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Question - 1:

Given Input  $\Sigma = \{a, b\}$

Language  $L = \{aa, aaa, aab, baa, bab, \dots\}$

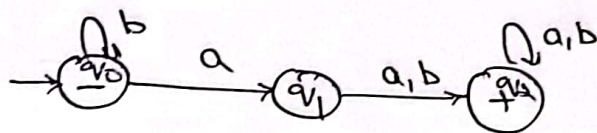
All words that have "a" as the 2<sup>nd</sup> letter and "a" as the 2<sup>nd</sup> and last letter

Solution:

Regular expression for the given is

$$b^* a (a+b) (a+b)^*$$

The finite automata (FA) for given regular expression is



$\rightarrow$  indicates starting state

$\circ$  indicates final state

\* The automata starts with "a" then it is processed to next state

\* After first state it is moving to next state upon a, b

\* In the final state it is accept any no. of a's and b's

Transition Table:

		a	b
-	$q_0$	$q_1$	$q_0$
	$q_1$	$q_2$	$q_2$
+	$q_2$	$q_2$	$q_2$

### Acceptable strings:

$$\begin{aligned} baa &= b^* a (a+b)(a+b)^* \\ &= b^1 a a \text{ (valid)} \end{aligned}$$

$$\begin{aligned} bab &= b^* a (a+b)(a+b)^* \\ &= b^1 a (b) \text{ (valid)} \end{aligned}$$

$$\begin{aligned} aabaa &= b^* a (a+b)(a+b)^* \\ &= a a b (a+b)^1 (a+b)^1 \text{ (valid)} \end{aligned}$$

$$\begin{aligned} aab &= b^* a (a+b)(a+b)^* \\ &= a (a+b) (a+b)^1 \text{ (valid)} \end{aligned}$$

### Invalid strings:

$$\begin{aligned} a &= b^* a (a+b)(a+b)^* \\ &= a \text{ (Invalid)} \end{aligned}$$

$$\begin{aligned} b &= b^* a (a+b)(a+b)^* \\ &= b \text{ (Invalid)} \end{aligned}$$