

Regression to the mean modeling

Mean pain rating of 5.2 at 0.5 correlation

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Generate 2x2 covariance matrix

Generate a covariance matrix using an SD of 1.2, 1.7, and 2.2, and correlation of 0.5.

```
# Correlation matrices
cor <- matrix(c(1, 0.5, 0.5, 1), ncol = 2)
```

```
# SDs
std_1 <- c(1.2, 1.2)
std_2 <- c(1.7, 1.7)
std_3 <- c(2.2, 2.2)
```

```
# Covariance matrices
cov_1 <- cor2cov(cor.mat = cor,
                 sd = std_1)
cov_1
```

```
##      [,1] [,2]
## [1,] 1.44 0.72
## [2,] 0.72 1.44
```

```
cov_2 <- cor2cov(cor.mat = cor,
                 sd = std_2)
cov_2
```

```
##      [,1] [,2]
## [1,] 2.890 1.445
## [2,] 1.445 2.890
```

```
cov_3 <- cor2cov(cor.mat = cor,
                 sd = std_3)
cov_3
```

```
##      [,1] [,2]
## [1,] 4.84 2.42
## [2,] 2.42 4.84
```

Mean = 5.2, SD = 1.2, r = 0.5

Generate and summarise data

Base data

```
# Set the random seed for reproducibility
set.seed(2019)

# Generate the data
five_1.base <- as.data.frame(mvrnorm(n = 1000, mu = c(5.2, 5.2), Sigma = cov_1))

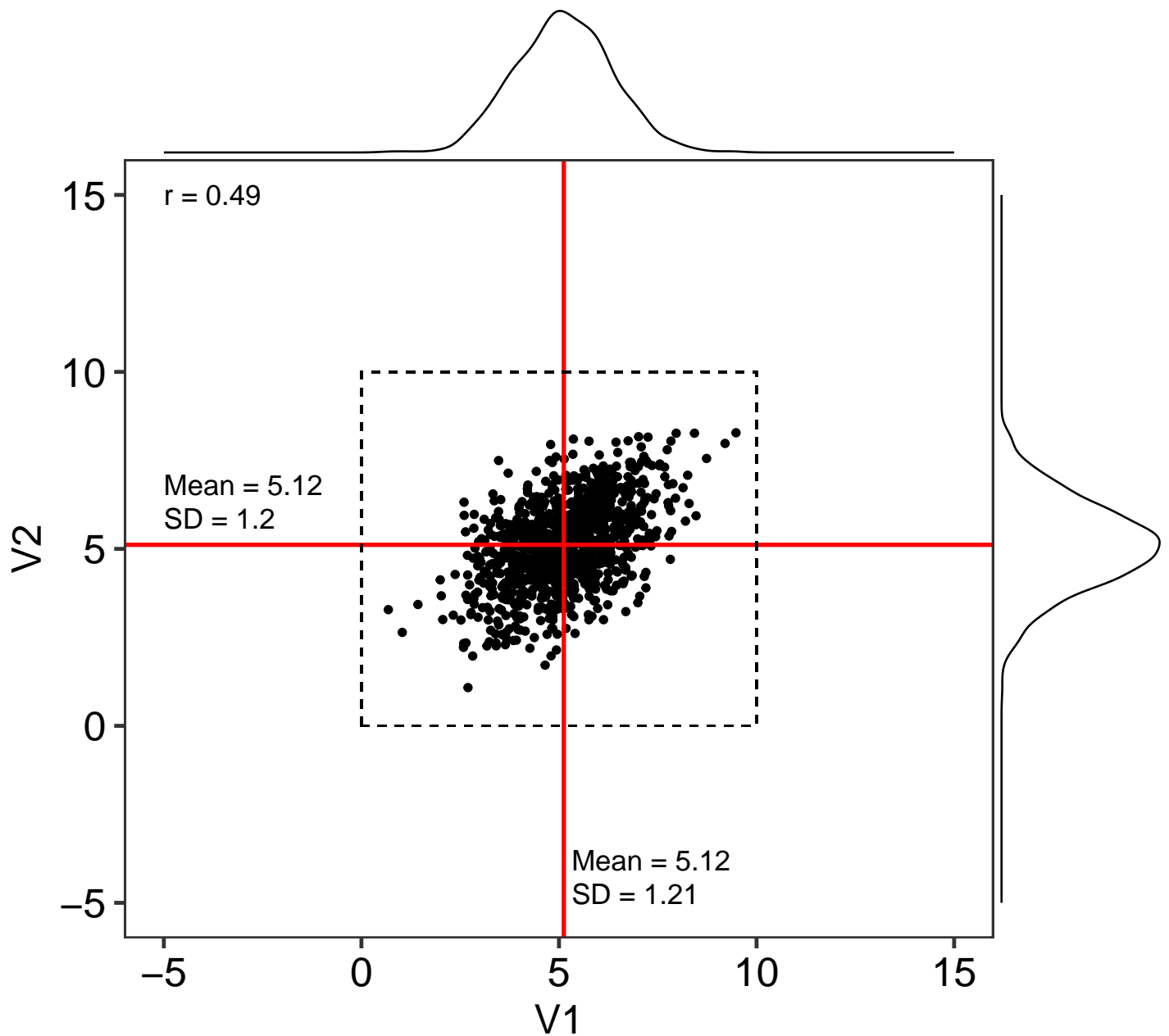
# Plot base data
ggMarginal(ggplot(data = five_1.base) +
  aes(x = V1, y = V2) +
  geom_point() +
  geom_hline(yintercept = mean(five_1.base$V2),
             colour = 'red', size = 1) +
  geom_vline(xintercept = mean(five_1.base$V1),
             colour = 'red', size = 1) +
```

```

geom_rect(ymin = 0, ymax = 10,
          xmin = 0, xmax = 10,
          colour = '#000000',
          alpha = 0,
          linetype = 2) +
annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5,
         label = str_glue("r = {round(cor(five_1.base$V1,
         five_1.base$V2), 2)}")) +
annotate(geom = 'text', x = -5, y = mean(five_1.base$V2) + 1.7,
         hjust = 0, size = 5,
         label = str_glue("Mean = {round(mean(five_1.base$V2), 2)}")) +
annotate(geom = 'text', x = -5, y = mean(five_1.base$V2) + 0.75,
         hjust = 0, size = 5,
         label = str_glue("SD = {round(sd(five_1.base$V2), 2)}")) +
annotate(geom = 'text', x = mean(five_1.base$V1) + 0.2, y = -3.8,
         hjust = 0, size = 5,
         label = str_glue("Mean = {round(mean(five_1.base$V1), 2)}")) +
annotate(geom = 'text', x = mean(five_1.base$V1) + 0.2, y = -4.75,
         hjust = 0, size = 5,
         label = str_glue("SD = {round(sd(five_1.base$V1), 2)}")) +
labs(title = 'A: Unconstained',
     caption = 'Parameters: Mean = 5.2, SD = 1.2, r = 0.5') +
scale_y_continuous(limits = c(-5, 15)) +
scale_x_continuous(limits = c(-5, 15)) +
theme(plot.caption = element_text(size = 14))

```

A: Unconstrained



Parameters: Mean = 5.2, SD = 1.2, $r = 0.5$

Constrain values to 0-10 range

```
# Process data
five_1 <- five_1.base %>%
  mutate(V1 = case_when(
    V1 < 1 ~ 1,
    V1 > 10 ~ 10,
    TRUE ~ V1)) %>%
  mutate(V2 = case_when(
    V2 < 0 ~ 0,
    V2 > 10 ~ 10,
    TRUE ~ V2)) %>%
```

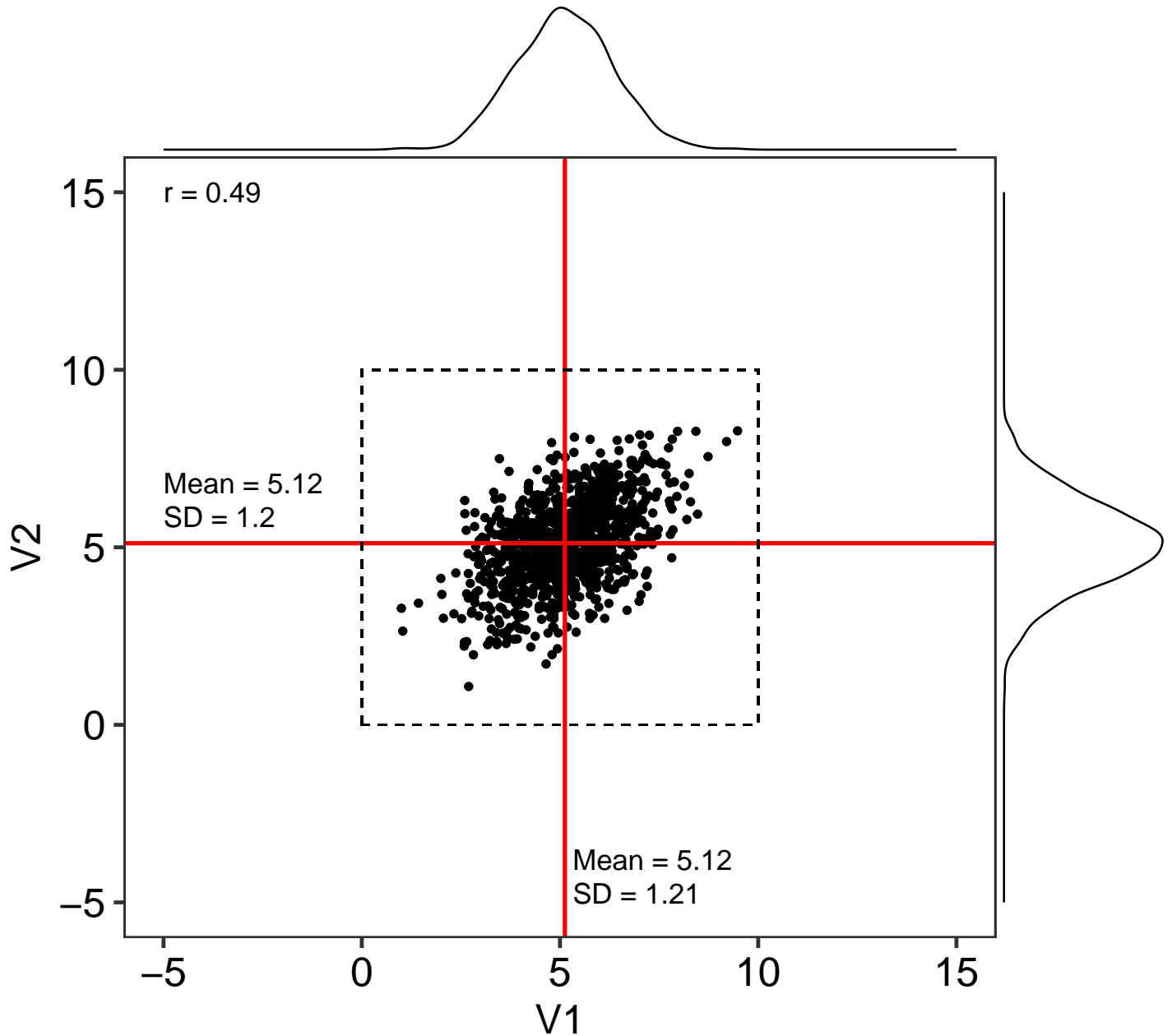
```

mutate(group = 'No threshold')

# Plot processed data
ggMarginal(ggplot(data = five_1) +
  aes(x = V1, y = V2) +
  geom_point() +
  geom_hline(yintercept = mean(five_1$V2),
    colour = 'red', size = 1) +
  geom_vline(xintercept = mean(five_1$V1),
    colour = 'red', size = 1) +
  geom_rect(ymin = 0, ymax = 10,
    xmin = 0, xmax = 10,
    colour = '#000000',
    alpha = 0,
    linetype = 2) +
  annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5,
    label = str_glue("r = {round(cor(five_1$V1, five_1$V2), 2)}")) +
  annotate(geom = 'text', x = -5, y = mean(five_1$V2) + 1.7,
    hjust = 0, size = 5,
    label = str_glue("Mean = {round(mean(five_1$V2), 2)}")) +
  annotate(geom = 'text', x = -5, y = mean(five_1$V2) + 0.75,
    hjust = 0, size = 5,
    label = str_glue("SD = {round(sd(five_1$V2), 2)}")) +
  annotate(geom = 'text', x = mean(five_1$V1) + 0.2, y = -3.8,
    hjust = 0, size = 5,
    label = str_glue("Mean = {round(mean(five_1$V1), 2)}")) +
  annotate(geom = 'text', x = mean(five_1$V1) + 0.2, y = -4.75,
    hjust = 0, size = 5,
    label = str_glue("SD = {round(sd(five_1$V1), 2)}")) +
  labs(title = 'B: Constrained (0-10 range)',
    caption = 'Parameters: Mean = 5.2, SD = 1.2, r = 0.5') +
  scale_y_continuous(limits = c(-5, 15)) +
  scale_x_continuous(limits = c(-5, 15)) +
  theme(plot.caption = element_text(size = 14)))

```

B: Constrained (0–10 range)



Parameters: Mean = 5.2, SD = 1.2, $r = 0.5$

Model mean of V1 with increasing V1 thresholds from 0 to 5

```
# Extract visit 1 data
five_1V1 <- five_1$V1

# Generate a vector of threshold values to iterate over
cutoff <- 0:5

# Generate a vector of V1 means at each V1 threshold
five_1V1.shift <- sapply(cutoff, function(x){mean(five_1V1[five_1V1 > x])})

# Calculate deviation
```

```

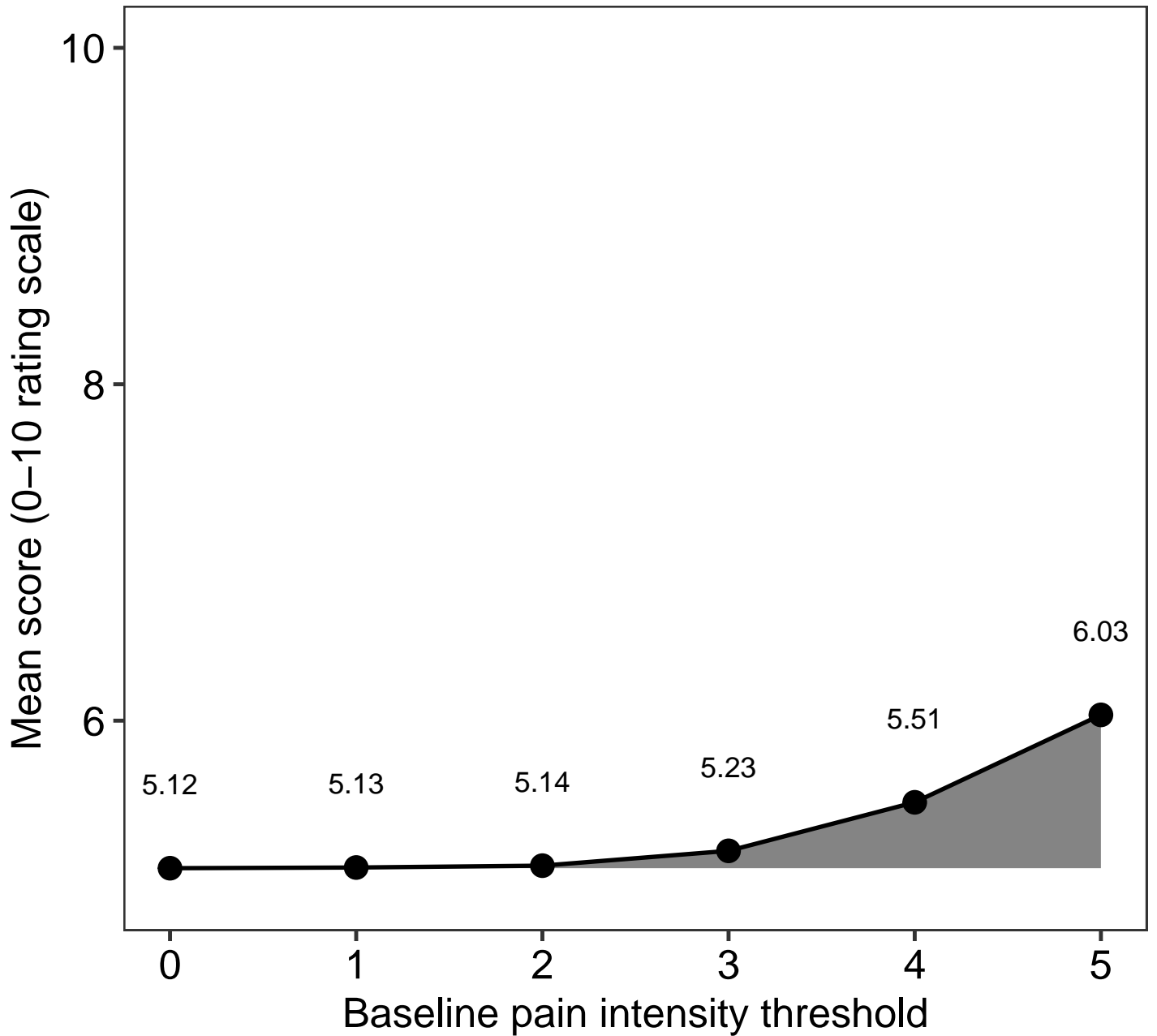
(five_1V1.df <- data.frame(time = 'V1',
                           cutoff = cutoff,
                           cutoff2 = cutoff - 0.15,
                           mean = five_1V1.shift) %>%
  mutate(deviation = mean - mean(five_1V1),
         time = as.character(time)))

##   time cutoff cutoff2    mean  deviation
## 1   V1      0   -0.15 5.122791 0.000000000
## 2   V1      1    0.85 5.126918 0.004126918
## 3   V1      2    1.85 5.137883 0.015091815
## 4   V1      3    2.85 5.225994 0.103203603
## 5   V1      4    3.85 5.514581 0.391790095
## 6   V1      5    4.85 6.034325 0.911534105

# Plot data
ggplot(data = five_1V1.df) +
  aes(x = cutoff, y = mean, ymin = mean(five_1V1), ymax = mean) +
  geom_ribbon(alpha = 0.6) +
  geom_point(size = 5) +
  geom_line(size = 1) +
  geom_text(aes(label = round(mean, 2)),
            nudge_y = 0.5, size = 5) +
  scale_y_continuous(limits = c(5, 10),
                     breaks = c(0, 2, 4, 6, 8, 10)) +
  labs(title = 'A: Shift in V1 mean with increasing V1 threshold value',
       caption = 'Parameters: Mean = 5.2, SD = 1.2, r = 0.5',
       x = 'Baseline pain intensity threshold',
       y = 'Mean score (0-10 rating scale)') +
  theme(plot.caption = element_text(size = 14))

```

A: Shift in V1 mean with increasing V1 threshold value



Parameters: Mean = 5.2, SD = 1.2, $r = 0.5$

Model mean of V2 with increasing V1 thresholds from 0 to 5

```
# Extract visit 2 data
five_1V2 <- five_1$V2

# Generate a vector of threshold values to iterate over
cutoff <- 0:5

# Generate a vector of V2 means at each V1 threshold
five_1V2.shift <- map_dbl(.x = cutoff,
  ~ five_1 %>%
    filter(V1 > .x) %>%
```



```

        .$V2 %>%
        mean(.))

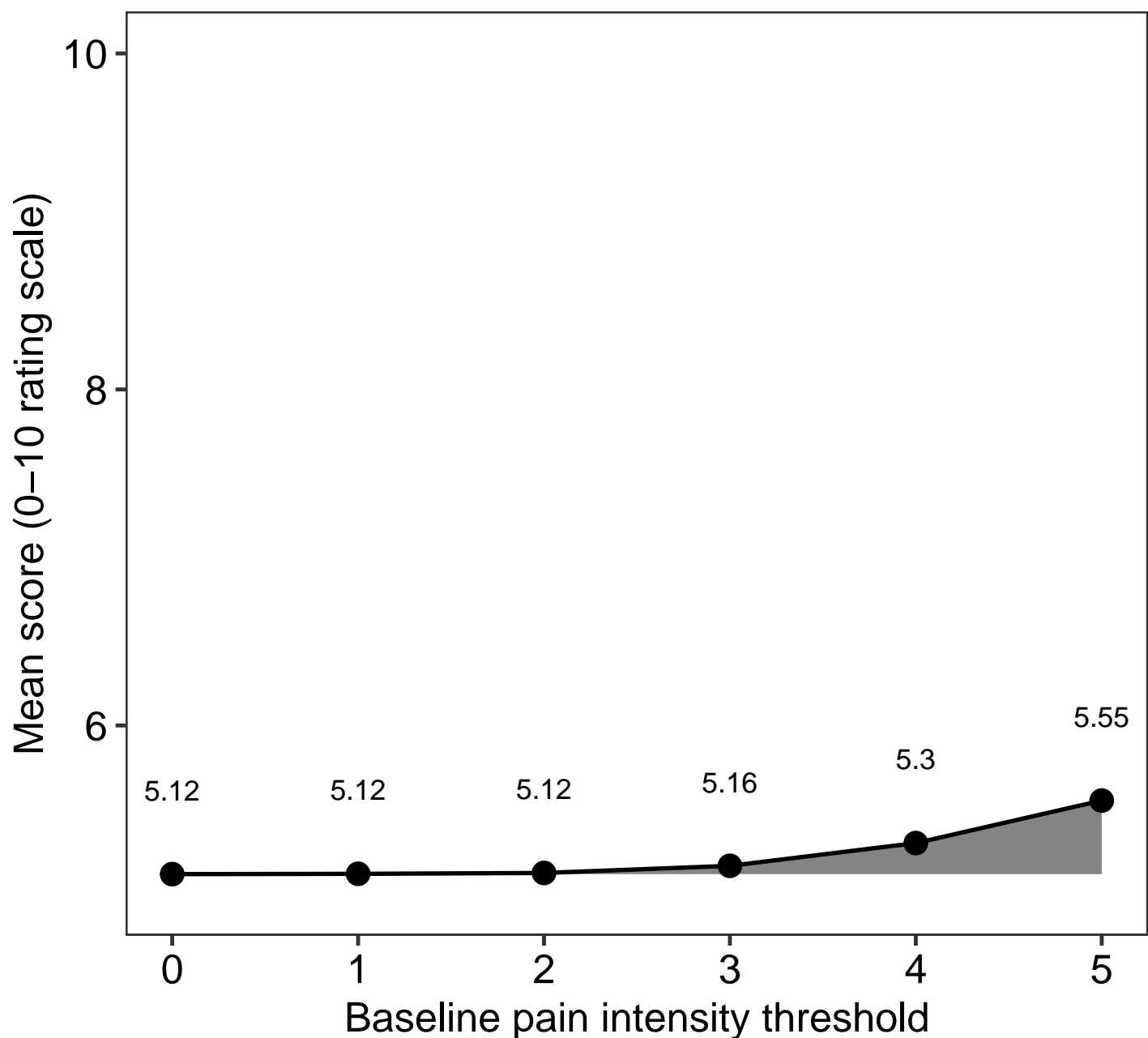
# Calculate deviation
(five_1V2.df <- data.frame(time = 'V2',
                           cutoff = cutoff,
                           cutoff2 = cutoff + 0.15,
                           mean = five_1V2.shift) %>%
  mutate(deviation = mean - mean(five_1V1),
         time = as.character(time)))

##   time cutoff cutoff2    mean    deviation
## 1   V2      0    0.15 5.115030 -0.0077613213
## 2   V2      1    1.15 5.116863 -0.0059274982
## 3   V2      2    2.15 5.122042 -0.0007484872
## 4   V2      3    3.15 5.164573  0.0417824284
## 5   V2      4    4.15 5.300008  0.1772171572
## 6   V2      5    5.15 5.553082  0.4302911319

# Plot data
ggplot(data = five_1V2.df) +
  aes(x = cutoff, y = mean, ymin = mean(five_1V2), ymax = mean) +
  geom_ribbon(alpha = 0.6) +
  geom_point(size = 5) +
  geom_line(size = 1) +
  geom_text(aes(label = round(mean, 2)),
            nudge_y = 0.5, size = 5) +
  scale_y_continuous(limits = c(5, 10),
                     breaks = c(0, 2, 4, 6, 8, 10)) +
  labs(title = 'B: Shift in V2 mean with increasing V1 threshold value',
       caption = 'Parameters: Mean = 5.2, SD = 1.2, r = 0.5',
       x = 'Baseline pain intensity threshold',
       y = 'Mean score (0-10 rating scale)') +
  theme(plot.caption = element_text(size = 14))

```

B: Shift in V2 mean with increasing V1 threshold value



Parameters: Mean = 5.2, SD = 1.2, $r = 0.5$

Placebo response

threshold: 0

```
# Process data
placebo_1.0 <- five_1 %>%
  filter(V1 >= 0) %>%
  mutate(difference = V1 - V2) %>%
  mutate(group = 'Threshold')

# Calculate the mean (95%CI) difference between V1 and V2
diff_1.0 <- groupwiseMean(difference ~ 1,
```

```

data = placebo_1.0,
R = 2000,
traditional = FALSE,
bca = TRUE)

diff_1.0$.id <- 0

kable(diff_1.0)

```

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
0	1000	0.00776	0.95	-0.0706	0.0823

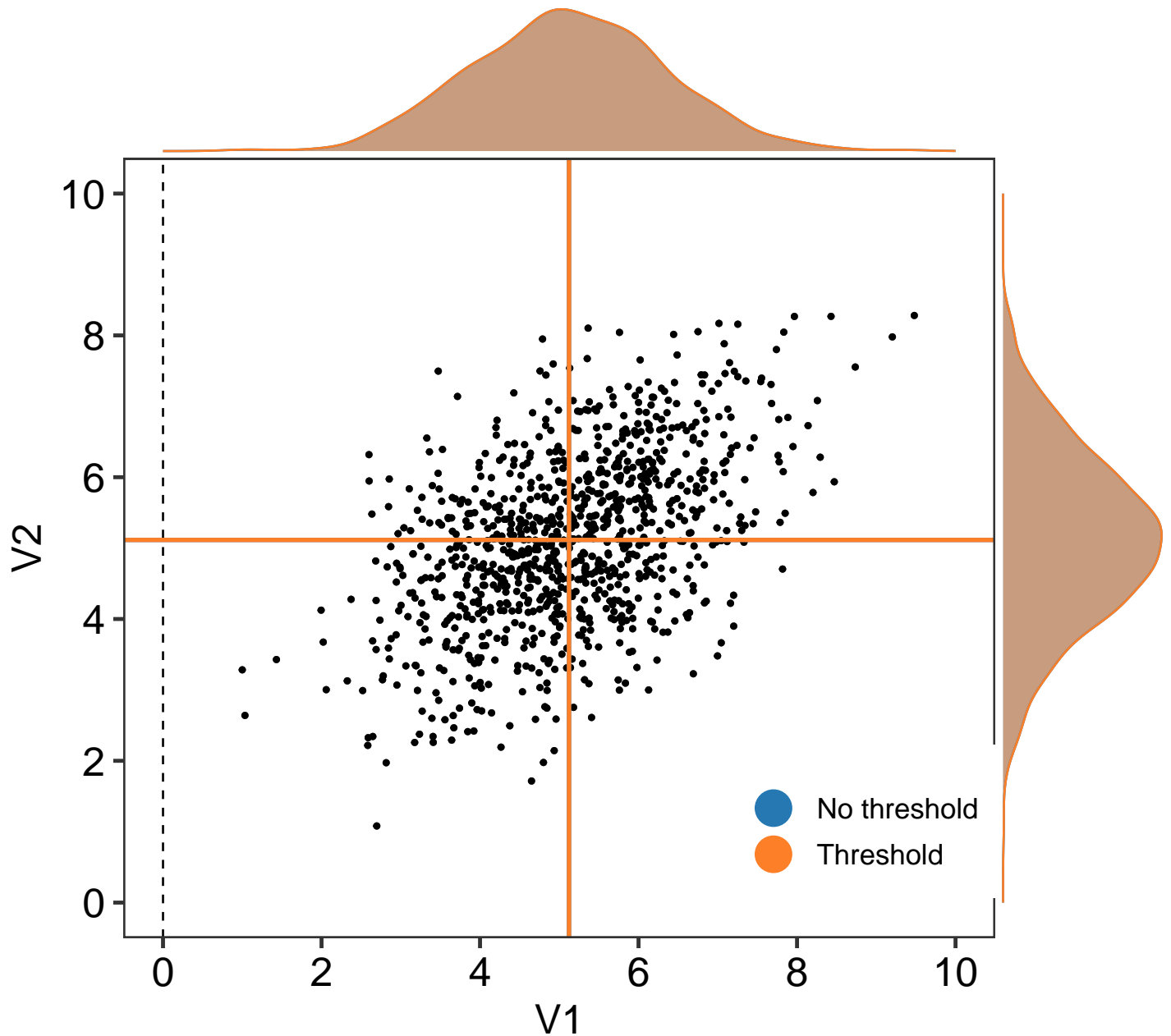
```

# Plot the data
ggMarginal(placebo_1.0[, 1:3] %>%
  bind_rows(five_1) %>%
  mutate(group = factor(group,
    levels = c('No threshold', 'Threshold'),
    ordered = TRUE)) %>%

  ggplot(data = .) +
  aes(x = V1, y = V2) +
  geom_point(aes(colour = group, fill = group),
    size = 1) +
  guides(colour = guide_legend(override.aes = list(size = 8))) +
  geom_point(data = five_1,
    colour = '#999999',
    size = 1) +
  geom_point(data = placebo_1.0,
    size = 1,
    colour = '#000000') +
  geom_vline(xintercept = mean(five_1$V1),
    colour = pal[1], size = 1) +
  geom_vline(xintercept = mean(placebo_1.0$V1),
    colour = pal[2], size = 1) +
  geom_vline(xintercept = 0, linetype = 2) +
  geom_hline(yintercept = mean(five_1$V2),
    colour = pal[1], size = 1) +
  geom_hline(yintercept = mean(placebo_1.0$V2),
    colour = pal[2], size = 1) +
  scale_y_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_x_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_fill_manual(values = pal) +
  scale_colour_manual(values = pal) +
  labs(title = 'A: Baseline pain threshold = 0',
    caption = 'Parameters: Mean = 5.2, SD = 1.2, r = 0.5') +
  theme(legend.title = element_blank(),
    legend.position = c(0.85, 0.15),
    plot.caption = element_text(size = 14)),
  groupColour = TRUE,
  groupFill = TRUE)

```

A: Baseline pain threshold = 0



Parameters: Mean = 5.2, SD = 1.2, $r = 0.5$

threshold: 3

```
# Process data
placebo_1.3 <- five_1 %>%
  filter(V1 >= 3) %>%
  mutate(difference = V1 - V2) %>%
  mutate(group = 'Threshold')

# Calculate the mean (95%CI) difference between V1 and V2
diff_1.3 <- groupwiseMean(difference ~ 1,
  data = placebo_1.3,
  R = 2000,
```

```

      traditional = FALSE,
      bca = TRUE)

diff_1.3$.id <- 3

kable(diff_1.3)

```

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
3	961	0.0614	0.95	-0.0141	0.134

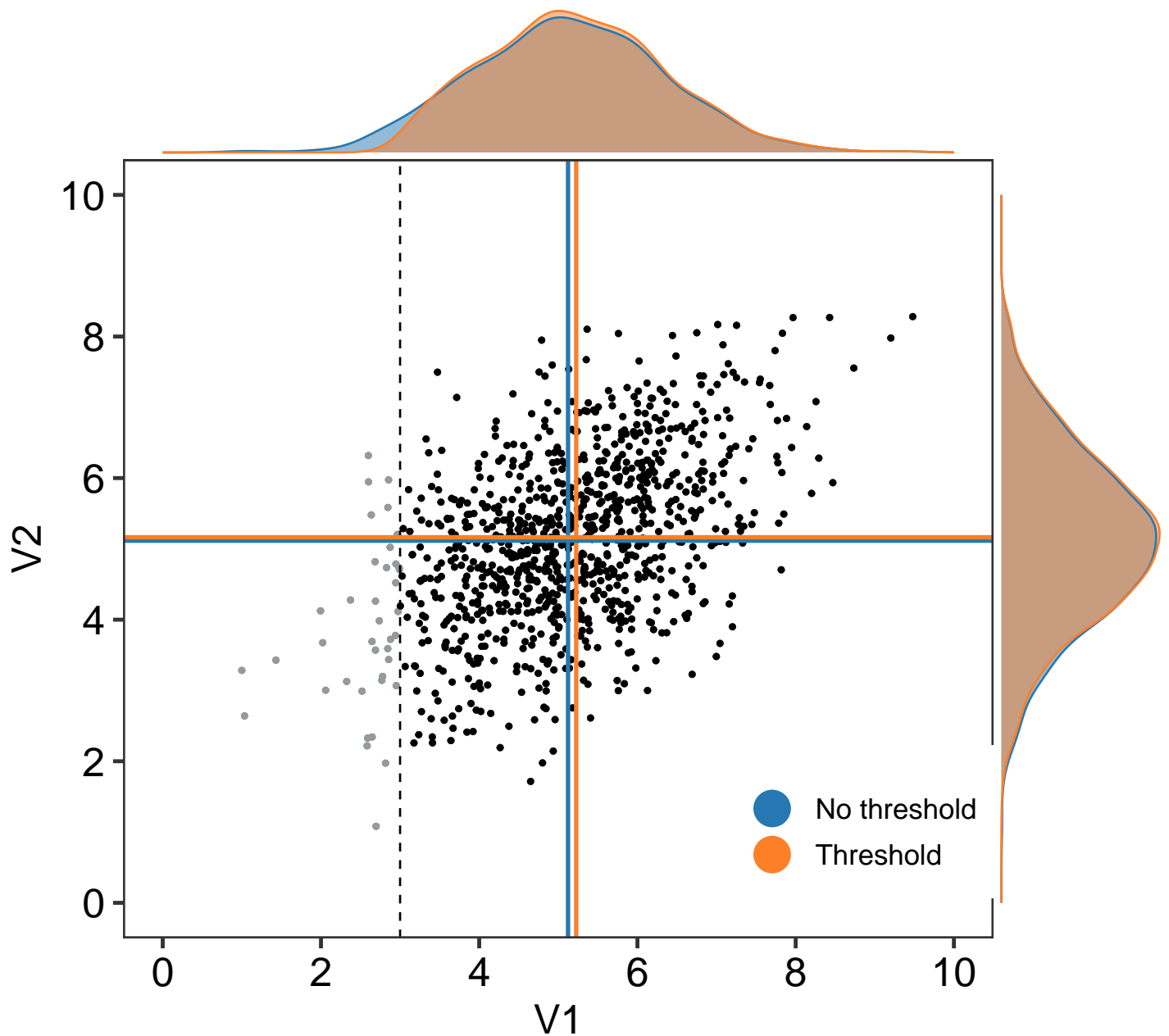
```

# Plot the data
ggMarginal(placebo_1.3[, 1:3] %>%
  bind_rows(five_1) %>%
  mutate(group = factor(group,
    levels = c('No threshold', 'Threshold'),
    ordered = TRUE)) %>%

  ggplot(data = .) +
  aes(x = V1, y = V2) +
  geom_point(aes(colour = group, fill = group),
    size = 1) +
  guides(colour = guide_legend(override.aes = list(size = 8))) +
  geom_point(data = five_1,
    colour = '#999999',
    size = 1) +
  geom_point(data = placebo_1.3,
    size = 1,
    colour = '#000000') +
  geom_vline(xintercept = mean(five_1$V1),
    colour = pal[1], size = 1) +
  geom_vline(xintercept = mean(placebo_1.3$V1),
    colour = pal[2], size = 1) +
  geom_vline(xintercept = 3, linetype = 2) +
  geom_hline(yintercept = mean(five_1$V2),
    colour = pal[1], size = 1) +
  geom_hline(yintercept = mean(placebo_1.3$V2),
    colour = pal[2], size = 1) +
  scale_y_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_x_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_fill_manual(values = pal) +
  scale_colour_manual(values = pal) +
  labs(title = 'B: Baseline pain threshold = 3',
    caption = 'Parameters: Mean = 5.2, SD = 1.2, r = 0.5') +
  theme(legend.title = element_blank(),
    legend.position = c(0.85, 0.15),
    plot.caption = element_text(size = 14)),
  groupColour = TRUE,
  groupFill = TRUE)

```

B: Baseline pain threshold = 3



Parameters: Mean = 5.2, SD = 1.2, $r = 0.5$

threshold: 4

```
# Process that data
placebo_1.4 <- five_1 %>%
  filter(V1 >= 4) %>%
  mutate(difference = V1 - V2) %>%
  mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
```

```
diff_1.4 <- groupwiseMean(difference ~ 1,
  data = placebo_1.4,
  R = 2000,
  traditional = FALSE,
  bca = TRUE)

diff_1.4$.id <- 4

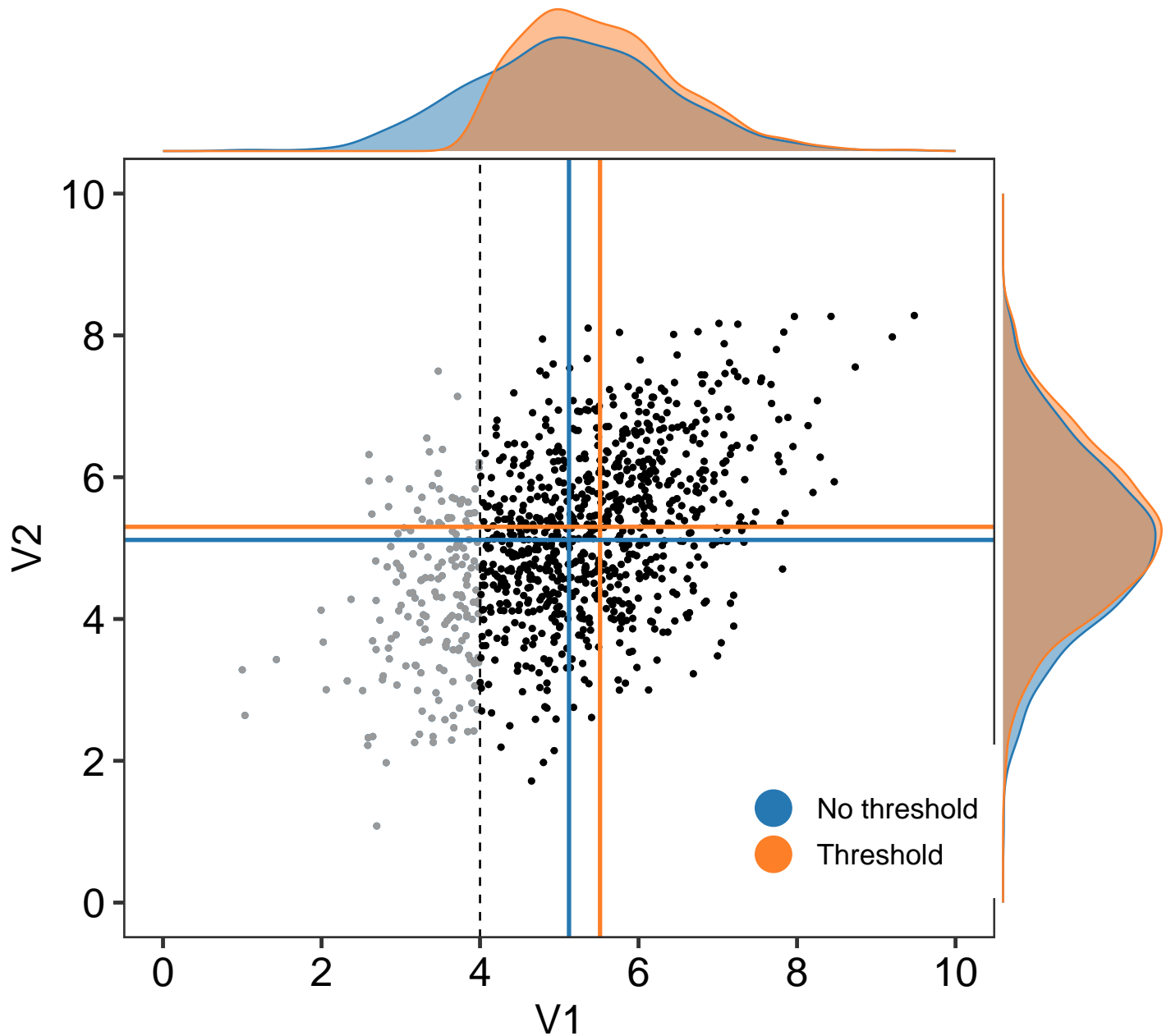
kable(diff_1.4)
```

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
4	817	0.215	0.95	0.136	0.292

```
# Plot the data
ggMarginal(placebo_1.4[, 1:3] %>%
  bind_rows(five_1) %>%
  mutate(group = factor(group,
    levels = c('No threshold', 'Threshold'),
    ordered = TRUE)) %>%

  ggplot(data = .) +
  aes(x = V1, y = V2) +
  geom_point(aes(colour = group, fill = group),
    size = 1) +
  guides(colour = guide_legend(override.aes = list(size = 8))) +
  geom_point(data = five_1,
    colour = '#999999',
    size = 1) +
  geom_point(data = placebo_1.4,
    size = 1,
    colour = '#000000') +
  geom_vline(xintercept = mean(five_1$V1),
    colour = pal[1], size = 1) +
  geom_vline(xintercept = mean(placebo_1.4$V1),
    colour = pal[2], size = 1) +
  geom_vline(xintercept = 4, linetype = 2) +
  geom_hline(yintercept = mean(five_1$V2),
    colour = pal[1], size = 1) +
  geom_hline(yintercept = mean(placebo_1.4$V2),
    colour = pal[2], size = 1) +
  scale_y_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_x_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_fill_manual(values = pal) +
  scale_colour_manual(values = pal) +
  labs(title = 'C: Baseline pain threshold = 4',
    caption = 'Parameters: Mean = 5.2, SD = 1.2, r = 0.5') +
  theme(legend.title = element_blank(),
    legend.position = c(0.85, 0.15),
    plot.caption = element_text(size = 14)),
  groupColour = TRUE,
  groupFill = TRUE)
```

C: Baseline pain threshold = 4



Parameters: Mean = 5.2, SD = 1.2, $r = 0.5$

threshold: 5

```
# Process that data
placebo_1.5 <- five_1 %>%
  filter(V1 >= 5) %>%
  mutate(difference = V1 - V2) %>%
  mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
```



```
diff_1.5 <- groupwiseMean(difference ~ 1,
  data = placebo_1.5,
  R = 2000,
  traditional = FALSE,
  bca = TRUE)

diff_1.5$.id <- 5

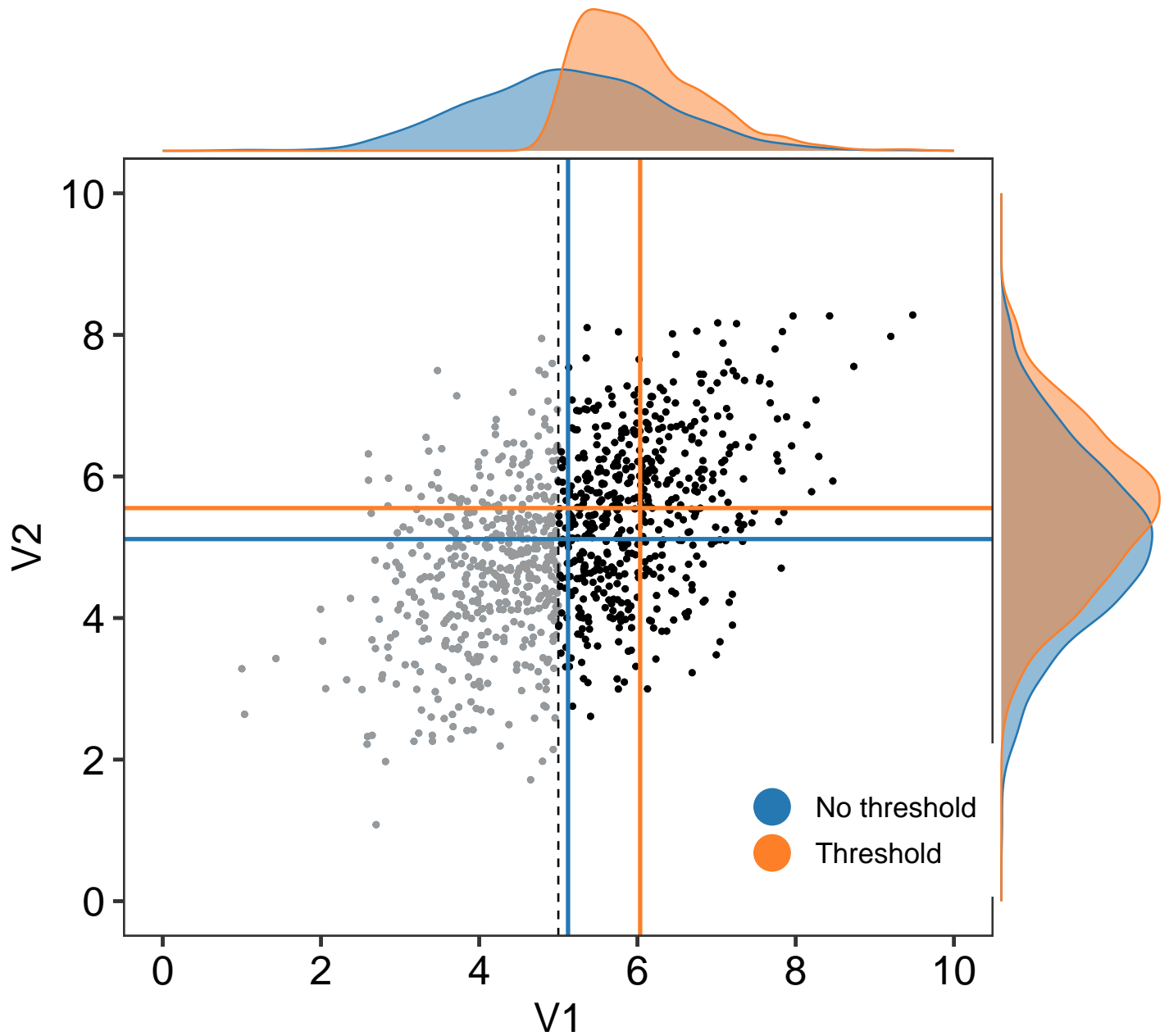
kable(diff_1.5)
```

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
5	528	0.481	0.95	0.385	0.574

```
# Plot the data
ggMarginal(placebo_1.5[, 1:3] %>%
  bind_rows(five_1) %>%
  mutate(group = factor(group,
    levels = c('No threshold', 'Threshold'),
    ordered = TRUE)) %>%

  ggplot(data = .) +
  aes(x = V1, y = V2) +
  geom_point(aes(colour = group, fill = group),
    size = 1) +
  guides(colour = guide_legend(override.aes = list(size = 8))) +
  geom_point(data = five_1,
    colour = '#999999',
    size = 1) +
  geom_point(data = placebo_1.5,
    size = 1,
    colour = '#000000') +
  geom_vline(xintercept = mean(five_1$V1),
    colour = pal[1], size = 1) +
  geom_vline(xintercept = mean(placebo_1.5$V1),
    colour = pal[2], size = 1) +
  geom_vline(xintercept = 5, linetype = 2) +
  geom_hline(yintercept = mean(five_1$V2),
    colour = pal[1], size = 1) +
  geom_hline(yintercept = mean(placebo_1.5$V2),
    colour = pal[2], size = 1) +
  scale_y_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_x_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_fill_manual(values = pal) +
  scale_colour_manual(values = pal) +
  labs(title = 'D: Baseline pain threshold = 5',
    caption = 'Parameters: Mean = 5.2, SD = 1.2, r = 0.5') +
  theme(legend.title = element_blank(),
    legend.position = c(0.85, 0.15),
    plot.caption = element_text(size = 14)),
  groupColour = TRUE,
  groupFill = TRUE)
```

D: Baseline pain threshold = 5



Parameters: Mean = 5.2, SD = 1.2, $r = 0.5$

Publication plots

```
# Plot 1
shift_1 <- five_1V1.df %>%
  bind_rows(five_1V2.df) %>%
  ggplot(data = .) +
  aes(y = mean,
      x = cutoff2,
      fill= time) +
  geom_hline(yintercept = 5.2,
             linetype = 2) +
  geom_point(shape = 21,
```

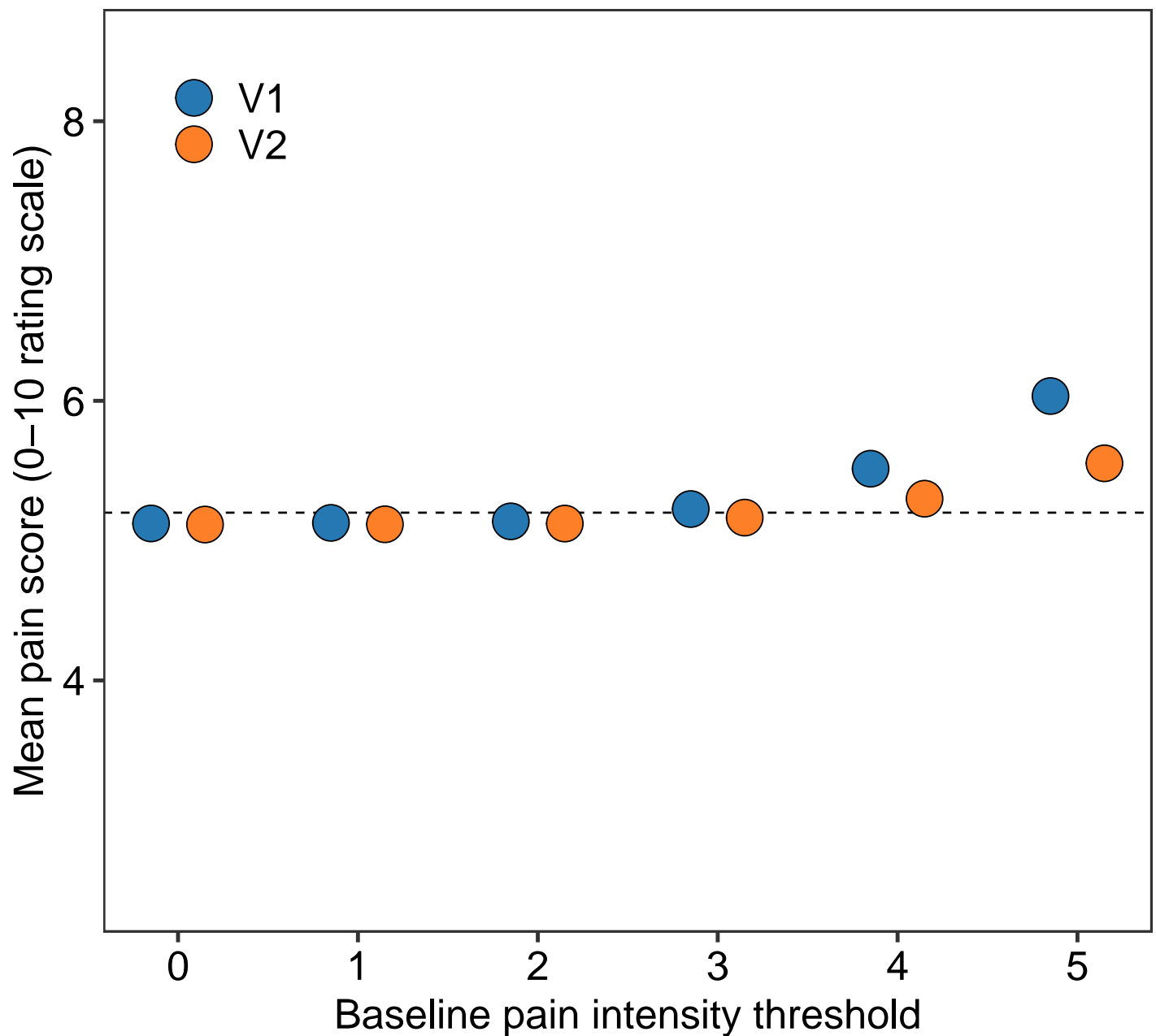
```

size = 8) +
labs(title = 'A',
      subtitle = 'Parameters: Mean = 5.2, SD = 1.2, r = 0.5',
      x = 'Baseline pain intensity threshold',
      y = 'Mean pain score (0-10 rating scale)') +
scale_x_continuous(breaks = 0:5) +
scale_y_continuous(limits = c(2.5, 8.5)) +
scale_fill_manual(values = pal) +
theme(legend.title = element_blank(),
      legend.position = c(0.12, 0.89),
      legend.text = element_text(size = 20)); shift_1

```

A

Parameters: Mean = 5.2, SD = 1.2, r = 0.5



```

# Plot 2
# Bind diff_*. dataframes

```

```

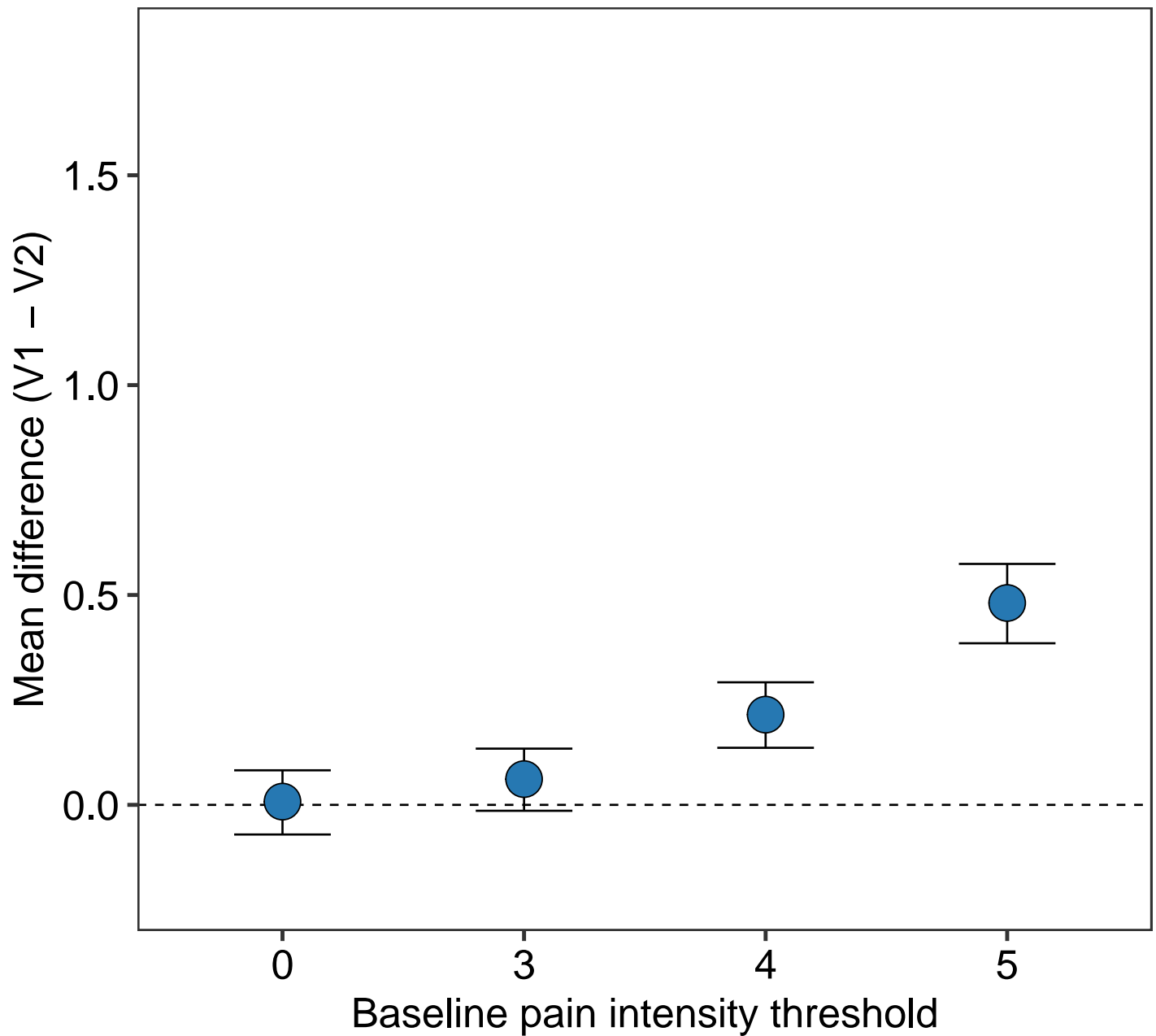
diff_all_1 <- diff_1.0 %>%
  bind_rows(diff_1.3, diff_1.4, diff_1.5)

pp_1 <- diff_all_1 %>%
  mutate(Threshold = factor(.id)) %>%
  ggplot(data = .) +
  aes(x = Threshold,
      y = Mean,
      ymin = Bca.lower,
      ymax = Bca.upper) +
  geom_hline(yintercept = 0,
             linetype = 2) +
  geom_errorbar(width = 0.4) +
  geom_point(shape = 21,
             fill = pal[[1]],
             size = 8) +
  labs(title = 'A',
       subtitle = 'Parameters: Mean = 5.2, SD = 1.2, r = 0.5',
       x = 'Baseline pain intensity threshold',
       y = 'Mean difference (V1 - V2)') +
  scale_y_continuous(limits = c(-0.2, 1.8)); pp_1

```

A

Parameters: Mean = 5.2, SD = 1.2, $r = 0.5$



Mean = 5.2, SD = 1.7, $r = 0.5$

Generate and summarise data

Base data

```
# Set the random seed for reproducibility
set.seed(2019)

# Generate the data
```

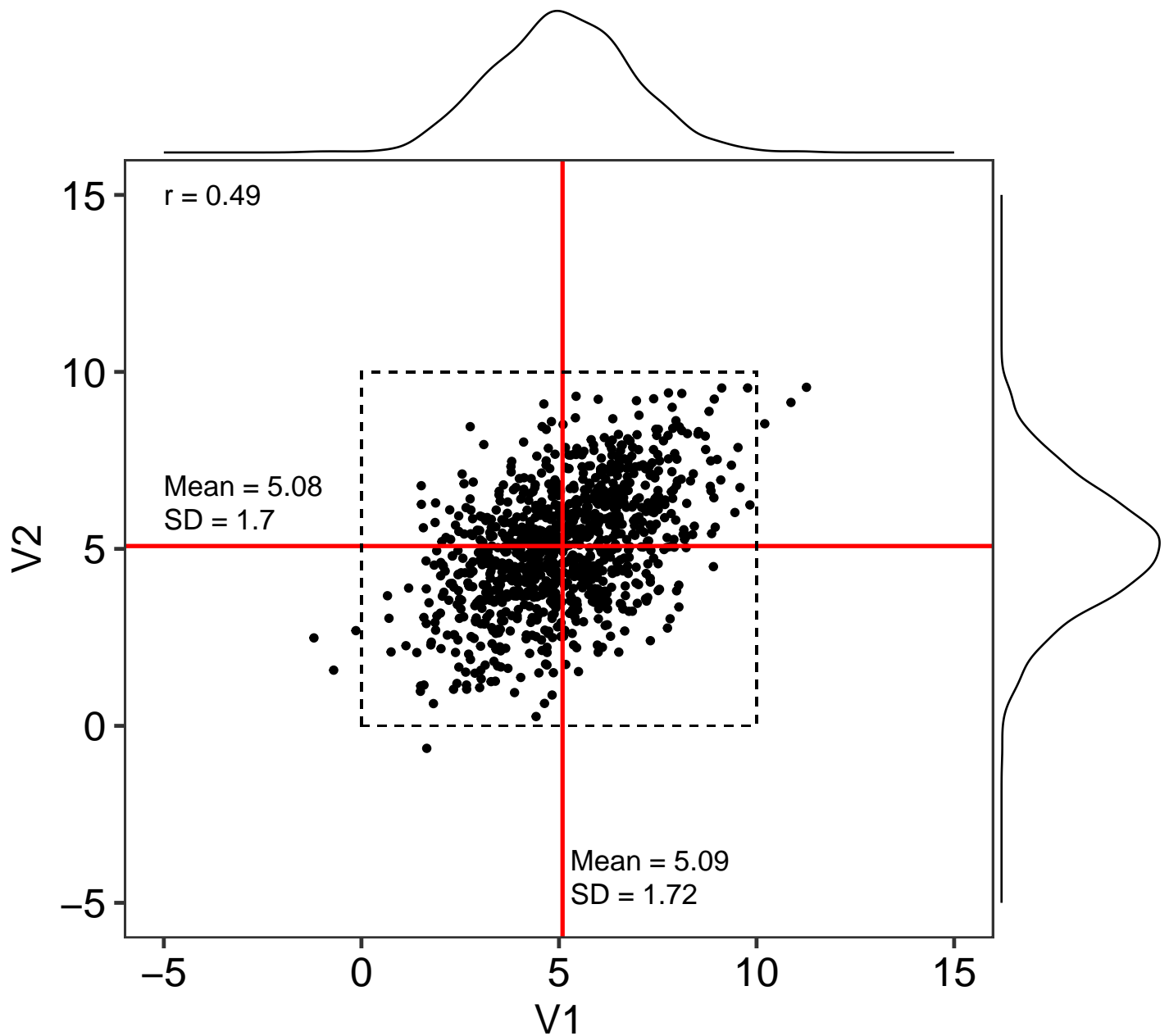
```

five_2.base <- as.data.frame(mvrnorm(n = 1000, mu = c(5.2, 5.2), Sigma = cov_2))

# Plot base data
ggMarginal(ggplot(data = five_2.base) +
  aes(x = V1, y = V2) +
  geom_point() +
  geom_hline(yintercept = mean(five_2.base$V2),
    colour = 'red', size = 1) +
  geom_vline(xintercept = mean(five_2.base$V1),
    colour = 'red', size = 1) +
  geom_rect(ymin = 0, ymax = 10,
    xmin = 0, xmax = 10,
    colour = '#000000',
    alpha = 0,
    linetype = 2) +
  annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5,
    label = str_glue("r = {round(cor(five_2.base$V1,
      five_2.base$V2), 2)}")) +
  annotate(geom = 'text', x = -5, y = mean(five_2.base$V2) + 1.7,
    hjust = 0, size = 5,
    label = str_glue("Mean = {round(mean(five_2.base$V2), 2)}")) +
  annotate(geom = 'text', x = -5, y = mean(five_2.base$V2) + 0.75,
    hjust = 0, size = 5,
    label = str_glue("SD = {round(sd(five_2.base$V2), 2)}")) +
  annotate(geom = 'text', x = mean(five_2.base$V1) + 0.2, y = -3.8,
    hjust = 0, size = 5,
    label = str_glue("Mean = {round(mean(five_2.base$V1), 2)}")) +
  annotate(geom = 'text', x = mean(five_2.base$V1) + 0.2, y = -4.75,
    hjust = 0, size = 5,
    label = str_glue("SD = {round(sd(five_2.base$V1), 2)}")) +
  labs(title = 'A: Unconstrained',
    caption = 'Parameters: Mean = 5.2, SD = 1.7, r = 0.5') +
  scale_y_continuous(limits = c(-5, 15)) +
  scale_x_continuous(limits = c(-5, 15)) +
  theme(plot.caption = element_text(size = 14)))

```

A: Unconstrained



Parameters: Mean = 5.2, SD = 1.7, $r = 0.5$

Constrain values to 0-10 range

```
# Process data
five_2 <- five_2.base %>%
  mutate(V1 = case_when(
    V1 < 1 ~ 1,
    V1 > 10 ~ 10,
    TRUE ~ V1)) %>%
  mutate(V2 = case_when(
    V2 < 0 ~ 0,
    V2 > 10 ~ 10,
    TRUE ~ V2)) %>%
```

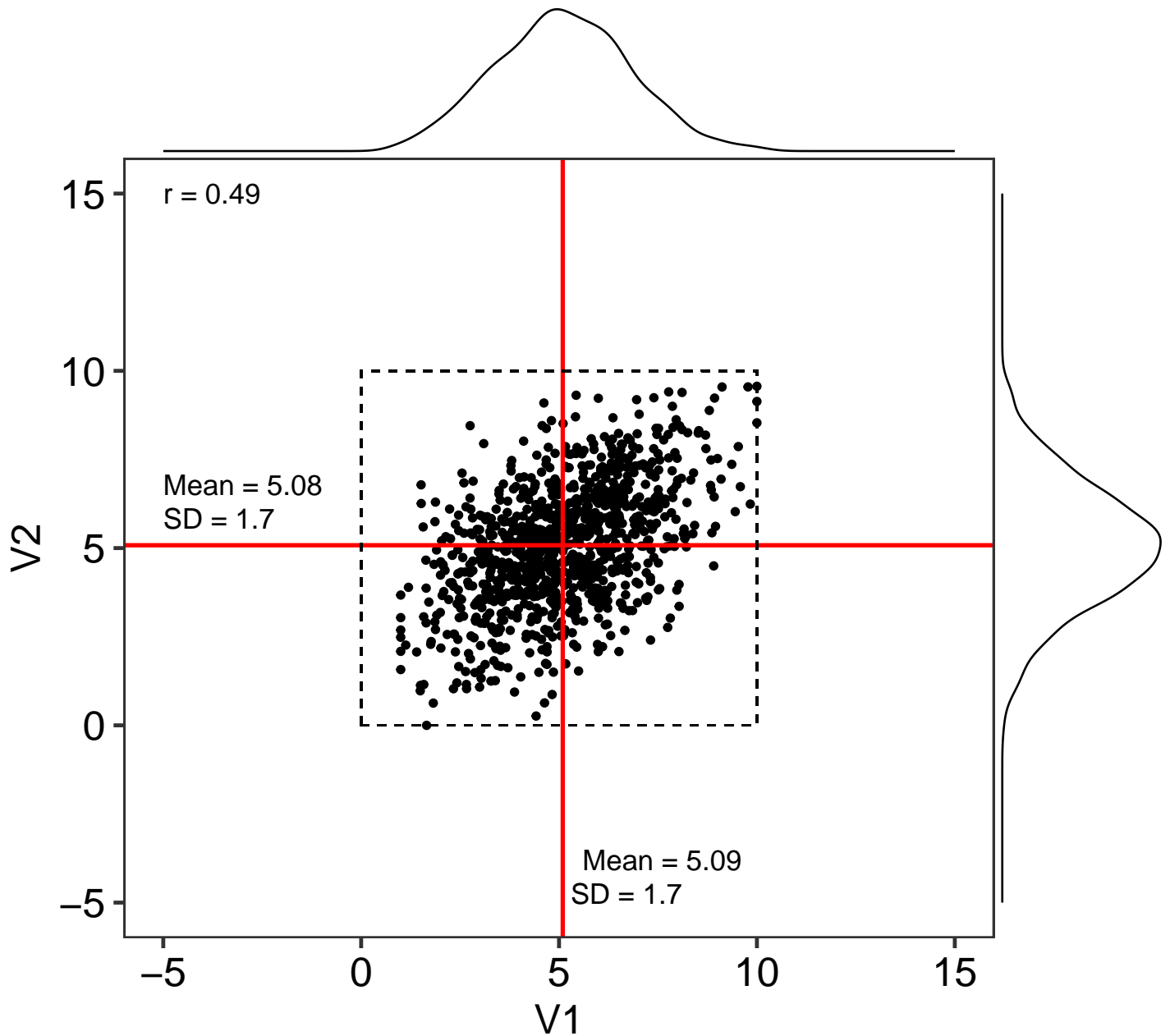
```

mutate(group = 'No threshold')

# Plot processed data
ggMarginal(ggplot(data = five_2) +
  aes(x = V1, y = V2) +
  geom_point() +
  geom_hline(yintercept = mean(five_2$V2),
    colour = 'red', size = 1) +
  geom_vline(xintercept = mean(five_2$V1),
    colour = 'red', size = 1) +
  geom_rect(ymin = 0, ymax = 10,
    xmin = 0, xmax = 10,
    colour = '#000000',
    alpha = 0,
    linetype = 2) +
  annotate(geom = 'text', x = -5, y = 15, hjust = 0, size = 5,
    label = str_glue("r = {round(cor(five_2$V1,
      five_2$V2), 2)}")) +
  annotate(geom = 'text', x = -5, y = mean(five_2$V2) + 1.7,
    hjust = 0, size = 5,
    label = str_glue("Mean = {round(mean(five_2$V2), 2)}")) +
  annotate(geom = 'text', x = -5, y = mean(five_2$V2) + 0.75,
    hjust = 0, size = 5,
    label = str_glue("SD = {round(sd(five_2$V2), 2)}")) +
  annotate(geom = 'text', x = mean(five_2$V1) + 0.5, y = -3.8,
    hjust = 0, size = 5,
    label = str_glue("Mean = {round(mean(five_2$V1), 2)}")) +
  annotate(geom = 'text', x = mean(five_2$V1) + 0.2, y = -4.75,
    hjust = 0, size = 5,
    label = str_glue("SD = {round(sd(five_2$V1), 2)}")) +
  labs(title = 'B: Constrained (0-10 range)',
    caption = 'Parameters: Mean = 5.2, SD = 1.7, r = 0.5') +
  scale_y_continuous(limits = c(-5, 15)) +
  scale_x_continuous(limits = c(-5, 15)) +
  theme(plot.caption = element_text(size = 14)))

```


B: Constrained (0–10 range)



Parameters: Mean = 5.2, SD = 1.7, $r = 0.5$

Model mean of V1 with increasing V1 thresholds from 0 to 5

```
# Extract visit 1 data
five_2V1 <- five_2$V1

# Generate a vector of threshold values to iterate over
cutoff <- 0:5

# Generate a vector of V1 means at each V1 threshold
five_2V1.shift <- sapply(cutoff, function(x){mean(five_2V1[five_2V1 > x])})

# Calculate deviation
```

```

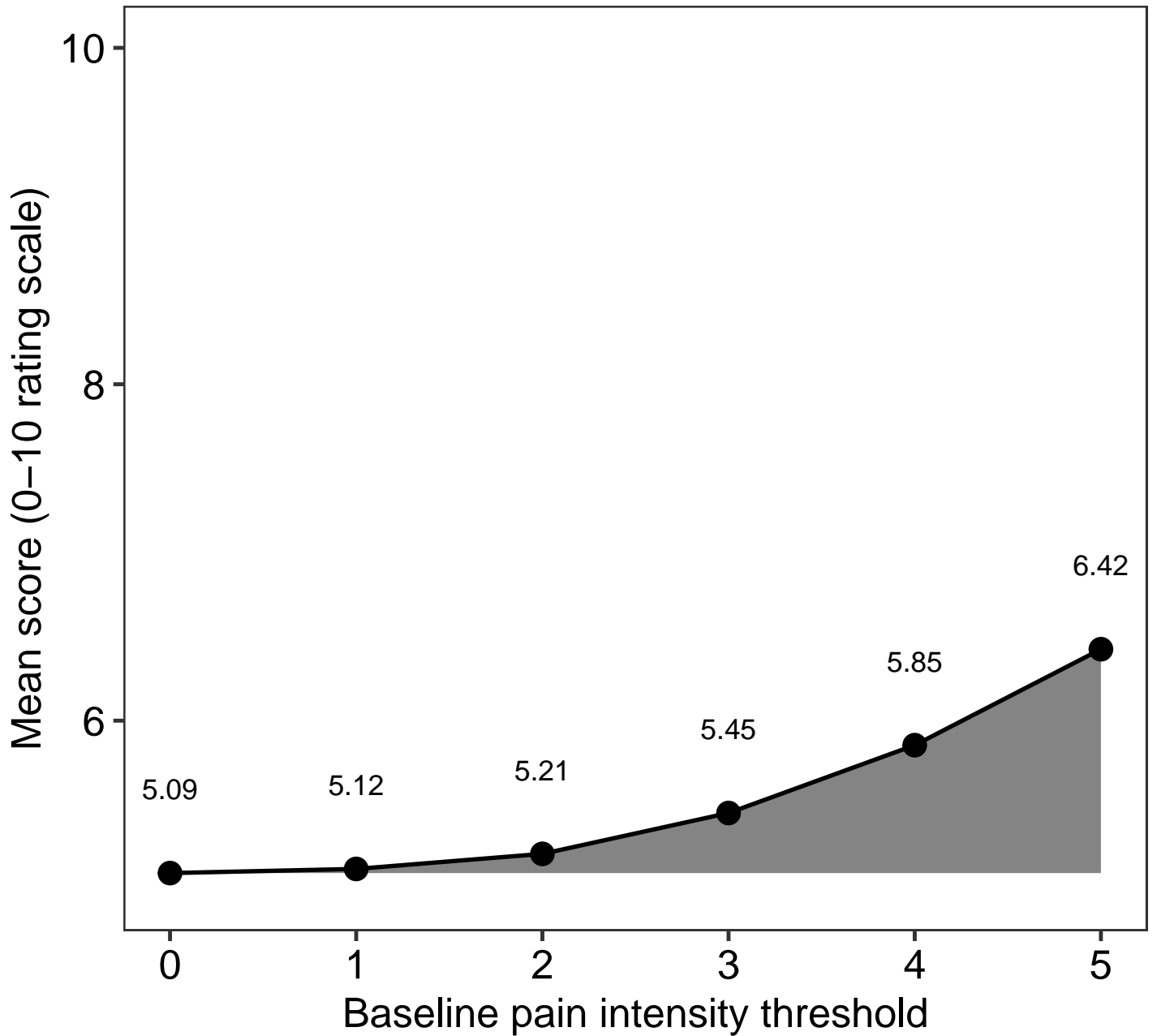
(five_2V1.df <- data.frame(time = 'V1',
                           cutoff = cutoff,
                           cutoff2 = cutoff - 0.15,
                           mean = five_2V1.shift) %>%
  mutate(deviation = mean - mean(five_2V1),
         time = as.character(time)))

##   time cutoff cutoff2    mean deviation
## 1   V1      0   -0.15 5.093762 0.00000000
## 2   V1      1    0.85 5.118473 0.02471084
## 3   V1      2    1.85 5.207945 0.11418329
## 4   V1      3    2.85 5.450979 0.35721683
## 5   V1      4    3.85 5.854175 0.76041340
## 6   V1      5    4.85 6.424720 1.33095827

# Plot data
ggplot(data = five_2V1.df) +
  aes(x = cutoff, y = mean, ymin = mean(five_2V1), ymax = mean) +
  geom_ribbon(alpha = 0.6) +
  geom_point(size = 5) +
  geom_line(size = 1) +
  geom_text(aes(label = round(mean, 2)),
            nudge_y = 0.5, size = 5) +
  scale_y_continuous(limits = c(5, 10),
                    breaks = c(0, 2, 4, 6, 8, 10)) +
  labs(title = 'A: Shift in V1 mean with increasing V1 threshold value',
       caption = 'Parameters: Mean = 5.2, SD = 1.7, r = 0.5',
       x = 'Baseline pain intensity threshold',
       y = 'Mean score (0-10 rating scale)') +
  theme(plot.caption = element_text(size = 14))

```

A: Shift in V1 mean with increasing V1 threshold value



Parameters: Mean = 5.2, SD = 1.7, $r = 0.5$

Model mean of V2 with increasing V1 thresholds from 0 to 5

```
# Extract visit 2 data
five_2V2 <- five_2$V2

# Generate a vector of threshold values to iterate over
cutoff <- 0:5

# Generate a vector of V2 means at each V1 threshold
five_2V2.shift <- map_dbl(.x = cutoff,
  ~ five_2 %>%
    filter(V1 > .x) %>%
```

```

        .$V2 %>%
        mean(.))

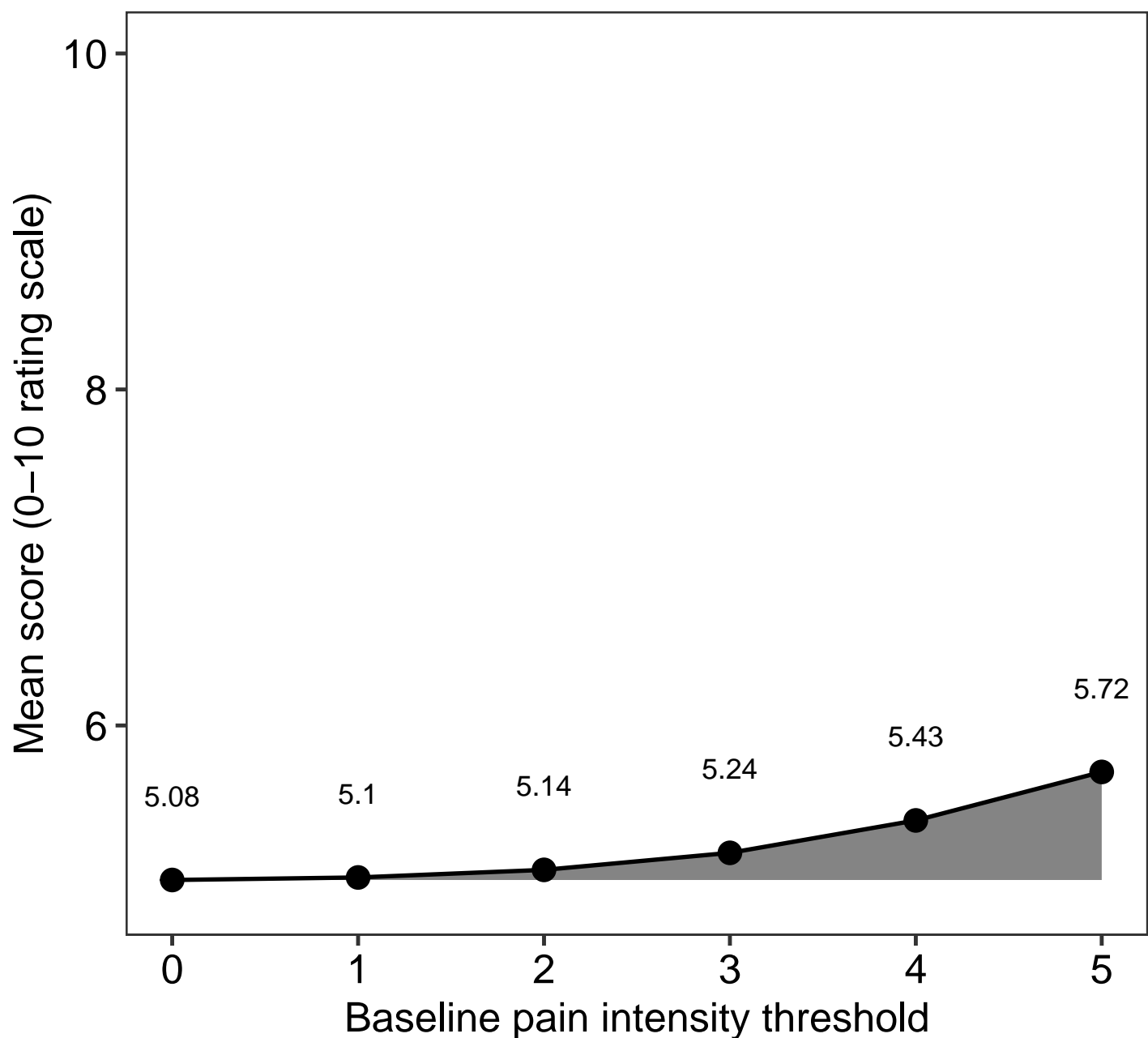
# Calcaulate deviation
(five_2V2.df <- data.frame(time = 'V2',
                           cutoff = cutoff,
                           cutoff2 = cutoff + 0.15,
                           mean = five_2V2.shift) %>%
  mutate(deviation = mean - mean(five_2V1),
         time = as.character(time)))

##   time cutoff cutoff2    mean  deviation
## 1   V2      0    0.15 5.080261 -0.01350081
## 2   V2      1    1.15 5.095284  0.00152173
## 3   V2      2    2.15 5.140449  0.04668704
## 4   V2      3    3.15 5.241791  0.14802904
## 5   V2      4    4.15 5.434797  0.34103527
## 6   V2      5    5.15 5.723440  0.62967833

# Plot data
ggplot(data = five_2V2.df) +
  aes(x = cutoff, y = mean, ymin = mean(five_2V2), ymax = mean) +
  geom_ribbon(alpha = 0.6) +
  geom_point(size = 5) +
  geom_line(size = 1) +
  geom_text(aes(label = round(mean, 2)),
            nudge_y = 0.5, size = 5) +
  scale_y_continuous(limits = c(5, 10),
                     breaks = c(0, 2, 4, 6, 8, 10)) +
  labs(title = 'B: Shift in V2 mean with increasing V1 threshold value',
       caption = 'Parameters: Mean = 5.2, SD = 1.7, r = 0.5',
       x = 'Baseline pain intensity threshold',
       y = 'Mean score (0-10 rating scale)') +
  theme(plot.caption = element_text(size = 14))

```

B: Shift in V2 mean with increasing V1 threshold value



Parameters: Mean = 5.2, SD = 1.7, $r = 0.5$

Placebo response

threshold: 0

```
# Process data
placebo_2.0 <- five_2 %>%
  filter(V1 >= 0) %>%
  mutate(difference = V1 - V2) %>%
  mutate(group = 'Threshold')

# Calculate the mean (95%CI) difference between V1 and V2
diff_2.0 <- groupwiseMean(difference ~ 1,
```

```

data = placebo_2.0,
R = 2000,
traditional = FALSE,
bca = TRUE)

diff_2.0$.id <- 0

kable(diff_2.0)

```

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
0	1000	0.0135	0.95	-0.0955	0.119

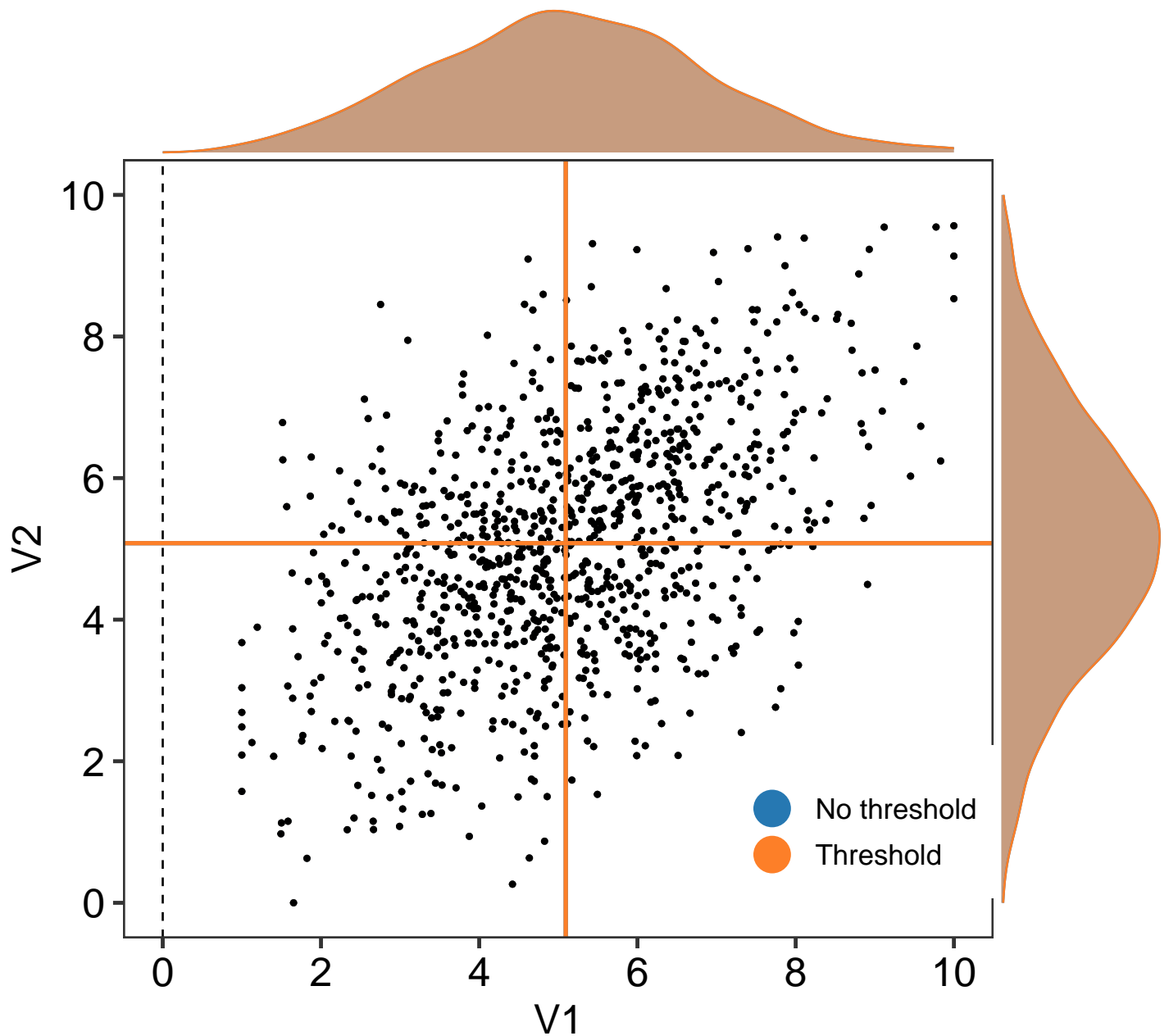
```

# Plot the data
ggMarginal(placebo_2.0[, 1:3] %>%
  bind_rows(five_2) %>%
  mutate(group = factor(group,
    levels = c('No threshold', 'Threshold'),
    ordered = TRUE)) %>%

  ggplot(data = .) +
  aes(x = V1, y = V2) +
  geom_point(aes(colour = group, fill = group),
    size = 1) +
  guides(colour = guide_legend(override.aes = list(size = 8))) +
  geom_point(data = five_2,
    colour = '#999999',
    size = 1) +
  geom_point(data = placebo_2.0,
    size = 1,
    colour = '#000000') +
  geom_vline(xintercept = mean(five_2$V1),
    colour = pal[1], size = 1) +
  geom_vline(xintercept = mean(placebo_2.0$V1),
    colour = pal[2], size = 1) +
  geom_vline(xintercept = 0, linetype = 2) +
  geom_hline(yintercept = mean(five_2$V2),
    colour = pal[1], size = 1) +
  geom_hline(yintercept = mean(placebo_2.0$V2),
    colour = pal[2], size = 1) +
  scale_y_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_x_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_fill_manual(values = pal) +
  scale_colour_manual(values = pal) +
  labs(title = 'A: Baseline pain threshold = 0',
    caption = 'Parameters: Mean = 5.2, SD = 1.7, r = 0.5') +
  theme(legend.title = element_blank(),
    legend.position = c(0.85, 0.15),
    plot.caption = element_text(size = 14)),
groupColour = TRUE,
groupFill = TRUE)

```

A: Baseline pain threshold = 0



Parameters: Mean = 5.2, SD = 1.7, $r = 0.5$

threshold: 3

```
# Process data
placebo_2.3 <- five_2 %>%
  filter(V1 >= 3) %>%
  mutate(difference = V1 - V2) %>%
  mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
```

```
diff_2.3 <- groupwiseMean(difference ~ 1,
  data = placebo_2.3,
  R = 2000,
  traditional = FALSE,
  bca = TRUE)

diff_2.3$.id <- 3

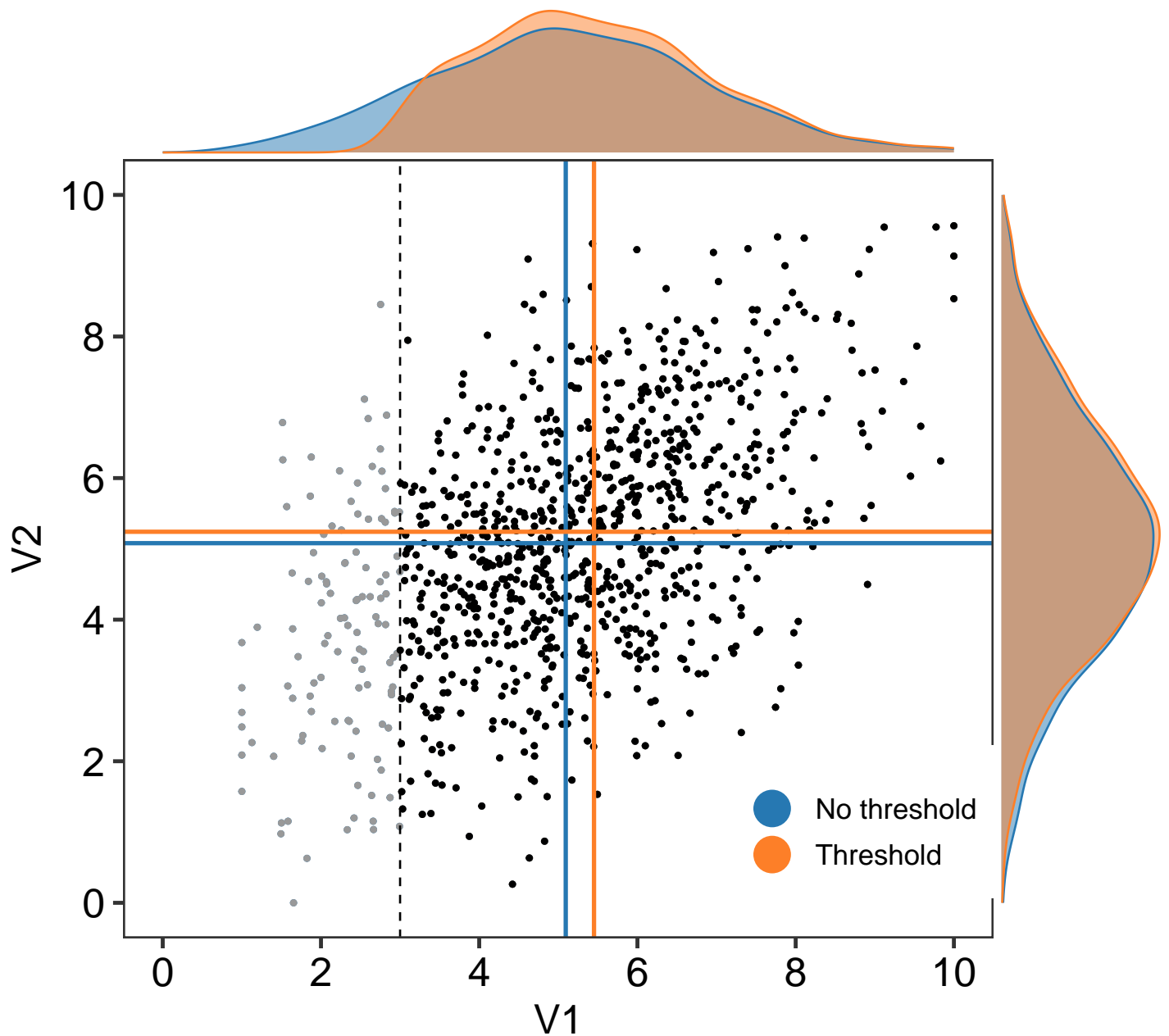
kable(diff_2.3)
```

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
3	888	0.209	0.95	0.107	0.316

```
# Plot the data
ggMarginal(placebo_2.3[, 1:3] %>%
  bind_rows(five_2) %>%
  mutate(group = factor(group,
    levels = c('No threshold', 'Threshold'),
    ordered = TRUE)) %>%

  ggplot(data = .) +
  aes(x = V1, y = V2) +
  geom_point(aes(colour = group, fill = group),
    size = 1) +
  guides(colour = guide_legend(override.aes = list(size = 8))) +
  geom_point(data = five_2,
    colour = '#999999',
    size = 1) +
  geom_point(data = placebo_2.3,
    size = 1,
    colour = '#000000') +
  geom_vline(xintercept = mean(five_2$V1),
    colour = pal[1], size = 1) +
  geom_vline(xintercept = mean(placebo_2.3$V1),
    colour = pal[2], size = 1) +
  geom_vline(xintercept = 3, linetype = 2) +
  geom_hline(yintercept = mean(five_2$V2),
    colour = pal[1], size = 1) +
  geom_hline(yintercept = mean(placebo_2.3$V2),
    colour = pal[2], size = 1) +
  scale_y_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_x_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_fill_manual(values = pal) +
  scale_colour_manual(values = pal) +
  labs(title = 'B: Baseline pain threshold = 3',
    caption = 'Parameters: Mean = 5.2, SD = 1.7, r = 0.5') +
  theme(legend.title = element_blank(),
    legend.position = c(0.85, 0.15),
    plot.caption = element_text(size = 14)),
  groupColour = TRUE,
  groupFill = TRUE)
```


B: Baseline pain threshold = 3



Parameters: Mean = 5.2, SD = 1.7, $r = 0.5$

threshold: 4

```
# Process that data
placebo_2.4 <- five_2 %>%
  filter(V1 >= 4) %>%
  mutate(difference = V1 - V2) %>%
  mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
```

```
diff_2.4 <- groupwiseMean(difference ~ 1,
  data = placebo_2.4,
  R = 2000,
  traditional = FALSE,
  bca = TRUE)

diff_2.4$.id <- 4

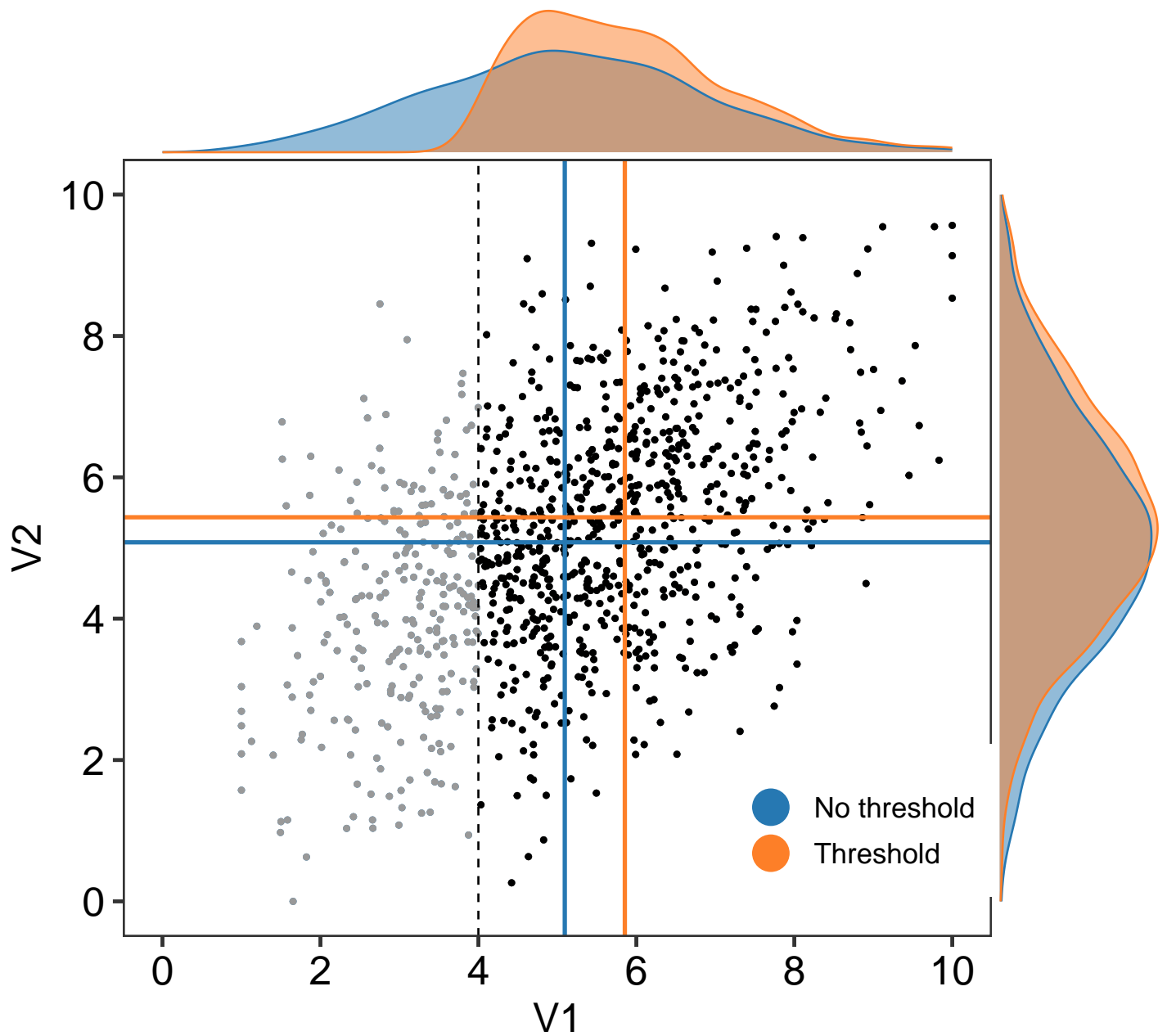
kable(diff_2.4)
```

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
4	735	0.419	0.95	0.307	0.539

```
# Plot the data
ggMarginal(placebo_2.4[, 1:3] %>%
  bind_rows(five_2) %>%
  mutate(group = factor(group,
    levels = c('No threshold', 'Threshold'),
    ordered = TRUE)) %>%

  ggplot(data = .) +
  aes(x = V1, y = V2) +
  geom_point(aes(colour = group, fill = group),
    size = 1) +
  guides(colour = guide_legend(override.aes = list(size = 8))) +
  geom_point(data = five_2,
    colour = '#999999',
    size = 1) +
  geom_point(data = placebo_2.4,
    size = 1,
    colour = '#000000') +
  geom_vline(xintercept = mean(five_2$V1),
    colour = pal[1], size = 1) +
  geom_vline(xintercept = mean(placebo_2.4$V1),
    colour = pal[2], size = 1) +
  geom_vline(xintercept = 4, linetype = 2) +
  geom_hline(yintercept = mean(five_2$V2),
    colour = pal[1], size = 1) +
  geom_hline(yintercept = mean(placebo_2.4$V2),
    colour = pal[2], size = 1) +
  scale_y_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_x_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_fill_manual(values = pal) +
  scale_colour_manual(values = pal) +
  labs(title = 'C: Baseline pain threshold = 4',
    caption = 'Parameters: Mean = 5.2, SD = 1.7, r = 0.5') +
  theme(legend.title = element_blank(),
    legend.position = c(0.85, 0.15),
    plot.caption = element_text(size = 14)),
  groupColour = TRUE,
  groupFill = TRUE)
```

C: Baseline pain threshold = 4



Parameters: Mean = 5.2, SD = 1.7, $r = 0.5$

threshold: 5

```
# Process that data
placebo_2.5 <- five_2 %>%
  filter(V1 >= 5) %>%
  mutate(difference = V1 - V2) %>%
  mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
```

```
diff_2.5 <- groupwiseMean(difference ~ 1,
  data = placebo_2.5,
  R = 2000,
  traditional = FALSE,
  bca = TRUE)

diff_2.5$.id <- 5

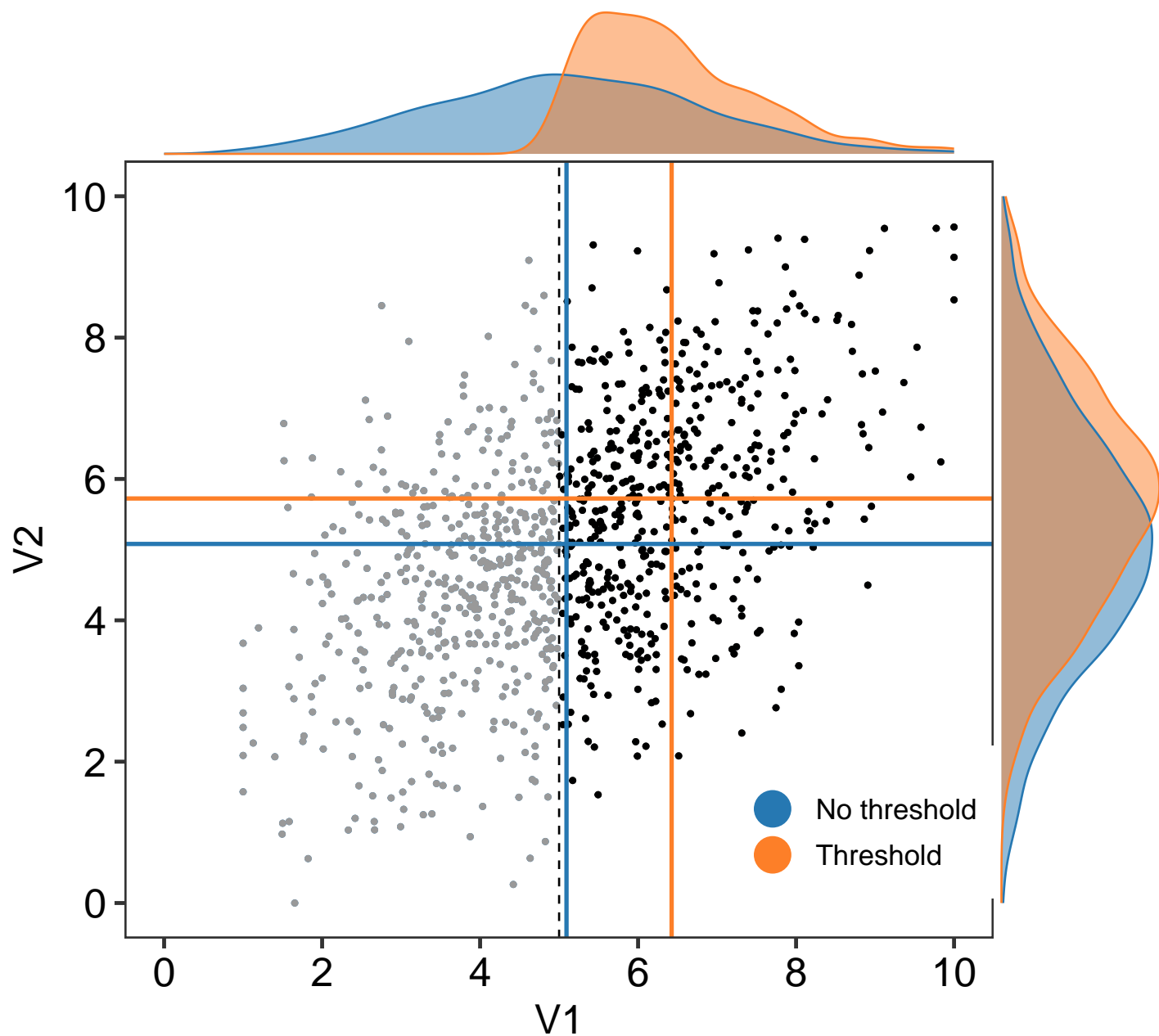
kable(diff_2.5)
```

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
5	511	0.701	0.95	0.571	0.832

```
# Plot the data
ggMarginal(placebo_2.5[, 1:3] %>%
  bind_rows(five_2) %>%
  mutate(group = factor(group,
    levels = c('No threshold', 'Threshold'),
    ordered = TRUE)) %>%

  ggplot(data = .) +
  aes(x = V1, y = V2) +
  geom_point(aes(colour = group, fill = group),
    size = 1) +
  guides(colour = guide_legend(override.aes = list(size = 8))) +
  geom_point(data = five_2,
    colour = '#999999',
    size = 1) +
  geom_point(data = placebo_2.5,
    size = 1,
    colour = '#000000') +
  geom_vline(xintercept = mean(five_2$V1),
    colour = pal[1], size = 1) +
  geom_vline(xintercept = mean(placebo_2.5$V1),
    colour = pal[2], size = 1) +
  geom_vline(xintercept = 5, linetype = 2) +
  geom_hline(yintercept = mean(five_2$V2),
    colour = pal[1], size = 1) +
  geom_hline(yintercept = mean(placebo_2.5$V2),
    colour = pal[2], size = 1) +
  scale_y_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_x_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_fill_manual(values = pal) +
  scale_colour_manual(values = pal) +
  labs(title = 'D: Baseline pain threshold = 5',
    caption = 'Parameters: Mean = 5.2, SD = 1.7, r = 0.5') +
  theme(legend.title = element_blank(),
    legend.position = c(0.85, 0.15),
    plot.caption = element_text(size = 14)),
  groupColour = TRUE,
  groupFill = TRUE)
```

D: Baseline pain threshold = 5



Parameters: Mean = 5.2, SD = 1.7, r = 0.5

Publication plots

```
# Plot 1
shift_2 <- five_2V1.df %>%
  bind_rows(five_2V2.df) %>%
  ggplot(data = .) +
  aes(y = mean,
       x = cutoff2,
       fill = time) +
  geom_hline(yintercept = 5.2,
             linetype = 2) +
  geom_point(shape = 21,
```

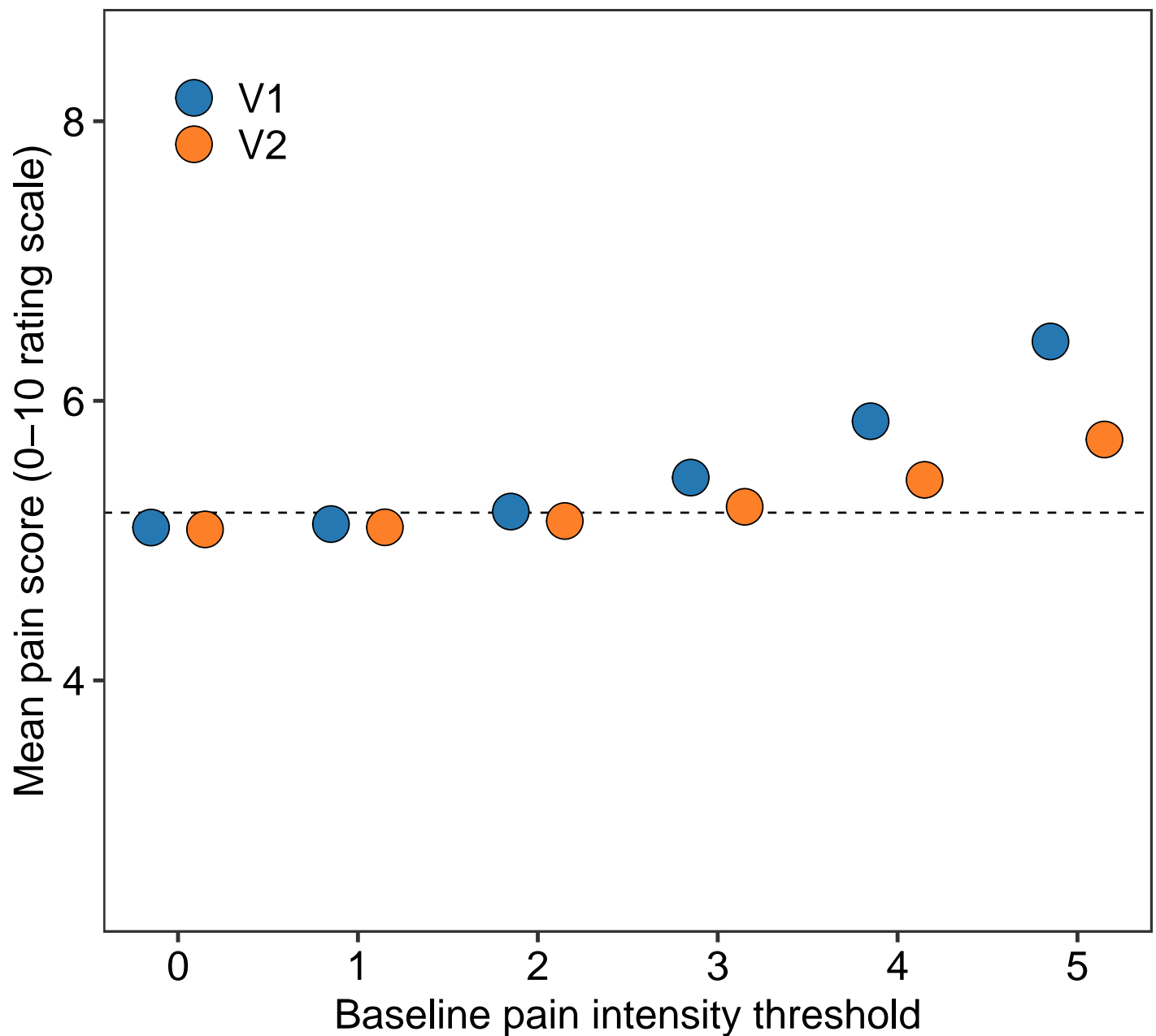
```

size = 8) +
labs(title = 'B',
      subtitle = 'Parameters: Mean = 5.2, SD = 1.7, r = 0.5',
      x = 'Baseline pain intensity threshold',
      y = 'Mean pain score (0-10 rating scale)') +
scale_x_continuous(breaks = 0:5) +
scale_y_continuous(limits = c(2.5, 8.5)) +
scale_fill_manual(values = pal) +
theme(legend.title = element_blank(),
      legend.position = c(0.12, 0.89),
      legend.text = element_text(size = 20)); shift_2

```

B

Parameters: Mean = 5.2, SD = 1.7, r = 0.5



```

# Plot 2
# Bind diff_*. dataframes

```

```

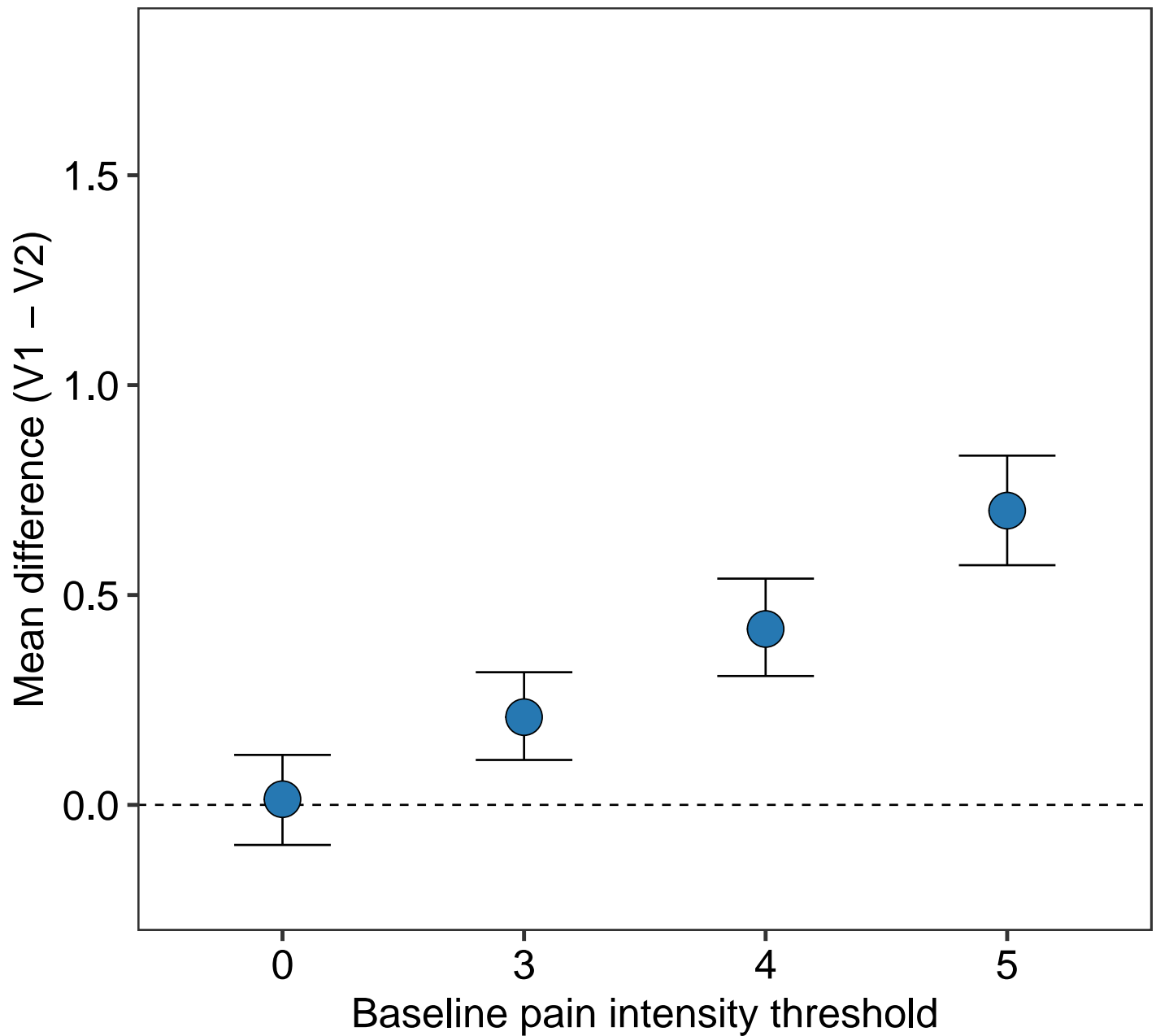
diff_all_2 <- diff_2.0 %>%
  bind_rows(diff_2.3, diff_2.4, diff_2.5)

pp_2 <- diff_all_2 %>%
  mutate(Threshold = factor(.id)) %>%
  ggplot(data = .) +
  aes(x = Threshold,
      y = Mean,
      ymin = Bca.lower,
      ymax = Bca.upper) +
  geom_hline(yintercept = 0,
             linetype = 2) +
  geom_errorbar(width = 0.4) +
  geom_point(shape = 21,
             fill = pal[[1]],
             size = 8) +
  labs(title = 'B',
       subtitle = 'Parameters: Mean = 5.2, SD = 1.7, r = 0.5',
       x = 'Baseline pain intensity threshold',
       y = 'Mean difference (V1 - V2)') +
  scale_y_continuous(limits = c(-0.2, 1.8)); pp_2

```

B

Parameters: Mean = 5.2, SD = 1.7, $r = 0.5$



Mean = 5.2, SD = 2.2, $r = 0.5$

Generate and summarise data

Base data

```
# Set the random seed for reproducibility
set.seed(2019)

# Generate the data
```



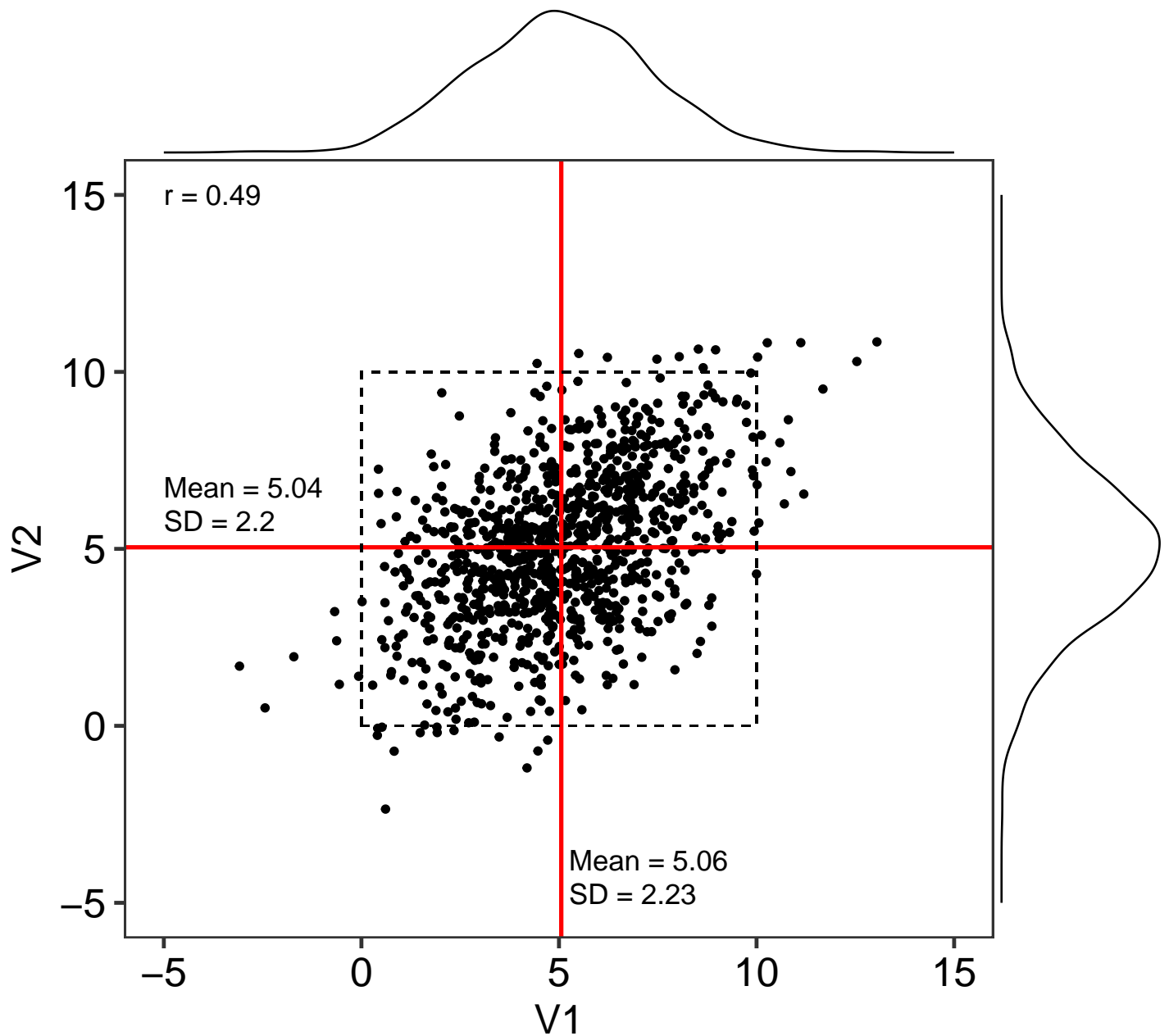
```

five_3.base <- as.data.frame(mvrnorm(n = 1000, mu = c(5.2, 5.2), Sigma = cov_3))

# Plot base data
ggMarginal(ggplot(data = five_3.base) +
  aes(x = V1, y = V2) +
  geom_point() +
  geom_hline(yintercept = mean(five_3.base$V2),
    colour = 'red', size = 1) +
  geom_vline(xintercept = mean(five_3.base$V1),
    colour = 'red', size = 1) +
  geom_rect(ymin = 0, ymax = 10,
    xmin = 0, xmax = 10,
    colour = '#000000',
    alpha = 0,
    linetype = 2) +
  annotate(geom = 'text', x = -5, y = 15,
    hjust = 0, size = 5,
    label = str_glue("r = {round(cor(five_3.base$V1,
      five_3.base$V2), 2)}")) +
  annotate(geom = 'text', x = -5, y = mean(five_3.base$V2) + 1.7,
    hjust = 0, size = 5,
    label = str_glue("Mean = {round(mean(five_3.base$V2), 2)}")) +
  annotate(geom = 'text', x = -5, y = mean(five_3.base$V2) + 0.75,
    hjust = 0, size = 5,
    label = str_glue("SD = {round(sd(five_3.base$V2), 2)}")) +
  annotate(geom = 'text', x = mean(five_3.base$V1) + 0.2, y = -3.8,
    hjust = 0, size = 5,
    label = str_glue("Mean = {round(mean(five_3.base$V1), 2)}")) +
  annotate(geom = 'text', x = mean(five_3.base$V1) + 0.2, y = -4.75,
    hjust = 0, size = 5,
    label = str_glue("SD = {round(sd(five_3.base$V1), 2)}")) +
  labs(title = 'A: Unconstrained',
    caption = 'Parameters: Mean = 5.2, SD = 2.2, r = 0.5') +
  scale_y_continuous(limits = c(-5, 15)) +
  scale_x_continuous(limits = c(-5, 15)) +
  theme(plot.caption = element_text(size = 14)))

```

A: Unconstrained



Parameters: Mean = 5.2, SD = 2.2, $r = 0.5$

Constrain values to 0-10 range

```
# Process data
five_3 <- five_3.base %>%
  mutate(V1 = case_when(
    V1 < 1 ~ 1,
    V1 > 10 ~ 10,
    TRUE ~ V1)) %>%
  mutate(V2 = case_when(
    V2 < 0 ~ 0,
    V2 > 10 ~ 10,
    TRUE ~ V2)) %>%
```

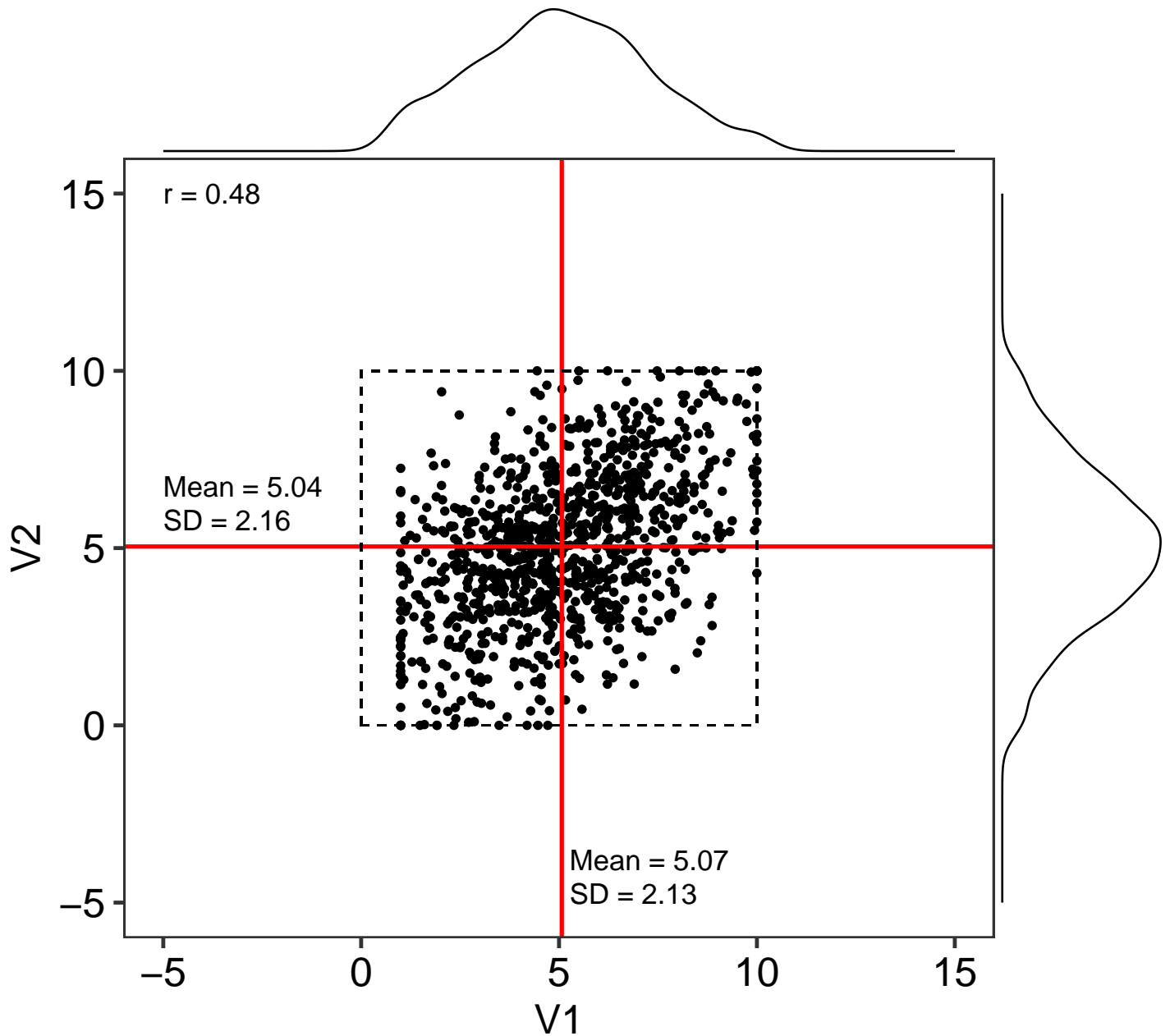
```

mutate(group = 'No threshold')

# Plot processed data
ggMarginal(ggplot(data = five_3) +
  aes(x = V1, y = V2) +
  geom_point() +
  geom_hline(yintercept = mean(five_3$V2),
    colour = 'red', size = 1) +
  geom_vline(xintercept = mean(five_3$V1),
    colour = 'red', size = 1) +
  geom_rect(ymin = 0, ymax = 10,
    xmin = 0, xmax = 10,
    colour = '#000000',
    alpha = 0,
    linetype = 2) +
  annotate(geom = 'text', x = -5, y = 15,
    hjust = 0, size = 5,
    label = str_glue("r = {round(cor(five_3$V1,
      five_3$V2), 2)}")) +
  annotate(geom = 'text', x = -5, y = mean(five_3$V2) + 1.7,
    hjust = 0, size = 5,
    label = str_glue("Mean = {round(mean(five_3$V2), 2)}")) +
  annotate(geom = 'text', x = -5, y = mean(five_3$V2) + 0.75,
    hjust = 0, size = 5,
    label = str_glue("SD = {round(sd(five_3$V2), 2)}")) +
  annotate(geom = 'text', x = mean(five_3$V1) + 0.2, y = -3.8,
    hjust = 0, size = 5,
    label = str_glue("Mean = {round(mean(five_3$V1), 2)}")) +
  annotate(geom = 'text', x = mean(five_3$V1) + 0.2, y = -4.75,
    hjust = 0, size = 5,
    label = str_glue("SD = {round(sd(five_3$V1), 2)}")) +
  labs(title = 'B: Constrained (0-10 range)',
    caption = 'Parameters: Mean = 5.2, SD = 2.2, r = 0.5') +
  scale_y_continuous(limits = c(-5, 15)) +
  scale_x_continuous(limits = c(-5, 15)) +
  theme(plot.caption = element_text(size = 14)))

```

B: Constrained (0–10 range)



Parameters: Mean = 5.2, SD = 2.2, $r = 0.5$

Model mean of V1 with increasing V1 thresholds from 0 to 5

```
# Extract visit 1 data
five_3V1 <- five_3$V1

# Generate a vector of threshold values to iterate over
cutoff <- 0:5

# Generate a vector of V1 means at each V1 threshold
five_3V1.shift <- sapply(cutoff, function(x){mean(five_3V1[five_3V1 > x])})

# Calculate deviation
```

```

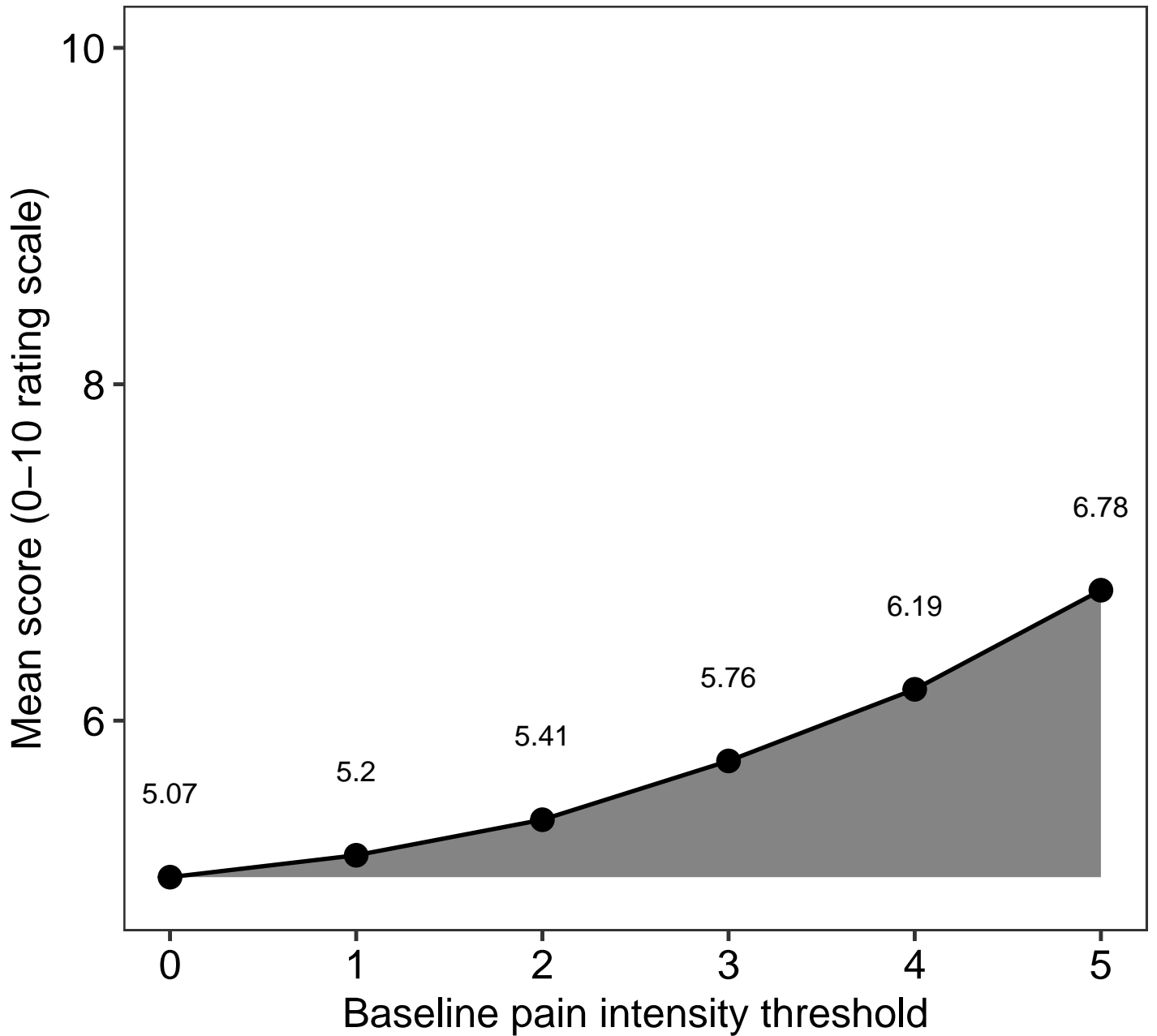
(five_3V1.df <- data.frame(time = 'V1',
                           cutoff = cutoff,
                           cutoff2 = cutoff - 0.15,
                           mean = five_3V1.shift) %>%
  mutate(deviation = mean - mean(five_3V1),
         time = as.character(time)))

##   time cutoff cutoff2    mean deviation
## 1   V1      0   -0.15 5.069509 0.0000000
## 2   V1      1    0.85 5.199700 0.1301907
## 3   V1      2    1.85 5.410951 0.3414419
## 4   V1      3    2.85 5.760471 0.6909618
## 5   V1      4    3.85 6.186270 1.1167604
## 6   V1      5    4.85 6.775409 1.7058995

# Plot data
ggplot(data = five_3V1.df) +
  aes(x = cutoff, y = mean, ymin = mean(five_3V1), ymax = mean) +
  geom_ribbon(alpha = 0.6) +
  geom_point(size = 5) +
  geom_line(size = 1) +
  geom_text(aes(label = round(mean, 2)),
            nudge_y = 0.5, size = 5) +
  scale_y_continuous(limits = c(5, 10),
                     breaks = c(0, 2, 4, 6, 8, 10)) +
  labs(title = 'A: Shift in V1 mean with increasing V1 threshold value',
       caption = 'Parameters: Mean = 5.2, SD = 2.2, r = 0.5',
       x = 'Baseline pain intensity threshold',
       y = 'Mean score (0-10 rating scale)') +
  theme(plot.caption = element_text(size = 14))

```

A: Shift in V1 mean with increasing V1 threshold value



Parameters: Mean = 5.2, SD = 2.2, $r = 0.5$

Model mean of V2 with increasing V1 thresholds from 0 to 5

```
# Extract visit 2 data
five_3V2 <- five_3$V2

# Generate a vector of threshold values to iterate over
cutoff <- 0:5

# Generate a vector of V2 means at each V1 threshold
five_3V2.shift <- map_dbl(.x = cutoff,
  ~ five_3 %>%
    filter(V1 > .x) %>%
```

```

        .$V2 %>%
        mean(.))

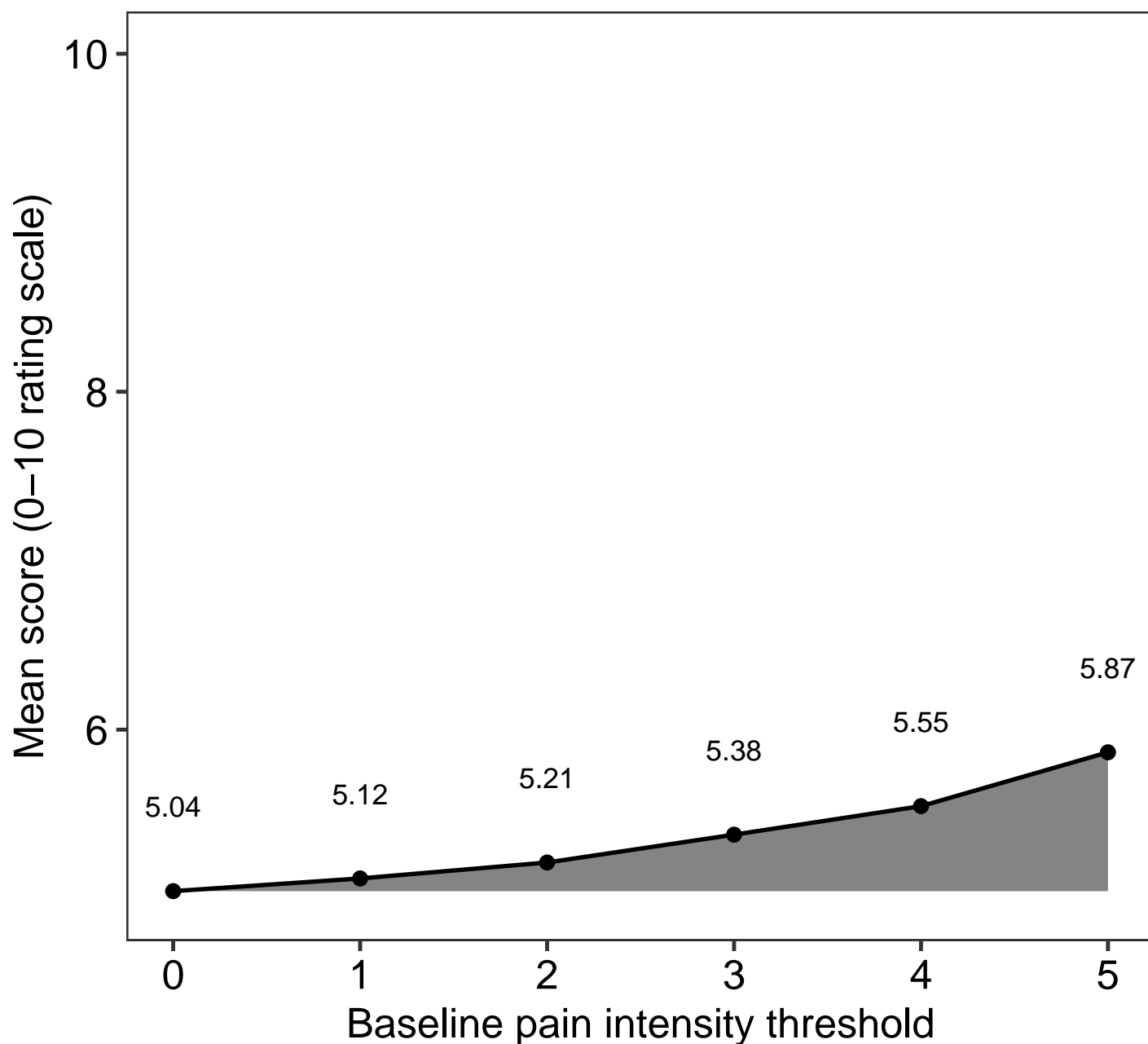
# Calculate deviation
(five_3V2.df <- data.frame(time = 'V2',
                           cutoff = cutoff,
                           cutoff2 = cutoff + 0.15,
                           mean = five_3V2.shift) %>%
  mutate(deviation = mean - mean(five_3V1),
         time = as.character(time)))

##   time cutoff cutoff2    mean  deviation
## 1   V2      0    0.15 5.044282 -0.02522702
## 2   V2      1    1.15 5.119444  0.04993433
## 3   V2      2    2.15 5.213786  0.14427618
## 4   V2      3    3.15 5.378531  0.30902169
## 5   V2      4    4.15 5.547313  0.47780325
## 6   V2      5    5.15 5.866011  0.79650120

# Plot data
ggplot(data = five_3V2.df) +
  aes(x = cutoff, y = mean, ymin = mean(five_3V2), ymax = mean) +
  geom_ribbon(alpha = 0.6) +
  geom_point(size = 3) +
  geom_line(size = 1) +
  geom_text(aes(label = round(mean, 2)),
            nudge_y = 0.5, size = 5) +
  scale_y_continuous(limits = c(5, 10),
                     breaks = c(0, 2, 4, 6, 8, 10)) +
  labs(title = 'B: Shift in V2 mean with increasing V1 threshold value',
       caption = 'Parameters: Mean = 5.2, SD = 2.2, r = 0.5',
       x = 'Baseline pain intensity threshold',
       y = 'Mean score (0-10 rating scale)') +
  theme(plot.caption = element_text(size = 14))

```

B: Shift in V2 mean with increasing V1 threshold value



Parameters: Mean = 5.2, SD = 2.2, $r = 0.5$

Placebo response

threshold: 0

```
# Process data
placebo_3.0 <- five_3 %>%
  filter(V1 >= 0) %>%
  mutate(difference = V1 - V2) %>%
  mutate(group = 'Threshold')

# Calculate the mean (95%CI) difference between V1 and V2
diff_3.0 <- groupwiseMean(difference ~ 1,
```



```

data = placebo_3.0,
R = 2000,
traditional = FALSE,
bca = TRUE)

diff_3.0$.id <- 0

kable(diff_3.0)

```

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
0	1000	0.0252	0.95	-0.112	0.159

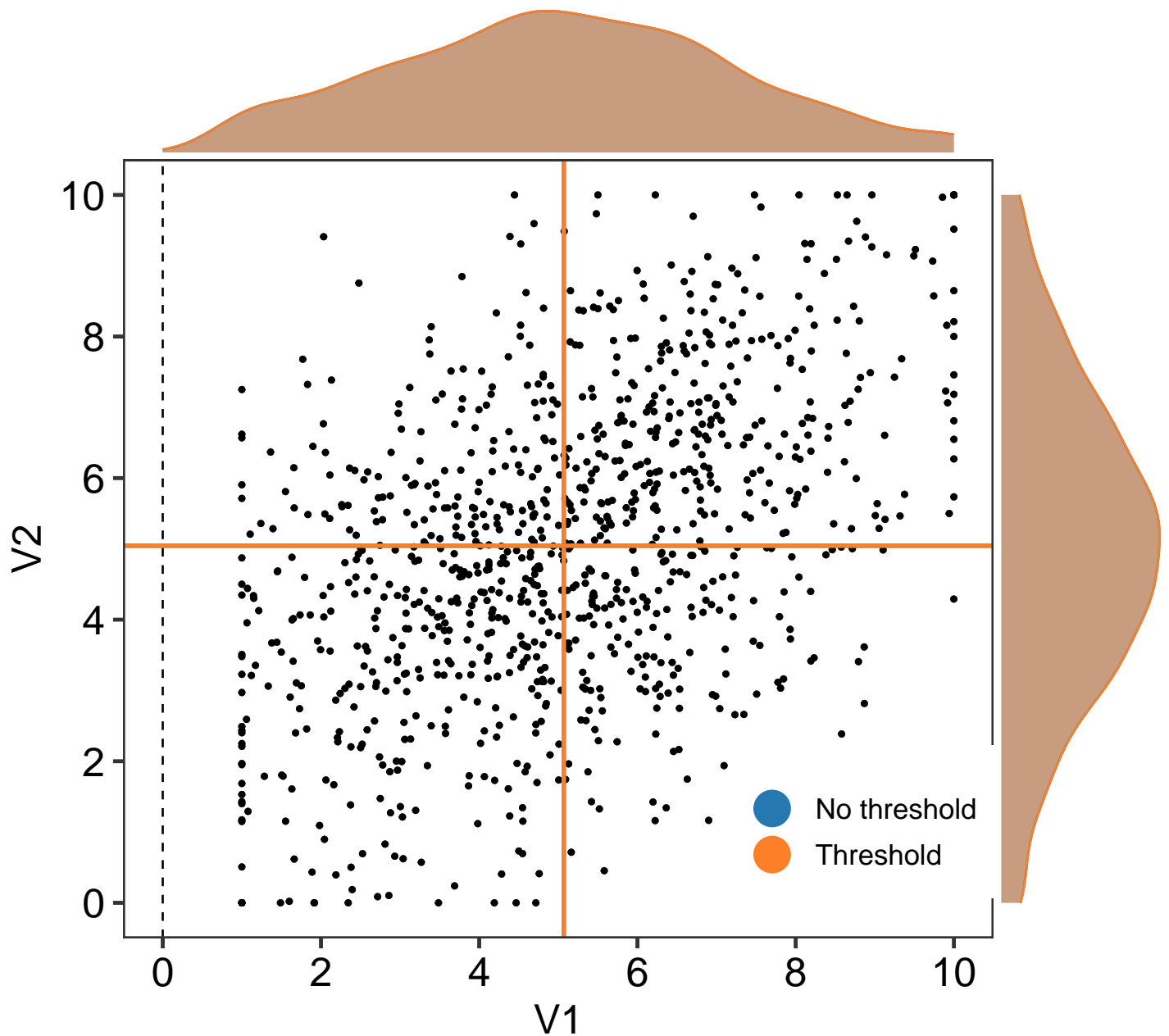
```

# Plot the data
ggMarginal(placebo_3.0[, 1:3] %>%
  bind_rows(five_3) %>%
  mutate(group = factor(group,
    levels = c('No threshold', 'Threshold'),
    ordered = TRUE)) %>%

  ggplot(data = .) +
  aes(x = V1, y = V2) +
  geom_point(aes(colour = group, fill = group),
    size = 1) +
  guides(colour = guide_legend(override.aes = list(size = 8))) +
  geom_point(data = five_3,
    colour = '#999999',
    size = 1) +
  geom_point(data = placebo_3.0,
    size = 1,
    colour = '#000000') +
  geom_vline(xintercept = mean(five_3$V1),
    colour = pal[1], size = 1) +
  geom_vline(xintercept = mean(placebo_3.0$V1),
    colour = pal[2], size = 1) +
  geom_vline(xintercept = 0, linetype = 2) +
  geom_hline(yintercept = mean(five_3$V2),
    colour = pal[1], size = 1) +
  geom_hline(yintercept = mean(placebo_3.0$V2),
    colour = pal[2], size = 1) +
  scale_y_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_x_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_fill_manual(values = pal) +
  scale_colour_manual(values = pal) +
  labs(title = 'A: Baseline pain threshold = 0',
    caption = 'Parameters: Mean = 5.2, SD = 2.2, r = 0.5') +
  theme(legend.title = element_blank(),
    legend.position = c(0.85, 0.15),
    plot.caption = element_text(size = 14)),
groupColour = TRUE,
groupFill = TRUE)

```

A: Baseline pain threshold = 0



Parameters: Mean = 5.2, SD = 2.2, $r = 0.5$

threshold: 3

```
# Process data
placebo_3.3 <- five_3 %>%
  filter(V1 >= 3) %>%
  mutate(difference = V1 - V2) %>%
  mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
```

```
diff_3.3 <- groupwiseMean(difference ~ 1,
  data = placebo_3.3,
  R = 2000,
  traditional = FALSE,
  bca = TRUE)

diff_3.3$.id <- 3

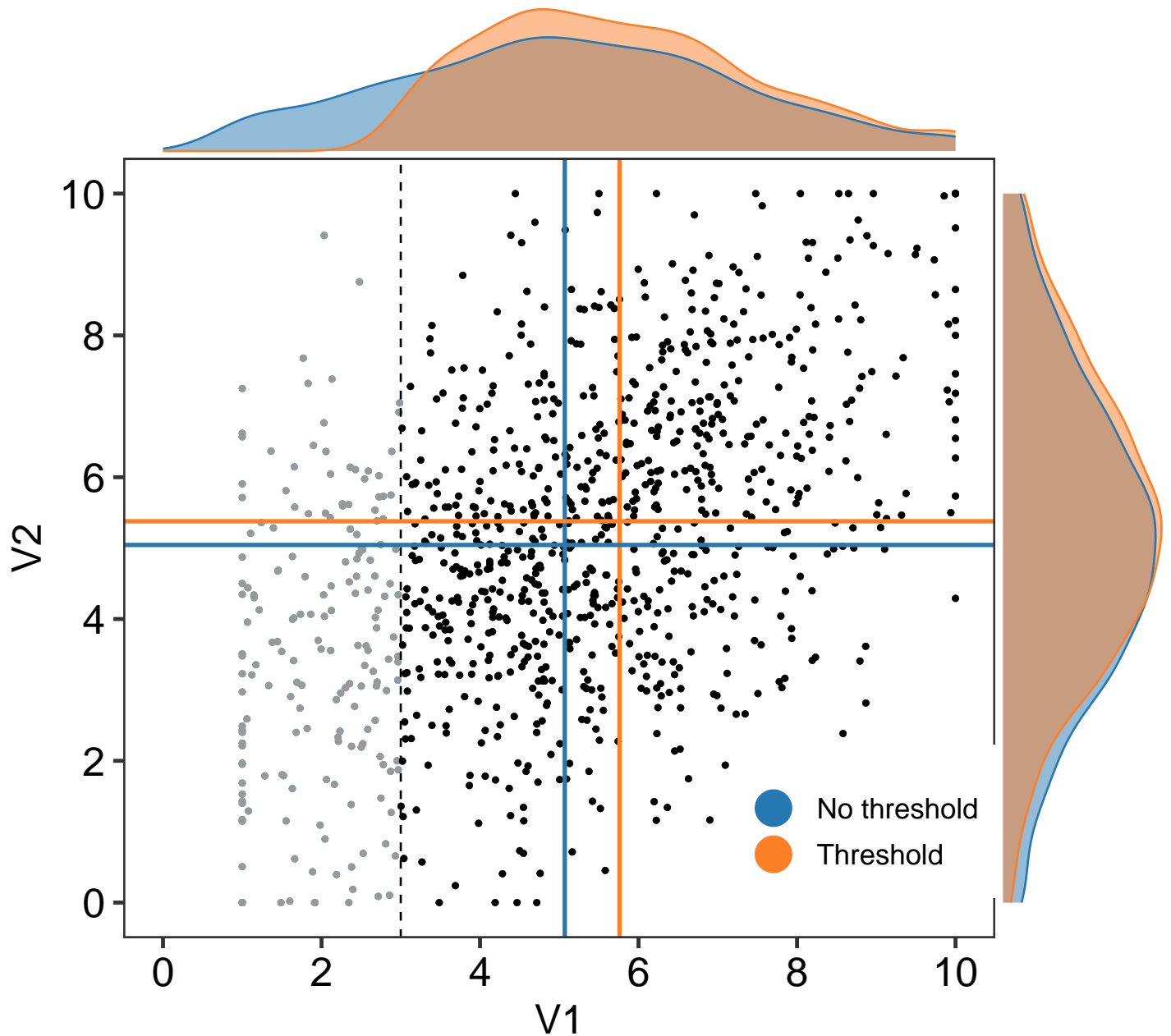
kable(diff_3.3)
```

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
3	817	0.382	0.95	0.243	0.527

```
# Plot the data
ggMarginal(placebo_3.3[, 1:3] %>%
  bind_rows(five_3) %>%
  mutate(group = factor(group,
    levels = c('No threshold', 'Threshold'),
    ordered = TRUE)) %>%

  ggplot(data = .) +
  aes(x = V1, y = V2) +
  geom_point(aes(colour = group, fill = group),
    size = 1) +
  guides(colour = guide_legend(override.aes = list(size = 8))) +
  geom_point(data = five_3,
    colour = '#999999',
    size = 1) +
  geom_point(data = placebo_3.3,
    size = 1,
    colour = '#000000') +
  geom_vline(xintercept = mean(five_3$V1),
    colour = pal[1], size = 1) +
  geom_vline(xintercept = mean(placebo_3.3$V1),
    colour = pal[2], size = 1) +
  geom_vline(xintercept = 3, linetype = 2) +
  geom_hline(yintercept = mean(five_3$V2),
    colour = pal[1], size = 1) +
  geom_hline(yintercept = mean(placebo_3.3$V2),
    colour = pal[2], size = 1) +
  scale_y_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_x_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_fill_manual(values = pal) +
  scale_colour_manual(values = pal) +
  labs(title = 'B: Baseline pain threshold = 3',
    caption = 'Parameters: Mean = 5.2, SD = 2.2, r = 0.5') +
  theme(legend.title = element_blank(),
    legend.position = c(0.85, 0.15),
    plot.caption = element_text(size = 14)),
  groupColour = TRUE,
  groupFill = TRUE)
```

B: Baseline pain threshold = 3



Parameters: Mean = 5.2, SD = 2.2, $r = 0.5$

threshold: 4

```
# Process that data
placebo_3.4 <- five_3 %>%
  filter(V1 >= 4) %>%
  mutate(difference = V1 - V2) %>%
  mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
```

```
diff_3.4 <- groupwiseMean(difference ~ 1,
  data = placebo_3.4,
  R = 2000,
  traditional = FALSE,
  bca = TRUE)

diff_3.4$.id <- 4

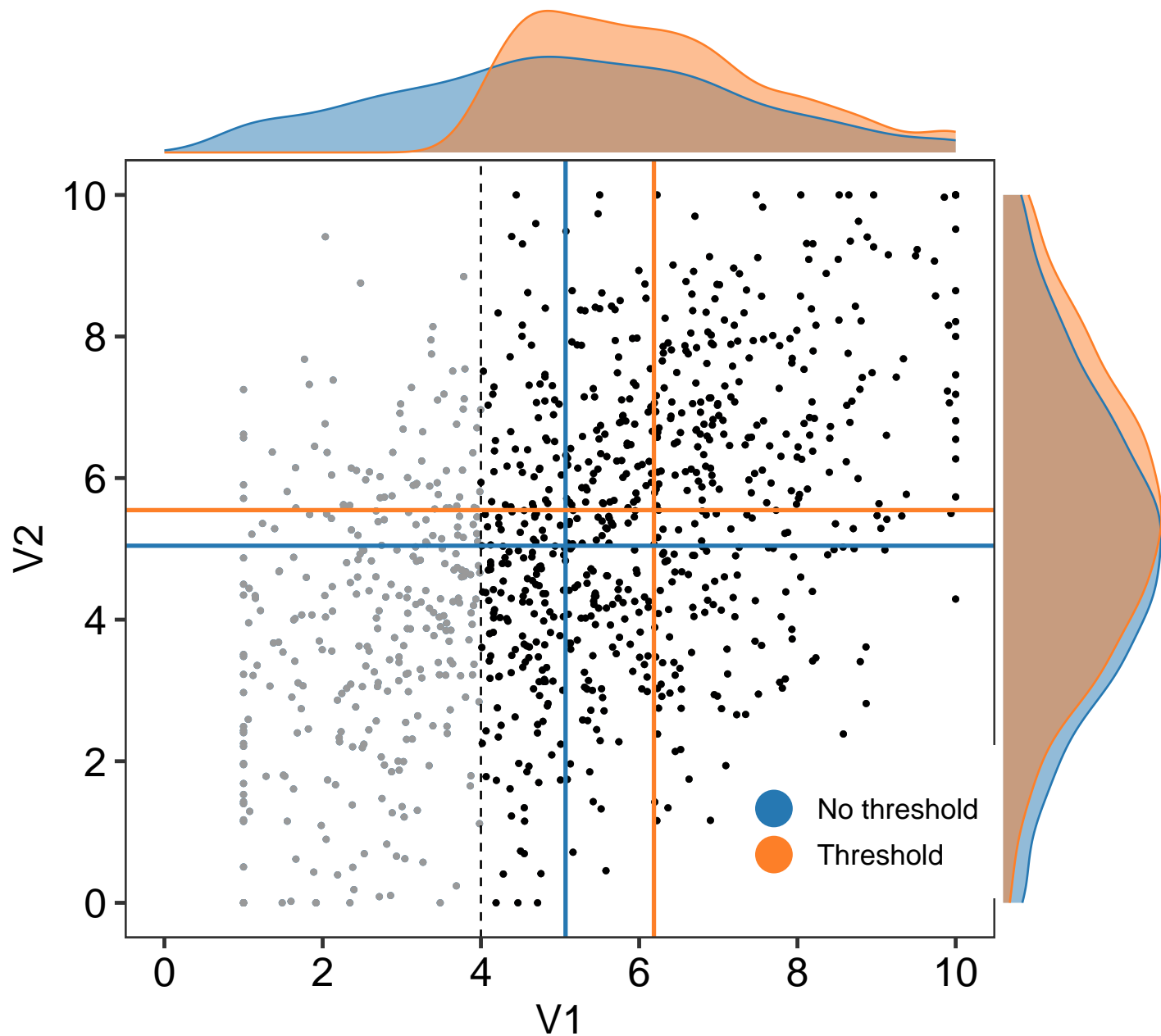
kable(diff_3.4)
```

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
4	687	0.639	0.95	0.507	0.783

```
# Plot the data
ggMarginal(placebo_3.4[, 1:3] %>%
  bind_rows(five_3) %>%
  mutate(group = factor(group,
    levels = c('No threshold', 'Threshold'),
    ordered = TRUE)) %>%

  ggplot(data = .) +
  aes(x = V1, y = V2) +
  geom_point(aes(colour = group, fill = group),
    size = 1) +
  guides(colour = guide_legend(override.aes = list(size = 8))) +
  geom_point(data = five_3,
    colour = '#999999',
    size = 1) +
  geom_point(data = placebo_3.4,
    size = 1,
    colour = '#000000') +
  geom_vline(xintercept = mean(five_3$V1),
    colour = pal[1], size = 1) +
  geom_vline(xintercept = mean(placebo_3.4$V1),
    colour = pal[2], size = 1) +
  geom_vline(xintercept = 4, linetype = 2) +
  geom_hline(yintercept = mean(five_3$V2),
    colour = pal[1], size = 1) +
  geom_hline(yintercept = mean(placebo_3.4$V2),
    colour = pal[2], size = 1) +
  scale_y_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_x_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_fill_manual(values = pal) +
  scale_colour_manual(values = pal) +
  labs(title = 'C: Baseline pain threshold = 4',
    caption = 'Parameters: Mean = 5.2, SD = 2.2, r = 0.5') +
  theme(legend.title = element_blank(),
    legend.position = c(0.85, 0.15),
    plot.caption = element_text(size = 14)),
  groupColour = TRUE,
  groupFill = TRUE)
```

C: Baseline pain threshold = 4



Parameters: Mean = 5.2, SD = 2.2, $r = 0.5$

threshold: 5

```
# Process that data
placebo_3.5 <- five_3 %>%
  filter(V1 >= 5) %>%
  mutate(difference = V1 - V2) %>%
  mutate(group = 'Threshold')

# Set seed
set.seed(2019)

# Calculate the mean (95%CI) difference between V1 and V2
```

```
diff_3.5 <- groupwiseMean(difference ~ 1,
  data = placebo_3.5,
  R = 2000,
  traditional = FALSE,
  bca = TRUE)

diff_3.5$.id <- 5

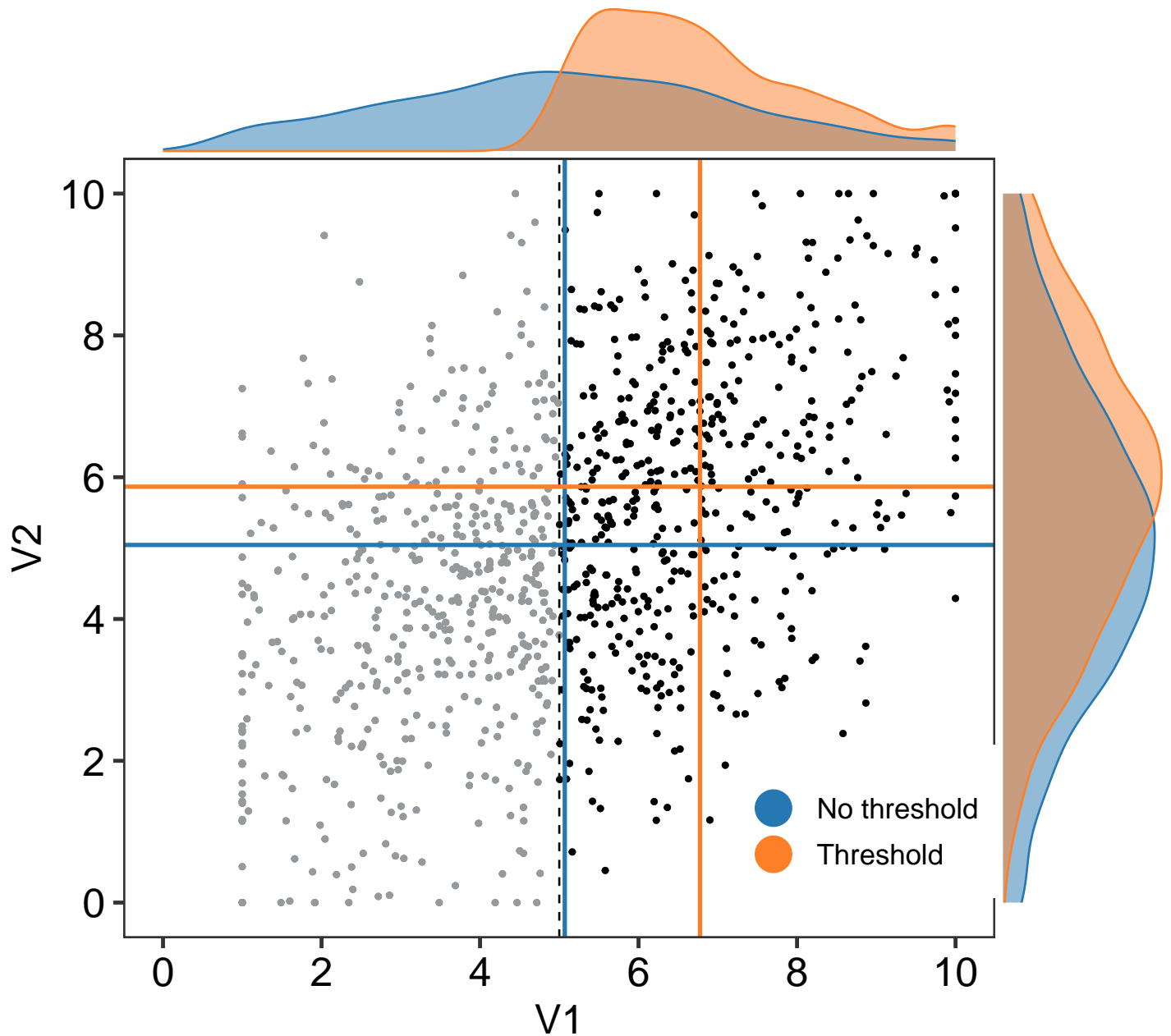
kable(diff_3.5)
```

.id	n	Mean	Conf.level	Bca.lower	Bca.upper
5	508	0.909	0.95	0.731	1.1

```
# Plot the data
ggMarginal(placebo_3.5[, 1:3] %>%
  bind_rows(five_3) %>%
  mutate(group = factor(group,
    levels = c('No threshold', 'Threshold'),
    ordered = TRUE)) %>%

  ggplot(data = .) +
  aes(x = V1, y = V2) +
  geom_point(aes(colour = group, fill = group),
    size = 1) +
  guides(colour = guide_legend(override.aes = list(size = 8))) +
  geom_point(data = five_3,
    colour = '#999999',
    size = 1) +
  geom_point(data = placebo_3.5,
    size = 1,
    colour = '#000000') +
  geom_vline(xintercept = mean(five_3$V1),
    colour = pal[1], size = 1) +
  geom_vline(xintercept = mean(placebo_3.5$V1),
    colour = pal[2], size = 1) +
  geom_vline(xintercept = 5, linetype = 2) +
  geom_hline(yintercept = mean(five_3$V2),
    colour = pal[1], size = 1) +
  geom_hline(yintercept = mean(placebo_3.5$V2),
    colour = pal[2], size = 1) +
  scale_y_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_x_continuous(limits = c(0, 10),
    breaks = c(0, 2, 4, 6, 8, 10)) +
  scale_fill_manual(values = pal) +
  scale_colour_manual(values = pal) +
  labs(title = 'D: Baseline pain threshold = 5',
    caption = 'Parameters: Mean = 5.2, SD = 2.2, r = 0.5') +
  theme(legend.title = element_blank(),
    legend.position = c(0.85, 0.15),
    plot.caption = element_text(size = 14)),
  groupColour = TRUE,
  groupFill = TRUE)
```

D: Baseline pain threshold = 5



Parameters: Mean = 5.2, SD = 2.2, $r = 0.5$

Publication plots

```
# Plot 1
shift_3 <- five_3V1.df %>%
  bind_rows(five_3V2.df) %>%
  ggplot(data = .) +
  aes(y = mean,
       x = cutoff2,
       fill = time) +
  geom_hline(yintercept = 5.2,
             linetype = 2) +
  geom_point(shape = 21,
```



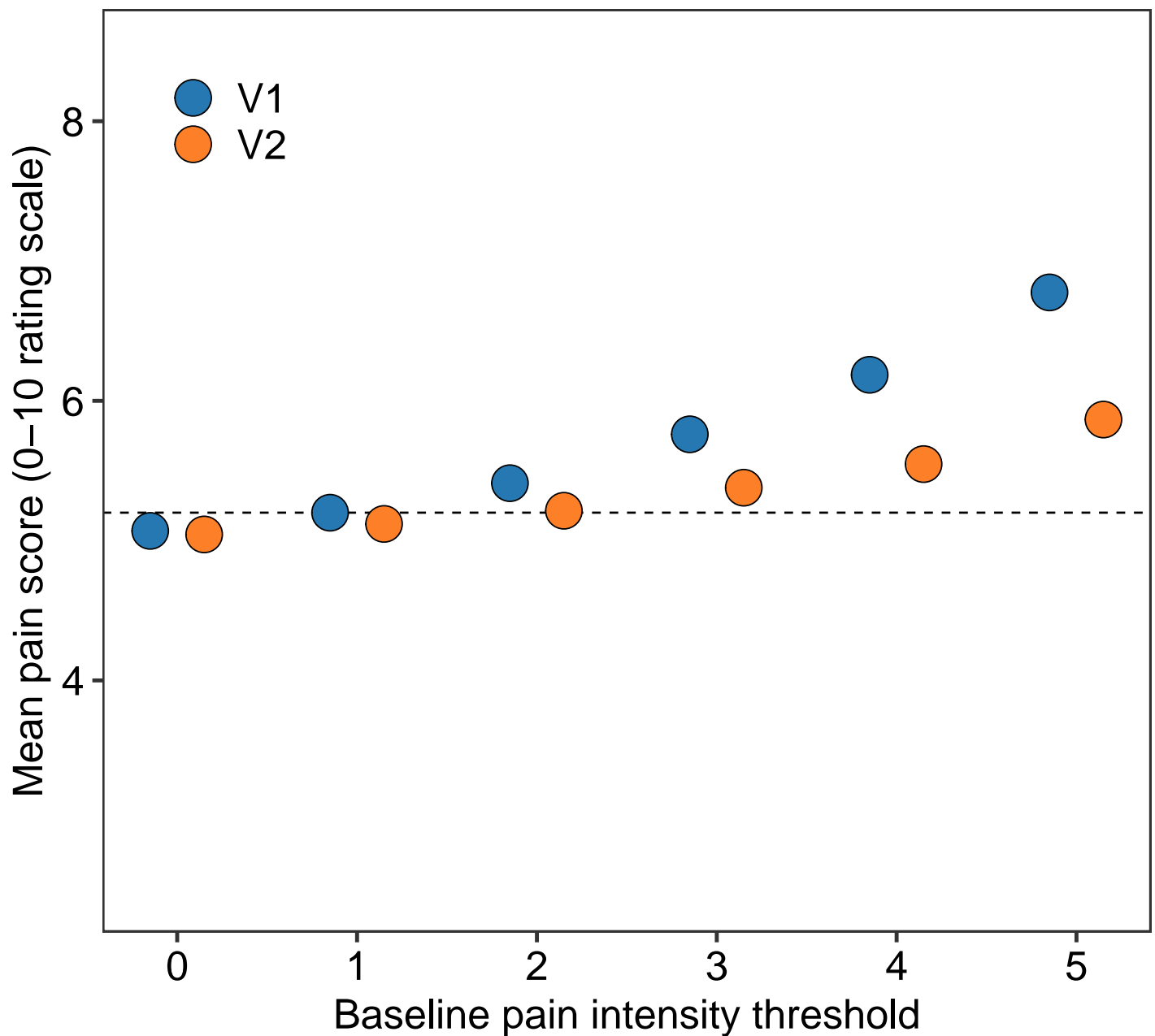
```

size = 8) +
labs(title = 'C',
      subtitle = 'Parameters: Mean = 5.2, SD = 2.2, r = 0.5',
      x = 'Baseline pain intensity threshold',
      y = 'Mean pain score (0-10 rating scale)') +
scale_x_continuous(breaks = 0:5) +
scale_y_continuous(limits = c(2.5, 8.5)) +
scale_fill_manual(values = pal) +
theme(legend.title = element_blank(),
      legend.position = c(0.12, 0.89),
      legend.text = element_text(size = 20)); shift_3

```

C

Parameters: Mean = 5.2, SD = 2.2, r = 0.5



```

# Plot 2
# Bind diff_*. dataframes

```

```

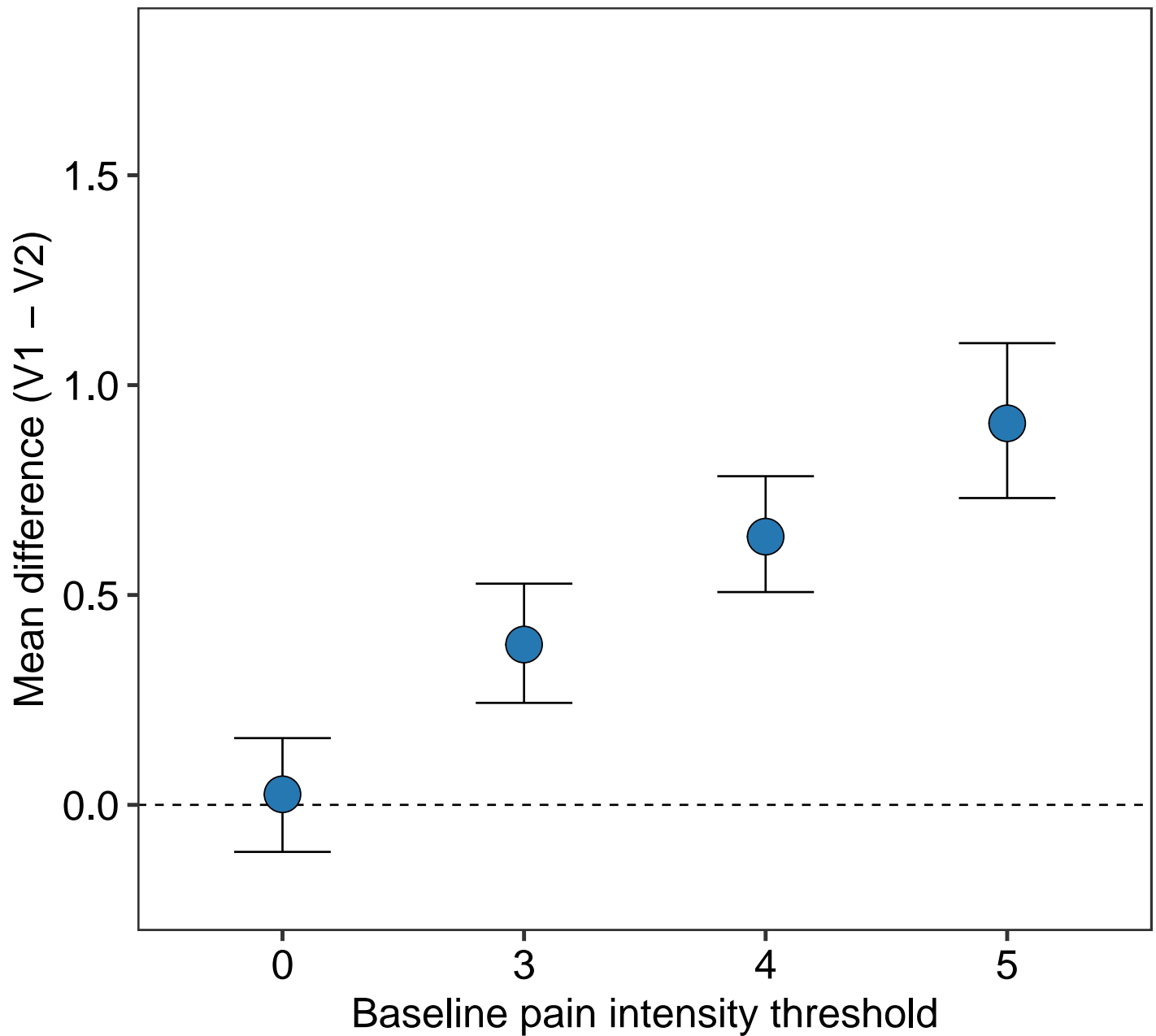
diff_all_3 <- diff_3.0 %>%
  bind_rows(diff_3.3, diff_3.4, diff_3.5)

pp_3 <- diff_all_3 %>%
  mutate(Threshold = factor(.id)) %>%
  ggplot(data = .) +
  aes(x = Threshold,
      y = Mean,
      ymin = Bca.lower,
      ymax = Bca.upper) +
  geom_hline(yintercept = 0,
             linetype = 2) +
  geom_errorbar(width = 0.4) +
  geom_point(shape = 21,
             fill = pal[[1]],
             size = 8) +
  labs(title = 'C',
       subtitle = 'Parameters: Mean = 5.2, SD = 2.2, r = 0.5',
       x = 'Baseline pain intensity threshold',
       y = 'Mean difference (V1 - V2)') +
  scale_y_continuous(limits = c(-0.2, 1.8)); pp_3

```

C

Parameters: Mean = 5.2, SD = 2.2, $r = 0.5$



Publication composite plots

```
shift_4 <- shift_1 + shift_2 + shift_3
ggsave('figures/5.2_0.5a.png', shift_4, width = 17, height = 7)

pp_4 <- pp_1 + pp_2 + pp_3
ggsave('figures/5.2_0.5b.png', pp_4, width = 17, height = 7)
```

Session information

```
sessionInfo()
```

```
## R version 3.6.1 (2019-07-05)
## Platform: x86_64-apple-darwin15.6.0 (64-bit)
## Running under: macOS Mojave 10.14.6
##
## Matrix products: default
## BLAS:   /Library/Frameworks/R.framework/Versions/3.6/Resources/lib/libRblas.0.dylib
## LAPACK: /Library/Frameworks/R.framework/Versions/3.6/Resources/lib/libRlapack.dylib
##
## locale:
## [1] en_US.UTF-8/en_US.UTF-8/en_US.UTF-8/C/en_US.UTF-8/en_US.UTF-8
##
## attached base packages:
## [1] stats      graphics  grDevices  utils      datasets  methods    base
##
## other attached packages:
## [1] patchwork_0.0.1  knitr_1.25      MBESS_4.6.0     ggExtra_0.9
## [5] rcompanion_2.3.7 MASS_7.3-51.4   magrittr_1.5     forcats_0.4.0
## [9] stringr_1.4.0    dplyr_0.8.3     purrr_0.3.2     readr_1.3.1
## [13] tidyr_1.0.0      tibble_2.1.3    ggplot2_3.2.1   tidyverse_1.2.1
##
## loaded via a namespace (and not attached):
## [1] nlme_3.1-141      matrixStats_0.55.0 lubridate_1.7.4
## [4] httr_1.4.1        tools_3.6.1        backports_1.1.5
## [7] R6_2.4.0          nortest_1.0-4      lazyeval_0.2.2
## [10] colorspace_1.4-1 withr_2.1.2         tidyselect_0.2.5
## [13] compiler_3.6.1    cli_1.1.0          rvest_0.3.4
## [16] expm_0.999-4      xml2_1.2.2         sandwich_2.5-1
## [19] labeling_0.3      scales_1.0.0       lmtest_0.9-37
## [22] mvtnorm_1.0-11    multcompView_0.1-7 digest_0.6.21
## [25] rmarkdown_1.16    pkgconfig_2.0.3    htmltools_0.4.0
## [28] fastmap_1.0.1     highr_0.8          rlang_0.4.0
## [31] readxl_1.3.1      rstudioapi_0.10    shiny_1.4.0
## [34] generics_0.0.2    zoo_1.8-6          jsonlite_1.6
## [37] modeltools_0.2-22 Matrix_1.2-17      Rcpp_1.0.2
## [40] DescTools_0.99.29 munsell_0.5.0      lifecycle_0.1.0
## [43] stringi_1.4.3     multcomp_1.4-10    yaml_2.2.0
## [46] plyr_1.8.4        grid_3.6.1         parallel_3.6.1
## [49] promises_1.1.0    crayon_1.3.4       miniUI_0.1.1.1
## [52] lattice_0.20-38   haven_2.1.1        splines_3.6.1
## [55] hms_0.5.1         zeallot_0.1.0      pillar_1.4.2
## [58] EMT_1.1           boot_1.3-23        codetools_0.2-16
## [61] stats4_3.6.1      glue_1.3.1         evaluate_0.14
## [64] modelr_0.1.5      vctrs_0.2.0        httpuv_1.5.2
## [67] cellranger_1.1.0  gtable_0.3.0       assertthat_0.2.1
## [70] xfun_0.10         mime_0.7            coin_1.3-1
## [73] libcoin_1.0-5     xtable_1.8-4       broom_0.5.2
## [76] later_1.0.0       survival_2.44-1.1  TH.data_1.0-10
```