House prices

1) Implement by hand equations of derivative using LaTeX (I will use similar format in LibreOffice/ODF, sorry)

$$f_{x} = \frac{\partial f}{\partial x} = \lim_{h \to 0} \frac{f(x+h, y) - f(x, y)}{h}$$
 why did I wrote them here?

$$f_{x} = \frac{\partial f}{\partial y} = \lim_{h \to 0} \frac{f(x, y+h) - f(x, y)}{h}$$

2) Writing equations for housings:
$$dw \, linear : \frac{\delta}{\delta \, W} [\, W \cdot x + b\,] = x$$
$$dx \, linear : \frac{\delta}{\delta \, x} [\, W \cdot x + b\,] = W$$
$$db \, linear : \frac{\delta}{\delta \, b} [\, W \cdot x + b\,] = 1$$

3) Cost function

We will use mean squared error cost function:

$$J(\theta_0, \theta_1) = L_{MSE} = \frac{1}{N} \cdot \sum_{i=0}^{N} (h_{\theta}(x_i) - y_i)^2$$

where $h_{\theta}(x_i) = \theta_0 + \theta_1 \cdot x_i$ (is our model)

We need to minimize cost function's result.

4) Gradient descent

The goal of this is to update θ_0 , b and θ_1 , W to minimize cost function result.

$$\begin{aligned} \boldsymbol{\theta}_{0} &:= \boldsymbol{\theta}_{0} - \boldsymbol{\alpha} \cdot \frac{\partial}{\partial \boldsymbol{\theta}_{0}} J(\boldsymbol{\theta}_{0}, \boldsymbol{\theta}_{1}) \\ \boldsymbol{b} &:= \boldsymbol{b} - \boldsymbol{\alpha} \cdot \frac{\partial}{\partial \boldsymbol{b}} J(\boldsymbol{b}, \boldsymbol{W}) \end{aligned}$$

$$\begin{aligned} &\boldsymbol{\theta}_{1} \!:=\! \boldsymbol{\theta}_{1} \!-\! \boldsymbol{\alpha} \!\cdot\! \! \frac{\partial}{\partial \boldsymbol{\theta}_{1}} J(\boldsymbol{\theta}_{0}, \! \boldsymbol{\theta}_{1}) \\ &\boldsymbol{W} \!:=\! \boldsymbol{W} \!-\! \boldsymbol{\alpha} \!\cdot\! \! \frac{\partial}{\partial \boldsymbol{W}} J(\boldsymbol{b}, \! \boldsymbol{W}) \end{aligned}$$

but to simultaneously update both variables we need to assign them to temporary variables first, so b doesn't affect calculation of the W.

 α - is a learning rate, which defines how fast we are going to change b and W.

By intuition what is going to happen – partial derivative of the cost function will be a positive slope (will return a positive number) if the mse will on the right side of the local minima, as a result we will subtract a slope value multiplied by learning rate from W (or b). Otherwise we will add it. In ideal situation once MSE is 0 – we don't move anymore.

Sorry, I still don't get how to write the rest. I have watched tons of Khan Academy videos on youtube regarding derivatives. I have watched lessons on Coursera regarding Machine Learning, Cost function, Gradient Descent... All the different notations of the same things drive me crazy.