

Question - 1:

Given Input $\Sigma = \{a, b\}$

all words that have "a" as the 2nd letter and

"a" as the 2nd last letter over given input

Possible Combinations = $\{aa, aaa, aab, baa, bab, aaaa\}$

Regular Expression:

$$(a+b)^* a (a+b)^* (ab+aa)$$

* Using this regular expression we can form the given string examples

* With this regular expression, string can start with any letter ~~a~~ a's and last 2nd letter is a's.

* The second letter can be followed by any number of a's so that given regular expression passes with all the combinations

Examples

$$\begin{aligned} 1. \quad aa &= (a+b)^* a (a+b)^* (ab+aa) \\ &= (a+b)^1 a \quad (\text{valid}) \end{aligned}$$

$$\begin{aligned} 2. \quad aaa &= (a+b)^* a (a+b)^* (ab+aa) \\ &= (a+b)^1 a (a+b)^1 (\text{valid}) \end{aligned}$$

$$\begin{aligned} 3. \quad baa &= (a+b)^* a (a+b)^* (ab+aa) \\ &= \bullet (\text{valid}) \end{aligned}$$