

hence of the minimal subvalued primes) remains the same.
 Suppose that y_i are permuted such that, x_k, y_k are in the
 same minimal subvalued prime q , then $x_k \mid (y_k^r, x) =$
 $(y_k, y_1 y_2 \dots y_m) = y_k$ that is $x_k \mid y_k$, and similarly we can
 show that $y_k \mid x_k$. I.e. for each packet $x_k \mid x = x_1 x_2 \dots x_n$ there
 exists its associate $y_k \mid x = y_1 y_2 \dots y_m$ which is the required
 result.
 Corollary 1. In an HCF *-GKD a packet is rigid and hence
 an HCF *-GKD is a Semirigid Domain.
 Proof. We recall that a *-GKD R is a ring of Krull type
 with the family $\{P_i^{\alpha_i}\}$ of primes defining it, such that for
 $\alpha \neq \beta \in I, P_\alpha \cap P_\beta$ contains no non zero prime ideal (cf
 Def. 3 Ch. 2, and Def. 3 of this chapter).
 Let q be a packet in the HCF *-GKD R and let Q be the
 minimal subvalued prime containing q (it can be easily
 deduced from Lemmas 2 and 3 that in an HCF ring of Krull
 type an element x is a packet iff it has a single minimal
 subvalued prime), then q is contained in a single valued
 prime P of R (because of * 3 of Def. 3, Ch. 2). And obviously
 every non unit factor of q is in P (since otherwise q will
 not be in a single minimal subvalued prime e.g. if $q \in P, P'$
 with no containment relation between P and P' ; P' contains a
 minimal subvalued prime q' of q such that $q \neq q'$).
 Now let q_1, q_2 be two non unit factors of q then
 $q_1, q_2 \in P$. We claim that $(q_1, q_2) \neq 1$ for if $(q_1, q_2) = 1$ in R
 then since R is an HCF domain $(q_1, q_2) = 1$ in R_P i.e. at least
 one of q_1, q_2 is a unit in R_P which in other words means that
 at least one of q_1, q_2 is not in P a contradiction implying
 that no two non unit factors of q are co-prime. We now take
 any two non unit factors q', q'' of q and