

12/03/19

Q. find a person can play or not in weather conditions; Outlook = rainy, temperature = ~~rainy~~
windy = weak. Probability that can play a game.

80

$$P(\text{Outlook} = \text{rainy} | \text{play} = \text{yes}) = 3/9.$$

$$P(\text{temp} = \text{mild} | \text{play} = \text{yes}) = 4/9$$

$$P(\text{humidity} = \text{normal} | \text{play} = \text{yes}) = 6/9$$

$$P(\text{windy} = \text{weak} | \text{play} = \text{yes}) = 6/9$$

Probability that can't play a game.

$$P(\text{outlook} = \text{rainy} | \text{play} = \text{no}) = 2/5$$

$$P(\text{temp} = \text{mild} | \text{play} = \text{no}) = 2/5$$

$$P(\text{humidity} = \text{normal} | \text{play} = \text{no}) = 1/5$$

$$P(\text{windy} = \text{weak} | \text{play} = \text{no}) = 2/5$$

$$P(x | \text{play} = \text{yes}) \times P(\text{play} = \text{yes})$$

$$= \left(\frac{3}{9} \times \frac{4}{9} \times \frac{6}{9} \times \frac{6}{9} \right) \times \frac{9}{14} = 0.0423$$

0.0423

0.009

0.046

$$P(x | \text{play} = \text{no}) \times P(\text{play} = \text{no})$$

$$= \frac{2}{5} \times \frac{2}{5} \times \frac{1}{5} \times \frac{2}{5} \times \frac{5}{14} = 0.0045$$

$$P(A|C) = \frac{P(C|A)P(A)}{P(C)} \quad \text{to get } P_C = 0.0468$$

$$P(\text{play} = \text{yes} | x) = 0.0423 / 0.0468 = 0.925 \cdot 0.903$$

$$P(\text{play} = \text{NO} | x) = 0.0045 / 0.0468 = 0.0965$$

2. for a given dataset patient details with attribute, cold, runny nose, headache, fever, flu find whether the person is having flu or not for the given symptoms cold = yes, runny nose = no, headache = mild, fever = yes.

	cold	Runny nose	headache	fever	Classlabel
1	Yes	No	Mild	Yes	No
2	Yes	Yes	No	No	Yes
3	Yes	No	Strong	Yes	Yes
4	No	Yes	Mild	Yes	Yes
5	No	No	No	No	No
6	No	Yes	Strong	Yes	Yes
7	No	Yes	Strong	No	No
8	Yes	Yes	Mild	Yes	Yes

Cold

Yes

No

Yes No

P(Yes) P(No)

~~1/8~~ 3/8 1/3

P(Yes) = 5/8

P(No) = 3/8

Runny nose

No

Yes No f(Yes) f(No)

~~1/8~~ 3/8 1/3

Compare with Classlabel

Headache

Mild

Severe

Yes No f(Yes) f(No)

2 1 2/5 1/3

2/03/19

1 find a person can play or not is weather conditions; outlook = rainy, temperature = nominal, wind = weak. Probability that can play a game.

$$P(\text{outlook} = \text{rainy} | \text{play} = \text{yes}) = 3/9.$$

$$P(\text{temp} = \text{mild} | \text{play} = \text{yes}) = 4/9$$

$$P(\text{humidity} = \text{nominal} | \text{play} = \text{yes}) = 6/9$$

$$P(\text{windy} = \text{weak} | \text{play} = \text{yes}) = 7/9.$$

Probability that can't play a game.

$$P(\text{outlook} = \text{rainy} | \text{play} = \text{no}) = 2/5$$

$$P(\text{temp} = \text{mild} | \text{play} = \text{no}) = 2/5$$

$$P(\text{humidity} = \text{nominal} | \text{play} = \text{no}) = 1/5$$

$$P(\text{windy} = \text{weak} | \text{play} = \text{no}) = 2/5$$

$$P(x | \text{play} = \text{yes}) \times P(\text{play} = \text{yes})$$

$$= \left(\frac{3}{9} * \frac{4}{9} * \frac{6}{9} * \frac{7}{9} \right) \times \frac{9}{14} = 0.0423$$

0.0423

0.2041

0.0465

$$P(x | \text{play} = \text{no}) \times P(\text{play} = \text{no})$$

$$= \frac{2}{5} * \frac{2}{5} * \frac{1}{5} * \frac{2}{5} * \frac{5}{14} = 0.0045$$

$$P(A|C) = \frac{P(C|A)P(A)}{P(C)}$$

$$\text{to get } P_C = 0.0468$$

$$P(\text{play} = \text{yes} | x) = 0.0423 / 0.0468 = 0.903$$

$$P(\text{play} = \text{NO} | x) = 0.0045 / 0.0468 = 0.0967$$

2. for a given dataset patient details with attribute, cold, runny nose, headache, fever, flu find whether the person is having flu or not for the given symptoms cold = yes, runny nose = no, headache = mild, fever = yes.

	cold	Runny nose	headache	fever	Classlabel
1	Yes	No	Mild	Yes	No
2	Yes	Yes	No	No	Yes
3	Yes	No	Strong	Yes	Yes
4	No	Yes	Mild	Yes	Yes
5	No	No	No	No	No
6	No	Yes	Strong	Yes	Yes
7	No	Yes	Strong	No	Yes
8	Yes	Yes	Mild	Yes	No

Cold

Yes

Yes No

P(Yes) P(No)

P(Yes) = 5/8

No

3/5 2/3

P(No) = 3/8

Runny nose

Yes

Yes No f(Yes) f(No)

Compare with

No

No f(Yes) f(No)

Classlabel

headache

Mild

Yes No f(Yes) f(No)

Severe

2 1 2/5 1/3

<u>fever</u>	yes	no	$P(\text{yes})$	$P(\text{no})$
yes	4	1	$4/5$	$1/5$

Probability of having flu.

$$P(\text{cold} = \text{yes} \mid \text{flu} = \text{yes}) = 3/5$$

$$P(\text{runny nose} = \text{no} \mid \text{flu} = \text{yes}) = 1/5$$

$$P(\text{headache} = \text{mild} \mid \text{flu} = \text{yes}) = 2/5$$

$$P(\text{fever} = \text{yes} \mid \text{flu} = \text{yes}) = 4/5$$

Probability of not having flu

$$P(\text{cold} = \text{yes} \mid \text{flu} = \text{no}) = 1/3$$

$$P(\text{runny nose} = \text{no} \mid \text{flu} = \text{no}) = 2/3$$

$$P(\text{headache} = \text{mild} \mid \text{flu} = \text{no}) = 1/3$$

$$P(\text{fever} = \text{yes} \mid \text{flu} = \text{no}) = 1/3$$

$$P(x \mid \text{play} = \text{yes}) \times P(\text{play} = \text{yes})$$

$$= \frac{3}{5} \times \frac{1}{5} \times \frac{2}{5} \times \frac{4}{5} \times \frac{5}{8} = 0.024$$

$$P(x \mid \text{play} = \text{no}) \times P(\text{play} = \text{no})$$

$$= \frac{1}{3} \times \frac{2}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{3}{8} = 0.009$$

$$P(c) = 0.024 + 0.009 = 0.033$$

$$P(\text{flu} = \text{yes} \mid x) = 0.024 / 0.033 = 0.727$$

$$P(\text{flu} = \text{no} \mid x) = 0.009 / 0.033 = 0.273$$

14/03/19

2 2 4 4

Distance Based algorithms

Classification is determining the what group something belongs to.

User sets a value for k.

for the data record that needs to be classified, the alg computes the distance b/w the database records and all of the reference data records.

3. find the k no. of closest data records

4. the majority of the class of the 'k' data records is the predicted class.

for a given dataset with the attributes weight as well as height and the class label. find the person belongs to which class based on given weight 57kgs & height 170cm.

<u>weight</u>	<u>height</u>	<u>class</u>	<u>distance</u>
51	167	Under weight	6.7
62	182	normal	13
69	176	"	13.4
64	173	"	7.6
65	179	Over weight	15.2
56	174	Under weight	4.1
58	169	Normal	1.4 (N1)
57	173	"	3 (N3)
55	170	"	2 (N2)

Step 1: let. $K=3$

Step 2: distance can be find.

$$= \sqrt{(57-51)^2 + (170-167)^2} = 6.7$$

$$\sqrt{(57-62)^2 + (170-182)^2} = 13$$

etc... we hire class
80 57 170 normal

The datapoint or 3 neighbours belongs to normal class. Hence, the given datapoint can be classified or placed into the normal class.

→ if no. of. parameters for a given class label is 2, then it is called as binary classification.

Remarks abt K: K must be the integer.

→ K must not be a multiple of a given no. of. class labels.

→ $K \geq 1$. The least dist. will be the neighbour for given data record.

Q: The given data record contains 3 attributes name, age & gender and the class label is fan following, find the person belongs to which class when the age = 20 & gender = male.

age = 20, gender = M^o fanfollowing? Name dist

age	gender	fanfollowing	x_1
32	male o		
40	male o		
16	dom i		
14	f i		
55	m. o		
40	m o		
20	f i		
15	m o		

A	12
B	20
C	4.16 (2)
D	6.1
E	35
F	20
G	1 (x 1)
H	25 (3)

$$\sqrt{(5)^2 + 0^2}$$

let k=3.

assume the M=0, f=1

$$\sqrt{(20-32)^2 + (0-0)^2} = 12 \cdot \sqrt{ }$$

$$\sqrt{(20)^2} = 20$$

$$\sqrt{16+1} = \sqrt{17}$$

$$\sqrt{36+1} = \sqrt{37}$$

efc.

This given datapoint can be classified or placed into the fanfollowing x_2 .

3) For the given set of attributes age, income, student rating, credit, Churnlabel vice computer, find whether a person buys Computer or not with a given value
 age = youth, income = medium, student = yes, credit rating = fair. classify

<u>age</u>	<u>income</u>	<u>student</u>	<u>credit rating</u>
1. Youth	high	no	fair, no
2. Youth	high	no	excellent, no
3. middle aged	high	no	fair, yes
4. Senior	medium	no	fair, yes
5. Senior	low	yes	fair, yes
6. Senior	low	yes	excellent, no
7. middle aged	low	yes	excellent, yes
8. Youth	medium	no	fair, no
9. Youth	low	yes	fair, yes
10. Senior	medium	yes	fair, yes
11. Youth	medium	yes	excellent, yes
12. middle aged	medium	no	excellent, yes
13. middle aged	high	yes	fair, yes
14. Senior	medium	no	excellent, no

$$\begin{array}{cccc}
 \cancel{\text{ages}} & \cancel{P_i} & \cancel{n_i} & P(\text{Yes}) = 9/14 \\
 \cancel{\text{youth}} & 2 & 3 & \\
 \end{array}
 \quad P(\text{No}) = 5/14$$

$$D_2(P_{\text{Yes}}) = \frac{0.4}{8} \log_2 \left(\frac{2}{3} \right) + \frac{0.6}{8} \log_2 \left(\frac{3}{5} \right)$$

$$0.4 \log_2 (0.4) + 0.6 \log_2 (0.6)$$

age: youth

$$P(\text{age} = \text{youth} | \text{buys - computer} = \text{yes}) = 2/9$$

$$P(\text{age} = \text{youth} | \text{buys - computer} = \text{no}) = 3/5$$

income: medium

$$P(\text{income} = \text{medium} | \text{buys - computer} = \text{yes}) = 4/9$$

$$P(\text{income} = \text{medium} | \text{buys - computer} = \text{no}) = 2/5.$$

Student:

$$P(\text{student} = \text{yes} | \text{buys - computer} = \text{yes}) = 6/9$$

$$P(\text{student} = \text{yes} | \text{buys - computer} = \text{no}) = 1/5.$$

credit - rating:

$$P(\text{Credit - rating} = \text{fair} | \text{buys - computer} = \text{yes}) = 6/9$$

$$P(\text{Credit - rating} = \text{fair} | \text{buys - computer} = \text{no}) = 2/5$$

$$P(X | \text{buys - computer} = \text{yes}) \times P(\text{buys - computer} = \text{yes})$$

$$\geq \frac{2}{9} \times \frac{4}{9} \times \frac{6}{9} \times \frac{6}{9} \times \frac{9}{14}$$

$$\approx \frac{16}{867} = 0.0185$$

$$P(X | \text{buys - computer} = \text{no}) \times P(\text{buys - computer} = \text{no}) = \frac{3}{5} \times \frac{2}{5} \times \frac{1}{5} \times \frac{2}{5} \times \frac{5}{14}$$

$$= 0.0068$$

$$P(C) = 0.0185 + 0.0068$$

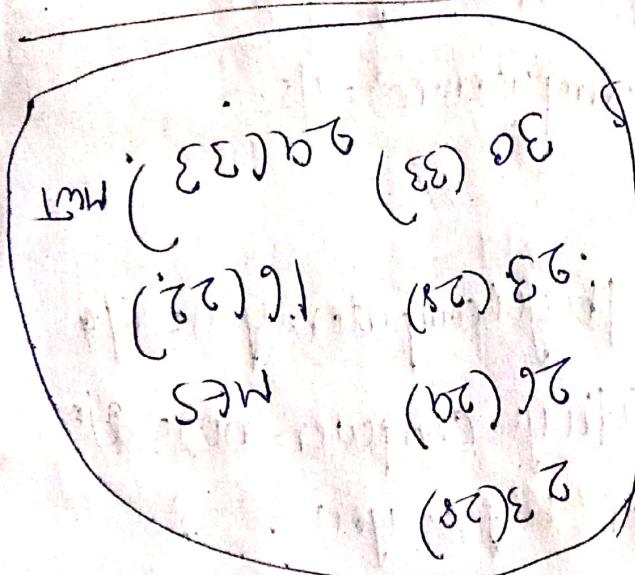
$$= 0.0253 = 0.0348$$

for "Yes":

$$\frac{P(X|\text{boys: yes}) P(\text{boys: yes})}{P(C)} = \frac{0.028}{0.034} = 0.80$$

for NO:

$$\frac{P(X|\text{boys: no}) P(\text{boys: no})}{P(C)} = \frac{0.0068}{0.034} = 0.19.$$



30(33) ACC

24(28) MWT

27(29) CN

26(28) PWT

30(33)
24(28)

The probability of yes is having ~~high~~ [>] than probability of no.

- 1. The person can go for buying a Computer
- 2. This is ~~false~~ positive.

18/03/19

Decision tree

1. consider the following small datasets for the 2 classes of woods. using info gain construct a decision tree to classify the data set.

<u>Density</u>	<u>Grain</u>	<u>Hardness</u>	<u>Class</u>
Heavy	Small	Hard	Oak
Heavy	Large	Hard	Oak
Heavy	Small	Hard	Oak
Light	Large	Soft	Oak
Light	Large	Hard	Pine
Heavy	Small	Soft	Pine
Heavy	Large	"	Pine
Heavy	Small	Soft	Pine

→ which attribute the info gain chooses as the root of the tree.

→ what class does the tree infer for the sample Density = light, grain = small, hardness = hard

→ what class does the tree infer for the sample d = light, grain = small, hardness = soft.

→ d = heavy, grain = small, h = hard.

Assume P = Oak, M = pine.

4 4

$$IG = -\frac{P}{P+N} \log_2 \left(\frac{P}{P+N} \right) - \frac{N}{P+N} \log_2 \left(\frac{N}{P+N} \right)$$

$$IG(4,4) = -\frac{4}{8} \log_2 \left(\frac{4}{8} \right) - \frac{4}{8} \log_2 \left(\frac{4}{8} \right) \Rightarrow -\frac{1}{2} \log_2 \left(\frac{1}{2} \right) - \frac{1}{2} \log_2 \left(\frac{1}{2} \right)$$

If P, n = Same then $\Omega G = 1$

Entropy for the density.

		E for density we have	
heavy	P_i	n_i	$\Omega G(P_i, n_i)$
	3	3	1
light	1	1	1

$$\Omega G(3,3) = 1$$

$$\Omega G(1,1) = 1$$

$$E(d) = \sum_{i=1}^2 \frac{P_i + n_i}{P+n} \Omega G(P_i, n_i)$$

$$= \frac{8}{8} = 1$$

Entropy for Grain

		n_i	$\Omega G(P_i, n_i)$	$\Omega G(D) = \Omega G - E(G)$
large	P_i	2	1	$= 1 - 1$
small	2	2	1	$= 0$

$$\Omega G(2,2) = 1$$

$$\Omega G(2,2) = 1$$

$$E(G) = \sum_{i=1}^2 \frac{P_i + n_i}{P+n} \Omega G(P_i, n_i)$$

$$\frac{4}{8}(1) + \frac{4}{8}(1) \Rightarrow \frac{1}{2} + \frac{1}{2} = 1$$

$$\Omega G(G) = \Omega G - E(G)$$

$$= 1 - 1 = 0.$$

Entropy for hardness

	P _i	n _i	I.G(P _i , n _i)
hard	3	1	0.81
soft	1	3	0.81

$$I.G(3,1) = -\frac{0.75}{4} \log_2\left(\frac{3}{4}\right) - \frac{0.25}{4} \log_2\left(\frac{1}{4}\right)$$

$$\approx -0.75 \log_2(0.75) - 0.25 \log_2(0.25) \\ \approx 0.81$$

$$I.G(1,3) = -\frac{1}{4} \log_2\left(\frac{1}{4}\right) - \frac{3}{4} \log_2\left(\frac{3}{4}\right)$$

$$\approx -0.25 \log_2(0.25) - 0.75 \log_2(0.75) \\ \approx 0.81$$

$$E(h) = \sum_{i=1}^4 \frac{P_i + n_i}{P+n} I.G(P_i, n_i)$$

$$\approx \frac{4}{8}(0.81) + \frac{4}{8}(0.81)$$

$$\approx 1.62 \cdot 0.81$$

$$H.G(h) = 1 - E(h)$$

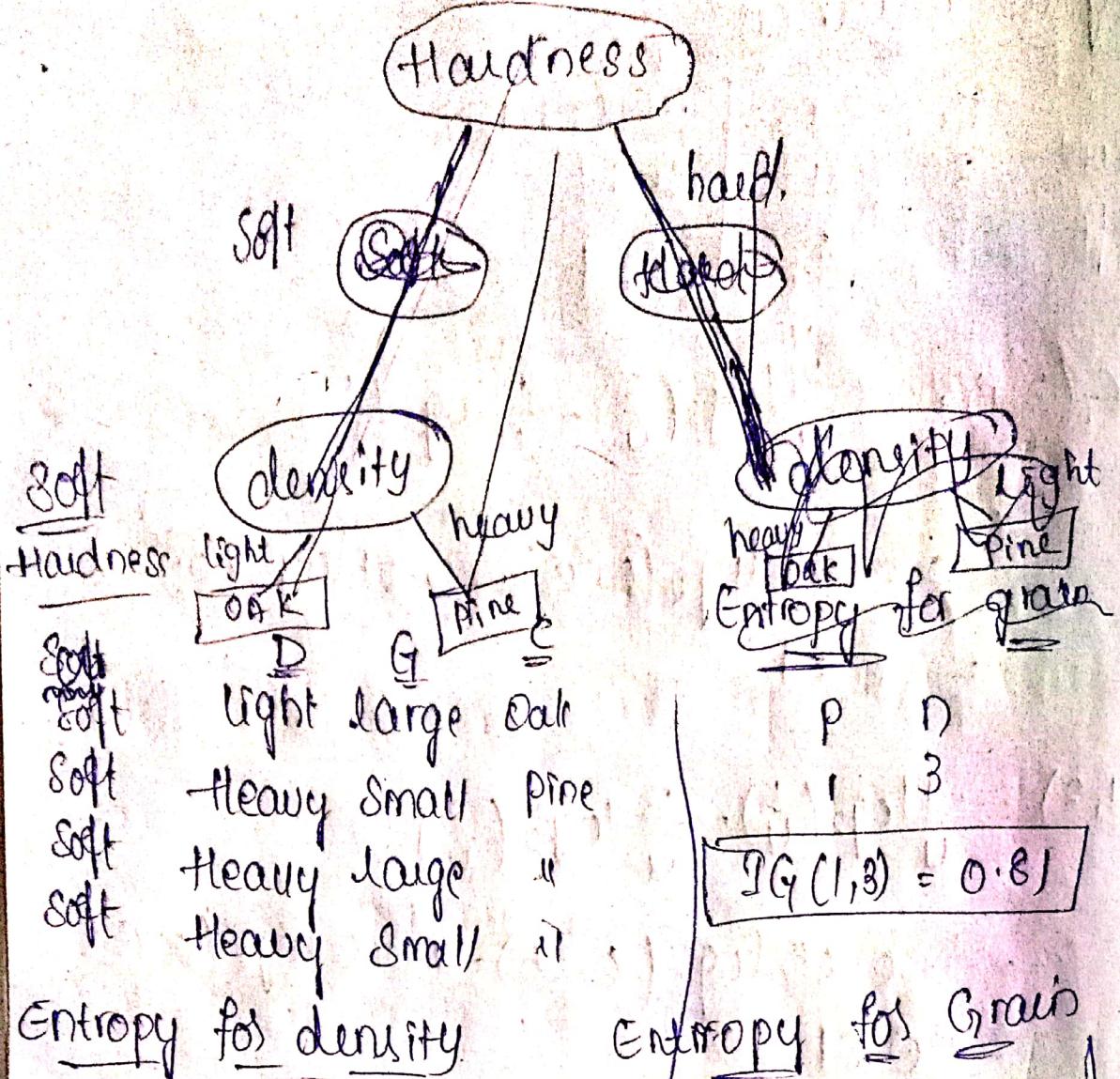
$$\approx 1 - 0.81$$

$$\approx 0.19$$

$$G(D) = 0$$

$$G(G) = 0$$

$$G(H) = 0.19 \quad \left. \begin{array}{l} \text{high heat value} \\ \text{in } G(H) \end{array} \right\}$$



Entropy for density

light	1	0		0
heavy	0	3		0

$$E(D) = 0$$

$$\text{Gain}(D) = 0.81 - 0.$$

Flora

$$G(D) = 0.819 \text{ max.}$$

$$G(G) = 0.3)$$

density



bcoz heavily fol pine

above datafile.

Scanned by CamScanner

<u>hardness</u>	<u>d</u>	<u>Grain</u>	<u>clay</u>
hard	heavy	Small	Oak
hard	heavy	large	Oak
hard	heavy	small	Oak
hard	light	large	Pine

<u>Entropy (d)</u>	<u>E(d)</u>	p_i	n_i	$DG(p_i, n_i)$
heavy		3	0	0
light		0	1	0

$$E(D) = 0$$

$$G(D) = 0.81 - 0$$

<u>Entropy (G)</u>	<u>G(G)</u>	n_i	p_i	$DG(p_i, n_i)$
small		2	0	0
large		1	1	1

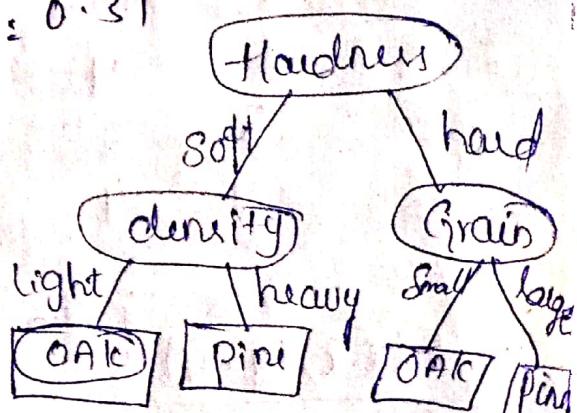
$$E(G) = \frac{1}{2}$$

$$G(G) = 0.31$$

$$G(D) = 0.81 \quad \left. \begin{array}{l} \\ \end{array} \right\} \text{Max}$$

$$G(G) = 0.31 \quad \left. \begin{array}{l} \\ \end{array} \right\}$$

<u>Grain</u>	<u>d</u>	<u>h</u>	<u>clay</u>
large	heavy	hard	Oak
large	light	soft	Oak
large	light	hard	Pine
large	heavy	soft	Pine



$$E(d)$$

$$\begin{matrix} \text{heavy} \\ \text{light} \end{matrix}$$

$$\begin{matrix} 1 & 1 & 1 & 1 \end{matrix}$$

$$DG(d) = 1 - 0$$

$$= 1$$

Statistical Based algorithms

• 1. Bayes

2. regression line,

→ find the regression line for given data.

By using the regression we can predict

the regression line or the best fit line

→ If there is only one dependent variable
then it is called as linear regression

$$y = mx + c.$$

→ In the multiple regression we may have
diff no. of dependent variables.

x	y	$x - \bar{x}$	$y - \bar{y}$	$(x - \bar{x})(y - \bar{y})$	$(x - \bar{x})^2$
1	3	-2	-0.6	1.2	4
2	4	-1	0.4	-0.4	1
3	2	0	-1.6	0	0
4	4	1	0.4	0.4	1
$\bar{x} = 3$	$\bar{y} = 3.6$			<u>1.28</u>	<u>4</u>
				<u><u>4.8</u></u>	<u><u>10</u></u>

$$m = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x - \bar{x})^2}$$

$$= \frac{4.8}{10} = 0.48$$

$$y = mx + c.$$

$$3.6 = 0.4(3) + c.$$

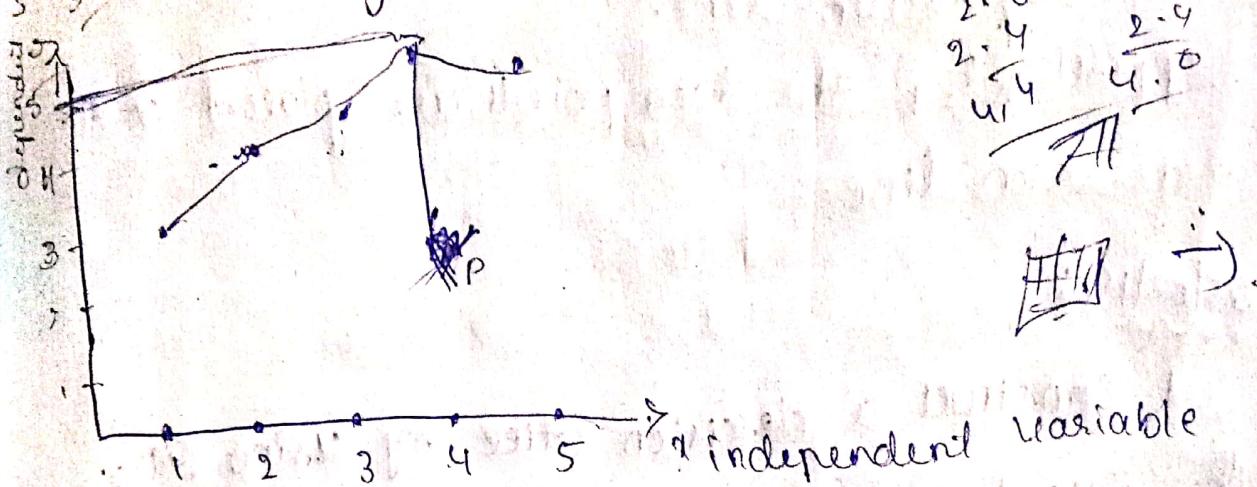
$$c = 2.4$$

$$\boxed{y = 0.4x + 2.4}$$

$$x=1 \quad y = 0.4 + 2.4 \Rightarrow 2.8$$

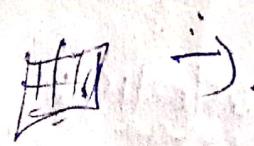
$$x=2 \quad y = 3.2$$

$$\begin{array}{lll} x=3 & y = 3.6 \\ x=4 & y = 4.0 \\ x=5 & y = 4.4 \end{array}$$



$$\begin{array}{r}
 0.4 \\
 3.1 \\
 1.2 \\
 2.4 \\
 \hline
 7.6 \\
 \hline
 0.4 \\
 1.6 \\
 \hline
 5 \\
 \hline
 2.0 \\
 2.4 \\
 \hline
 4.4 \\
 \hline
 4.0
 \end{array}$$

All



The distance b/w actual point and the predicted line can be called as error.

* The line with the least error is regression.

line of best fit.

R^2 is a statistical measure of how close the data are fitted to the regression line.

It is also known as coefficient of determination.

$$R^2 = \frac{\sum (y_p - \bar{y})^2}{\sum (y - \bar{y})^2} \quad y_p \text{ is predicted values}$$

x	y	y_p	$y_p - \bar{y}$	$(y_p - \bar{y})^2$	$y - \bar{y}$	$(y - \bar{y})^2$
1	2.8	2.8	-0.8	0.64	-0.6	0.36
2	3.2	3.2	-0.4	0.16	0.4	0.16
3	3.6	3.6	0	0	-1.6	2.56
4	4.0	4.0	0.4	0.16	0.4	0.16
5	4.4	4.4	0.8	0.64	1.4	1.96
$\Sigma = 2.6$				$\Sigma = 1.6$		$\Sigma = 5.2$

$$R^2 = \frac{1.6}{5.2} \approx 0.32.$$

$R^2 = 0.32$ (is not a good fit line) that means the data points are far away from the regression line.

Suppose $R^2 = 1$ the data points are placed in a regression line

Q5/03/19:

1. Construct a decision tree by using ID₃.
the procedure for constructing a decision by using ID₃ is similar to procedure of J_{4.8}.
But in the ID₃ entropy can be used as a splitting parameter.

→ whereas in J_{4.8} gain ratio or gini can be used as splitting parameter.

→ C_{4.5} classifier improves the ID₃ alg in the following ways.

It is similar to ID₃.

→ (i) missing data: whether decision tree is built missing data is ignored.

→ pruning: there are 2 primary pruning strategies proposed in C_{4.5} the 1st one is

Subtree replacement, the second one is Subtree raising.

(i) Subtree replacement: A subtree is replaced by a leaf node. If this replacement results in a error rate close to that of original tree.

→ Subtree replacement works from the bottom of the tree upto the root.

(ii) Subtree raising: It replaces a subtree by its most used subtree.

(iii) Splitting: C4.5 uses the largest gain ratio for the splitting.

$$\text{Gain ratio } (D, S) = \frac{\text{Gain}(D, S)}{H\left(\frac{|D_1|}{|D|}, \dots, \frac{|D_S|}{|D|}\right)}$$

$$\text{Gain}(D) = H(D) - \sum_{i=1}^S P(D_i) H(D_i)$$

$$H(p_1, p_2, p_3) = \sum_{i=1}^S \left(p_i \cdot \log\left(\frac{1}{p_i}\right) \right)$$

CART: Classification and regression tree is a technique that generates a binary decision tree. If with ID₃, entropy is used as a measure to choose the best splitting attribute.

Neural Network Based alg

<u>Gender</u>	<u>Height</u>	<u>Class</u>
F	1.6m	short
M	2m	tall
F	1.9m	medium
F	1.88m	medium
F	1.7m	short
M	1.45m	medium
P	1.7m	Tall

- Advantages: Neural nets are more robust than the decision tree because of the weights.
- NN improves its performance by learning.
 - There is a slow error rate and thus a high degree of accuracy once the appropriate training has been performed.
 - NN are more robust than decision trees in the noisy environments.

Neural N/w: A neural n/w is a set of connected imp & op units or nodes in which each connection has a weight associated with it.

disadvantages of ANN:

Neural nets are difficult

to understand

→ Generating rules from NN is not straight forward.

→ learning its with decision trees : Overfitting may result.

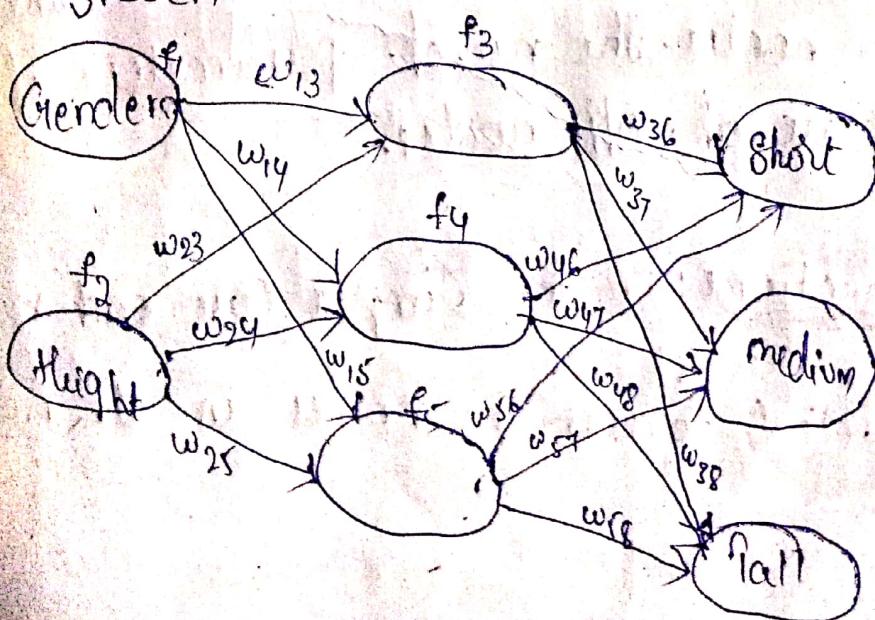
→ the learning phase may fail to converge

→ NN may be quite expensive to use.

→ I/P all values must be numeric

for numeric NW dataset

<u>name</u>	<u>Gender</u>	<u>height</u>	<u>class</u>
K	f	1.6m	short
Pim	m	2m	tall
maggie	f	1.9m	medium
Bob	m	1.88m	medium
Dare	m	1.7m	short
steven	m	2.0m	tall



There are several issues to be examined
attribute (no. of source nodes); all can be used
as I/Ps (or) source nodes.

→ Determining which attributes to use as I/Ps is an issue.

→ no. of hidden layers: in the simpler case there
is only one hidden layer.

hidden layer: the layer which is in b/w. source
node and destination node.

no. of hidden nodes: the nodes of hidden layer
called as hidden nodes.

Choosing the best no. of hidden nodes for
hidden layer is one of the difficult prob
in neural netw.

Training data: no. of sinks (or) destination of op
the class parameter can be used at the node
destination nodes. The no. of parameters of a
class are no. of O/P nodes.

Interconnection:

In the simpler case each node
is connected to all the nodes in the next
level.

weight: the weight assigned to the edges indicates the relative weight b/w 2 nodes.
→ initial weights are usually assumed to be small +ve numbers and are assigned randomly.

activation functions: many diff types of activation functions can be used.

learning technique: the technique for adjusting the weights is called learning technique. many approaches can be used but the most common approach is some form of back propagation.

Stop the learning may stop when all the training tuples have propagated through

the Net.. Perceptron: A single neural net is called Perceptron.

→ A perceptron is a single neuron with multiple I/p & one o/p.

→ The activation function can be used as a sigmoid function

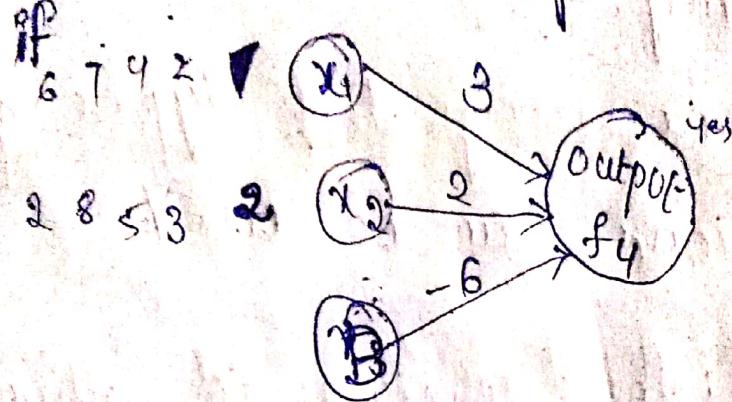
→ A simple perceptron can be used to classify into 2 classes.

→ using a unipolar activation function an o/p of 1 could be used to reclassify into 2 class

while output of 0 ~~would~~ be classified into another class.

Perception

Sigmoidal



5

if $S > 0$.

$$f_4 = \begin{cases} 1 & S > 0 \\ 0 & \text{Otherwise} \end{cases}$$

$3+4-6 = 1 \text{ yes}$

$6+0-6 = 0 \text{ no}$

$12+10-6 = 16 \text{ yes}$

$\frac{27}{35} - 6 = 31$

let us take simple dataset

16 = yes

n	x	class	predicted
1	2	yes	Yes (TP)
2	3	no	Yes (FP)
4	5	yes	Yes (TP)
7	8	yes	Yes (TP)
6	2	no	Yes (FP)

Correctly predicted $\Rightarrow \frac{3}{5} = 0.6 \Rightarrow 60\% \text{ predicted.}$

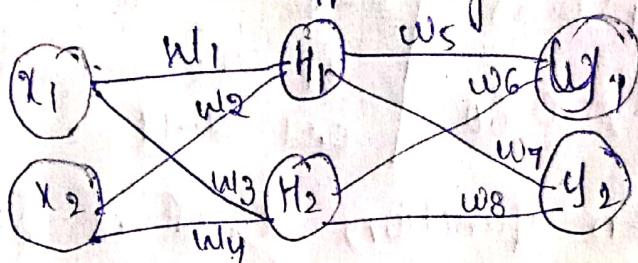
Total

Propagation: Normal approach used for processing is called propagation.

Processing: Taking i/p & producing o/p is called processing.

Given a tuple of values i/p to the neural net,

$X = \{x_1, x_2, \dots, x_n\}$ one value is i/p at each node in the i/p layer.



$$y_1 = H_1 w_5 + H_2 w_6$$
$$y_2 = H_1 w_7 + H_2 w_8$$
$$H_1 = x_1 w_1 + x_2 w_3$$
$$H_2 = x_1 w_2 + x_2 w_4$$

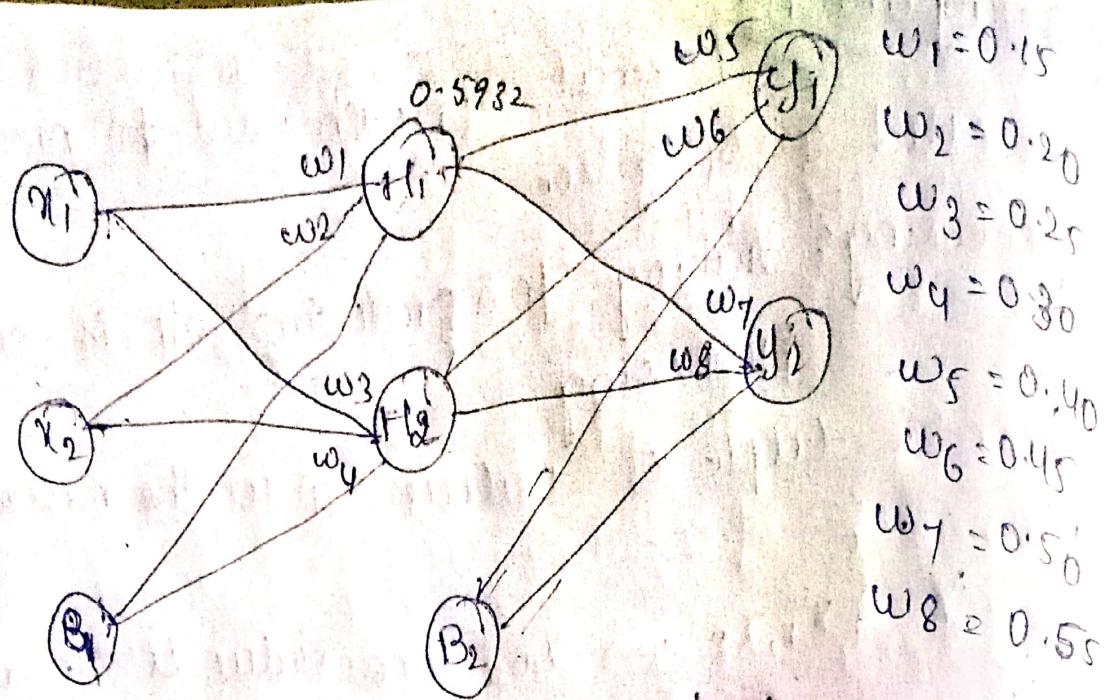
Then the summation and activation functions are applied at each node with an o/p value created for each o/p, ~~created~~ edge from that node.

→ These values are in turn send to the subsequent nodes.

→ This process continues until a tuple of o/p values $Y = \{y_1, y_2, y_3, \dots, y_n\}$

Backpropagation: It is a learning technique that adjusts weights in the neural net by propagating weight changes backward from sink to the same nodes.

Ex:



$$\begin{aligned}
 w_1 &= 0.15 \\
 w_2 &= 0.20 \\
 w_3 &= 0.25 \\
 w_4 &= 0.30 \\
 w_5 &= 0.40 \\
 w_6 &= 0.45 \\
 w_7 &= 0.50 \\
 w_8 &= 0.55
 \end{aligned}$$

$$\begin{array}{l|l}
 x_1 = 0.05 & B_1 = 0.35 \\
 \hline
 x_2 = 0.10 & B_2 = 0.60
 \end{array}
 \quad \text{Target value} \quad
 \begin{array}{ll}
 P_1 & P_2 \\
 0.01 & 0.99
 \end{array}$$

The activation function used is sigmoidal

$$f(x) = \frac{1}{1+e^{-x}}$$

Cal the value H₁,

$$\begin{aligned}
 H_1 &= x_1 w_1 + x_2 w_2 + B_1 \\
 &= 0.05 \times 0.15 + 0.10 \times 0.20 + 0.35 \\
 &\approx 0.3775
 \end{aligned}$$

$$\text{Op of } H_1 = \frac{1}{1+e^{-H_1}} = \frac{1}{1+e^{-0.3775}}$$

$$\begin{aligned}
 H_2 &= x_1 w_3 + x_2 w_4 + B_2 \\
 &= 0.05 (0.25) + 0.10 (0.30) + 0.35 \\
 &= 0.3925
 \end{aligned}$$

$$O.P \text{ of } H_2 \geq \frac{1}{1+e^{-0.5968}} = 0.5968$$

$$\begin{aligned} y_1 &= H_1 w_5 + H_2 w_6 + B_2 \\ &= 0.5932(0.40) + 0.5968(0.45) + 0.60 \\ &= 0.19728 + 0.5934 = 1.10584 \end{aligned}$$

$$O.P \text{ of } y_1 = \frac{1}{1+e^{-y_1}} = \frac{1}{1+e^{-1.105}} = 0.75$$

$$\begin{aligned} y_2 &= H_1 w_7 + H_2 w_8 + B_2 \\ &= 0.5932(0.50) + (0.5968)(0.55) + 0.60 \\ &= 1.22485 \end{aligned}$$

$$O.P \text{ of } y_2 = \frac{1}{1+e^{-y_2}} = \frac{1}{1+e^{-1.22485}} = 0.77294$$

~~O.P.~~ the O.P of y_1 & y_2 are not matching with

T_1, T_2 . Hence back propagate i.e., adjust the values of all the weights. The errors for each O.P node can be cal by

$$\sum_{i=1}^m \left(\frac{\text{Target - output of } y_i}{m} \right) \text{ m = no. of nodes}$$

$$< \text{total} = \frac{1}{2} (T_1 - \text{output of } y_1) + \frac{1}{2} (T_2 - \text{output of } y_2)$$

