

Definition 3. A quantum q in an integral domain R will be called a prime quantum if

- (1) for every n and for every $q_1, q_2 \mid q^n$, $q_1 \mid q_2$ or $q_2 \mid q_1$
 (2) if q is non co-prime to ab then for every n and for every $q_1 \mid q^n$ which divides ab , $q_1 = q_1' q_2$ such that $q_1' \mid a$ and $q_2 \mid b$ i.e. every factor of q^n is primal.

We recall that an element x in an integral domain is

called primal if $x \mid ab$ implies that $x = yz$, $y \mid a$ and $z \mid b$

and an integrally closed integral domain in which every

non zero element is primal is a Schreier domain. More over an HCF domain is a Schreier domain (cf [5] p.254).

Looking back at the Definitions 1 and 3, we note that

an atom vacuously satisfies the condition for an element to be a quantum, while a prime p is a prime quantum because every factor of p^n is primal and this marks the basic

difference between the concepts of a quantum and of a prime quantum.

Definition 4. Two prime quanta will be called similar if

they are non co-prime and dissimilar or distinct otherwise.

Lemma 1. In any integral domain R .

- (1) Any non unit factor of a prime quantum is a prime

quantum.

- (2) If q_1, q_2 are similar prime quanta then $q_1 \mid q_2$ or $q_2 \mid q_1$.
 (3) If q_1, q_2 are similar prime quanta then $q_1 q_2$ is a

prime quantum similar to them.

- (4) If a prime quantum q divides ab completely, that is there is no prime quantum $q' \mid ab$ such that $q \nmid q'$ properly;

then $q = q_1 q_2$ where $a = a_1 q_1$, $b = b_1 q_2$ and

$$(a_1, q) = 1 = (b_1, q).$$

- (5) The relation of similarity between prime quanta is