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**Influence of a mixture composition
and initial pressure on the
auto-ignition temperature of
methane-air and hydrogen-air
mixture**

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Computational Methods in Combustion

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Contents

1 Introduction

Autoignition occurs when a mixture of gases or vapors ignites spontaneously with no external ignition source and after reaching a certain temperature, the autoignition temperature. The autoignition temperature is not an intrinsic property of the gases or vapors (Kanury 1975) but is the lowest temperature in a system where the rate of heat evolved from the gases or vapors increases beyond the rate of heat loss to the surroundings, resulting in ignition. The autoignition temperature of a mixture of gases or vapors is affected by pressure, vessel shape and volume, surface activity, contaminants, flow rate, reaction rate, droplet and mist formation, gravity, and reactant concentration (Benz et al. 1988).

In general, decreased pressure leads to an increased autoignition temperature (Furno, Imhof, and Kuchta 1968; Benz and Phippen 1980; Bodurtha 1980), whereas increased vessel size leads to a decreased autoignition temperature (Setchkin 1954). For fuels in general, the autoignition temperature is not very sensitive to fuel concentration except at near limiting concentrations (Furno et al. 1968); however, some studies with hydrazine show that off-stoichiometric mixtures lead to increased autoignition temperatures (Miller and Schluter 1978). The effect of catalytic surfaces on autoignition temperature varies with the system. Some studies show that catalytic surfaces in some systems increase the autoignition temperature (Lewis and von Elbe 1961; Miller and Schluter 1978), whereas others indicate that the reaction between the fuel and the surface material leads to a decreased autoignition temperature (Scott, Burns, and Lewis 1949; Stevens and Benz 1978).

Autoignition or the kindling point is described as the lowest temperatures at which a material will spontaneously ignite under normal ambient condition without an external initiator such as a flame or a spark. These temperatures are critical especially for the shipping, storage, and use of various plastic objects and the associated fire hazards. Autoignition temperatures are of more prominence for liquid materials and gases than solid materials.

2 Auto-ignition theory

The autoignition temperature (AIT) of a gaseous mixture of fuel and oxidizer is the lowest possible temperature at which the mixture ignites spontaneously i.e. without an outside source of ignition such as an electrical spark or an open flame. The enthalpy of the mixture at autoignition temperature is high enough to serve as a source of activation energy for the process of combustion.

2.1 Expressing the composition of the mixture

The ratio of the mixture's fuel-to-oxidizer ratio to stoichiometric fuel-to-air ratio is called an equivalence ratio of said mixture - Φ .

$$FAR = \frac{n_{fuel}}{n_{air}}$$

$$n = \text{number of moles}$$

$$\phi = \frac{FAR}{FAR_{stoichiometry}}$$

Φ greater than one means that the mixture is rich and not all of the the fuel undergoes combustion due to lack of oxidizer. Alternatively, Φ lower than one indicates a lean mixture which has an excess of oxidizer.

Another way to describe the composition of a mixture is to use molar fractions. Molar fraction is the ratio of the number of moles of any given component to the overall number of moles of a mixture.

$$X_{fuel}[\%] = n_{fuel}/n_{mixture}$$

Determining the auto-ignition temperature through analysis of the chain reaction alone is impossible. Therefore using experimental methods and simulations are necessary.

2.2 Methane

In the case of methane, which is the shortest hydrocarbon in terms of average carbon chain length, this activation energy is the highest of all hydrocarbons. Longer and therefore heavier (per unit volume) hydrocarbons tend to auto-ignite before methane does.

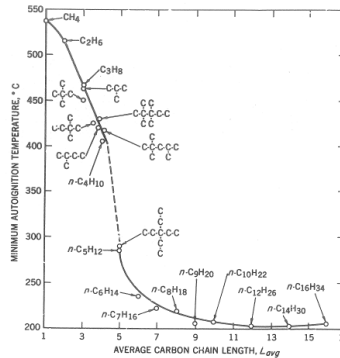
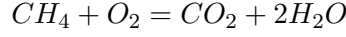
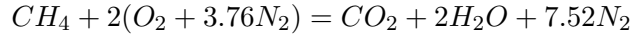


Figure 2.2.1: AIT as a function of carbon chain length (Zabetakis^[4])

Mentioned combustion process is a chain of hundreds of different chemical reactions. The initial reactions heat up the mixture through slow oxidation which incites faster reactions which cause the actual autoignition. The chain could be described with one global equation:



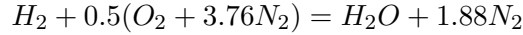
or in case of combustion in air:



As shown in the equation, in case of methane-air combustion, for every mole of methane 9.52 moles of air are necessary for stoichiometric combustion.

2.3 Hydrogene

The reaction of hydrogene's combustion in air is as follows:



For every one mole of hydrogene 2.38 moles of air are needed.

3 Simulation

3.1 Methodology

The influence of initial parameters such as chemical composition and absolute pressure was examined utilizing Cantera environment for chemical kinetics calculations in Python. The simulation is run inside a reactor network including a singular 0-dimensional adiabatic reactor.

A perfectly homogeneous fuel-air mixture is placed inside at $t=0$ and its parameters i.e. molar fractions of its components, initial temperature and initial absolute pressure are set. Subsequently, simulation time advances by 600s which according to previous researches is predominantly long enough for auto-ignition to occur. Only one time step was used in order to minimize computing time since autoignition delay time is negligible to this simulation.

Autoignition is determined to have had occurred if the temperature inside of the reactor is at least 200K higher than the initial. Every set of parameters resulting in an autoignition is stored for later use in graphs.

The following simulations were carried out:

1. 60% methane in air combustion.
2. 9.5% methane in air combustion (stoichiometric)
3. 60% hydrogen in air combustion
4. 29.5% hydrogen in air combustion (stoichiometric)

The first task of the simulation is to find the autoignition temperature of a mixture as a function of absolute pressure changing from 0.5 bar to 35 bar by calculating the AIT every 0.5 bar.

The second task is to examine how the AIT changes with the equivalence ratio. Pressure of one atmosphere was set while the number of moles changes from 0.1 to 10 with a step of 0.1 moles. It was then converted into equivalence ratios.

Respecting calculation speed, the autoignition temperature is first approximated within a 50K-wide window. Then, more precise calculations take place within that window in order to determine the AIT down to 0.5K.

In order to obtain smoother plots a pressure and temperature step could be reduced at will, but in this way calculations would last longer respectively.

Calculations were repeated for two different molar ratios of methane and hydrogen in air (60% and stoichiometric)

3.2 Code description on example of first simulation

```
#importing necessary libraries
import numpy as np
from cantera import *
import matplotlib.pyplot as plt
from scipy.optimize import curve_fit

#selecting reaction mechanisms
gas = Solution('gri30.xml')

#setting minimal, maximal temperature and two step sizes
Tmin=500
Tmax=1500
temp_step=0.5
temp_step_coarse=50

#setting minimal, maximal pressure and a step size
Pmin=100000
Pmax=3500000
P_step=50000

#setting time step size
time_step=600
```

```

#calculating number of temperature loop iterations for different
    levels of precision
temp_steps_coarse_no=int(((Tmax-Tmin) // temp_step_coarse)+1)
temp_steps_no=int((temp_step_coarse// temp_step)+1)

#calculating number of pressure loop iterations
P_steps_no=((Pmax-Pmin)//P_step)+1

#creating storage arrays
autoign_temp = []
autoign_P=[]
autoign_temp_X=[]
autoign_X=[]
autoign_X_fr=[]
autoign_X_FAR=[]

#initializing stoichiometric fuel-to-air ratio
FARst=0.5/4.76

#TASK1 – AIT as a function of initial pressure
print ("Task_1")
#setting initial pressure for the pressure loop
P=Pmin

#pressure loop start
for p in range (0, P_steps_no):

    #setting default state of trigger variable
    auto=0

    #setting initial temperature for the approximate temperature
    loop
    T=Tmin

    #approximate temperature loop start
    for tc in range(0,temp_steps_coarse_no):
        #creating the gas, the reactor and the reactor network
        #for 4.76 moles of air, 7.14 moles of methane translate
        to 60% molar fraction
        gas.TPX = T, P, 'CH4:7.14,O2:1,N2:3.76'
        r=IdealGasReactor(gas)
        net=ReactorNet([r])

        #advancing simulation time
        net.advance(time_step)

        #checking whether autoignition occurred
        if (r.T-T)>200:
            #setting the mixture's temperature to the lower
            limit of the approximate temperature window
            T=temp_step_coarse

```

```

#precise temperature loop start
for t in range(0,temp_steps_no):
    #creating the gas, the reactor and the reactor
    #network for precise calculations
    #temperature and pressure change with iterations
    #, mixture composition is constant
    gas.TPX = T, P, 'CH4:7.14,O2:1,N2:3.76'
    r=IdealGasReactor(gas)
    net=ReactorNet([r])

    #advancing simulation time
    net.advance(time_step)

    #checking whether autoignition occurred
    if (r.T-T)>200:
        #setting trigger variable value to break the
        #outer loop
        auto=1
        #storing current initial temperature and
        #pressure in arrays
        autoign_temp.append(T)
        autoign_P.append(P/1000000)
        #printing current initial conditions
        print("X: 7.14, T: ", '%.1f' % T, "P: ", P)
        #breaking the precise temperature loop, AI
        #occured
        #higher temperatures do not need to be
        #verified
        break
    #raising the initial precise temperature in case
    #autoignition didn't occur
    T+=temp_step

    #breaking the approximate temperature loop if AI occurred
    #higher temperatures do not need to be verified
    if auto==1:
        break
    #raising the initial approximate temperature in case
    #autoignition didn't occur
    T+=temp_step_coarse
    #raising the pressure
    P+=P_step

#storing results as x, y for clarity
x = autoign_temp
y = autoign_P

#setting plot size
plt.figure(figsize=(7,5))

#creating, labeling and saving the Initial Pressure vs AIT plot
plt.plot(x, y, '-', color='orange')

```



```

plt.grid()
plt.xlabel("Autoignition_Temperature_[K]")
plt.ylabel(r'Initial_Pressure_[MPa]')
plt.savefig('1.png', bbox_inches='tight')
plt.show()

#TASK2 – AIT as a function of equivalence ratio
print ("_____")
print ("Task_2")
#setting minimal, maximal number of moles of methane, step size
X_min=0.1
X_max=10
X_step=0.1

#calculating number of molar loop iterations
X_steps_no=int((X_max-X_min)//X_step+1)

#setting initial number of moles
X=X_min

#changing the precision of calculations – raising the size of
    temperature step
#calculating new number of steps
temp_step=0.5
temp_steps_no=int((temp_step-coarse// temp_step)+1)

#molar loop start
for x in range(0, X_steps_no):
    #setting default state of trigger variable
    auto = 0
    #setting initial temperature for the approximate temperature
        loop
    T=Tmin
    #approximate temperature loop start
    for tc in range(0,temp_steps_coarse-no):
        #creating the gas, the reactor and the reactor network
            for approximate calculations
        #temperature mixture composition change with iterations,
            pressure is constant and equal to one atmosphere
        #calculations look just like in Task 1
        gas.TPX = T, one_atm, {'CH4':X, 'O2':1, 'N2':3.76}
        r=IdealGasReactor(gas)
        net=ReactorNet([r])

        net.advance(time_step)

        if (r.T-T)>200:

            T=temp_step_coarse

        for t in range(0,temp_steps_no):
            gas.TPX = T, one_atm, {'CH4':X, 'O2':1, 'N2':3.76}

```

```

        r=IdealGasReactor(gas)
        net=ReactorNet([r])
        net.advance(time_step)
        if (r.T-T)>200:
            auto=1
            autoign_temp_X.append(T)
            autoign_X.append(X/(X+4.76))
            autoign_X_FAR.append((X/4.76)/FARst)
            print("X: ", '%.1f' % X, "T: ", T, "P: ",
                  '%.0f' % one_atm)
            break
        T+=temp_step
    if auto==1:
        break

    T+=temp_step_coarse
    X+=X_step

#creating plots
y2 = autoign_temp_X
x2 = autoign_X

plt.figure(figsize=(7,5))
plt.plot(x2, y2, '-', color='orange')
plt.grid()
plt.xlabel(r'Molar_fraction_of_methane')
plt.ylabel("Autoignition_temperature_[K]")
plt.savefig('2.png', bbox_inches='tight')
plt.show()

y3 = autoign_temp_X
x3 = autoign_X_FAR

plt.figure(figsize=(7,5))
plt.plot(x3, y3, '-', color='orange')
plt.grid()
plt.xlabel(r'Equivalence_ratio')
plt.ylabel("Autoignition_temperature_[K]")
plt.savefig('3.png', bbox_inches='tight')
plt.show()

```

4 Results

4.1 AIT as a function of initial pressure

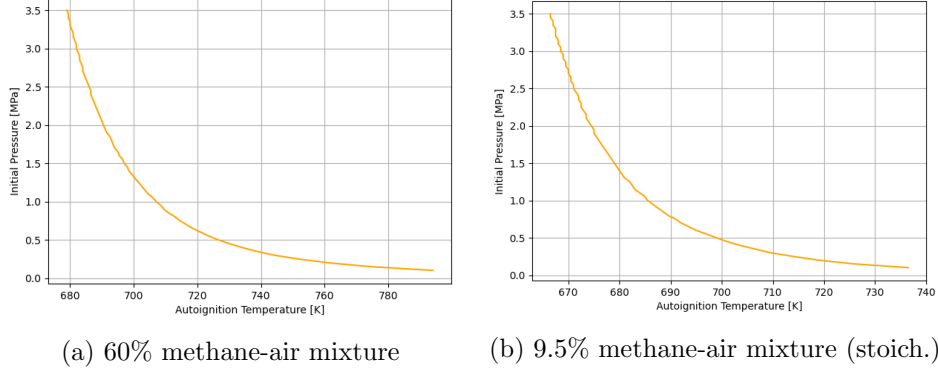


Figure 4.1.1: Autoignition temperature as function of initial pressure in methane-air mixture

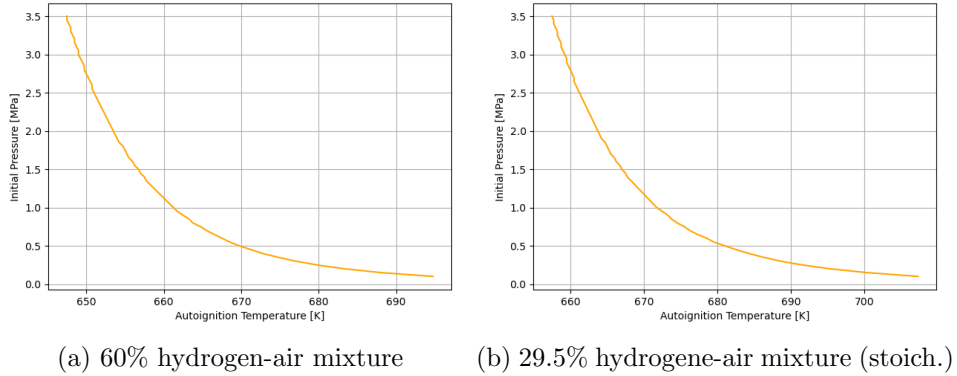


Figure 4.1.2: Autoignition temperature as function of initial pressure in hydrogen-air mixture

As expected, the relationship between autoignition temperature and initial total pressure of mixture is exponential. As the pressure increases, the temperature drops. The first two plots relate to methane-air mixture in different composition – first one is 60% and second 9.5% (stoichiometric). For example, for the initial pressure of 1MPa, from the left plot we observe the AIT of 708K and for the right plot – 686K. It suggests, that in case of methane the richer mixture (Φ more than one) increases AIT, which is beneficial from the point of view of storing flammable methane.

These findings correspond to the results of Frederik Norman's study^[3] presented on the Fig. 4.1.3

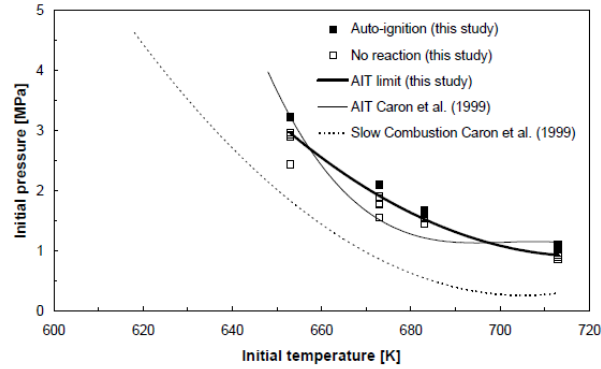
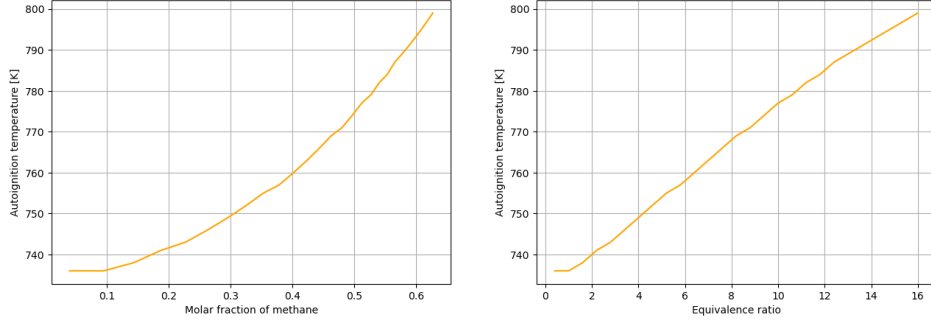


Figure 4.1.3: Results of Norman’s study. Initial pressure vs AIT

The study determined that the auto-ignition temperature of 60% methane-air mixture at pressure of 1MPa is about 715K.

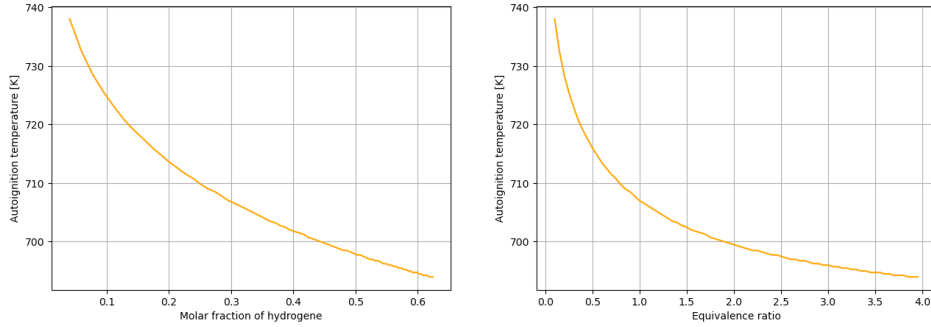
In case of the hydrogen, the AIT is lower comparing to the same molar fractions in methane-air mixture. This means that hydrogen is more dangerous to be stored. From figure 4.1.2 (a) we can see that for the initial pressure of 1MPa the AIT is about 661K, whilst from figure 4.1.2 (b) for the same pressure the AIT stands at 672K. In other words, richer mixture decreases AIT. This informs us, that hydrogen should be stored in lower molar fractions, on the contrary to methane.

4.2 AIT as a function of mixture's composition



(a) AIT as a function of molar fraction (b) AIT as a function of equivalence ratio

Figure 4.2.1: AIT as a function of molar fractions for methane combustion in air



(a) AIT as a function of molar fraction (b) AIT as a function of equivalence ratio

Figure 4.2.2: AIT as a function of molar fractions for hydrogen combustion in air

This simulation confirms the results obtained in chapter 4.1. The growth of molar fraction in methane-air mixture increases AIT, oppositely to hydrogen-air mixture. The character of the plot 4.2.1 (a) is exponential, but the relation between AIT and equivalence ratio is linear (plot 4.2.1 (b)).

On the other hand, on the example of hydrogen we can notice two exponential correlations. For the hydrogen the AIT is the lowest (around 700K) when equivalence ratio is equal to 4.0. For methane the lowest autoignition temperature is 735K for molar fraction near stoichiometric.

5 Conclusions

The purpose of this report was to examine the influence of the initial total pressure and mixture composition on the autoignition temperature of two flammable mixtures on the examples of methane and hydrogen.

The results are unambiguous. The pressure of the mixture ought to close to atmospheric in order to avoid auto-ignition. Gaseous methane is more exposed to auto-ignition with a great amount of oxidizer, entirely oppositely to hydrogen.

Knowing about auto-ignition temperature is very important when it comes to storage of flammable gases.

6 References

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