

# Localization and identification of Neural Sources from simulated EEG Signals

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# Introduction

Electroencephalography (EEG) is a method for recording electric potentials stemming from neural activity at the surface of the human head, and it has important scientific and clinical applications. An important issue in EEG signal analysis is so-called source localization where the goal is to localize the source generators, that is, the neural populations that are generating specific EEG signal components. An important example is the localization of the seizure onset zone in EEG recordings from patients with epilepsy. A drawback of EEG signals is however that they tend to be difficult to link to the exact neural activity that is generating the signals.

Source localization from EEG signals has been extensively investigated during the last decades, and a large variety of different methods have been developed. Source localization is very technically challenging: because the number of EEG electrodes is far lower than the number of neural populations that can potentially be contributing to the EEG signal, the problem is mathematically under-constrained, and additional constraints on the number of neural populations and their locations must therefore be introduced to obtain a unique solution.

For the purpose of analyzing EEG signals, the neural sources are treated as equivalent current dipoles. This is because the electric potentials stemming from the neural activity of a population of neurons will tend to look like the potential from a current dipole when recorded at a sufficiently large distance, as in EEG recordings. Source localization is therefore typically considered completed when the location of the current dipoles has been obtained. However, an exciting possibility is to try to go one step further and identify the type of neural activity that caused a localized current dipole. For example, the type of synaptic input (excitatory or inhibitory) to a population of neurons, and the location of the synaptic input (apical or basal) will result in different current dipoles (Ness et al., 2022). It has also been speculated that dendritic calcium spikes can be detected from EEG signals, which could lead to exciting new possibilities for studying learning mechanisms in the human brain (Suzuki & Larkum, 2017). Identifying different types of neural activity from EEG signals would however require knowledge of how different types of neural activity are reflected in EEG signals. Tools for calculating EEG signals from biophysically detailed neural simulations

have however recently been developed, and are available through the software LFPy 2.0 (Hagen et al., 2018; Næss et al., 2021). This allows for simulations of different types of neural activity and the resulting EEG signals, opening up for a more thorough investigation of the link between EEG signals and the underlying neural activity.

The past decade has seen a rapid increase in the availability and sophistication of machine learning techniques based on artificial neural networks, like Convolutional Neural Networks (CNNs). These methods have also been applied to EEG source localization with promising results. However, it has not been investigated if CNNs can also identify the neural origin of EEG signals, in addition to localizing neural sources. In this Master's thesis, the aim will be to investigate the possibility of using CNNs to not only localize current dipoles but also identify the neural origin of different types of neural activity, based on simulated data of different types of neural activity and the ensuing EEG signal.

## **0.1 Motivation**

## **0.2 Goal and Objectives**

## **0.3 Structure of the Thesis**



# Chapter 1

## Background

Neurobiology is the study of the nervous system, including the structure, function, and development of neurons and neural circuits. The physics of the neuron is an important component of neurobiology, as it involves understanding the mechanisms by which neurons generate and transmit electrical signals. The basic unit of the nervous system is the neuron, which is capable of producing and transmitting electrical signals, or action potentials, across its membrane. These electrical signals are generated by the flow of charged ions into and out of the neuron, and are essential for communication between neurons and the transmission of information throughout the nervous system.

One technique for studying the electrical activity of the brain is electroencephalography (EEG), which measures the voltage fluctuations resulting from the electrical activity of neurons. EEG is a non-invasive technique that involves placing electrodes on the scalp, and has been used to study a wide range of cognitive and neural processes, including perception, attention, and memory. One of the challenges of interpreting EEG signals is the "inverse problem," which involves determining the location and nature of the underlying sources of electrical activity in the brain.

One approach to solving the inverse problem is source localization, which involves estimating the location and strength of the electrical sources in the brain that are responsible for the measured EEG signals. Source localization is a challenging problem due to the complexity of the brain and the fact that EEG signals are affected by a range of factors, including the conductivity of the scalp and the position and orientation of the electrodes. However, there are a number of techniques and algorithms that have been developed to address these challenges, including dipole modeling, distributed source modeling, and beamforming (Hämäläinen et al., 1993; Grech et al., 2008).

Overall, the physics of the neuron, EEG, and source localization are all important components of neurobiology that have contributed to our understanding of the nervous system and its functioning. By combining knowledge of the physical principles of neural signaling with advanced analytical tech-

niques, researchers are able to gain valuable insights into the underlying neural processes that give rise to behavior and cognition.

## **1.1 Introduction to Neuroscience**

## **1.2 Electroencephalography**

## **1.3 EEG Forward modeling**

## **1.4 The Inverse Problem**

## Chapter 2

# Electroencephalography

Neurons communicate with each other through the use of electrical currents. When a neuron receives a signal, it generates an electrical current that propagates along the axon and causes the release of neurotransmitters that diffuse across the gap between the sending and the receiving neuron. If the neurotransmitters are accepted by the receptors on the receiving neuron, a new electrical signal will be generated. This process of electrical communication between neurons creates electromagnetic fields that can be measured using electroencephalography (EEG).

Electroencephalography (EEG) is a non-invasive technique that has been used for almost a century to study the electrical potentials in the human brain. It remains one of the most important methods for investigating the brain's activity, with significant applications in both neuroscientific and clinical research [1].

An EEG signal is believed to originate from large numbers of synaptic inputs to populations of geometrically aligned pyramidal neurons [5]. The signal can be understood as a signature of neural activities that are generated from synaptic inputs to cells in the cortex. Synaptic inputs on its side are electrical or chemical signals that are being transmitted from one neuron to another, causing changes in the membrane potential of the neurons. In other words, neurons are specialized to pass signals, and synapses are the structures that make this transmission possible.

One of the primary uses of EEG is to investigate cognitive processes, diagnose diseases, and estimate functional connectivity. To measure the electrical activity in the brain, small metal disks called electrodes are placed on the scalp, which detect the electrical charges that result from the activity of brain cells. This technique can help identify abnormalities in specific areas of the brain, indicating potential signs of disease. Thus, EEG can be used to evaluate various brain disorders, including lesions, Alzheimer's disease, epilepsy, and brain tumors. An illustration of the typical EEG measurement setup is depicted in Figure 2.1.

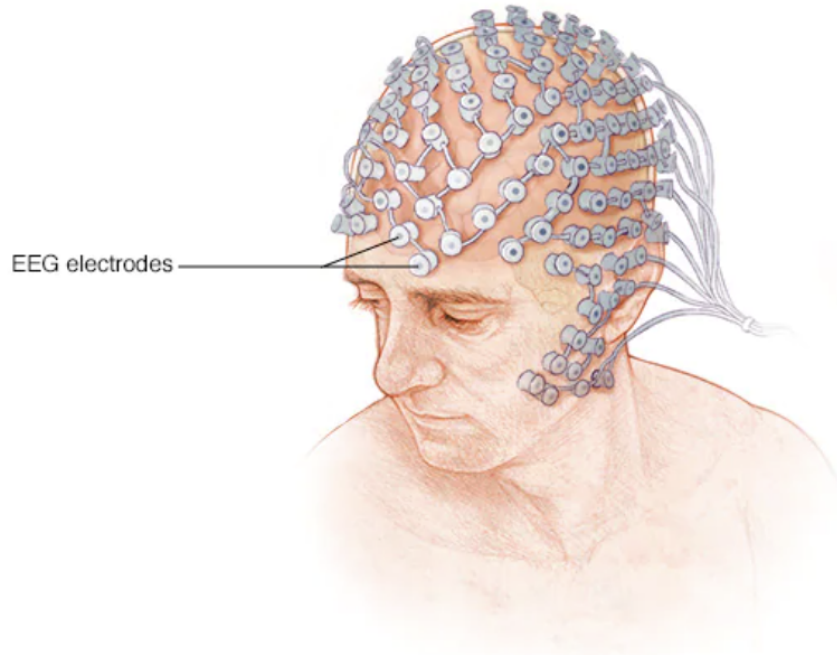


Figure 2.1: Illustration of the EEG method.

Source localization is a fundamental aspect of EEG signal analysis, with the ultimate aim of accurately identifying the location of neural current sources from EEG data. However, this is a challenging problem due to the inherent ill-posed nature of the inverse problem in electrostatics. This means that there is no unique solution, making it a difficult task to solve. Before digging deeper into the inverse problem, we will first look at how to simulate the electrical activity of the brain as it would be measured by electrodes on the scalp, better known as forward modeling.

## 2.1 Forward modeling of EEG signals

To better understand the complexities of the inverse problem and the nuances of source localization in EEG, it is helpful to gain a deeper comprehension of forward modeling, involving the simulation of electrical activity of the brain as it would be measured by electrodes on the scalp.

As explained in chapter 1, neural activity generates electric currents in the brain, which in turn create electromagnetic fields. In order to calculate extracellular electric potentials, one can envision the head as a 3D volume conduction, and combine Maxwell's equations with the current conservation law. The Poisson equation for computing extracellular potentials then goes as follows:



$$\nabla \cdot \mathbf{J} = \nabla \cdot (\sigma \nabla \phi) \quad (2.1)$$

where  $\mathbf{J}$  is the electric current density in extracellular space,  $\sigma$  is the extracellular conductivity and  $\phi$  is the extracellular electric potential [2]. For simple, symmetric head models, the Poisson equation can naturally be solved analytically. However, as for the New York Head which is a complex model that we will be utilize in this thesis, we will be using the numerical method known as Finite Element Method (FEM) when solve the equation.

To accurately calculate the extracellular potential(s),  $\phi$ , a well-established two-step forward-modeling approach is used. In the first step, a multicompartmental model is utilized, which takes into account the intricate details of neuron morphologies to determine the transmembrane currents,  $I_n$ . In the second step, equation 2.1 is solved, under the assumptions that the extracellular medium acts as a volume conductor with the following properties:

- infinitely large
- linear
- ohmic
- isotropic
- homogeneous
- frequency-independent

The origin of extracellular potentials is spatially distributed membrane currents, entering and escaping the extracellular medium. These currents can be understood as current sources and sinks, and give the extracellular potential,  $\phi$  at the electrode location  $\mathbf{r}$ :

$$\phi(\mathbf{r}) = \frac{1}{4\pi\sigma} \sum_{n=1}^N \frac{I_n}{|\mathbf{r} - \mathbf{r}_n|} \quad (2.2)$$

where  $\mathbf{r}_n$  is the location of the transmembrane current  $I_n$ ,  $N$  is the number of transmembrane currents and  $\sigma$  is the extracellular conductivity [2].

## 2.2 Multicompartmental modeling

The potential over the membrane,  $V_m$ , in long neurons with multi-branched dendrites varies depending on whether the potential is measured in the soma or at the tip of a distal dendrite [2]. Multicompartmental (MC) models are models that account for this spatial variability in  $V_m$ . In such models, the neural morphology commonly is represented as isopotential cylindrical compartments, with lengths and diameters derived from reconstructed morphologies,

connected with resistors [sterratt2011principles]. Single values of  $V_m$  can then be computed for each individual compartment, as depicted in Figure 2.2.

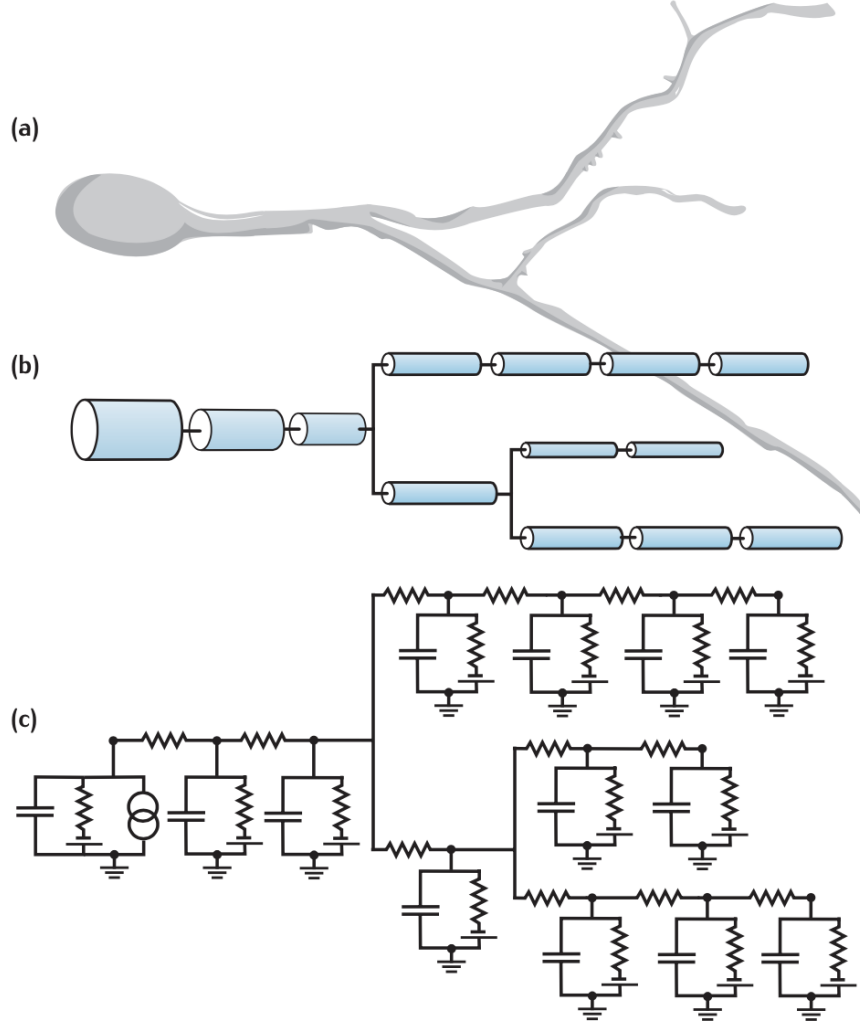


Figure 2.2: A diagram of the development of a multi-compartmental model. (a) The cell morphology is represented by (b) a set of connected cylinders. An electrical circuit consisting of (c) interconnected RC circuits is then built from the geometrical properties of the cylinders, together with the membrane properties of the cell.

The fundamental equation for MC models is given as:

$$c_m \frac{dV_{m,n}}{dt} = -i_{L,n} - \sum_w i_{w,n} - \frac{I_{\text{syn},n}}{\pi dL} + \frac{I_{\text{ext},n}}{\pi dL} \frac{d}{4r_a} \left( \frac{V_{m,n+1} - V_{m,n}}{L^2} - \frac{V_{m,n} - V_{m,n-1}}{L^2} \right) \quad (2.3)$$

where ....

This equation (2.3) assumes that a compartment  $n$  has two neighbors - one at  $n - 1$  and the second at  $n + 2$ . However, when considering the endpoint compartments, this clearly will not be true. A commonly used boundary condition, is the sealed-end condition, where no axial currents leave at the cable endpoints. With other words this means that  $I_{0,1} = 0$  in one end of the cable, and  $I_{N,N+1} = 0$  in the other end. For the cable endpoints, we are then left with the following expressions:

$$c_m \frac{dV_{m,1}}{dt} = -i_{L,1} - \sum_w i_{w,1} - \frac{I_{\text{syn},1}}{\pi dL} + \frac{I_{\text{ext},1}}{\pi dL} \frac{d}{4r_a} \left( \frac{V_{m,2} - V_{m,1}}{L^2} \right) \quad (2.4)$$

and

$$c_m \frac{dV_{m,N}}{dt} = -i_{L,N} - \sum_w i_{w,N} - \frac{I_{\text{syn},N}}{\pi dL} + \frac{I_{\text{ext},n}}{\pi dL} \frac{d}{4r_a} \left( \frac{V_{m,N} - V_{m,N-1}}{L^2} \right) \quad (2.5)$$

## 2.3 Volume conductors

As mentioned above, we can use volume conductor (VC) theory to predict the resulting extracellular potential  $V_e$  at any given point in space, given that the distribution of neuronal membrane currents is known.

## 2.4 Current Dipole Approximation

EEG signals are generated from synaptic inputs to cells in the cortex. Synaptic inputs are electrical (or chemical) signals that are being transmitted from one neuron to another, causing changes in the membrane potential of the neurons. In other words, neurons are specialized to pass signals, and synapses are the structures that make this transmission possible.

When calculating extracellular potentials,  $V_e$ , at large distances from the underlying current sources, one is typically benefitted with using the current-dipole approximation. This approximation is justified by the fact that a neuron's contribution to  $V_e$  becomes increasingly dipolar with increasingly distance and is commonly utilized when simulating EEG signals.

We know that electrical charges can create current multipoles, depending on coordinates and symmetry of the charge distribution [3]. Analogous, the combination of current sinks and sources set up such charge multipoles. When the distance  $R$  from the center of the volume to the recording point is larger than the distance from the volume center to the most peripheral source, multipole expansion can be used [4]. When utilizing the multipole expansion theorem equations 2.4 can be expressed as follows:

$$\phi(R) = \frac{C_{\text{monopole}}}{R} + \frac{C_{\text{dipole}}}{R^2} + \frac{C_{\text{quadrupole}}}{R^3} + \frac{C_{\text{octopole}}}{R^4} + \dots \quad (2.6)$$

where the numerators represents the contributions to the extracellular potential. The terms denoted  $C_{\text{monopole}}$ ,  $C_{\text{dipole}}$  and  $C_{\text{quadrupole}}$  represents contributions to the extracellular potential,  $V_e$ , and can in general be extremely complicated as they depend on the relationship between radial coordinates and symmetry of the current source and measurement electrode. However, multiple expansions are often beneficial as usually only the first few terms are needed in order to provide an accurate approximation of the original function. This also turns out to be true in our case, as the quadrupole, octopole and higher-order contributions to  $V_e$  decay more rapidly with distance  $R$  than the dipole contribution. Assuming that we are sufficiently far away from the source distribution, all terms above the dipole contribution vanish. As for the monopole contribution, we know that since ..... the net sum of currents over a neuronal membrane is always zero. This means that also the monopole term vanishes, and the expression for the extracellular potential,  $V_e$  is approximated by the dipole contribution alone:

$$\phi(\mathbf{r}) \approx \frac{C_{\text{dipole}}}{R^2} = \frac{1}{4\pi\sigma} \frac{|\mathbf{p}| \cos\theta}{|\mathbf{r} - \mathbf{r}_p|^2}. \quad (2.7)$$

where we have substituted for  $C_{\text{dipole}}$  in terms of other properties.  $\mathbf{p}$  denotes the current dipole moment in a medium with conductivity  $\sigma$ .  $R = |\mathbf{R}| = |\mathbf{r} - \mathbf{r}_p|$  is the distance between the current dipole moment at  $\mathbf{r}_p$  and the electrode location  $\mathbf{r}$ . Finally  $\theta$  represents the angle between  $\mathbf{p}$  and  $\mathbf{R}$ . This equation is known as the dipole approximation and is a precise approximation for calculating extracellular potential, given that  $R$  is much larger than the dipole length  $d = |\mathbf{d}|$ , like in the case of EEG [2].

Having that a current dipole moment  $\mathbf{p}$  can be predicted from an axial current  $I$  inside a neuron and the distance vector  $\mathbf{d}$  traveled by the axial current we get the following expression:  $\mathbf{p} = I\mathbf{d}$ . Generalising this equation, we get that the relationship between the current dipole moment,  $\mathbf{p}$  and a set of neural current sources can be expressed as follows:

$$\mathbf{p} = \sum_{n=1}^N I_n \mathbf{r}_n \quad (2.8)$$

In figure 2.3 we have provided a simulation of the extracellular potential generated by a neuron in response to a single synaptic input, where the spatial distribution of membrane current was explicitly taken into consideration. Based on the figure, it is apparent that the distribution of electric charge in the extracellular potential of the neurons surroundings exhibits distinct dipole patterns when observed from a greater distance.

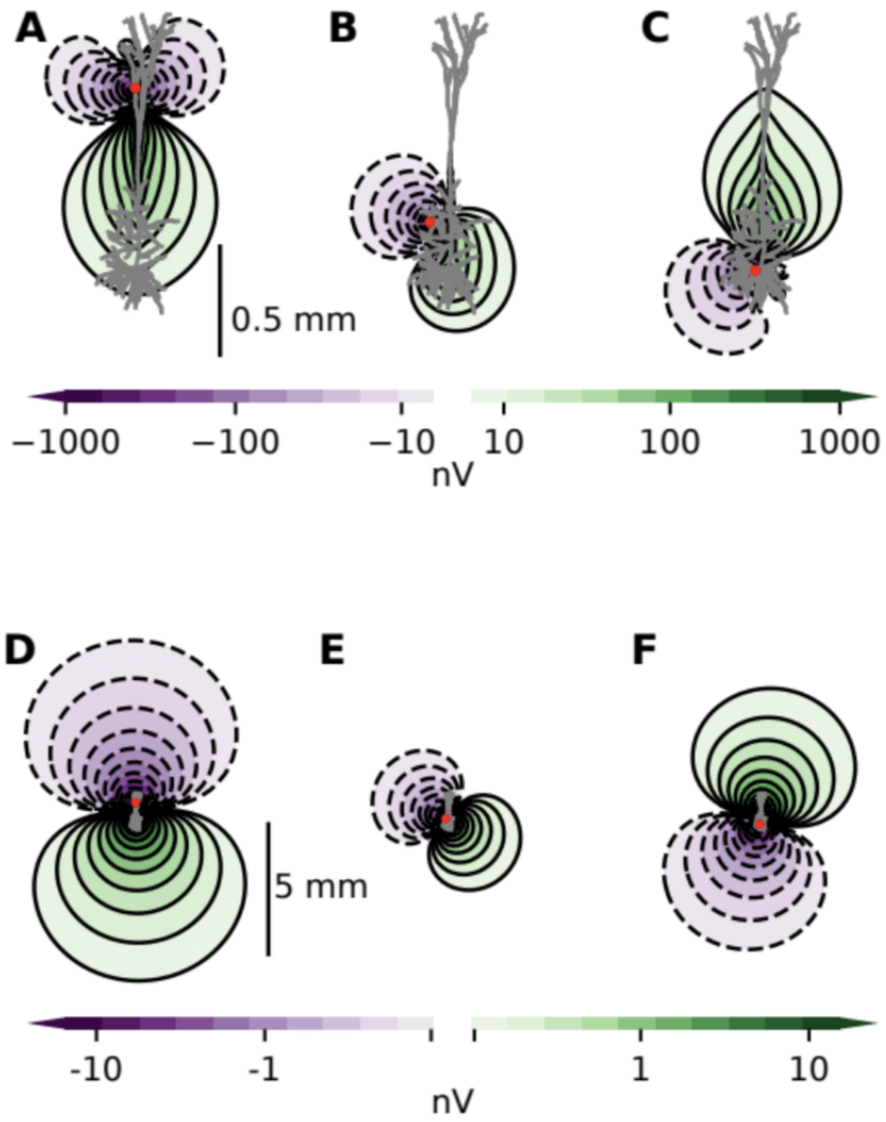


Figure 2.3: Source and explanation.

## 2.5 Head Models

The analytical formula presented in Equation 2.6 was derived based on the assumption of a constant tissue conductivity, denoted as  $\sigma$ . However, because the EEG signals is measured outside the head, it is affected by the different conductivities of the brain, cerebrospinal fluid (CSF), skull and scalp. Depending on problem, it may be important to keep in mind that EEG signals, in general, are significantly affected by biophysically details of the head. For instance, the conductivity of the cerebrospinal fluid exhibits a conductivity of approximately 1.7 S/m, while the conductivity of the skull and scalp is approximately 0.01 S/m and 0.5 S/m, respectively. These conductivity variations highlight the need for more comprehensive and realistic models of the head, known as head models, which take into account such conductivity variations. In addition to account for the variations in conductivity across different regions of the head, head models also takes into account that the EEG signal from a neuronal population will depend on whether the population is located in a *sulcus* or a *gyrus* [2]. Said with other words, by integrating biophysical details into models, a deeper understanding emerges regarding the impact of various tissues on the distribution of extracellular potential, which in turn, can lead to improvements in the accuracy of EEG signal analysis.

### 2.5.1 The New York Head

A central problem for EEG is to relate scalp data to brain *current sources* (Electric Fields of the Brain: The Neurophysics of EEG)....

Especially important for electrode locations outside of the brain, such as EEG, is the knowledge about how the electrical potentials will be affected by the geometries and conductivities of the various parts of the head (Biophysically detailed forward modeling of the neural origin of EEG and MEG signals). A model that takes these details into account is the New York Head Model. The model is based on anatomical and electrical characteristics of 152 adult human brains and is solved for 231 electrode locations.

The New York Head Model is a computer model of the human head used to simulate the electrical activity of the brain. It was created by the Electrical Geodesics Incorporated (EGI) in 2004, and is based on the anatomical and electrical characteristics of the head of a typical adult human. The model consists of a three-dimensional (3D) representation of the head and brain, with detailed information on the geometry and electrical properties of the different tissues and structures within the head. The model includes the scalp, skull, cerebrospinal fluid, gray matter, and white matter. The electrical properties of each of these tissues, such as conductivity and permittivity, are also included in the model.

The model was developed to be used for, and improve the accuracy

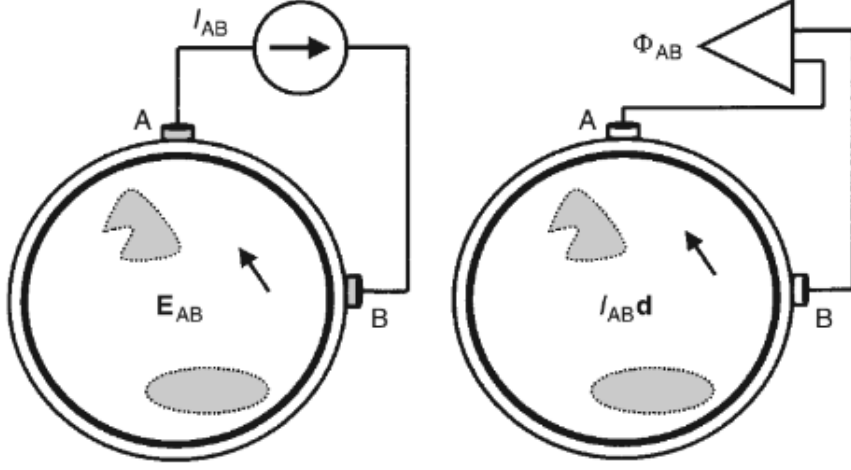


Figure 2.4: A caption here is needed.

of EEG source localization (The New York Head—A precise standardized volume conductor model for EEG source localization and tES targeting). To generate predictions of the EEG signals recorded from different scalp locations in response to a given set of source currents, the New York head model uses the lead field matrix (SOURCE), which is a mathematical representation of the relationship between the electrical activity in the brain and the electrical potentials recorded on the scalp.

The lead field matrix is constructed by taking advantage of the reciprocity theorem that states that knowledge of the current density through a volume conductor caused by an injection of current between two stimulating electrodes completely specifies how those same recording electrodes pick up potentials caused by dipole sources in the volume conductor. If one suppose that a pair of stimulating electrodes is placed at locations A and B on the scalp as provided in figure 2.4, an external current source will cause current to flow from electrode B through the brain, and all the way to electrode A. However, due to the geometry, inhomogeneity, and anisotropy of the head, the current density will vary with location. The amount of current that pass through the brain depends, to a great extent, on the location of the electrodes. In general, the brain currents will decrease with decreasing distance between electrodes. Thus, for a fixed pair of electrodes, the lead field vectors can be calculated as a function of position throughout the volume conductor. At each location, the orientation of the lead field vector  $L_{AB}$  is the orientation of the dipole source that produces the largest potential difference between the electrodes. The lead field matrix,  $\mathbf{L}$  is given as:

$$L = \frac{E}{I}, \quad (2.9)$$

where  $I$  is the injected current at the electrode locations and  $E$  is the resulting electric field in the brain (Biophysically detailed forward modeling of the neural origin of EEG and MEG signals). Moreover, the precise link between a current dipole moment  $p$  in the brain and the resulting EEG signals  $\Phi$  is then related to the lead field matrix as follows:

$$\Phi_{AB} = L_{AB} \cdot p, \quad (2.10)$$

Here, an injected current  $I$  of 1 mA gives an electric potential  $E$  in V/m, meaning that a current dipole moment  $\mathbf{p}$  in the unit of mAm gives EEG signals in the unit of V.

The New York Head model has been incorporated in the Python module LFPy, which provides classes for calculation of extracellular potentials from multicompartement neuron models. These tools will be utilized in this thesis. For more information read: <https://lfp.readthedocs.io/en/latest/readme.html#summary>

## 2.6 The Inverse Problem and Source Localization



## Chapter 3

# Results

As mentioned in chapter 1, an important topic in EEG signal analysis is the inverse problem of going from measured EEG signals to localized equivalent current dipoles, so-called source localization. In this chapter we will present the training and performance of the neural networks presented in chapter 4. Section ... and ... deal with training of the simple feed forward neural network and presenting its results, while section ... will discuss how a convolution neural network can be used to obtain the same results. But first, we will take a look at the dataset being feed to the different networks.

### 3.1 Simulation of EEG Signals

The cortex matrix of the New York Head Model (NYHM) consists of 74382 points, which refer to the number of possible positions for localization of dipole sources. We will train the neural networks using a dataset of self-simulated EEG measurements that correspond to the electromagnetic fields generated by dipole sources. These sources will have randomly selected positions within the cortex matrix. However, to simplify the problem, the strengths of single dipoles (amplitude) are set to  $10^7$  nA  $\mu$  m. Moreover, in the cases of single dipole source localization, the direction of the dipole moment is always rotated so that it is normal to the cerebral cortex. In some cases this will result in a dipole moment pointing perpendicular to the skull (directed towards an EEG electorde), while in other cases, due to the structure of the cortex, the dipole moment will point back into the cortex (but eventually towards an EEG electorde). The reason for this is that the human cortex is strongly folded, and the contribution to the EEG signal from a neural population (dipole moment) will depend on whether a dipole is located in a sulcus or a gyrus (source: BookTVN).

### 3.1.1 Effect of dipole location and orientation on EEG signals

As shown by/ discussed in .... (source: BookTVN) EEG signals are relatively insensitive to small changes in the *location* of neural current dipoles. Even though the intuitive thought might be that neurons in the upper cortical layers dominate the EEG due to the closer distance to the EEG electrode compared to neurons in the lower cortical layers, such differences in location acutually does not make considerable differences. This finding can be explained by fact that the low conductivity of the skull generates a certain spatial low-pass filtering, that ....

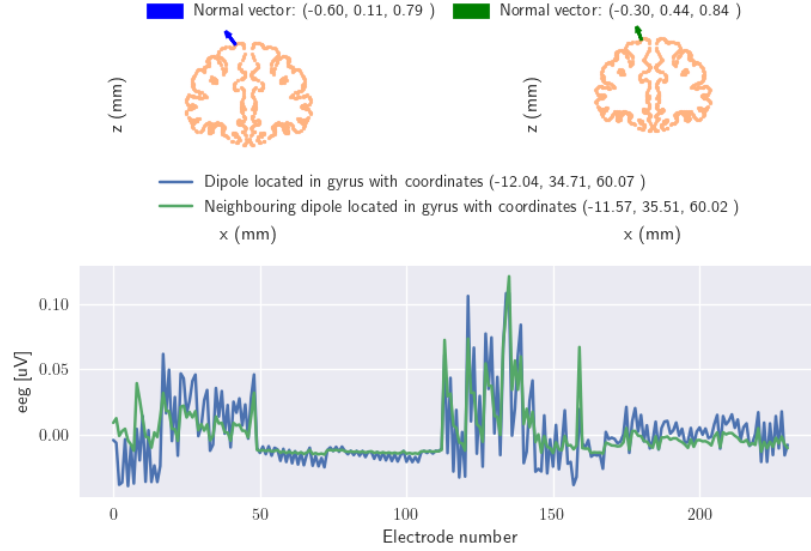


Figure 3.1: EEG signal for neighbouring dipoles.

However, in order to decribe the effect of the *orientation* of the dipoles relative to the EEG electrodes, we have in Figure 3.2 provided the EEG signals from two manually chosen dipole locations in the New York head model. The two dipoles illusrated are located in a gyrus and in a sulcus, both providing a different EEG outcome. In general, the EEG signal contribution from a single current dipole is maximized if the dipole is located in a gyrus, perpendicular oriented. Such a case is depiced in Figure 3.2B. However, if we place a dipole in a sulcus, again with perpendicular orientation, we can observe a substantial EEG contribution, but in contrast to the dipole in the gyrus we notice a more dipolar pattern 3.2C.

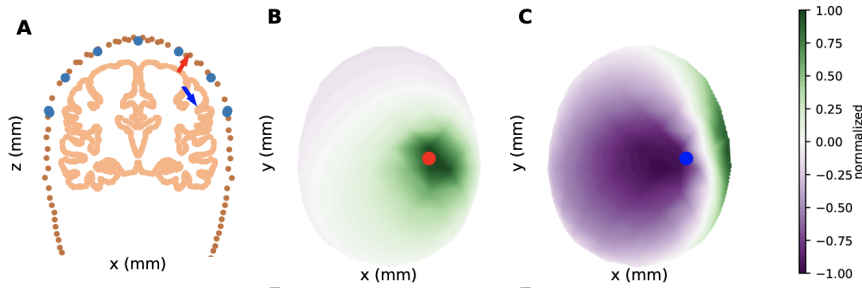


Figure 3.2: A: Two manually chosen dipole locations in the New York head model, located in a gyrus (red) and a sulcus (blue). The head model is seen from the side (x, z-plane). EEG electrode locations close to the chosen cross section plane are marked in light blue. The available dipole locations close to the cortical cross section effectively draw an outline of the cortical sheet, and are marked in pink. The current dipole moment was in all cases  $10^7$  nA $\mu$ m. B: Interpolated color plot of EEG signal from the dipole in gyrus, seen from the top (x, y-plane). The plotted EEG signal is normalized but the maximal value was 1.1  $\mu$ V. C: Interpolated color plot of EEG signal from the dipole in sulcus. The plotted EEG signal is normalized but the maximal value was 0.7  $\mu$ V. (source: BookTVN)

### 3.1.2 Noise

As for all experimental data, real EEG recordings contain noise. Artifacts are signals recorded by EEG but with a origin different from those generated by human brain activity. As some artifact may mimic true epileptiform abnormalities or seizures, awareness of artifacts and methods for distinguishing such signals from brain waves is highly important ([https://link.springer.com/chapter/10.1007/978-3-030-03511-2\\_8](https://link.springer.com/chapter/10.1007/978-3-030-03511-2_8)).

There are two different dypes of artifacts, classified according to their origin. Physiological artifacts originate from the patient itself, where the most usual ones are ocular activity, muscle activity, cardiac activity, perspiration and respiration. Technical artifacts, on the other hand, is generated from the environment of the patient, such as cable and body movements or electromagnetic interferences. (<https://www.bitbrain.com/blog/eeg-artifacts>).

Filtering techniques are usually utilized in order to remove artifact from EEG before analyzation of the recordings. But, when it comes to the simulated EEG data of ours, we are in no need to remove such noise, as there simply is none. The simulated EEG data can be understood as already filtered data that has undergone preprocessing steps, to ensure a high signal-to-noise ratio (<https://en.wikipedia.org/wiki/Signal-to-noise-ratio>). Moreover we understand the simulated data as an averaged measure of the typical EEG time series. However, in order to avoid overfitting and for other tecnical detailes, we do need to ass noise to tha data before feeding it to

the neural network. Therefore, to the final dataset of ours we add normally distributed noise of 10 %, with mean .... and standard deviation ... .

## 3.2 Localizing Single Dipole Sources

### 3.2.1 The dataset

The data set used to train a simple feed forward neural network consists of 10 000 rows, where each row corresponds to one sample, or let us say - one patient. Within the data set we have 231 columns, also referred to as features, representing the EEG measure at every recording electrode. Thus, we are left with a design matrix of size 10 000 x 231.

An example of how the input EEG data may look like for one sample (before adding noise) is provided in figure 3.3. The figure illustrates the EEG result from a sample containing a single current dipole source at a random position within the cerebral cortex. As also can be seen from the characteristic dipolar pattern, the dipole is located in a sulcus. The EEG measure is seen from both sides (x-, z-plane and y-, z-plane) and above (the x-, y-plane). EEG electrode locations are presented as filled circles, where the color of the fill represents the amplitude of the measured signal for the given electrode. The position of the current dipole moment is marked with a yellow star. As can be read off from the figure, the EEG signals, for this given sample, range from between -1 to 1  $\mu V$ .

### 3.2.2 Validation accuracy

In Figure 3.6 we have provided the validation accuracy, using mean squared error (MSE) and the coefficient of determination (R2-score).

The expression for MSE when predicting the x-, y- and z-coordinate, goes as follows:

$$MSE(\hat{y}, \tilde{y}) = \frac{1}{n} \sum_{i=1}^n (y_i - \tilde{y}_i)^2 = \frac{1}{3} \sum_{i=1}^3 ((x - \tilde{x})^2 + (y - \tilde{y})^2 + (z - \tilde{z})^2) \quad (3.1)$$

The coefficient of determination is given as follows:

$$R^2(\hat{y}, \tilde{y}) = 1 - \frac{\sum_{i=0}^{n-1} (y_i - \tilde{y}_i)^2}{\sum_{i=0}^{n-1} (y_i - \bar{y})^2}, \quad (3.2)$$

Where the mean value of  $y_i$  is defined by  $\bar{y}$ :

$$\bar{y} = \frac{1}{n} \sum_{i=0}^{n-1} y_i.$$

### 3.3. CONVOLUTION NEURAL NETWORK APPROACH FOR LOCALIZING SINGLE DIPOLE SOURCES

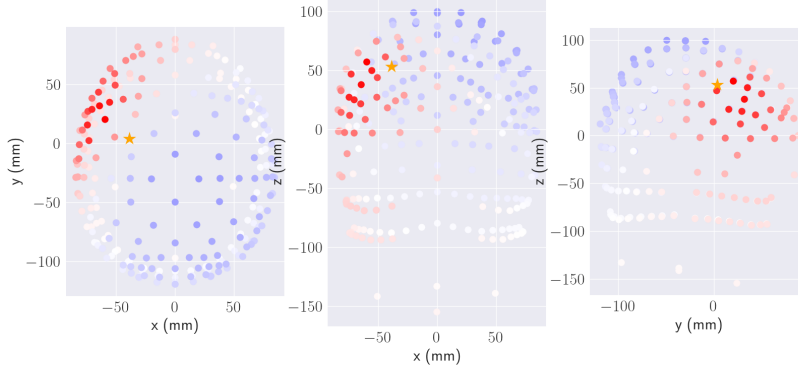


Figure 3.3: EEG for a sample containing one single current dipole source at a random position within the cerebral cortex. The EEG measure is seen from both sides (x-, z-plane and y-, z-plane) and above (the x-, y-plane). EEG electrode locations are presented as filled circles, where the color of the fill represents the amplitude of the measured signal for the given electrode. The position of the current dipole moment is marked with a yellow star.

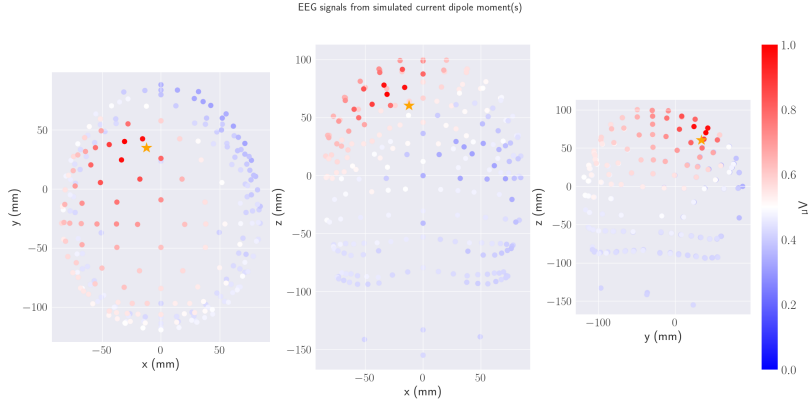


Figure 3.4: The EEG data of a randomly picked sample. As for all samples, 10 percent of normally distributed noise has been added to the original signal.

### 3.3 Convolution Neural Network Approach for localizing single dipole sources

Some results for the prediction of location for single current dipoles.

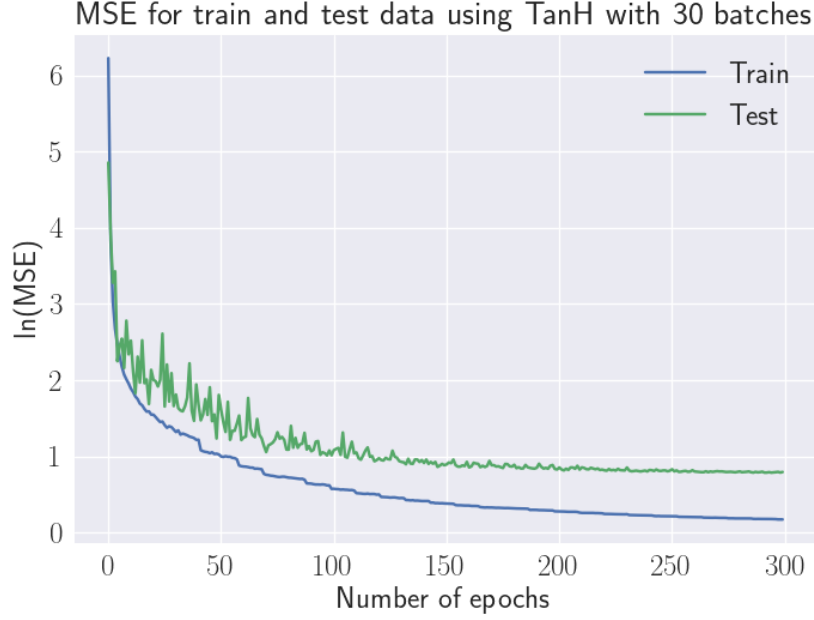


Figure 3.5: The validation accuracy for the simple Feed Forward Neural Network with 50 000 samples and tanh as activation function.

### 3.4 Region of Active Correlated Current Dipoles

Some results for the prediction of the size and location of current dipole populations.

Printed in terminal:

Epoch 9898/9999 | Train: 0.187 | Test: 4.275

Epoch 9899/9999 | Train: 0.184 | Test: 4.288

Epoch 9900/9999 | Train: 0.201 | Test: 4.279

Target: tensor([-1.0800, -1.9594, 0.4290, 11.0140])

Predicted: tensor([-1.1171, -1.9642, 0.4575, 16.5920])

Target: tensor([-6.7642e-02, 1.5426e+00, -1.0356e-02, 1.5576e+01])

Predicted: tensor([-0.3908, 1.4285, -0.1167, 15.9222])

Target: tensor([-0.6671, -1.0569, 1.8694, 7.1385])

Predicted: tensor([-0.7248, -1.0950, 1.9903, 6.2405])

### 3.5 Localizing Multiple Dipole Sources

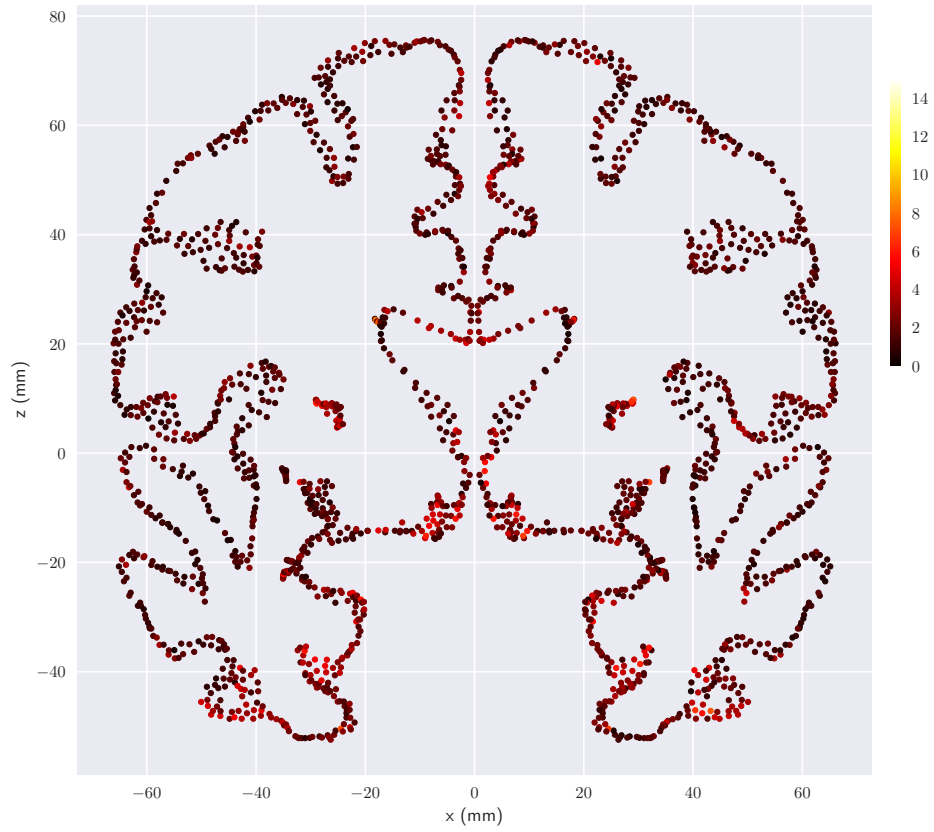


Figure 3.6: Mean absolute error of the network for each dipole location in the cortical y-plane cross section at  $y = 0$ .

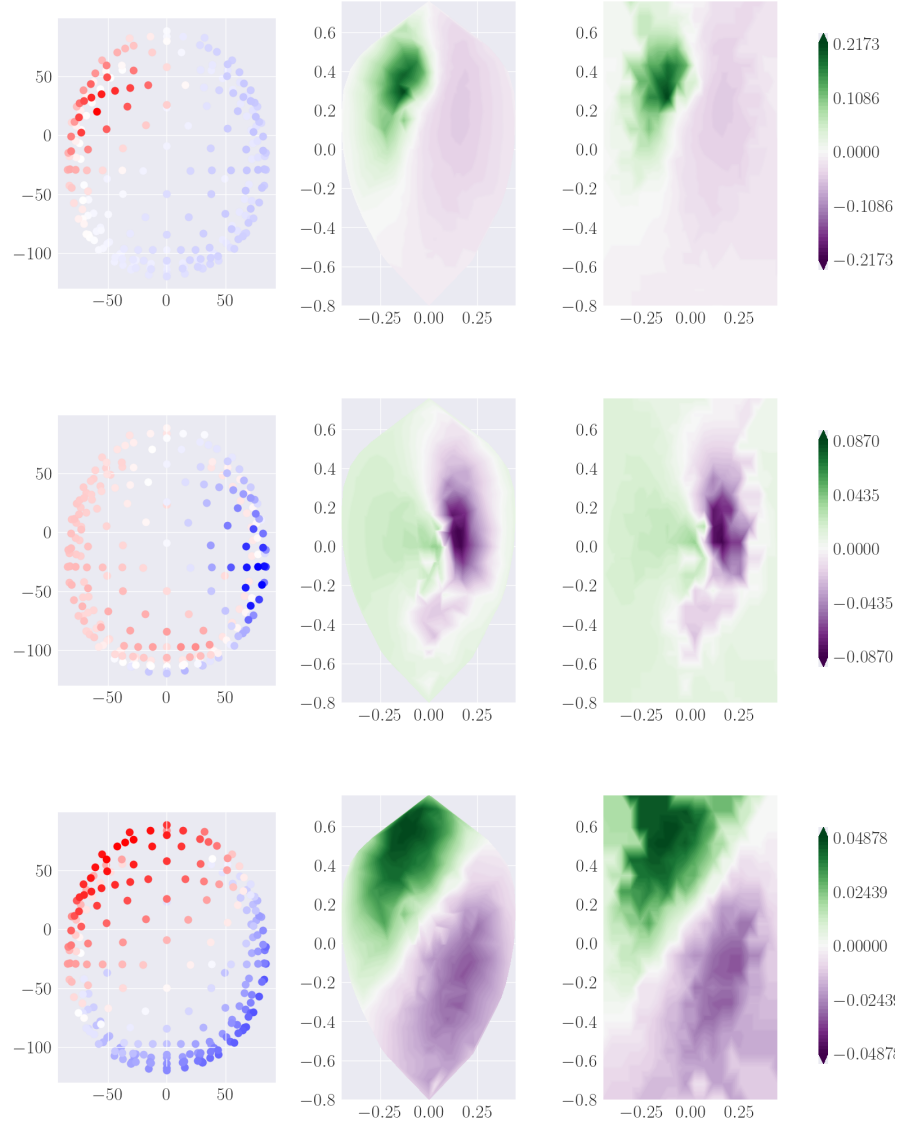


Figure 3.7:

**Right:** EEG measure for 3 different samples measured in  $\mu V$ .

**Middle and Left:** Illustration of the interpolation of the EEG data into two-dimensional matrix.



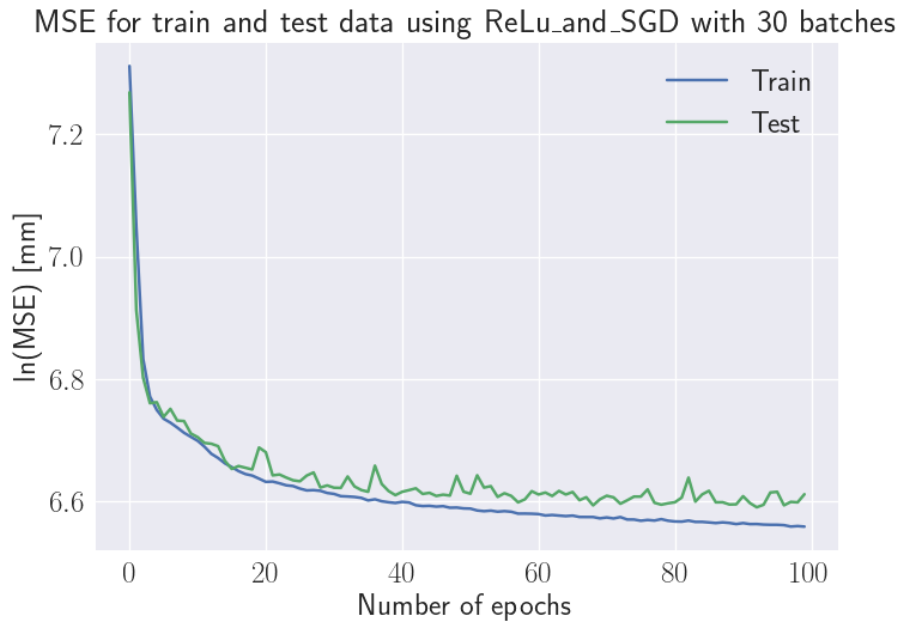


Figure 3.8: The validation accuracy for Convolutional Neural Network with 10 000 samples (20x20 matrix) with ReLU activation function.

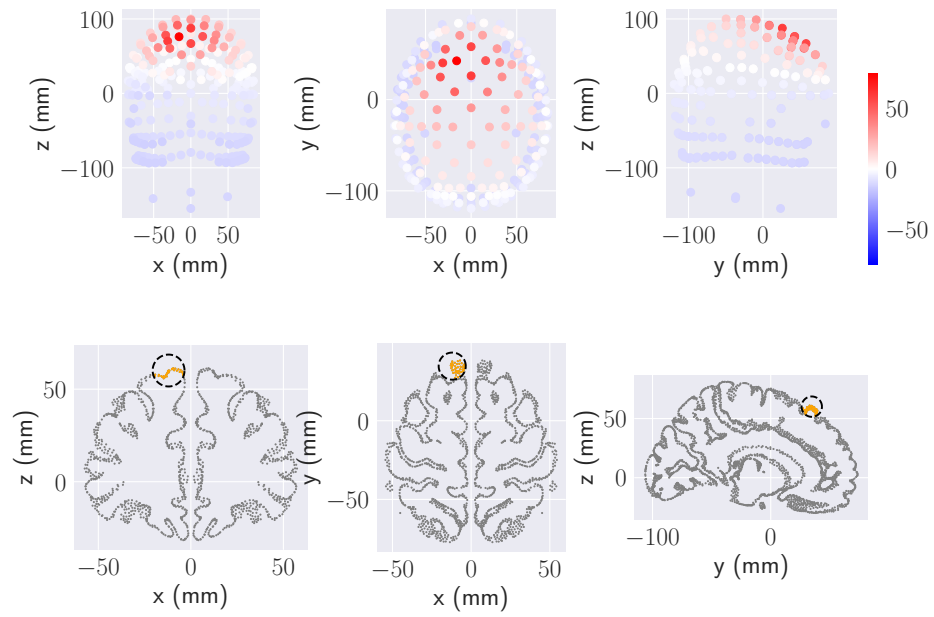


Figure 3.9: EEG for a sample containing a spherical population of current dipole sources with a random center within the cerebral cortex. The EEG measure is seen from both sides (x-, z-plane and y-, z-plane) and above (the x-, y-plane). EEG electrode locations are presented as filled circles, where the color of the fill represents the amplitude of the measured signal for the given electrode.

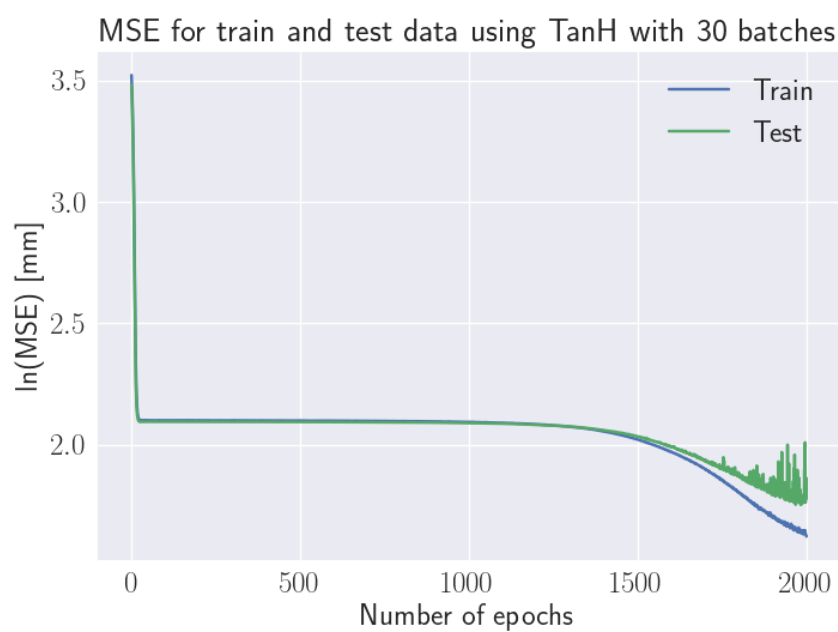


Figure 3.10: The validation accuracy for the simple Feed Forward Neural Network, predicting both center and radius for 10 000 samples, for 2000 epochs, with a learning rate equal to 0.0001.

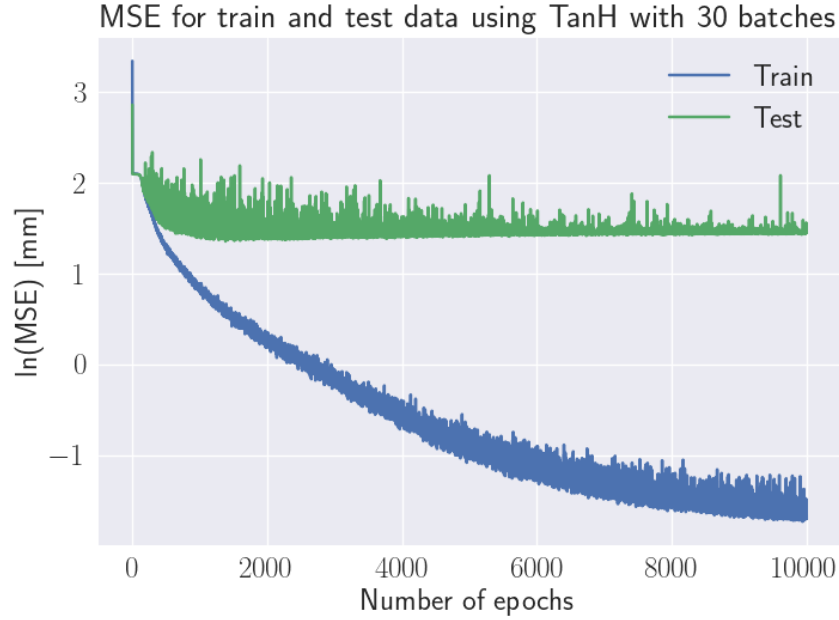


Figure 3.11: The validation accuracy for the simple Feed Forward Neural Network, predicting both center and radius for 10 000 samples, for 10000 epochs, with a learning rate equal to 0.001.

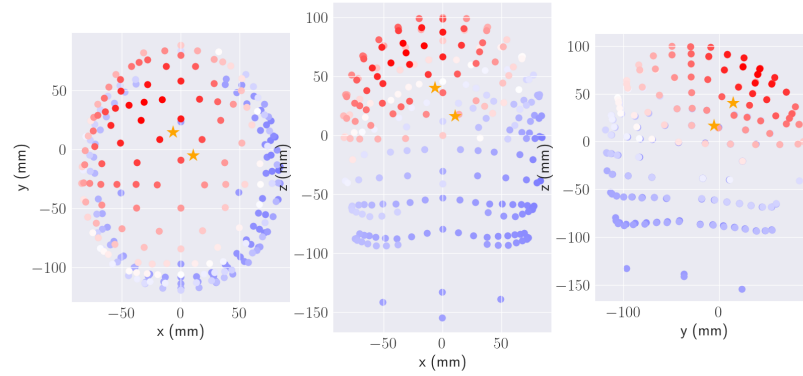


Figure 3.12: EEG for a sample containing two current dipole sources at random positions within the cerebral cortex. The EEG measure is seen from both sides (x-, z-plane and y-, z-plane) and above (the x-, y-plane). EEG electrode locations are presented as filled circles, where the color of the fill represents the amplitude of the measured signal for the given electrode. The positions of the current dipole moments are marked with yellow stars.

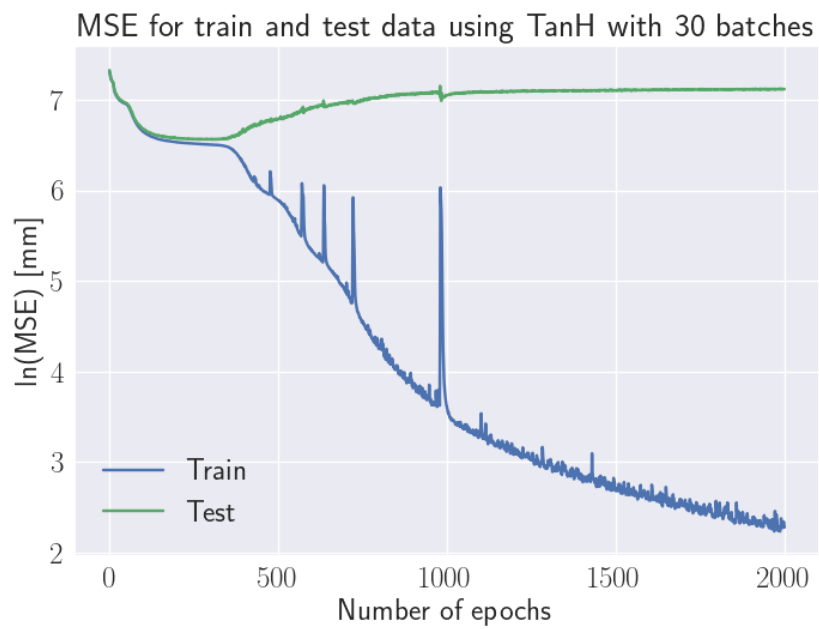


Figure 3.13: The validation accuracy for the simple Feed Forward Neural Network, predicting two current dipole sources.



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