g<sup>8</sup> ∈ d<sup>7</sup> − d<sup>8</sup>).

Replacing  $d_2$  by  $d_3=(y_2,d_2)$ , where  $y_2\in q_1-q_4$ , and repeating the process, we conclude that there exists a factor d of x such that d  $\in q_1$  and d  $\not\in q_i$  (  $j=2,3,\ldots,r$ ). In other words, with a suitable permutation of  $\{q_i\}_{j=1}^r$  we have

proved the

Lemma 2. Let x be a non zero non unit of an HCF ring R of

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Krull type with the family {  $P_{\alpha}$  { $_{\alpha \in \ I}$  of valued primes defining  $R_{\mathfrak{p}}$  {  $P_{\mathfrak{p}}$  ,..., $P_{\mathfrak{p}}$  } be the set of all the valued primes containing x and let {  $q_{\mathfrak{j}}$  }  $^{\mathfrak{p}}_{\mathfrak{j}=1}$  be the set of all the distinct minimal subvalued primes of x, then corresponding to each  $q_{\mathfrak{j}}$  there exists a  $p_{\mathfrak{j}}$  | x such that  $p_{\mathfrak{j}}$   $\mathfrak{e}$   $q_{\mathfrak{j}}$  and to each  $q_{\mathfrak{j}}$  there exists a  $p_{\mathfrak{j}}$  | x such that  $p_{\mathfrak{j}}$   $\mathfrak{e}$   $q_{\mathfrak{j}}$  and  $p_{\mathfrak{k}}$   $\mathfrak{e}$   $\mathfrak{f}$   $\mathfrak{f}$ 

 $p_j \not\in q_K \text{ for all } k \not\neq j \text{ ( } K,j = 1,2,\ldots,r\text{).}$  Lemma 2 leads to the notion of an element( in an HCF

ring of Krull type at present) with a single minimal subvalued prime and to study the properties of such elements

Lemma 3. Let d be a non zero non unit element in an HCF ring of Krull type R. Let  $P_1$ ,  $P_2$ ,..., $P_r$  be the only valued primes (in the family  $\{P_{\alpha}\}_{\alpha\in I}$ ) of R containing d and suppose that d has only one minimal subvalued prime q then (1) If  $d = d_1 d_2$ , then  $(d_1, d_2) = 1$  only if either of  $d_l$ 

is a unit ( i = 1,2).

(2) If  $x \notin q$  but the set of all the valued primes containing x is a subset of {  $P_1, P_2, \ldots, P_r$ } then  $x^n \mid d$  for all positing

tive integers n.

q as the only minimal subvalued prime containing it, then d'belongs to P<sub>1</sub>, P<sub>2</sub>,... P<sub>r</sub> and to no other valued prime in the defining family and there exists a positive integer n such