 1) +
               geom_point(data = placebo_3.5,
                          size = 1,
                          colour = '#000000') +
               geom_vline(xintercept = mean(five_3$V1),
                          colour = pal[1], size = 1) +
               geom_vline(xintercept = mean(placebo_3.5$V1),
                          colour = pal[2], size = 1) +
               geom_vline(xintercept = 5, linetype = 2) +
               geom_hline(yintercept = mean(five_3$V2),
                          colour = pal[1], size = 1) +
               geom_hline(yintercept = mean(placebo_3.5$V2),
                          colour = pal[2], size = 1) +
               scale y continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_x_continuous(limits = c(0, 10),
                                  breaks = c(0, 2, 4, 6, 8, 10)) +
               scale_fill_manual(values = pal) +
               scale_colour_manual(values = pal) +
               labs(title = 'D: Baseline pain threshold = 5',
                    caption = 'Parameters: Mean = 5.2, SD = 2.2, Cor = 0.5') +
               theme(legend.title = element_blank(),
                     legend.position = c(0.85, 0.15),
                     plot.caption = element_text(size = 14)),
           groupColour = TRUE,
           groupFill = TRUE)
```

D: Baseline pain threshold = 5



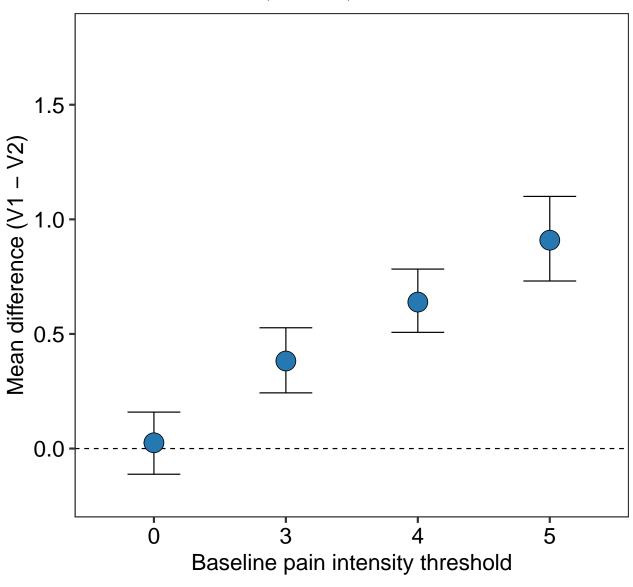
Parameters: Mean = 5.2, SD = 2.2, Cor = 0.5

Difference plot

```
# Bind diff_*.* dataframes
diff_all_3 <- diff_3.0 %>%
  bind_rows(diff_3.3, diff_3.4, diff_3.5)

pp_3 <- diff_all_3 %>%
  mutate(Threshold = factor(.id)) %>%
  ggplot(data = .) +
  aes(x = Threshold,
    y = Mean,
    ymin = Bca.lower,
    ymax = Bca.upper) +
```

Parameters: Mean = 5.2, SD = 2.2, Cor = 0.5



Publication plot

```
pp_4 <- pp_1 + pp_2 + pp_3
ggsave('figures/5.2_0.5.png', pp_4, width = 17, height = 7)</pre>
```

Session information

[61] stats4_3.6.0

```
sessionInfo()
## R version 3.6.0 (2019-04-26)
## Platform: x86_64-apple-darwin15.6.0 (64-bit)
## Running under: macOS Mojave 10.14.6
##
## Matrix products: default
          /Library/Frameworks/R.framework/Versions/3.6/Resources/lib/libRblas.0.dylib
## LAPACK: /Library/Frameworks/R.framework/Versions/3.6/Resources/lib/libRlapack.dylib
## locale:
## [1] en_US.UTF-8/en_US.UTF-8/en_US.UTF-8/C/en_US.UTF-8/en_US.UTF-8
## attached base packages:
## [1] stats
                 graphics grDevices utils
                                               datasets methods
                                                                   base
##
## other attached packages:
## [1] patchwork_0.0.1 knitr_1.24
                                          MBESS_4.6.0
                                                           ggExtra_0.8
## [5] rcompanion_2.2.2 MASS_7.3-51.4
                                          magrittr_1.5
                                                           forcats_0.4.0
## [9] stringr_1.4.0
                         dplyr_0.8.3
                                          purrr_0.3.2
                                                           readr_1.3.1
## [13] tidyr_0.8.3.9000 tibble_2.1.3
                                          ggplot2_3.2.0
                                                           tidyverse_1.2.1
##
## loaded via a namespace (and not attached):
## [1] nlme 3.1-141
                           matrixStats 0.54.0 lubridate 1.7.4
## [4] httr_1.4.1
                           tools_3.6.0
                                              backports_1.1.4
## [7] R6_2.4.0
                           nortest_1.0-4
                                              lazyeval_0.2.2
## [10] colorspace_1.4-1
                           withr_2.1.2.9000
                                              tidyselect_0.2.5
## [13] compiler_3.6.0
                           cli_1.1.0
                                              rvest_0.3.4
## [16] expm_0.999-4
                           xml2_1.2.2
                                              sandwich_2.5-1
## [19] labeling_0.3
                           scales_1.0.0
                                              lmtest_0.9-37
## [22] mvtnorm_1.0-11
                           multcompView_0.1-7 digest_0.6.20
## [25] foreign_0.8-72
                           rmarkdown_1.14
                                              pkgconfig_2.0.2
## [28] htmltools_0.3.6
                           manipulate_1.0.1
                                              highr_0.8
## [31] rlang_0.4.0
                           readxl_1.3.1
                                              rstudioapi_0.10
## [34] shiny_1.3.2
                           generics_0.0.2
                                              zoo_1.8-6
## [37] jsonlite_1.6
                           modeltools_0.2-22 Matrix_1.2-17
## [40] Rcpp_1.0.2
                           DescTools_0.99.28
                                              munsell_0.5.0
## [43] stringi_1.4.3
                           multcomp_1.4-10
                                              yaml 2.2.0
## [46] plyr_1.8.4
                           grid 3.6.0
                                              parallel 3.6.0
## [49] promises_1.0.1
                           crayon_1.3.4
                                              miniUI_0.1.1.1
## [52] lattice_0.20-38
                           haven_2.1.1
                                              splines_3.6.0
## [55] hms_0.5.0
                           zeallot_0.1.0
                                              pillar_1.4.2
## [58] EMT_1.1
                           boot_1.3-23
                                              codetools_0.2-16
```

evaluate_0.14

glue_1.3.1

##	[64]	modelr_0.1.5	vctrs_0.2.0	httpuv_1.5.1
##	[67]	cellranger_1.1.0	gtable_0.3.0	assertthat_0.2.1
##	[70]	xfun_0.8	mime_0.7	coin_1.3-0
##	[73]	libcoin_1.0-4	xtable_1.8-4	broom_0.5.2
##	[76]	later 0.8.0	survival 2.44-1.1	TH.data 1.0-10