Final Project Submission

Student name: Kamile YagciStudent pace: self paced

• Scheduled project review date/time:

· Instructor name: Claude Fried

Blog post URL:

King County House Sales Study

Overview

In this project, I will analyze the King County House Sales. I will use the Multiple Linear Regression to model the data and predict the house sale prices in King County.

Business Problem

The Windermere Real Estate Agency hired me to develop a model to predict the house sale prices in King County. The agency plans to use the results of this study when advising their customers/homeowners on determining the value of their houses. They believe that the pricing the house correctly will increase the efficiency of sales. The agency also would like to learn about the effect of renovations on house sale prices, so they can advise the customers to do renovation or not.

Questions:

- What are the main predictors for House Sale Price?
- Create a model to predict the House Sale Price.
- Do house renovation affects the Sale Price?

Data

I will use the King County Data for this study. The data contain the information about the houses sold in 2014-2015.

Let's load data and take a look.

```
In [1]: #Import Libraries
   import pandas as pd
   import matplotlib.pyplot as plt
   %matplotlib inline
   import seaborn as sns
   import numpy as np
   from sklearn.linear_model import LinearRegression
```

```
In [2]: df = pd.read_csv('data/kc_house_data.csv')
    df.head()
```

Out[2]:

	id	date	price	bedrooms	bathrooms	sqft_living	sqft_lot	floors	waterfront
0	7129300520	10/13/2014	221900.0	3	1.00	1180	5650	1.0	NaN
1	6414100192	12/9/2014	538000.0	3	2.25	2570	7242	2.0	0.0
2	5631500400	2/25/2015	180000.0	2	1.00	770	10000	1.0	0.0
3	2487200875	12/9/2014	604000.0	4	3.00	1960	5000	1.0	0.0
4	1954400510	2/18/2015	510000.0	3	2.00	1680	8080	1.0	0.0

5 rows × 21 columns

```
In [3]: #Checking the house sold date
    df['date']=pd.to_datetime(df['date'])
    df.sort_values(by=['date'], ascending=False)
```

Out[3]:

	id	date	price	bedrooms	bathrooms	sqft_living	sqft_lot	floors	waterfront
16580	9106000005	2015- 05-27	1310000.0	4	2.25	3750	5000	2.0	0.0
13040	5101400871	2015- 05-24	445500.0	2	1.75	1390	6670	1.0	0.0
5632	7923600250	2015- 05-15	450000.0	5	2.00	1870	7344	1.5	0.0
15797	7129304540	2015- 05-14	440000.0	5	2.00	1430	5600	1.5	0.0
927	8730000270	2015- 05-14	359000.0	2	2.75	1370	1140	2.0	0.0
7316	2202500290	2014- 05-02	435000.0	4	1.00	1450	8800	1.0	0.0
19661	7853220390	2014- 05-02	785000.0	5	3.25	3660	11995	2.0	0.0
6418	2011000010	2014- 05-02	257950.0	3	1.75	1370	5858	1.0	NaN
10689	2738600140	2014- 05-02	499950.0	4	2.50	2860	3345	2.0	0.0
4959	7525000080	2014- 05-02	588500.0	3	1.75	2330	14892	1.0	0.0

21597 rows × 21 columns

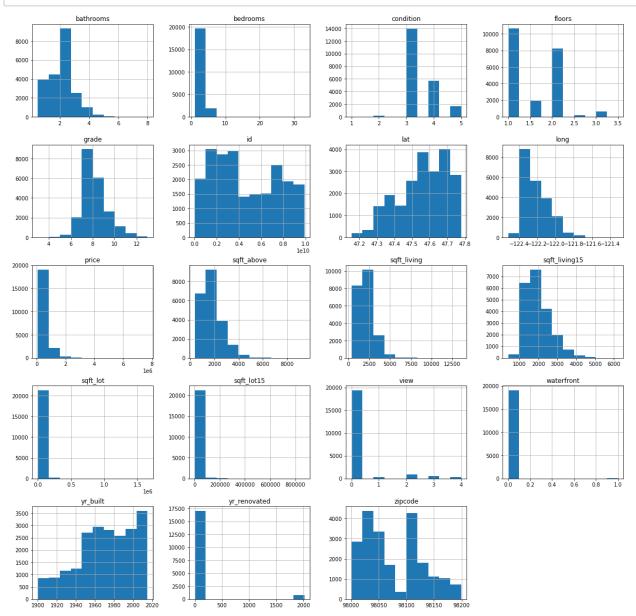
The data includes houses sold between May 2014 to May 2015. It is about 12 months, 1 full year. Let's list the types of the variables.

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 21597 entries, 0 to 21596
Data columns (total 21 columns):
Column Non-Null Count December 1975

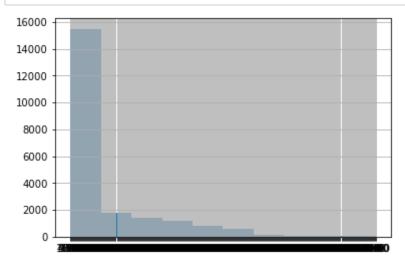
```
Non-Null Count Dtype
___
                                 ____
    -----
                  _____
0
    id
                  21597 non-null int64
1
    date
                  21597 non-null datetime64[ns]
                  21597 non-null float64
2
    price
 3
    bedrooms
                  21597 non-null int64
    bathrooms
                  21597 non-null float64
                  21597 non-null int64
5
    sqft_living
6
    sqft_lot
                  21597 non-null int64
7
    floors
                  21597 non-null float64
8
                  19221 non-null float64
    waterfront
9
    view
                  21534 non-null float64
                  21597 non-null int64
10 condition
11 grade
                  21597 non-null int64
12 sqft_above
                  21597 non-null int64
13 sqft_basement 21597 non-null object
14 yr built
                  21597 non-null int64
 15 yr_renovated
                  17755 non-null float64
 16 zipcode
                  21597 non-null int64
                  21597 non-null float64
17 lat
18 long
                  21597 non-null float64
19 sqft living15 21597 non-null int64
                  21597 non-null int64
20 sqft lot15
dtypes: datetime64[ns](1), float64(8), int64(11), object(1)
memory usage: 3.5+ MB
```

Let's plot the distributions to get a better understanding on the variables.

In [5]: df.hist(figsize=(20, 20));
plt.savefig('figures/histograms.png')



Why 'sqft_basement' is not plotted?



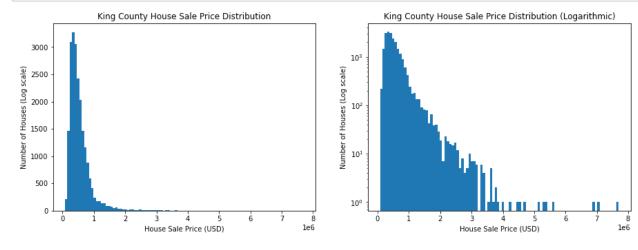
It looks like, there is some problem in 'sqft_basement' data. I'm not planning to use this variable, so I don't intend to dig in the issue.

The target varaible for this study is House Sale Price 'price'. Let's check the distribution closely.

```
In [61]: #Plot Sale price
fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(15, 5))

ax1.hist(df['price'], bins=100)
ax1.set_xlabel("House Sale Price (USD)")
ax1.set_ylabel("Number of Houses (Log scale)")
ax1.set_title("King County House Sale Price Distribution");
#ax1.set_xlim(0, 4000000)

ax2.hist(df['price'], bins=100, log=True)
ax2.set_xlabel("House Sale Price (USD)")
ax2.set_ylabel("Number of Houses (Log scale)")
ax2.set_title("King County House Sale Price Distribution (Logarithmic)");
plt.savefig('figures/priceDist.png')
```



The 'price' looks like a left-skewed normal distribution. There are fewer houses above \$3,000,000. I guess they will be outliers on the data.

Data Cleaning

The Project 2 infomation page recommends to remove these columns to ease the analysis: ['date', 'view', 'sqft_above', 'sqft_basement', 'yr_renovated', 'zipcode', 'lat', 'long', 'sqft_living15', 'sqft_lot15']

I will follow the advise and remove these variables except 'yr_renovated' and maybe 'zipcode'

- 'date' and 'view' are apparently not significant predictors for Sale Price; good to remove
- sqft_above' and 'sqft_basement' will have multicollinearity with 'sqft_living' (see hist plots); so better to remove
- 'lat' and 'long' determine the location; I will use the zipcode for location and so no need for these variables
- 'sqft_living15' and 'sqft_lot15' may have multicollinearity with 'sqft_living' and 'sqft_lot' (see hist plots); OK to remove

One of my business question is about the effect of renovation on sale price; so needs to keep 'yr renovated'

In general, location is an important factor in house prices. I want to take a closer look at 'zipcode', before making a decision on keeping it or not.

```
In [8]: # How many zipcodes?
         df['zipcode'].unique().size
 Out[8]: 70
 In [9]: # Group by zip code and aggragate
         df_zip_sale = df.groupby('zipcode').agg(['mean', 'count'])['price']
         df_zip_sale.columns = ['price_avg', 'count']
In [10]: # Plot
         df.plot.scatter(x='zipcode', y='price', figsize=(12,6), alpha=0.2, label='P
         df_zip_sale['price_avg'].plot(color='red', label='Average Price')
         plt.legend()
         #plt.legend(prop={"size":10})
         plt.savefig('figures/price-vs-zipCode.png')
           8
                                                                             Average Price
                                                                             Price
            7
            6
            5
            3
           2
           1
           0
```

98000

98025

98050

98075

98100

zipcode

98125

98150

98175

98200

```
In [11]: # Sort by average price per zipcode
df_zip_sale.sort_values(by='price_avg', ascending=False).head(10)
```

Out[11]:

price_avg count

zipcode		
98039	2.161300e+06	50
98004	1.356524e+06	317
98040	1.194874e+06	282
98112	1.096239e+06	269
98102	8.996077e+05	104
98109	8.800778e+05	109
98105	8.632289e+05	229
98006	8.599386e+05	498
98119	8.497148e+05	184
98005	8.102897e+05	168

The price vs zipcode graph shows that the house prices peak at few zipcodes. The ordered list also shows that 4 out of 70 zipcodes have higher average sale price than others. How significant is this?

I decided to keep 'zipcode' in my data.

Let's drop the uninterested columns and handle the missing data.

```
In [12]: # Drop columns
         columns_to_delete = ['date', 'view', 'sqft_above', 'sqft_basement', 'lat',
         df2 = df.drop(columns_to_delete, axis=1)
         df2.info()
         <class 'pandas.core.frame.DataFrame'>
         RangeIndex: 21597 entries, 0 to 21596
         Data columns (total 13 columns):
                            Non-Null Count Dtype
          #
              Column
          0
              id
                            21597 non-null
                                            int64
          1
                            21597 non-null float64
              price
          2
             bedrooms
                            21597 non-null int64
          3
            bathrooms
                            21597 non-null float64
          4
             sqft_living
                            21597 non-null int64
          5
            sqft\_lot
                            21597 non-null int64
          6
             floors
                            21597 non-null float64
          7
             waterfront
                            19221 non-null float64
                            21597 non-null int64
          8
            condition
          9
             grade
                            21597 non-null int64
          10 yr_built
                            21597 non-null int64
          11 yr_renovated 17755 non-null
                                            float64
          12 zipcode
                            21597 non-null int64
         dtypes: float64(5), int64(8)
         memory usage: 2.1 MB
In [13]: df2.isna().sum()
Out[13]: id
                            0
         price
                            0
                            0
         bedrooms
                            0
         bathrooms
         sqft living
                            0
         sqft lot
                            0
         floors
                            0
         waterfront
                         2376
         condition
                            0
                            0
         grade
         yr built
                            0
         yr_renovated
                         3842
         zipcode
                            0
         dtype: int64
In [14]: #Check waterfront unique values
         df2['waterfront'].unique()
Out[14]: array([nan, 0., 1.])
         The 'waterfront' nan value most probably means that house is not on the waterfront. It is
```

reasonable to assign zero to missing data for these varaibles.

```
In [15]: df2['waterfront'].fillna(0., inplace=True)
```

The zero and 'nan' values in 'yr_renovated' means that the house is not renovated. I will replace them with the 'yr_built', since yr_built can be considered as the last renovation. However, I will like to keep a booelan variable for 'yr_renovated'.

```
In [17]: df2.head()
```

Out[17]:

	id	price	bedrooms	bathrooms	sqft_living	sqft_lot	floors	waterfront	condition
0	7129300520	221900.0	3	1.00	1180	5650	1.0	0.0	3
1	6414100192	538000.0	3	2.25	2570	7242	2.0	0.0	3
2	5631500400	180000.0	2	1.00	770	10000	1.0	0.0	3
3	2487200875	604000.0	4	3.00	1960	5000	1.0	0.0	5
4	1954400510	510000.0	3	2.00	1680	8080	1.0	0.0	3

```
In [18]: # Fill null with 0, create a boolean column, and replace 0 with yr_built
    df2['yr_renovated'].fillna(0., inplace=True)
    df2['yr_renovated_bool'] = df2['yr_renovated'] != 0
    df2['yr_renovated'].replace(0, df2['yr_built'], inplace=True)
    df2.head()
```

Out[18]:

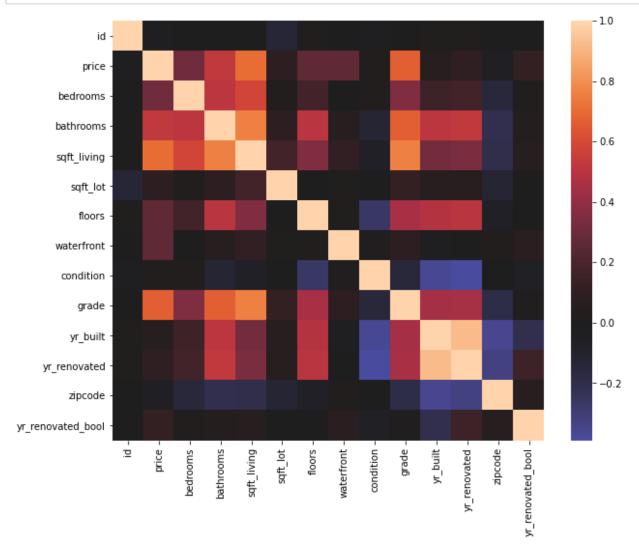
	id	price	bedrooms	bathrooms	sqft_living	sqft_lot	floors	waterfront	condition	!
0	7129300520	221900.0	3	1.00	1180	5650	1.0	0.0	3	
1	6414100192	538000.0	3	2.25	2570	7242	2.0	0.0	3	
2	5631500400	180000.0	2	1.00	770	10000	1.0	0.0	3	
3	2487200875	604000.0	4	3.00	1960	5000	1.0	0.0	5	
4	1954400510	510000.0	3	2.00	1680	8080	1.0	0.0	3	

```
In [19]: df2.isna().sum()
Out[19]: id
                               0
                               0
         price
                               0
         bedrooms
                               0
         bathrooms
                               0
         sqft_living
         sqft_lot
                               0
         floors
                               0
                               0
         waterfront
         condition
                               0
                               0
         grade
                               0
         yr_built
                               0
         yr_renovated
         zipcode
                               0
         yr_renovated_bool
                               0
         dtype: int64
```

Correlation

Let's draw the correlation heat map to see the correlations between varaibles.

```
In [76]: #Plot heatmap
plt.figure(figsize=(10,8))
sns.heatmap(df2.corr(), center=0);
plt.savefig('figures/heatMap.png')
```



Scatter graph shows good correlation between Price and (bedrooms, bathrooms, sqft_living, grade).

There is also correlation among bedrooms, bathrooms, sqft_living, grade. We have to consider multicollinearity effects using them in modeling. I should only use one of them in my model.

There is also high correlation between yr_renovated and yr_built. Again, only one of them can be used in my model.

```
In [21]: # Correlation values between price and other variables
         df2.corr()['price']
Out[21]: id
                              -0.016772
         price
                               1.000000
         bedrooms
                               0.308787
         bathrooms
                               0.525906
         sqft_living
                               0.701917
         sqft_lot
                               0.089876
         floors
                               0.256804
         waterfront
                               0.264306
         condition
                               0.036056
         grade
                               0.667951
         yr_built
                               0.053953
         yr_renovated
                               0.097541
```

The variables that have highest correlation with Sale Price are 'sqft_living' and 'grade'. Definition of these variables:

sqft_living: square footage of the home (continious variable_

-0.053402

0.117543

 grade: overall grade given to the housing unit, based on King County grading system (categorical varible)

hot-encoding for 'zipcode'

zipcode

yr renovated bool

Name: price, dtype: float64

I decided to keep zipcode in my dataframe since I believe location has a considerable effect on sale price. I want to investigate it. Zipcode is a categorical variable, therefore I will use dummy indexing and create a seperate column for each zip code. It will increase the number of columns, but I belive it worths.

```
In [22]: zipcodes = pd.get_dummies(df2['zipcode'], prefix='zip', drop_first=True)
          df3 = pd.concat([df2, zipcodes], axis=1)
          df3.drop('zipcode', axis=1, inplace=True)
          df3.columns
Out[22]: Index(['id', 'price', 'bedrooms', 'bathrooms', 'sqft_living', 'sqft_lot',
                  'floors', 'waterfront', 'condition', 'grade', 'yr_built',
                  'yr_renovated', 'yr_renovated_bool', 'zip_98002', 'zip_98003',
                  'zip_98004', 'zip_98005', 'zip_98006', 'zip_98007', 'zip_98008',
                  'zip_98010', 'zip_98011', 'zip_98014', 'zip_98019', 'zip_98022',
                  'zip_98023', 'zip_98024', 'zip_98027', 'zip_98028', 'zip_98029', 'zip_98030', 'zip_98031', 'zip_98032', 'zip_98033', 'zip_98034',
                  'zip_98038', 'zip_98039', 'zip_98040', 'zip_98042', 'zip_98045',
                  'zip_98052', 'zip_98053', 'zip_98055', 'zip_98056', 'zip_98058',
                  'zip_98059', 'zip_98065', 'zip_98070', 'zip_98072', 'zip_98074',
                  'zip_98075', 'zip_98077', 'zip_98092', 'zip_98102', 'zip_98103', 'zip_98105', 'zip_98106', 'zip_98107', 'zip_98108', 'zip_98109',
                  'zip_98112', 'zip_98115', 'zip_98116', 'zip_98117', 'zip_98118',
                  'zip_98119', 'zip_98122', 'zip_98125', 'zip_98126', 'zip_98133',
                  'zip_98136', 'zip_98144', 'zip_98146', 'zip_98148', 'zip_98155',
                  'zip_98166', 'zip_98168', 'zip_98177', 'zip_98178', 'zip_98188',
                  'zip_98198', 'zip_98199'],
                 dtype='object')
In [78]: df3.corr()['price']
Out[78]: id
                         -0.016772
          price
                          1.000000
          bedrooms
                          0.308787
          bathrooms
                          0.525906
          sqft_living
                          0.701917
          zip 98177
                          0.040503
          zip 98178
                         -0.069286
          zip 98188
                         -0.054438
          zip 98198
                         -0.074064
          zip 98199
                          0.083688
          Name: price, Length: 82, dtype: float64
```

Modeling

My main goal for this project is predicting the House Sale Price. Therefore 'price' variable is my target dependent variable (X). And all other variables are predictors, independent variables (y).

This modeling process will tell me which variables are good predictors and produce a fit algorithm which calculates the predicted sale price.

I will use multiple linear regression for this study.

```
In [23]: y = df3['price'] # Target, dependent variable
X = df3.drop('price', axis=1) # Predictors, independent variables
```

Baseline Model

I will start the modeling with only one variable. Then I will try to improve my baseline model by adding more variables step by step.

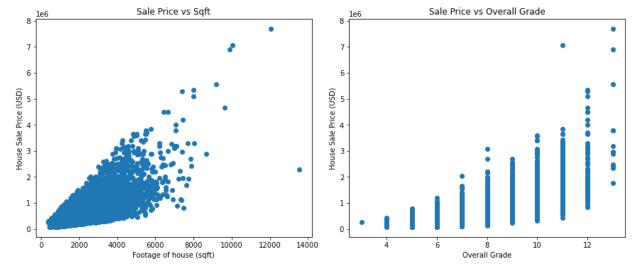
Based on my correlation study, the Sale price has best correlation with 'sqft_living' and 'grade'.

```
In [24]: import statsmodels.api as sm
    from statsmodels.formula.api import ols

In [25]: #Plot Sale price vs top two predictors
    fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(12, 5), constrained_layout=Tr

        ax1.scatter(X['sqft_living'], y)
        ax1.set_xlabel("Footage of house (sqft)")
        ax1.set_ylabel("House Sale Price (USD)")
        ax1.set_title("Sale Price vs Sqft");
        #ax1.set_xlim(0, 4000000)

        ax2.scatter(X['grade'], y)
        ax2.set_ylabel("House Sale Price (USD)")
        ax2.set_ylabel("House Sale Price (USD)")
        ax2.set_title("Sale Price vs Overall Grade");
        plt.savefig('figures/price-vs-sqftGrade.png')
```



The high correltaion is visible on both plots.

I choose to use 'sqft_living' in my baseline model since it is a continious variable.

There are three steps in modeling:

- 1. Seperate data into train and test splits.
- 2. Apply Linear Fit to training data and make predictions
- 3. Compare/validate predictions on test data

I plan to use 80% of the data for training and 20% for testing.

```
In [26]: # Seperate data into training and test splits
    from sklearn.model_selection import train_test_split

X_train, X_test, y_train, y_test = train_test_split(X, y, random_state=0)

print(f"X_train is a DataFrame with {X_train.shape[0]} rows and {X_train.sh
    print(f"y_train is a Series with {y_train.shape[0]} values")

# We always should have the same number of rows in X as values in y
    assert X_train.shape[0] == y_train.shape[0]

X_train is a DataFrame with 16197 rows and 81 columns
    y_train is a Series with 16197 values
In [27]: # Apply linear fit predict and validate
```

```
In [27]: # Apply linear fit, predict, and validate
    from sklearn.linear_model import LinearRegression

baseline_model = LinearRegression()

X_train_sqft = X_train[['sqft_living']]

X_test_sqft = X_test[['sqft_living']]

regline = baseline_model.fit(X_train_sqft, y_train)

y_train_hat = baseline_model.predict(X_train_sqft)

y_test_hat = baseline_model.predict(X_test_sqft)

print("Slope:", regline.coef_)

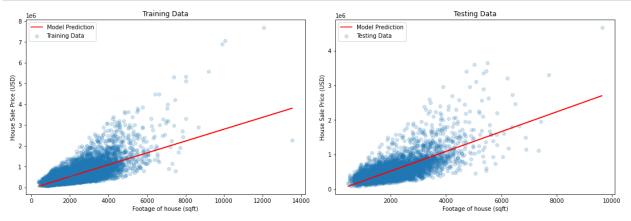
print("y-intercept:", regline.intercept_)

print("R squared for Training:", regline.score(X_train_sqft, y_train))

print("R squared for Testing:", regline.score(X_test_sqft, y_test))
```

Slope: [285.58593563]
y-intercept: -53321.493253810564
R squared for Training: 0.4951005996564265
R squared for Testing: 0.48322207729033984

```
In [62]:
         #Visualization of fit on training and testing data
         fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(15, 5), constrained layout=Tr
         ax1.scatter(X_train_sqft, y_train, label='Training Data', alpha=0.2)
         ax1.plot(X_train_sqft, y_train_hat, color='red', label='Model Prediction')
         ax1.set_xlabel("Footage of house (sqft)")
         ax1.set_ylabel("House Sale Price (USD)")
         ax1.set title("Training Data")
         ax1.legend()
         ax2.scatter(X_test_sqft, y_test, label='Testing Data', alpha=0.2)
         ax2.plot(X_test_sqft, y_test_hat, color='red', label='Model Prediction')
         ax2.set_xlabel("Footage of house (sqft)")
         ax2.set ylabel("House Sale Price (USD)")
         ax2.set_title("Testing Data")
         ax2.legend()
         plt.savefig('figures/baselineFit sqft.png')
```



The R squared score for training and test scores are similar. The Training and Testing graphs also show similar fitting behavior. Therefore, we can say that the baseline model is a good fit, not overfitted or underfitted.

Model Validation with Multiple splits of data

Seperating the data in training and test splits is a random process. We can improve the validation by repeating the process (split, fit, predict, compare) multiple times and finding the mean R squared scores.

As the number of splits increase, the difference between the Train and Test score decreases.

The R squared value for baseline model with one predictor (sqft_living) is around 0.49. However, the score is not high enough. We should try to improve our model by adding more predictors.

Second Model with 2 predictors

In the second model, I plan to add a second predictor to my fit in order to improve the R squared score.

First I will iterate over all the remaining predictors to find the best 2nd predictor.

I will remove the 'sqft_living' and its correlated variables ('bedrooms', 'bathrooms', 'grade') from my predictor list.

```
In [30]: # Remove correlated predictors and sqft_living
predictors_left = list(set(list(X.columns)) - set(['sqft_living', 'bedrooms
print(predictors_left)
```

['zip_98117', 'sqft_lot', 'zip_98052', 'zip_98007', 'zip_98072', 'zip_981
08', 'zip_98136', 'zip_98092', 'zip_98031', 'zip_98199', 'zip_98034', 'zi
p_98070', 'zip_98059', 'zip_98155', 'id', 'zip_98003', 'zip_98107', 'zip_
98005', 'zip_98024', 'zip_98105', 'zip_98168', 'zip_98115', 'zip_98102',
'zip_98126', 'yr_built', 'zip_98055', 'zip_98116', 'zip_98133', 'zip_9803
3', 'zip_98177', 'zip_98144', 'zip_98053', 'zip_98023', 'zip_98077', 'zip_
98040', 'zip_98006', 'zip_98002', 'zip_98028', 'zip_98011', 'zip_98065',
'zip_98148', 'zip_98119', 'zip_98056', 'zip_98038', 'zip_98045', 'zip_980
42', 'zip_98058', 'zip_98008', 'zip_98112', 'zip_98029', 'zip_98188', 'zi
p_98146', 'condition', 'zip_98022', 'zip_98125', 'floors', 'zip_98166',
'zip_98118', 'zip_98039', 'zip_98198', 'zip_98075', 'zip_98014', 'zip_981
06', 'zip_98010', 'zip_98004', 'zip_98032', 'zip_98178', 'zip_98030', 'zi
p_98109', 'zip_98103', 'yr_renovated_bool', 'zip_98027', 'zip_98074', 'zi
p_98122', 'waterfront', 'yr_renovated', 'zip_98019']

```
In [31]: # Find the 2nd best predictor
         second_model = LinearRegression()
         selected predictors = []
         R_squared_train = []
         R_squared_test = []
         for col in predictors left:
             pred = ['sqft_living'] + [col]
             second_model.fit(X_train[pred], y_train)
             R2 train = second model.score(X train[pred], y train)
             R2_test = second_model.score(X_test[pred], y_test)
             selected_predictors.append(pred)
             R squared_train.append(R2_train)
             R_squared_test.append(R2_test)
         df_two_predictors = pd.DataFrame(list(zip(selected predictors, R_squared tr
                                          columns=['two_predictors', 'R_squared_trai
         df_two_predictors.sort_values('R_squared train', ascending=False, inplace=T
         df two predictors.head(15)
```

Out[31]:

	two_predictors	R_squared_train	R_squared_test
0	[sqft_living, zip_98004]	0.533440	0.520127
1	[sqft_living, waterfront]	0.529563	0.528285
2	[sqft_living, yr_built]	0.526124	0.518243
3	[sqft_living, zip_98039]	0.517281	0.506499
4	[sqft_living, yr_renovated]	0.516954	0.507128
5	[sqft_living, zip_98112]	0.511713	0.506115
6	[sqft_living, zip_98040]	0.508561	0.496405
7	[sqft_living, zip_98023]	0.504133	0.492635
8	[sqft_living, zip_98038]	0.502710	0.491157
9	[sqft_living, zip_98042]	0.502537	0.492249
10	[sqft_living, zip_98105]	0.502214	0.491189
11	[sqft_living, zip_98092]	0.501713	0.491271
12	[sqft_living, yr_renovated_bool]	0.501480	0.491107
13	[sqft_living, zip_98119]	0.501165	0.493318
14	[sqft_living, condition]	0.501093	0.489588

Adding a 2nd predictor to baseline model improved the R squared value both on training and testing data.

As I guessed, zipcode plays a significant role in House Sale price.

The R_squared values for top 2nd predictors are very close to each other. Moreover, model validation on test data is also good for all.

I will not choose a 2nd predictor for this step. Instead I will search for the best set of predictors.

Third Model with 3 predictors

In this step, I will try to find the best set of 2nd and 3rd predictors in addition to the 'sqft_living'.

```
In [32]: from itertools import combinations
         third model = LinearRegression()
         selected predictors = []
         R squared train = []
         R squared test = []
         for (col1, col2) in list(combinations(predictors left, 2)):
             pred = ['sqft_living'] + [col1, col2]
             third_model.fit(X_train[pred], y_train)
             R2_train = third_model.score(X_train[pred], y_train)
             R2_test = third_model.score(X_test[pred], y_test)
             selected predictors.append(pred)
             R squared train.append(R2 train)
             R_squared_test.append(R2_test)
         df three predictors = pd.DataFrame(list(zip(selected predictors, R squared
                                          columns=['three predictors', 'R squared tr
         df three predictors.sort values('R squared train', ascending=False, inplace
         df three predictors.head(15)
```

Out[32]:

	three_predictors	R_squared_train	R_squared_test
0	[sqft_living, zip_98004, waterfront]	0.569135	0.566727
1	[sqft_living, yr_built, zip_98004]	0.562154	0.552604
2	[sqft_living, yr_built, waterfront]	0.556858	0.558546
3	[sqft_living, zip_98039, zip_98004]	0.556583	0.544304
4	[sqft_living, zip_98004, yr_renovated]	0.553657	0.543087
5	[sqft_living, zip_98039, waterfront]	0.551630	0.552382
6	[sqft_living, zip_98112, zip_98004]	0.551043	0.544249
7	[sqft_living, waterfront, yr_renovated]	0.549054	0.549292
8	[sqft_living, zip_98040, zip_98004]	0.548339	0.534251
9	[sqft_living, yr_built, zip_98039]	0.546934	0.539806
10	[sqft_living, zip_98112, waterfront]	0.546886	0.552160
11	[sqft_living, zip_98040, waterfront]	0.541900	0.539191
12	[sqft_living, zip_98023, zip_98004]	0.541846	0.528913
13	[sqft_living, zip_98105, zip_98004]	0.541012	0.528563
14	[sqft_living, zip_98038, zip_98004]	0.540323	0.527330

As the number of the predictors increase, R squared value increased. The validation is still good.

The predictors sets which includes variables "sqft_living, waterfront, zip_98004, yr_built, and zip_98039" give similar R_squared values for training and test.

Final Model with 5 predictors

In final model, I will use all the top 5 predictors to see how much our fit improves.

```
In [52]: final_model = LinearRegression()
    five_pred = ['sqft_living', 'waterfront', 'yr_built', 'zip_98004', 'zip_980

X_train_final = X_train[five_pred]

X_test_final = X_test[five_pred]

regline = final_model.fit(X_train[five_pred], y_train)

print('Final model predictors:', five_pred)
    print("R squared for Training:", regline.score(X_train_final, y_train))
    print("R squared for Testing:", regline.score(X_test_final, y_test))

Final model predictors: ['sqft_living', 'waterfront', 'yr_built', 'zip_98 004', 'zip_98039']
    R squared for Training: 0.6159271322430281
    R squared for Testing: 0.6178922353975156
```

As I guessed, adding more zipcodes will improve the model. However, I stop adding here.

Validation looks pretty good.

Let's double check the validation with multisplitter.

```
In [53]: splitter = ShuffleSplit(n_splits=10, test_size=0.20, random_state=0)
        final_model2 = LinearRegression()
        final_scores = cross_validate(
           estimator=final model2,
           X=X[five_pred],
           y=y,
           return_train_score=True,
           cv=splitter
        )
        print('Final model predictors:', five pred)
        print("Mean R squared for Testing:", final_scores["test_score"].mean())
        Final model predictors: ['sqft_living', 'waterfront', 'yr_built', 'zip_98
        004', 'zip_98039']
        Mean R squared for Training:
                                      0.6135724222328819
        Mean R squared for Testing: 0.6256321951893684
```

The multisplitted results mainly agree with the one split process. The difference is probably random.

For our final model, R squared score is acceptable. The model performance on training data is similar to test data. We conclude that there is no overfitting or underfitting.

RMSE calculation

```
In [55]: #Calculate MSE and RMSE
    from sklearn.metrics import mean_squared_error

#mean_squared_error(y_test, final_model.predict(X_test_final), squared=Fals
    mse = mean_squared_error(y_test, final_model.predict(X_test_final)) # gives
    rmse = np.sqrt(mse)
    print('MSE =', mse)
    print('RMSE =', rmse)

MSE = 45489203300.832375
    RMSE = 213281.9807223113
```

RMSE value is quite large. This is not a good sign.

We can also use statmodels for multiple linear regression modeling.

```
In [35]: import statsmodels.api as sm
from statsmodels.formula.api import ols
```

```
In [36]: outcome = 'price'

#pred_sum = '+'.join(X.columns)
pred_sum = '+'.join(five_pred)

#pred_sum = '+'.join(['sqft_living', 'waterfront', 'yr_built'])

#pred_sum = '+'.join(['sqft_living', 'waterfront', 'zip_98004', 'zip_98039'

#pred_sum = '+'.join(['sqft_living'])

formula = outcome + '~' + pred_sum
model = ols(formula=formula, data=df3).fit()
model.summary()
```

Out[36]: OLS Regression Results

Dep. Variable: price 0.617 R-squared: OLS 0.617 Model: Adj. R-squared: Method: Least Squares 6946. F-statistic: **Date:** Sat, 11 Dec 2021 Prob (F-statistic): 0.00 15:25:05 **Log-Likelihood:** -2.9704e+05 Time:

No. Observations: 21597 **AIC:** 5.941e+05

Df Residuals: 21591 **BIC:** 5.941e+05

Df Model: 5

Covariance Type: nonrobust

	coef	std err	t	P> t	[0.025	0.975]
Intercept	4.004e+06	1.09e+05	36.819	0.000	3.79e+06	4.22e+06
sqft_living	279.9645	1.812	154.525	0.000	276.413	283.516
waterfront	8.381e+05	1.9e+04	44.032	0.000	8.01e+05	8.75e+05
yr_built	-2061.3388	55.749	-36.975	0.000	-2170.611	-1952.067
zip_98004	5.997e+05	1.3e+04	46.260	0.000	5.74e+05	6.25e+05
zip_98039	1.143e+06	3.24e+04	35.317	0.000	1.08e+06	1.21e+06

 Omnibus:
 11494.937
 Durbin-Watson:
 1.967

 Prob(Omnibus):
 0.000
 Jarque-Bera (JB):
 321015.318

 Skew:
 2.012
 Prob(JB):
 0.00

 Kurtosis:
 21.454
 Cond. No.
 2.07e+05

Warnings:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 2.07e+05. This might indicate that there are strong multicollinearity or other numerical problems.

I did run the Statmodel OLS on different set of predictors. Here are my findings:

- As the number of predictors used increase the R squared value increases. However, also the condition number increases, which is not good
- R_squared = 0.795 and Cond. No. = 6.17e+11 when all predictors used (including hot-encoded zipcode and boolean yr_renovated).
- R_squared = 0.617 Cond. No. = 2.07e+05 when five final model predictors used ('sqft_living', 'waterfront', 'yr_built', 'zip_98004', 'zip_98039').
- R_squared = 0.592 Cond. No. = 4.75e+04 when four predictors used ('sqft_living', 'waterfront', 'zip_98004', 'zip_98039').
- R_squared = 0.493 Cond. No. = 5.63e+03 when one predictor, 'sqft_living', used

It is also interesting to note that 'yr_built' has negative coefficient.

Effect of House Renovations

I would like to see if and how much house renovations effect the House Sale Prices. Let's apply the linear fit with one predictor only: 'yr_renovated'.

```
In [38]: renovation_model = LinearRegression()

X_train_ren = X_train[['yr_renovated']]

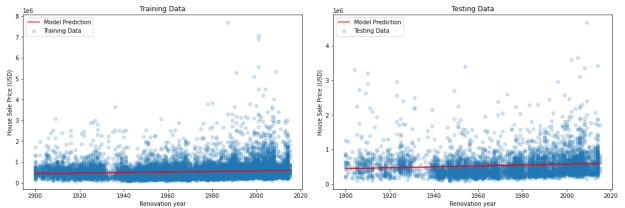
X_test_ren = X_test[['yr_renovated']]

regline = renovation_model.fit(X_train_ren, y_train)

print("Slope:", regline.coef_)
print("y-intercept:", regline.intercept_)
print("R squared for Training:", regline.score(X_train_ren, y_train))
print("R squared for Testing:", regline.score(X_test_ren, y_test))

Slope: [1300.35687138]
y-intercept: -2022535.979409572
R squared for Training: 0.010206187304151793
R squared for Testing: 0.006126113636745867
```

```
In [39]: #Visualization of yr renovation fit on training and testing data
         fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(15, 5), constrained layout=Tr
         ax1.scatter(X_train_ren, y_train, label='Training Data', alpha=0.2)
         ax1.plot(X_train_ren, regline.predict(X_train_ren), color='red', label='Mod
         ax1.set_xlabel("Renovation year")
         ax1.set_ylabel("House Sale Price (USD)")
         ax1.set title("Training Data")
         ax1.legend()
         ax2.scatter(X_test_ren, y_test, label='Testing Data', alpha=0.2)
         ax2.plot(X_test_ren, regline.predict(X_test_ren), color='red', label='Model
         ax2.set_xlabel("Renovation year")
         ax2.set_ylabel("House Sale Price (USD)")
         ax2.set_title("Testing Data")
         ax2.legend()
         plt.show()
         plt.savefig('figures/baselineFit_sqft.png')
```



<Figure size 432x288 with 0 Axes>

R squared value is very low. Apparently this is not a good fit.

I will now apply the linear regression on final model predictors + renovation year. I want to observe how much the R squared will improve.

```
In [40]: # Linear fit on final model + renovation predictors
    final_model_ren = LinearRegression()

pred = ['sqft_living', 'waterfront', 'yr_built', 'zip_98004', 'zip_98039',
    regline_ren = final_model_ren.fit(X_train[pred], y_train)

print('Final model + Renovation predictors:', pred)
    print("R squared for Training:", regline_ren.score(X_train[pred], y_train))
    print("R squared for Testing:", regline_ren.score(X_test[pred], y_test))

Final model + Renovation predictors: ['sqft_living', 'waterfront', 'yr_built', 'zip_98004', 'zip_98039', 'yr_renovated']
    R squared for Training: 0.6167249032808759
    R squared for Testing: 0.618146687048683
```

Renovation does improve the R squared score slightly on training data, but not on testing data.

I conclude that House Renovation doesn't have significant effect on House Sale Price.

Final Model Interpretation

Here is the parameters for my final model:

Observations:

- The y-intercept is guite large, about 4,000,000, and the price goes down with year built.
- The 'year_built' has negative coefficient, which is interesting. The old houses are more expensive than the new ones. Are the old, established neigborhoods more valuable? Are old neighborhoods close to downtown? Why? This can be investigated for future study.

Here is the linear equation for our final model:

```
House Sale Price = 4014990.7576159136 + (2.844667e+02 * sqft_living) + (8.040627e+05 * waterfront) + (-2.071868e+03 * yr_built) + (6.201505e+05 * zip_98004) + (1.162237e+06 * zip_98039)
```

In general, the format of the linear equation:

y = b + mx (for one independent variable)

• y = b + m1x1 + m2x2 + m3x3 + m4x4 + m4x5 (for five independent varibles)

(where m is slope/coefficient, and b is y-intercept)

Let's write a small function to calculate the house sale price.

```
2: 1111595.4730236786
3: 1517404.8278655098
4: 636682.9802501751
5: 1333492.6308398792
```

6: 1875578.8361759782

Investigating Linearity

I will check the linearity between the model predicted value and actual value on the test data.

```
In [69]: # Plotting Predicted vs Actual Sale Price
y_pred = final_model.predict(X_test_final)
fig, ax = plt.subplots(figsize=(7,5))

perfect_line = np.arange(y_test.min(), y_test.max())
#perfect_line = np.arange(1000000, 3000000)
ax.plot(perfect_line, linestyle="--", color="orange", label="Perfect Fit")
ax.scatter(y_test, y_pred, alpha=0.5)
ax.set_xlabel("Actual Price")
ax.set_ylabel("Predicted Price")
ax.set_title('Predicted vs Actual House Sale Price (Testing Data)')
ax.legend(loc='upper left');
plt.savefig('figures/linearityCheck.png')
```



- The plot shows linear relation between the Actual and Predicted price.
- However, it is important to note that, at high sale prices (above 2,000,000), the predicted value is deflecting away from the perfect fit. I believe these are outliners.

I conclude that Linearity assumption holds for the majority of the data, except outliers at high sale prices.

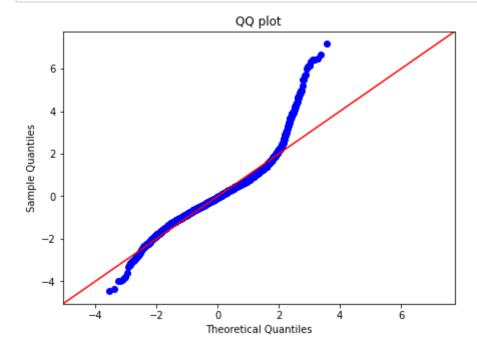
Investigating Normality

We will check normality by plotting the residual distribution vs normal distribution.

```
In [70]: # QQ Plot
import scipy.stats as stats

fig, ax = plt.subplots(figsize=(7,5))

residuals = (y_test - y_pred)
sm.graphics.qqplot(residuals, dist=stats.norm, line='45', fit=True, ax=ax);
ax.set_title('QQ plot');
plt.savefig('figures/normalityCheck_QQ.png')
```



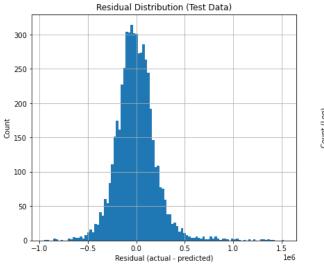
- The data looks like normal distribution close to center, but it is skewed at the tails.
- I believe skewness is caused by the outliners at the high sale prices.

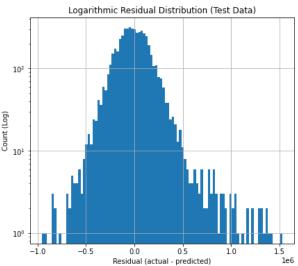
Let's look at the residual distributions closely.

```
In [46]: fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(15, 6))

residuals.hist(bins=100, ax=ax1)
ax1.set_title("Residual Distribution (Test Data)")
ax1.set_xlabel('Residual (actual - predicted)')
ax1.set_ylabel('Count')

residuals.hist(bins=100, ax=ax2, log=True)
ax2.set_title("Logarithmic Residual Distribution (Test Data)")
ax2.set_xlabel('Residual (actual - predicted)')
ax2.set_ylabel('Count (Log)')
plt.savefig('figures/residualDist.png')
```





Residual distribution looks normal except on the tails. The data in tails causes a bit skewness. I believe the residual values on the tails are caused by outliers, the houses at high sale prices.

I conclude that Normality assumption holds for the majority of the data, except outliers at high sale prices.

Investigating Multicollinearity (Independence Assumption)

```
In [47]: # VIF test
         from statsmodels.stats.outliers influence import variance inflation factor
         vif = [variance_inflation_factor(X_train_final.values, i) for i in range(X_
         pd.Series(vif, index=X_train_final.columns, name="Variance Inflation Factor
Out[47]: sqft living
                        6.460982
         waterfront
                        1.019214
         yr_built
                        6.320784
         zip_98004
                        1.029405
         zip_98039
                        1.010471
         Name: Variance Inflation Factor, dtype: float64
```

- The VIF values for variables, 'waterfront' 'zip_98004', 'zip_98004' are around 1. They are not correlated.
- However, the VIF values are around 6.4 for sqft_living and yr_built. These variables look correlated and causes multicollinearity.

I conclude that Independence Assumption is violated since significant multicollinearity is observed.

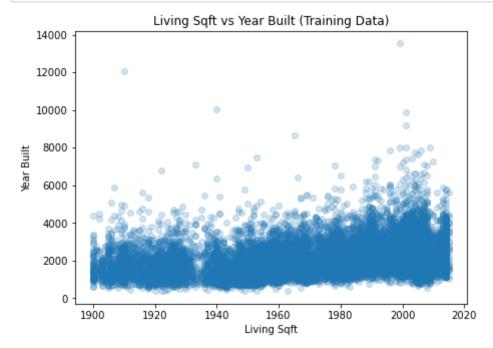
```
In [48]: # Correlation between sqft living and yr built
         X train final['sqft living'].corr(X train final['yr built'])
```

Out[48]: 0.32159976002317686

Even though the correlation is not high for the sqft_living and yr_built, it still caused considerable multicollinearity.

Why are they correlated?

```
In [74]: plt.figure(figsize=(7,5))
    plt.scatter(X_train_final['yr_built'], X_train_final['sqft_living'], alpha=
    plt.title("Living Sqft vs Year Built (Training Data)")
    plt.xlabel('Living Sqft')
    plt.ylabel('Year Built')
    plt.savefig('figures/yearBuilt-vs-sqft.png')
```



The plot shows slight correlation. The new houses looks like a bit larger.

The 'sqft_living' and 'yr_built' are main predictors. Should I remove 'year_built' from model? But It will decrease the R squared.

From Statmodel OLS fit:

- R_squared = 0.617 Cond. No. = 2.07e+05 when five final model predictors used ('sqft_living', 'waterfront', 'yr_built', 'zip_98004', 'zip_98039').
- R_squared = 0.592 Cond. No. = 4.75e+04 when four predictors used ('sqft_living', 'waterfront', 'zip_98004', 'zip_98039').

Investigating Homoscedasticity

I will look at the Residual vs Predicted values for house prices on testing data. The shape of the graph will tell me about the Homoscedasticity.

```
In [72]: fig, ax = plt.subplots(figsize=(7,5))

ax.scatter(y_pred, residuals, alpha=0.5)
ax.plot(y_pred, [0 for i in range(len(X_test))], color='orange')
ax.set_title('Residual vs Predicted House Sale Prices (Test Data)')
ax.set_xlabel("Predicted Value")
ax.set_ylabel("Actual - Predicted Value");
plt.savefig('figures/Homoscedasticity.png')
```



- The cone/funnel shape is observed on data.
- Funnel gets larger at high house sale prices.

I conclude that Homoscedasticity assumption is violated.

Linear Regression Assumptions Conclusion

- Linearity assumption holds for the majority of the data, except outliers at high sale prices.
- Normality assumption holds for the majority of the data, except outliers at high sale prices.
- Independence Assumption is violated since significant multicollinearity is observed.
- I conclude that Homoscedasticity assumption is violated.

- Two of four linear regression assuptions failed. The others two also fail at high sale prices. I
 guess one of the main causes for the violations is outliers. For future work, I need to study
 outliers, and maybe remove from data.
- The correlation betweern sqft_living and yr_built is interesting. This needs to be investigated. The multicollinearity caused by their correlation affects the model. Should 'yr_built' be removed from model? Advantages and disadvantages?
- Apparently residual increases as the sale price increases. Homoscedasticity even observed at low house sale prices. How can we avoid it? Can we?