Stanford University ACM Team Notebook (2013-14)

Table of Contents

Combinatorial optimization

- 1. Sparse max-flow (C++)
- 2. Min-cost max-flow (C++)
- 3. Push-relabel max-flow (C++)
- 4. Min-cost matching (C++)
- 5. Max bipartite matching (C++)
- 6. Global min cut (C++)
- 7. Graph cut inference (C++)

Geometry

- 8. Convex hull (C++)
- 9. Miscellaneous geometry (C++)
- 10. Java geometry (Java)
- 11. 3D geometry (Java)
- 12. Slow Delaunay triangulation (C++)

Numerical algorithms

- 13. <u>Number theoretic algorithms (modular, Chinese remainder, linear Diophantine)</u> (C++)
- 14. Systems of linear equations, matrix inverse, determinant (C++)

- 15. Reduced row echelon form, matrix rank (C++)
- 16. Fast Fourier transform (C++)
- 17. Simplex algorithm (C++)

Graph algorithms

- 18. Fast Dijkstra's algorithm (C++)
- 19. Strongly connected components (C)
- 20. Eulerian Path (C++)

Data structures

- 21. Suffix arrays (C++)
- 22. Binary Indexed Tree
- 23. Union-Find Set (C/C++)
- 24. <u>KD-tree (C++)</u>
- 25. Lazy Segment Tree (Java)
- 26. Lowest Common Ancestor (C++)

Miscellaneous

- 27. Longest increasing subsequence (C++)
- 28. <u>Dates (C++)</u>
- 29. Regular expressions (Java)
- 30. Prime numbers (C++)
- 31. <u>C++ input/output</u>
- 32. Knuth-Morris-Pratt (C++)

- 33. <u>Latitude/longitude</u>
- 34. Emacs settings

Dinic.cc 1/34

```
// Adjacency list implementation of Dinic's blocking flow algorithm.
// This is very fast in practice, and only loses to push-relabel flow.
// Running time:
      O(|V|^2 |E|)
//
// INPUT:
    - graph, constructed using AddEdge()
//
      - source
//
      - sink
//
// OUTPUT:
// - maximum flow value
       - To obtain the actual flow values, look at all edges with
         capacity > 0 (zero capacity edges are residual edges).
#include <cmath>
#include <vector>
#include <iostream>
#include <queue>
using namespace std;
const int INF = 2000000000;
struct Edge {
  int from, to, cap, flow, index;
  Edge(int from, int to, int cap, int flow, int index) :
    from(from), to(to), cap(cap), flow(flow), index(index) {}
};
struct Dinic {
  int N;
 vector<vector<Edge> > G;
 vector<Edge *> dad;
  vector<int> Q;
  Dinic(int N) : N(N), G(N), dad(N), Q(N) {}
  void AddEdge(int from, int to, int cap) {
    G[from].push back(Edge(from, to, cap, 0, G[to].size()));
    if (from == to) G[from].back().index++;
    G[to].push_back(Edge(to, from, 0, 0, G[from].size() - 1));
```

```
long long BlockingFlow(int s, int t) {
    fill(dad.begin(), dad.end(), (Edge *) NULL);
    dad[s] = &G[0][0] - 1;
    int head = 0, tail = 0;
    Q[tail++] = s;
    while (head < tail) {</pre>
      int x = Q[head++];
      for (int i = 0; i < G[x].size(); i++) {</pre>
       Edge &e = G[x][i];
       if (!dad[e.to] && e.cap - e.flow > 0) {
         dad[e.to] = &G[x][i];
         Q[tail++] = e.to;
      }
    if (!dad[t]) return 0;
    long long totflow = 0;
    for (int i = 0; i < G[t].size(); i++) {</pre>
      Edge *start = \&G[G[t][i].to][G[t][i].index];
      int amt = INF;
      for (Edge *e = start; amt && e != dad[s]; e = dad[e->from]) {
       if (!e) { amt = 0; break; }
       amt = min(amt, e->cap - e->flow);
      if (amt == 0) continue;
      for (Edge *e = start; amt && e != dad[s]; e = dad[e->from]) {
       e->flow += amt;
       G[e->to][e->index].flow -= amt;
      totflow += amt;
   return totflow;
 long long GetMaxFlow(int s, int t) {
    long long totflow = 0;
    while (long long flow = BlockingFlow(s, t))
      totflow += flow;
   return totflow;
};
```

MinCostMaxFlow.cc 2/34

```
// Implementation of min cost max flow algorithm using adjacency // matrix (Edmonds and Karp 1972). This implementation keeps track of // forward and reverse edges separately (so you can set cap[i][j] != // cap[j][i]). For a regular max flow, set all edge costs to 0. // Running time, O(|V|^2) cost per augmentation
```

```
//
                   O(|V|^3) augmentations
     max flow:
      min cost max flow: O(|V|^4 * MAX EDGE COST) augmentations
// INPUT:
    - graph, constructed using AddEdge()
//
      - source
//
      - sink
//
// OUTPUT:
    - (maximum flow value, minimum cost value)
       - To obtain the actual flow, look at positive values only.
#include <cmath>
#include <vector>
#include <iostream>
using namespace std;
typedef vector<int> VI;
typedef vector<VI> VVI;
typedef long long L;
typedef vector<L> VL;
typedef vector<VL> VVL;
typedef pair<int, int> PII;
typedef vector<PII> VPII;
const L INF = numeric limits<L>::max() / 4;
struct MinCostMaxFlow {
  int N;
  VVL cap, flow, cost;
 VI found;
 VL dist, pi, width;
  VPII dad;
 MinCostMaxFlow(int N) :
    N(N), cap(N, VL(N)), flow(N, VL(N)), cost(N, VL(N)),
    found(N), dist(N), pi(N), width(N), dad(N) {}
  void AddEdge(int from, int to, L cap, L cost) {
    this->cap[from][to] = cap;
    this->cost[from][to] = cost;
  }
  void Relax(int s, int k, L cap, L cost, int dir) {
    L val = dist[s] + pi[s] - pi[k] + cost;
    if (cap && val < dist[k]) {</pre>
     dist[k] = val;
     dad[k] = make pair(s, dir);
     width[k] = min(cap, width[s]);
  }
  L Dijkstra(int s, int t) {
    fill(found.begin(), found.end(), false);
    fill(dist.begin(), dist.end(), INF);
```

```
fill(width.begin(), width.end(), 0);
    dist[s] = 0;
    width[s] = INF;
    while (s != -1) {
      int best = -1;
      found[s] = true;
      for (int k = 0; k < N; k++) {</pre>
        if (found[k]) continue;
        Relax(s, k, cap[s][k] - flow[s][k], cost[s][k], 1);
        Relax(s, k, flow[k][s], -cost[k][s], -1);
        if (best == -1 || dist[k] < dist[best]) best = k;</pre>
      }
      s = best;
    for (int k = 0; k < N; k++)
      pi[k] = min(pi[k] + dist[k], INF);
    return width[t];
  }
  pair<L, L> GetMaxFlow(int s, int t) {
    L totflow = 0, totcost = 0;
    while (L amt = Dijkstra(s, t)) {
      totflow += amt;
      for (int x = t; x != s; x = dad[x].first) {
        if (dad[x].second == 1) {
          flow[dad[x].first][x] += amt;
          totcost += amt * cost[dad[x].first][x];
        } else {
          flow[x][dad[x].first] -= amt;
          totcost -= amt * cost[x][dad[x].first];
      }
    return make pair(totflow, totcost);
  }
} ;
```

PushRelabel.cc 3/34

```
// Adjacency list implementation of FIFO push relabel maximum flow // with the gap relabeling heuristic. This implementation is // significantly faster than straight Ford-Fulkerson. It solves // random problems with 10000 vertices and 1000000 edges in a few // seconds, though it is possible to construct test cases that // achieve the worst-case. // Running time: // O(|V|^3) // INPUT:
```

```
//
      - graph, constructed using AddEdge()
//
       - source
//
       - sink
// OUTPUT:
    - maximum flow value
//
       - To obtain the actual flow values, look at all edges with
        capacity > 0 (zero capacity edges are residual edges).
#include <cmath>
#include <vector>
#include <iostream>
#include <queue>
using namespace std;
typedef long long LL;
struct Edge {
  int from, to, cap, flow, index;
  Edge(int from, int to, int cap, int flow, int index) :
    from(from), to(to), cap(cap), flow(flow), index(index) {}
struct PushRelabel {
 int N;
 vector<vector<Edge> > G;
 vector<LL> excess;
 vector<int> dist, active, count;
 queue<int> Q;
  PushRelabel(int N): N(N), G(N), excess(N), dist(N), active(N), count(2*N)
{ }
  void AddEdge(int from, int to, int cap) {
    G[from].push back(Edge(from, to, cap, 0, G[to].size()));
   if (from == to) G[from].back().index++;
   G[to].push back(Edge(to, from, 0, 0, G[from].size() - 1));
  }
  void Enqueue(int v) {
   if (!active[v] && excess[v] > 0) { active[v] = true; Q.push(v); }
  void Push(Edge &e) {
    int amt = int(min(excess[e.from], LL(e.cap - e.flow)));
   if (dist[e.from] <= dist[e.to] || amt == 0) return;</pre>
    e.flow += amt;
    G[e.to][e.index].flow -= amt;
    excess[e.to] += amt;
    excess[e.from] -= amt;
   Enqueue(e.to);
  void Gap(int k) {
    for (int v = 0; v < N; v++) {</pre>
```

```
if (dist[v] < k) continue;</pre>
      count[dist[v]]--;
      dist[v] = max(dist[v], N+1);
      count[dist[v]]++;
      Enqueue (v);
    }
  }
  void Relabel(int v) {
    count[dist[v]]--;
    dist[v] = 2*N;
    for (int i = 0; i < G[v].size(); i++)</pre>
      if (G[v][i].cap - G[v][i].flow > 0)
        dist[v] = min(dist[v], dist[G[v][i].to] + 1);
    count[dist[v]]++;
    Enqueue (v);
  }
  void Discharge(int v) {
    for (int i = 0; excess[v] > 0 && i < G[v].size(); i++) Push(G[v][i]);</pre>
    if (excess[v] > 0) {
      if (count[dist[v]] == 1)
        Gap(dist[v]);
      else
       Relabel(v);
    }
  }
  LL GetMaxFlow(int s, int t) {
    count[0] = N-1;
    count[N] = 1;
    dist[s] = N;
    active[s] = active[t] = true;
    for (int i = 0; i < G[s].size(); i++) {</pre>
      excess[s] += G[s][i].cap;
      Push(G[s][i]);
    while (!Q.empty()) {
      int v = Q.front();
      Q.pop();
      active[v] = false;
      Discharge(v);
    LL totflow = 0;
    for (int i = 0; i < G[s].size(); i++) totflow += G[s][i].flow;</pre>
    return totflow;
  }
} ;
```

MinCostMatching.cc 4/34

```
// Min cost bipartite matching via shortest augmenting paths
// This is an O(n^3) implementation of a shortest augmenting path
// algorithm for finding min cost perfect matchings in dense
// graphs. In practice, it solves 1000x1000 problems in around 1
// second.
//
//
    cost[i][j] = cost for pairing left node i with right node j
    Lmate[i] = index of right node that left node i pairs with
    Rmate[j] = index of left node that right node j pairs with
// The values in cost[i][j] may be positive or negative. To perform
// maximization, simply negate the cost[][] matrix.
#include <algorithm>
#include <cstdio>
#include <cmath>
#include <vector>
using namespace std;
typedef vector<double> VD;
typedef vector<VD> VVD;
typedef vector<int> VI;
double MinCostMatching(const VVD &cost, VI &Lmate, VI &Rmate) {
 int n = int(cost.size());
 // construct dual feasible solution
 VD u(n);
 VD v(n);
 for (int i = 0; i < n; i++) {</pre>
   u[i] = cost[i][0];
   for (int j = 1; j < n; j++) u[i] = min(u[i], cost[i][j]);</pre>
 for (int j = 0; j < n; j++) {
   v[j] = cost[0][j] - u[0];
   for (int i = 1; i < n; i++) v[j] = min(v[j], cost[i][j] - u[i]);</pre>
 }
 // construct primal solution satisfying complementary slackness
 Lmate = VI(n, -1);
 Rmate = VI(n, -1);
 int mated = 0;
 for (int i = 0; i < n; i++) {</pre>
   for (int j = 0; j < n; j++) {</pre>
     if (Rmate[j] != -1) continue;
     if (fabs(cost[i][j] - u[i] - v[j]) < 1e-10) {
      Lmate[i] = j;
      Rmate[j] = i;
      mated++;
      break;
     }
   }
```

```
}
VD dist(n);
VI dad(n);
VI seen(n);
// repeat until primal solution is feasible
while (mated < n) {</pre>
  // find an unmatched left node
  int s = 0;
  while (Lmate[s] != -1) s++;
  // initialize Dijkstra
  fill(dad.begin(), dad.end(), -1);
  fill(seen.begin(), seen.end(), 0);
  for (int k = 0; k < n; k++)
    dist[k] = cost[s][k] - u[s] - v[k];
  int j = 0;
  while (true) {
    // find closest
    \dot{j} = -1;
    for (int k = 0; k < n; k++) {</pre>
     if (seen[k]) continue;
     if (j == -1 \mid \mid dist[k] < dist[j]) j = k;
    seen[j] = 1;
    // termination condition
    if (Rmate[j] == -1) break;
    // relax neighbors
    const int i = Rmate[j];
    for (int k = 0; k < n; k++) {
     if (seen[k]) continue;
     const double new dist = dist[j] + cost[i][k] - u[i] - v[k];
     if (dist[k] > new dist) {
        dist[k] = new dist;
        dad[k] = j;
     }
    }
  }
  // update dual variables
  for (int k = 0; k < n; k++) {
    if (k == j || !seen[k]) continue;
    const int i = Rmate[k];
    v[k] += dist[k] - dist[j];
    u[i] = dist[k] - dist[j];
  u[s] += dist[j];
  // augment along path
```

```
while (dad[j] >= 0) {
    const int d = dad[j];
    Rmate[j] = Rmate[d];
    Lmate[Rmate[j]] = j;
    j = d;
}
Rmate[j] = s;
Lmate[s] = j;

mated++;
}

double value = 0;
for (int i = 0; i < n; i++)
    value += cost[i][Lmate[i]];

return value;
}</pre>
```

MaxBipartiteMatching.cc 5/34

```
// This code performs maximum bipartite matching.
// Running time: O(|E|\ |V|) -- often much faster in practice
     INPUT: w[i][j] = edge between row node i and column node j
     OUTPUT: mr[i] = assignment for row node i, -1 if unassigned
             mc[j] = assignment for column node j, -1 if unassigned
             function returns number of matches made
#include <vector>
using namespace std;
typedef vector<int> VI;
typedef vector<VI> VVI;
bool FindMatch(int i, const VVI &w, VI &mr, VI &mc, VI &seen) {
  for (int j = 0; j < w[i].size(); j++) {</pre>
    if (w[i][j] && !seen[j]) {
      seen[j] = true;
      if (mc[j] < 0 \mid | FindMatch(mc[j], w, mr, mc, seen)) {
        mr[i] = j;
        mc[j] = i;
        return true;
  return false;
int BipartiteMatching(const VVI &w, VI &mr, VI &mc) {
 mr = VI(w.size(), -1);
```

```
mc = VI(w[0].size(), -1);
int ct = 0;
for (int i = 0; i < w.size(); i++) {
   VI seen(w[0].size());
   if (FindMatch(i, w, mr, mc, seen)) ct++;
}
return ct;
}</pre>
```

MinCut.cc 6/34

```
// Adjacency matrix implementation of Stoer-Wagner min cut algorithm.
// Running time:
// O(|V|^3)
// INPUT:
    - graph, constructed using AddEdge()
// OUTPUT:
     - (min cut value, nodes in half of min cut)
#include <cmath>
#include <vector>
#include <iostream>
using namespace std;
typedef vector<int> VI;
typedef vector<VI> VVI;
const int INF = 1000000000;
pair<int, VI> GetMinCut(VVI &weights) {
  int N = weights.size();
  VI used(N), cut, best cut;
  int best weight = -1;
  for (int phase = N-1; phase >= 0; phase--) {
    VI w = weights[0];
    VI added = used;
    int prev, last = 0;
    for (int i = 0; i < phase; i++) {</pre>
      prev = last;
      last = -1;
      for (int j = 1; j < N; j++)</pre>
       if (!added[j] && (last == -1 || w[j] > w[last])) last = j;
      if (i == phase-1) {
       for (int j = 0; j < N; j++) weights[prev][j] += weights[last][j];</pre>
       for (int j = 0; j < N; j++) weights[j][prev] = weights[prev][j];</pre>
       used[last] = true;
        cut.push back(last);
```

```
if (best_weight == -1 || w[last] < best_weight) {
    best_cut = cut;
    best_weight = w[last];
}

} else {
    for (int j = 0; j < N; j++)
        w[j] += weights[last][j];
    added[last] = true;
}

return make_pair(best_weight, best_cut);
}</pre>
```

GraphCutInference.cc 7/34

```
// Special-purpose {0,1} combinatorial optimization solver for
// problems of the following by a reduction to graph cuts:
                         sum i psi i(x[i])
         minimize
// x[1]...x[n] in {0,1} + sum_{i < j} phi_{ij}(x[i], x[j])
//
// where
// psi i : {0, 1} --> R
   phi_{ij} : {0, 1} x {0, 1} --> R
// such that
// phi {ij}(0,0) + phi {ij}(1,1) <= phi {ij}(0,1) + phi {ij}(1,0) (*)
// This can also be used to solve maximization problems where the
// direction of the inequality in (*) is reversed.
// INPUT: phi -- a matrix such that phi[i][j][u][v] = phi_{ij}(u, v)
        psi -- a matrix such that psi[i][u] = psi i(u)
//
         x -- a vector where the optimal solution will be stored
// OUTPUT: value of the optimal solution
// To use this code, create a GraphCutInference object, and call the
// DoInference() method. To perform maximization instead of minimization,
// ensure that #define MAXIMIZATION is enabled.
#include <vector>
#include <iostream>
using namespace std;
typedef vector<int> VI;
typedef vector<VI> VVI;
typedef vector<VVI> VVVI;
typedef vector<VVVI> VVVVI;
const int INF = 1000000000;
```

```
// comment out following line for minimization
#define MAXIMIZATION
struct GraphCutInference {
 int N;
 VVI cap, flow;
 VI reached;
  int Augment(int s, int t, int a) {
    reached[s] = 1;
    if (s == t) return a;
    for (int k = 0; k < N; k++) {
      if (reached[k]) continue;
      if (int aa = min(a, cap[s][k] - flow[s][k])) {
       if (int b = Augment(k, t, aa)) {
         flow[s][k] += b;
         flow[k][s] -= b;
         return b;
       }
      }
    return 0;
  }
  int GetMaxFlow(int s, int t) {
   N = cap.size();
    flow = VVI(N, VI(N));
    reached = VI(N);
    int totflow = 0;
    while (int amt = Augment(s, t, INF)) {
      totflow += amt;
      fill(reached.begin(), reached.end(), 0);
   return totflow;
  }
  int DoInference(const VVVVI &phi, const VVI &psi, VI &x) {
    int M = phi.size();
    cap = VVI(M+2, VI(M+2));
   VI b(M);
    int c = 0;
    for (int i = 0; i < M; i++) {</pre>
     b[i] += psi[i][1] - psi[i][0];
      c += psi[i][0];
      for (int j = 0; j < i; j++)</pre>
       b[i] += phi[i][j][1][1] - phi[i][j][0][1];
      for (int j = i+1; j < M; j++) {</pre>
       cap[i][j] = phi[i][j][0][1] + phi[i][j][1][0] - phi[i][j][0][0] -
phi[i][j][1][1];
       b[i] += phi[i][j][1][0] - phi[i][j][0][0];
       c += phi[i][j][0][0];
      }
    }
```

```
#ifdef MAXIMIZATION
    for (int i = 0; i < M; i++) {</pre>
      for (int j = i+1; j < M; j++)</pre>
       cap[i][j] *= -1;
      b[i] *= -1;
    c *= -1;
#endif
    for (int i = 0; i < M; i++) {</pre>
      if (b[i] >= 0) {
       cap[M][i] = b[i];
      } else {
       cap[i][M+1] = -b[i];
       c += b[i];
      }
    }
    int score = GetMaxFlow(M, M+1);
    fill(reached.begin(), reached.end(), 0);
    Augment (M, M+1, INF);
    x = VI(M);
    for (int i = 0; i < M; i++) x[i] = reached[i] ? 0 : 1;</pre>
    score += c;
#ifdef MAXIMIZATION
    score *=-1;
#endif
   return score;
 }
};
int main() {
  // solver for "Cat vs. Dog" from NWERC 2008
  int numcases;
  cin >> numcases;
  for (int caseno = 0; caseno < numcases; caseno++) {</pre>
    int c, d, v;
    cin >> c >> d >> v;
    VVVVI phi(c+d, VVVI(c+d, VVI(2, VI(2))));
    VVI psi(c+d, VI(2));
    for (int i = 0; i < v; i++) {</pre>
      char p, q;
      int u, v;
      cin >> p >> u >> q >> v;
      u--; v--;
      if (p == 'C') {
      phi[u][c+v][0][0]++;
       phi[c+v][u][0][0]++;
      } else {
       phi[v][c+u][1][1]++;
```

```
phi[c+u][v][1][1]++;
}

GraphCutInference graph;
VI x;
cout << graph.DoInference(phi, psi, x) << endl;
}

return 0;
}</pre>
```

ConvexHull.cc 8/34

```
// Compute the 2D convex hull of a set of points using the monotone chain
// algorithm. Eliminate redundant points from the hull if REMOVE REDUNDANT
is
// #defined.
// Running time: O(n log n)
     INPUT: a vector of input points, unordered.
   OUTPUT: a vector of points in the convex hull, counterclockwise,
starting
//
              with bottommost/leftmost point
#include <cstdio>
#include <cassert>
#include <vector>
#include <algorithm>
#include <cmath>
using namespace std;
#define REMOVE REDUNDANT
typedef double T;
const T EPS = 1e-7;
struct PT {
  T x, y;
  PT() {}
  PT(T x, T y) : x(x), y(y) {}
 bool operator<(const PT &rhs) const { return make pair(y,x) <</pre>
make pair(rhs.y,rhs.x); }
 bool operator == (const PT &rhs) const { return make pair (y,x) ==
make pair(rhs.y,rhs.x); }
};
T cross(PT p, PT q) { return p.x*q.y-p.y*q.x; }
T area2(PT a, PT b, PT c) { return cross(a,b) + cross(b,c) + cross(c,a); }
#ifdef REMOVE REDUNDANT
bool between(const PT &a, const PT &b, const PT &c) {
```

```
return (fabs(area2(a,b,c)) < EPS && (a.x-b.x)*(c.x-b.x) \leq 0 && (a.y-
b.y)*(c.y-b.y) <= 0);
#endif
void ConvexHull (vector<PT> &pts) {
  sort(pts.begin(), pts.end());
 pts.erase(unique(pts.begin(), pts.end()), pts.end());
  vector<PT> up, dn;
  for (int i = 0; i < pts.size(); i++) {</pre>
    while (up.size() > 1 \&\& area2(up[up.size()-2], up.back(), pts[i]) >= 0)
up.pop back();
    while (dn.size() > 1 && area2(dn[dn.size()-2], dn.back(), pts[i]) <= 0)</pre>
dn.pop back();
    up.push back(pts[i]);
    dn.push back(pts[i]);
  pts = dn;
  for (int i = (int) up.size() - 2; i \ge 1; i--) pts.push back(up[i]);
#ifdef REMOVE REDUNDANT
  if (pts.size() <= 2) return;</pre>
  dn.clear();
  dn.push back(pts[0]);
  dn.push back(pts[1]);
  for (int i = 2; i < pts.size(); i++) {</pre>
    if (between(dn[dn.size()-2], dn[dn.size()-1], pts[i])) dn.pop back();
    dn.push back(pts[i]);
  if (dn.size() >= 3 \&\& between(dn.back(), dn[0], dn[1])) {
    dn[0] = dn.back();
    dn.pop back();
  pts = dn;
#endif
```

Geometry.cc 9/34

```
// C++ routines for computational geometry.
#include <iostream>
#include <vector>
#include <cmath>
#include <cassert>
using namespace std;
double INF = 1e100;
double EPS = 1e-12;
struct PT {
```

```
double x, y;
  PT() {}
  PT(double x, double y) : x(x), y(y) {}
  PT(const PT &p) : x(p.x), y(p.y) {}
  PT operator + (const PT &p) const { return PT(x+p.x, y+p.y); }
  PT operator - (const PT &p) const { return PT(x-p.x, y-p.y); }
 PT operator * (double c) const { return PT(x*c, y*c ); }
PT operator / (double c) const { return PT(x/c, y/c ); }
double dot(PT p, PT q) { return p.x*q.x+p.y*q.y; }
double dist2(PT p, PT q) { return dot(p-q,p-q); }
double cross(PT p, PT q) { return p.x*q.y-p.y*q.x; }
ostream & operator << (ostream & os, const PT &p) {
  os << "(" << p.x << "," << p.y << ")";
// rotate a point CCW or CW around the origin
PT RotateCCW90(PT p) { return PT(-p.y,p.x); }
PT RotateCW90 (PT p)
                       { return PT(p.y,-p.x); }
PT RotateCCW(PT p, double t) {
 return PT(p.x*cos(t)-p.y*sin(t), p.x*sin(t)+p.y*cos(t));
// project point c onto line through a and b
// assuming a != b
PT ProjectPointLine(PT a, PT b, PT c) {
 return a + (b-a) *dot(c-a, b-a) /dot(b-a, b-a);
// project point c onto line segment through a and b
PT ProjectPointSegment(PT a, PT b, PT c) {
 double r = dot(b-a, b-a);
 if (fabs(r) < EPS) return a;</pre>
  r = dot(c-a, b-a)/r;
 if (r < 0) return a;</pre>
 if (r > 1) return b;
 return a + (b-a) *r;
}
// compute distance from c to segment between a and b
double DistancePointSegment(PT a, PT b, PT c) {
  return sqrt(dist2(c, ProjectPointSegment(a, b, c)));
// compute distance between point (x,y,z) and plane ax+by+cz=d
double DistancePointPlane (double x, double y, double z,
                           double a, double b, double c, double d)
 return fabs(a*x+b*y+c*z-d)/sqrt(a*a+b*b+c*c);
// determine if lines from a to b and c to d are parallel or collinear
bool LinesParallel(PT a, PT b, PT c, PT d) {
  return fabs(cross(b-a, c-d)) < EPS;</pre>
```

```
bool LinesCollinear(PT a, PT b, PT c, PT d) {
  return LinesParallel(a, b, c, d)
      && fabs(cross(a-b, a-c)) < EPS
      && fabs(cross(c-d, c-a)) < EPS;
}
// determine if line segment from a to b intersects with
// line segment from c to d
bool SegmentsIntersect(PT a, PT b, PT c, PT d) {
  if (LinesCollinear(a, b, c, d)) {
    if (dist2(a, c) < EPS || dist2(a, d) < EPS ||</pre>
      dist2(b, c) < EPS || dist2(b, d) < EPS) return true;
    if (dot(c-a, c-b) > 0 \&\& dot(d-a, d-b) > 0 \&\& dot(c-b, d-b) > 0)
      return false;
    return true;
  if (cross(d-a, b-a) * cross(c-a, b-a) > 0) return false;
  if (cross(a-c, d-c) * cross(b-c, d-c) > 0) return false;
  return true;
\ensuremath{//} compute intersection of line passing through a and b
// with line passing through c and d, assuming that unique
// intersection exists; for segment intersection, check if
// segments intersect first
PT ComputeLineIntersection (PT a, PT b, PT c, PT d) {
 b=b-a; d=c-d; c=c-a;
  assert(dot(b, b) > EPS && dot(d, d) > EPS);
  return a + b*cross(c, d)/cross(b, d);
// compute center of circle given three points
PT ComputeCircleCenter(PT a, PT b, PT c) {
 b = (a+b)/2;
  c = (a+c)/2;
  return ComputeLineIntersection(b, b+RotateCW90(a-b), c, c+RotateCW90(a-c));
// determine if point is in a possibly non-convex polygon (by William
// Randolph Franklin); returns 1 for strictly interior points, 0 for
// strictly exterior points, and 0 or 1 for the remaining points.
// Note that it is possible to convert this into an *exact* test using
// integer arithmetic by taking care of the division appropriately
// (making sure to deal with signs properly) and then by writing exact
// tests for checking point on polygon boundary
bool PointInPolygon(const vector<PT> &p, PT q) {
 bool c = 0;
  for (int i = 0; i < p.size(); i++) {</pre>
    int j = (i+1)%p.size();
    if ((p[i].y <= q.y && q.y < p[j].y ||</pre>
      p[j].y \le q.y \&\& q.y < p[i].y) \&\&
      q.x < p[i].x + (p[j].x - p[i].x) * (q.y - p[i].y) / (p[j].y - p[i].y))
  }
  return c;
```

```
// determine if point is on the boundary of a polygon
bool PointOnPolygon(const vector<PT> &p, PT q) {
  for (int i = 0; i < p.size(); i++)</pre>
    if (dist2(ProjectPointSegment(p[i], p[(i+1)%p.size()], q), q) < EPS)
      return true;
    return false;
}
// compute intersection of line through points a and b with
// circle centered at c with radius r > 0
vector<PT> CircleLineIntersection(PT a, PT b, PT c, double r) {
 vector<PT> ret;
 b = b-a;
  a = a-c;
  double A = dot(b, b);
  double B = dot(a, b);
  double C = dot(a, a) - r*r;
  double D = B*B - A*C;
  if (D < -EPS) return ret;</pre>
  ret.push back(c+a+b*(-B+sqrt(D+EPS))/A);
  if (D > EPS)
    ret.push back(c+a+b*(-B-sqrt(D))/A);
  return ret;
}
// compute intersection of circle centered at a with radius r
// with circle centered at b with radius R
vector<PT> CircleCircleIntersection(PT a, PT b, double r, double R) {
  vector<PT> ret;
  double d = sqrt(dist2(a, b));
  if (d > r+R \mid \mid d+min(r, R) < max(r, R)) return ret;
  double x = (d*d-R*R+r*r)/(2*d);
  double y = sqrt(r*r-x*x);
  PT v = (b-a)/d;
  ret.push back(a+v*x + RotateCCW90(v)*y);
  if (y > 0)
    ret.push back(a+v*x - RotateCCW90(v)*y);
  return ret;
}
// This code computes the area or centroid of a (possibly nonconvex)
// polygon, assuming that the coordinates are listed in a clockwise or
// counterclockwise fashion. Note that the centroid is often known as
// the "center of gravity" or "center of mass".
double ComputeSignedArea(const vector<PT> &p) {
  double area = 0;
  for(int i = 0; i < p.size(); i++) {</pre>
    int j = (i+1) % p.size();
    area += p[i].x*p[j].y - p[j].x*p[i].y;
  return area / 2.0;
}
double ComputeArea(const vector<PT> &p) {
  return fabs(ComputeSignedArea(p));
```

```
PT ComputeCentroid(const vector<PT> &p) {
  PT c(0,0);
  double scale = 6.0 * ComputeSignedArea(p);
  for (int i = 0; i < p.size(); i++) {</pre>
    int j = (i+1) % p.size();
    c = c + (p[i]+p[j])*(p[i].x*p[j].y - p[j].x*p[i].y);
 return c / scale;
// tests whether or not a given polygon (in CW or CCW order) is simple
bool IsSimple(const vector<PT> &p) {
  for (int i = 0; i < p.size(); i++) {</pre>
    for (int k = i+1; k < p.size(); k++) {</pre>
      int j = (i+1) % p.size();
      int 1 = (k+1) % p.size();
      if (i == 1 || j == k) continue;
      if (SegmentsIntersect(p[i], p[j], p[k], p[l]))
        return false;
  }
  return true;
int main() {
  // expected: (-5,2)
  cerr << RotateCCW90(PT(2,5)) << endl;</pre>
  // expected: (5,-2)
  cerr << RotateCW90(PT(2,5)) << endl;
  // expected: (-5,2)
  cerr << RotateCCW(PT(2,5),M PI/2) << endl;</pre>
  // expected: (5,2)
  cerr << ProjectPointLine(PT(-5,-2), PT(10,4), PT(3,7)) << endl;
  // expected: (5,2) (7.5,3) (2.5,1)
  cerr << ProjectPointSegment(PT(-5,-2), PT(10,4), PT(3,7)) << ""
       << ProjectPointSegment(PT(7.5,3), PT(10,4), PT(3,7)) << " "
       << ProjectPointSegment(PT(-5,-2), PT(2.5,1), PT(3,7)) << endl;
  // expected: 6.78903
  cerr << DistancePointPlane(4,-4,3,2,-2,5,-8) << endl;</pre>
  // expected: 1 0 1
  cerr << LinesParallel(PT(1,1), PT(3,5), PT(2,1), PT(4,5)) << " "
       << LinesParallel(PT(1,1), PT(3,5), PT(2,0), PT(4,5)) << " "
       << LinesParallel(PT(1,1), PT(3,5), PT(5,9), PT(7,13)) << endl;
  // expected: 0 0 1
  cerr << LinesCollinear(PT(1,1), PT(3,5), PT(2,1), PT(4,5)) << " "
       << LinesCollinear(PT(1,1), PT(3,5), PT(2,0), PT(4,5)) << " "
       << LinesCollinear(PT(1,1), PT(3,5), PT(5,9), PT(7,13)) << endl;
```

```
// expected: 1 1 1 0
  cerr << SegmentsIntersect(PT(0,0), PT(2,4), PT(3,1), PT(-1,3)) << ""
       << SegmentsIntersect(PT(0,0), PT(2,4), PT(4,3), PT(0,5)) << ""
       << SegmentsIntersect(PT(0,0), PT(2,4), PT(2,-1), PT(-2,1)) << " "
       << SegmentsIntersect(PT(0,0), PT(2,4), PT(5,5), PT(1,7)) << endl;
  // expected: (1,2)
  cerr << ComputeLineIntersection(PT(0,0), PT(2,4), PT(3,1), PT(-1,3)) <<
endl;
  // expected: (1,1)
  cerr << ComputeCircleCenter(PT(-3,4), PT(6,1), PT(4,5)) << endl;</pre>
  vector<PT> v;
  v.push back(PT(0,0));
  v.push back(PT(5,0));
  v.push back(PT(5,5));
  v.push back(PT(0,5));
  // expected: 1 1 1 0 0
  cerr << PointInPolygon(v, PT(2,2)) << " "</pre>
       << PointInPolygon(v, PT(2,0)) << " "
       << PointInPolygon(v, PT(0,2)) << " "
       << PointInPolygon(v, PT(5,2)) << " "
       << PointInPolygon(v, PT(2,5)) << endl;</pre>
  // expected: 0 1 1 1 1
  cerr << PointOnPolygon(v, PT(2,2)) << " "</pre>
       << PointOnPolygon(v, PT(2,0)) << " "
       << PointOnPolygon(v, PT(0,2)) << " "
       << PointOnPolygon(v, PT(5,2)) << " "
       << PointOnPolygon(v, PT(2,5)) << endl;
  // expected: (1,6)
  //
               (5,4) (4,5)
  //
               blank line
  //
               (4,5) (5,4)
  //
               blank line
               (4,5) (5,4)
  vector<PT> u = CircleLineIntersection(PT(0,6), PT(2,6), PT(1,1), 5);
  for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;</pre>
  u = CircleLineIntersection(PT(0,9), PT(9,0), PT(1,1), 5);
  for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;</pre>
  u = CircleCircleIntersection(PT(1,1), PT(10,10), 5, 5);
  for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;</pre>
  u = CircleCircleIntersection(PT(1,1), PT(8,8), 5, 5);
  for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;</pre>
  u = CircleCircleIntersection(PT(1,1), PT(4.5,4.5), 10, sqrt(2.0)/2.0);
  for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;</pre>
  u = CircleCircleIntersection(PT(1,1), PT(4.5,4.5), 5, sqrt(2.0)/2.0);
  for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;</pre>
  // area should be 5.0
  // centroid should be (1.1666666, 1.166666)
```

```
PT pa[] = { PT(0,0), PT(5,0), PT(1,1), PT(0,5) };
vector<PT> p(pa, pa+4);
PT c = ComputeCentroid(p);
cerr << "Area: " << ComputeArea(p) << endl;
cerr << "Centroid: " << c << endl;
return 0;
}</pre>
```

JavaGeometry.java 10/34

```
// In this example, we read an input file containing three lines, each
// containing an even number of doubles, separated by commas. The first two
// lines represent the coordinates of two polygons, given in counterclockwise
// (or clockwise) order, which we will call "A" and "B". The last line
// contains a list of points, p[1], p[2], ...
// Our goal is to determine:
// (1) whether B - A is a single closed shape (as opposed to multiple
shapes)
// (2) the area of B - A
    (3) whether each p[i] is in the interior of B - A
//
// INPUT:
// 0 0 10 0 0 10
    0 0 10 10 10 0
//
//
    5 1
// OUTPUT:
// The area is singular.
// The area is 25.0
   Point belongs to the area.
   Point does not belong to the area.
import java.util.*;
import java.awt.geom.*;
import java.io.*;
public class JavaGeometry {
    // make an array of doubles from a string
    static double[] readPoints(String s) {
        String[] arr = s.trim().split("\\s++");
        double[] ret = new double[arr.length];
        for (int i = 0; i < arr.length; i++) ret[i] =</pre>
Double.parseDouble(arr[i]);
        return ret;
    }
    // make an Area object from the coordinates of a polygon
    static Area makeArea(double[] pts) {
        Path2D.Double p = new Path2D.Double();
```

```
p.moveTo(pts[0], pts[1]);
        for (int i = 2; i < pts.length; i += 2) p.lineTo(pts[i], pts[i+1]);</pre>
        p.closePath();
        return new Area(p);
    }
    // compute area of polygon
    static double computePolygonArea(ArrayList<Point2D.Double> points) {
        Point2D.Double[] pts = points.toArray(new
Point2D.Double[points.size()]);
        double area = 0;
        for (int i = 0; i < pts.length; i++) {</pre>
            int j = (i+1) % pts.length;
            area += pts[i].x * pts[j].y - pts[j].x * pts[i].y;
        return Math.abs(area)/2;
    }
    // compute the area of an Area object containing several disjoint
polygons
    static double computeArea(Area area) {
        double totArea = 0;
        PathIterator iter = area.getPathIterator(null);
        ArrayList<Point2D.Double> points = new ArrayList<Point2D.Double>();
        while (!iter.isDone()) {
            double[] buffer = new double[6];
            switch (iter.currentSegment(buffer)) {
            case PathIterator.SEG MOVETO:
            case PathIterator.SEG LINETO:
                points.add(new Point2D.Double(buffer[0], buffer[1]));
                break;
            case PathIterator.SEG CLOSE:
                totArea += computePolygonArea(points);
                points.clear();
                break;
            iter.next();
        return totArea;
    }
    // notice that the main() throws an Exception -- necessary to
    // avoid wrapping the Scanner object for file reading in a
    // try { ... } catch block.
   public static void main(String args[]) throws Exception {
        Scanner scanner = new Scanner(new File("input.txt"));
        // also,
           Scanner scanner = new Scanner (System.in);
        double[] pointsA = readPoints(scanner.nextLine());
        double[] pointsB = readPoints(scanner.nextLine());
        Area areaA = makeArea(pointsA);
        Area areaB = makeArea(pointsB);
        areaB.subtract(areaA);
        // also,
```

```
// areaB.exclusiveOr (areaA);
           areaB.add (areaA);
            areaB.intersect (areaA);
        // (1) determine whether B - A is a single closed shape (as
        // opposed to multiple shapes)
        boolean isSingle = areaB.isSingular();
        // also,
        // areaB.isEmpty();
        if (isSingle)
            System.out.println("The area is singular.");
        else
            System.out.println("The area is not singular.");
        // (2) compute the area of B - A
        System.out.println("The area is " + computeArea(areaB) + ".");
        // (3) determine whether each p[i] is in the interior of B - A
        while (scanner.hasNextDouble()) {
            double x = scanner.nextDouble();
            assert(scanner.hasNextDouble());
            double y = scanner.nextDouble();
            if (areaB.contains(x,y)) {
                System.out.println ("Point belongs to the area.");
            } else {
                System.out.println ("Point does not belong to the area.");
            }
        }
        // Finally, some useful things we didn't use in this example:
        //
             Ellipse2D.Double ellipse = new Ellipse2D.Double (double x,
double v,
                                                               double w.
double h);
        //
               creates an ellipse inscribed in box with bottom-left corner
(x,y)
               and upper-right corner (x+y,w+h)
             Rectangle 2D. Double rect = new Rectangle 2D. Double (double x,
double y,
                                                                double w,
double h);
        //
        //
               creates a box with bottom-left corner (x,y) and upper-right
               corner (x+y, w+h)
       // Each of these can be embedded in an Area object (e.g., new Area
(rect)).
   }
}
```

Geom3D.java 11/34

```
public class Geom3D {
  // distance from point (x, y, z) to plane aX + bY + cZ + d = 0
  public static double ptPlaneDist(double x, double y, double z,
      double a, double b, double c, double d) {
   return Math.abs(a*x + b*y + c*z + d) / Math.sqrt(a*a + b*b + c*c);
  }
  // distance between parallel planes aX + bY + cZ + d1 = 0 and
  // aX + bY + cZ + d2 = 0
  public static double planePlaneDist(double a, double b, double c,
      double d1, double d2) {
   return Math.abs(d1 - d2) / Math.sqrt(a*a + b*b + c*c);
  }
  // distance from point (px, py, pz) to line (x1, y1, z1) - (x2, y2, z2)
  // (or ray, or segment; in the case of the ray, the endpoint is the
  // first point)
  public static final int LINE = 0;
  public static final int SEGMENT = 1;
  public static final int RAY = 2;
  public static double ptLineDistSq(double x1, double y1, double z1,
      double x2, double y2, double z2, double px, double py, double pz,
    double pd2 = (x1-x2)*(x1-x2) + (y1-y2)*(y1-y2) + (z1-z2)*(z1-z2);
   double x, y, z;
   if (pd2 == 0) {
     x = x1;
     y = y1;
      z = z1;
    } else {
     double u = ((px-x1)*(x2-x1) + (py-y1)*(y2-y1) + (pz-z1)*(z2-z1)) / pd2;
     x = x1 + u * (x2 - x1);
      y = y1 + u * (y2 - y1);
      z = z1 + u * (z2 - z1);
     if (type != LINE && u < 0) {</pre>
       x = x1;
       y = y1;
       z = z1;
      if (type == SEGMENT && u > 1.0) {
       x = x2;
       y = y2;
        z = z2;
      }
    }
   return (x-px)*(x-px) + (y-py)*(y-py) + (z-pz)*(z-pz);
  public static double ptLineDist(double x1, double y1, double z1,
      double x2, double y2, double z2, double px, double py, double pz,
```

```
int type) {
  return Math.sqrt(ptLineDistSq(x1, y1, z1, x2, y2, z2, px, py, pz, type));
  }
}
```

Delaunay.cc 12/34

```
// Slow but simple Delaunay triangulation. Does not handle
// degenerate cases (from O'Rourke, Computational Geometry in C)
//
// Running time: O(n^4)
// INPUT:
                                  x[] = x-coordinates
                                     y[] = y-coordinates
// OUTPUT:
                                triples = a vector containing m triples of indices
                                                                  corresponding to triangle vertices
#include<vector>
using namespace std;
typedef double T;
struct triple {
           int i, j, k;
           triple() {}
           triple(int i, int j, int k) : i(i), j(j), k(k) {}
};
vector<triple> delaunayTriangulation(vector<T>& x, vector<T>& y) {
                     int n = x.size();
                     vector<T> z(n);
                     vector<triple> ret;
                      for (int i = 0; i < n; i++)
                                  z[i] = x[i] * x[i] + y[i] * y[i];
                      for (int i = 0; i < n-2; i++) {</pre>
                                  for (int j = i+1; j < n; j++) {</pre>
                                            for (int k = i+1; k < n; k++) {</pre>
                                                       if (j == k) continue;
                                                       double xn = (y[j]-y[i])*(z[k]-z[i]) - (y[k]-y[i])*(z[j]-y[i])*(z[j]-y[i])*(z[j]-y[i])*(z[j]-y[i])*(z[j]-y[i])*(z[j]-y[i])*(z[j]-y[i])*(z[j]-y[i])*(z[j]-y[i])*(z[j]-y[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*(z[k]-z[i])*
z[i]);
                                                       double yn = (x[k]-x[i])*(z[j]-z[i]) - (x[j]-x[i])*(z[k]-
z[i]);
                                                       double zn = (x[j]-x[i])*(y[k]-y[i]) - (x[k]-x[i])*(y[j]-
y[i]);
                                                      bool flag = zn < 0;</pre>
                                                       for (int m = 0; flag && m < n; m++)</pre>
                                                                  flag = flag && ((x[m]-x[i])*xn +
                                                                                                              (y[m]-y[i])*yn +
                                                                                                              (z[m]-z[i])*zn <= 0);
                                                       if (flag) ret.push back(triple(i, j, k));
                                            }
```

```
    return ret;

int main()

{
    T xs[]={0, 0, 1, 0.9};
    T ys[]={0, 1, 0, 0.9};
    vector<T> x(&xs[0], &xs[4]), y(&ys[0], &ys[4]);
    vector<triple> tri = delaunayTriangulation(x, y);

    //expected: 0 1 3
    // 0 3 2

int i;
    for(i = 0; i < tri.size(); i++)
        printf("%d %d %d\n", tri[i].i, tri[i].j, tri[i].k);
    return 0;
}
</pre>
```

Euclid.cc 13/34

```
// This is a collection of useful code for solving problems that
\ensuremath{//} involve modular linear equations. Note that all of the
// algorithms described here work on nonnegative integers.
#include <iostream>
#include <vector>
#include <algorithm>
using namespace std;
typedef vector<int> VI;
typedef pair<int, int> PII;
// return a % b (positive value)
int mod(int a, int b) {
  return ((a%b)+b)%b;
// computes gcd(a,b)
int gcd(int a, int b) {
  int tmp;
  while(b) {a%=b; tmp=a; a=b; b=tmp;}
  return a;
// computes lcm(a,b)
int lcm(int a, int b) {
 return a/gcd(a,b)*b;
```

```
// returns d = gcd(a,b); finds x,y such that d = ax + by
int extended euclid(int a, int b, int &x, int &y) {
  int xx = y = 0;
  int yy = x = 1;
  while (b) {
    int q = a/b;
   int t = b; b = a%b; a = t;
   t = xx; xx = x-q*xx; x = t;
    t = yy; yy = y-q*yy; y = t;
  return a;
}
// finds all solutions to ax = b \pmod{n}
VI modular linear equation solver(int a, int b, int n) {
  int x, y;
 VI solutions;
  int d = extended euclid(a, n, x, y);
  if (!(b%d)) {
    x = mod (x*(b/d), n);
    for (int i = 0; i < d; i++)</pre>
      solutions.push back(mod(x + i*(n/d), n));
  return solutions;
// computes b such that ab = 1 \pmod{n}, returns -1 on failure
int mod inverse(int a, int n) {
  int x, y;
  int d = extended euclid(a, n, x, y);
 if (d > 1) return -1;
  return mod(x,n);
// Chinese remainder theorem (special case): find z such that
// z % x = a, z % y = b. Here, z is unique modulo M = lcm(x,y).
// Return (z,M). On failure, M=-1.
PII chinese remainder theorem(int x, int a, int y, int b) {
 int s, t;
  int d = extended euclid(x, y, s, t);
 if (a%d != b%d) return make_pair(0, -1);
  return make pair(mod(s*b*x+t*a*y,x*y)/d, x*y/d);
// Chinese remainder theorem: find z such that
//z % x[i] = a[i] for all i. Note that the solution is
// unique modulo M = lcm i (x[i]). Return (z,M). On
// failure, M = -1. Note that we do not require the a[i]'s
// to be relatively prime.
PII chinese remainder theorem(const VI &x, const VI &a) {
  PII ret = make pair(a[0], x[0]);
  for (int i = 1; i < x.size(); i++) {</pre>
    ret = chinese remainder theorem(ret.second, ret.first, x[i], a[i]);
    if (ret.second == -1) break;
  }
  return ret;
```

```
// computes x and y such that ax + by = c; on failure, x = y = -1
void linear diophantine(int a, int b, int c, int &x, int &y) {
  int d = gcd(a,b);
 if (c%d) {
   x = y = -1;
  } else {
   x = c/d * mod inverse(a/d, b/d);
    y = (c-a*x)/b;
 }
}
int main() {
  // expected: 2
  cout << gcd(14, 30) << endl;
  // expected: 2 -2 1
  int x, y;
  int d = extended euclid(14, 30, x, y);
  cout << d << " " << x << " " << y << endl;
  // expected: 95 45
 VI sols = modular linear equation solver(14, 30, 100);
  for (int i = 0; i < (int) sols.size(); i++) cout << sols[i] << " ";</pre>
  cout << endl;</pre>
  // expected: 8
  cout << mod inverse(8, 9) << endl;</pre>
  // expected: 23 56
               11 12
  int xs[] = {3, 5, 7, 4, 6};
  int as[] = \{2, 3, 2, 3, 5\};
  PII ret = chinese remainder theorem(VI (xs, xs+3), VI(as, as+3));
  cout << ret.first << " " << ret.second << endl;</pre>
  ret = chinese remainder theorem (VI(xs+3, xs+5), VI(as+3, as+5));
  cout << ret.first << " " << ret.second << endl;</pre>
  // expected: 5 -15
  linear diophantine(7, 2, 5, x, y);
  cout << x << " " << y << endl;
}
```

GaussJordan.cc 14/34

```
// Gauss-Jordan elimination with full pivoting.
//
// Uses:
// (1) solving systems of linear equations (AX=B)
// (2) inverting matrices (AX=I)
```

```
//
     (3) computing determinants of square matrices
// Running time: O(n^3)
//
// INPUT:
             a[][] = an nxn matrix
             b[][] = an nxm matrix
//
// OUTPUT:
            X = an nxm matrix (stored in b[][])
             A^{-1} = an nxn matrix (stored in a[][])
             returns determinant of a[][]
#include <iostream>
#include <vector>
#include <cmath>
using namespace std;
const double EPS = 1e-10;
typedef vector<int> VI;
typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;
T GaussJordan(VVT &a, VVT &b) {
 const int n = a.size();
  const int m = b[0].size();
 VI irow(n), icol(n), ipiv(n);
  T \det = 1;
  for (int i = 0; i < n; i++) {</pre>
    int pj = -1, pk = -1;
    for (int j = 0; j < n; j++) if (!ipiv[j])</pre>
      for (int k = 0; k < n; k++) if (!ipiv[k])</pre>
        if (pj == -1 \mid | fabs(a[j][k]) > fabs(a[pj][pk])) { pj = j; pk = k; }
    if (fabs(a[pj][pk]) < EPS) { cerr << "Matrix is singular." << endl;</pre>
exit(0); }
    ipiv[pk]++;
    swap(a[pj], a[pk]);
    swap(b[pj], b[pk]);
    if (pj != pk) det *= -1;
    irow[i] = pj;
    icol[i] = pk;
    T c = 1.0 / a[pk][pk];
    det *= a[pk][pk];
    a[pk][pk] = 1.0;
    for (int p = 0; p < n; p++) a[pk][p] *= c;</pre>
    for (int p = 0; p < m; p++) b[pk][p] *= c;</pre>
    for (int p = 0; p < n; p++) if (p != pk) {</pre>
      c = a[p][pk];
      a[p][pk] = 0;
      for (int q = 0; q < n; q++) a[p][q] -= a[pk][q] * c;
     for (int q = 0; q < m; q++) b[p][q] -= b[pk][q] * c;</pre>
  }
```

```
for (int p = n-1; p >= 0; p--) if (irow[p] != icol[p]) {
    for (int k = 0; k < n; k++) swap(a[k][irow[p]], a[k][icol[p]]);
 return det;
}
int main() {
  const int n = 4;
  const int m = 2;
  double A[n][n] = \{ \{1,2,3,4\}, \{1,0,1,0\}, \{5,3,2,4\}, \{6,1,4,6\} \};
  double B[n][m] = \{ \{1,2\}, \{4,3\}, \{5,6\}, \{8,7\} \};
  VVT a(n), b(n);
  for (int i = 0; i < n; i++) {</pre>
    a[i] = VT(A[i], A[i] + n);
    b[i] = VT(B[i], B[i] + m);
  double det = GaussJordan(a, b);
  // expected: 60
  cout << "Determinant: " << det << endl;</pre>
  // expected: -0.233333 0.166667 0.133333 0.0666667
                0.166667 0.166667 0.333333 -0.333333
  //
                0.233333 0.833333 -0.133333 -0.0666667
                0.05 -0.75 -0.1 0.2
  cout << "Inverse: " << endl;</pre>
  for (int i = 0; i < n; i++) {</pre>
    for (int j = 0; j < n; j++)</pre>
      cout << a[i][j] << ' ';
   cout << endl;
  }
  // expected: 1.63333 1.3
  //
                -0.166667 0.5
                2.36667 1.7
  //
                -1.85 - 1.35
  cout << "Solution: " << endl;</pre>
  for (int i = 0; i < n; i++) {</pre>
    for (int j = 0; j < m; j++)</pre>
      cout << b[i][j] << '
    cout << endl;
  }
}
```

ReducedRowEchelonForm.cc 15/34

```
// Reduced row echelon form via Gauss-Jordan elimination 
// with partial pivoting. This can be used for computing 
// the rank of a matrix. 
// 
// Running time: O(n^3)
```

```
// INPUT:
             a[][] = an nxm matrix
// OUTPUT:
            rref[][] = an nxm matrix (stored in a[][])
             returns rank of a[][]
#include <iostream>
#include <vector>
#include <cmath>
using namespace std;
const double EPSILON = 1e-10;
typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;
int rref(VVT &a) {
  int n = a.size();
  int m = a[0].size();
  int r = 0;
  for (int c = 0; c < m && r < n; c++) {
    int j = r;
    for (int i = r+1; i < n; i++)</pre>
      if (fabs(a[i][c]) > fabs(a[j][c])) j = i;
    if (fabs(a[j][c]) < EPSILON) continue;</pre>
    swap(a[j], a[r]);
    T s = 1.0 / a[r][c];
    for (int j = 0; j < m; j++) a[r][j] *= s;</pre>
    for (int i = 0; i < n; i++) if (i != r) {</pre>
      T t = a[i][c];
      for (int j = 0; j < m; j++) a[i][j] -= t * a[r][j];</pre>
    r++;
  }
  return r;
}
int main() {
  const int n = 5;
  const int m = 4;
  double A[n][m] = \{\{16,2,3,13\},\{5,11,10,8\},\{9,7,6,12\},\{4,14,15,1\},
{13,21,21,13} };
  VVT a(n);
  for (int i = 0; i < n; i++)</pre>
    a[i] = VT(A[i], A[i] + n);
  int rank = rref (a);
  // expected: 4
  cout << "Rank: " << rank << endl;</pre>
  // expected: 1 0 0 1
               0 1 0 3
```

```
// 0 0 1 -3
// 0 0 0 2.78206e-15
// 0 0 0 3.22398e-15
cout << "rref: " << endl;
for (int i = 0; i < 5; i++) {
   for (int j = 0; j < 4; j++)
      cout << a[i][j] << ' ';
   cout << endl;
}</pre>
```

FFT_new.cpp 16/34

```
#include <cassert>
#include <cstdio>
#include <cmath>
struct cpx
  cpx(){}
  cpx(double aa):a(aa){}
  cpx(double aa, double bb):a(aa),b(bb){}
  double a;
  double b;
  double modsq(void) const
    return a * a + b * b;
  cpx bar(void) const
   return cpx(a, -b);
};
cpx operator + (cpx a, cpx b)
 return cpx(a.a + b.a, a.b + b.b);
cpx operator *(cpx a, cpx b)
 return cpx(a.a * b.a - a.b * b.b, a.a * b.b + a.b * b.a);
cpx operator / (cpx a, cpx b)
 cpx r = a * b.bar();
 return cpx(r.a / b.modsq(), r.b / b.modsq());
cpx EXP (double theta)
```

```
return cpx(cos(theta), sin(theta));
const double two pi = 4 * acos(0);
// in:
           input array
// out:
          output array
// step:
           {SET TO 1} (used internally)
         length of the input/output {MUST BE A POWER OF 2}
// dir:
          either plus or minus one (direction of the FFT)
// RESULT: out[k] = \sum {j=0}^{s=0}^{s=0} in[j] * exp(dir * 2pi * i * j * k / s=0)
size)
void FFT(cpx *in, cpx *out, int step, int size, int dir)
  if(size < 1) return;</pre>
  if(size == 1)
    out[0] = in[0];
    return;
 FFT(in, out, step * 2, size / 2, dir);
  FFT(in + step, out + size / 2, step * 2, size / 2, dir);
  for(int i = 0 ; i < size / 2 ; i++)</pre>
    cpx even = out[i];
    cpx odd = out[i + size / 2];
    out[i] = even + EXP(dir * two pi * i / size) * odd;
    out[i + size / 2] = even + EXP(dir * two pi * (i + size / 2) / size) *
odd;
  }
}
// f[0...N-1] and g[0...N-1] are numbers
\ensuremath{//} Want to compute the convolution h, defined by
// h[n] = sum \ of \ f[k]g[n-k] \ (k = 0, ..., N-1).
// Here, the index is cyclic; f[-1] = f[N-1], f[-2] = f[N-2], etc.
// Let F[0...N-1] be FFT(f), and similarly, define G and H.
// The convolution theorem says H[n] = F[n]G[n] (element-wise product).
// To compute h[] in O(N log N) time, do the following:
//
   1. Compute F and G (pass dir = 1 as the argument).
   2. Get H by element-wise multiplying F and G.
     3. Get h by taking the inverse FFT (use dir = -1 as the argument)
        and *dividing by N*. DO NOT FORGET THIS SCALING FACTOR.
int main(void)
 printf("If rows come in identical pairs, then everything works.\n");
  cpx \ a[8] = \{0, 1, cpx(1,3), cpx(0,5), 1, 0, 2, 0\};
  cpx b[8] = \{1, cpx(0,-2), cpx(0,1), 3, -1, -3, 1, -2\};
  cpx A[8];
  cpx B[8];
  FFT(a, A, 1, 8, 1);
  FFT(b, B, 1, 8, 1);
```

```
for(int i = 0 ; i < 8 ; i++)</pre>
    printf("%7.21f%7.21f", A[i].a, A[i].b);
  printf("\n");
  for(int i = 0 ; i < 8 ; i++)</pre>
    cpx Ai(0,0);
    for (int j = 0; j < 8; j++)
      Ai = Ai + a[j] * EXP(j * i * two_pi / 8);
   printf("%7.21f%7.21f", Ai.a, Ai.b);
 printf("\n");
  cpx AB[8];
  for(int i = 0 ; i < 8 ; i++)</pre>
   AB[i] = A[i] * B[i];
  cpx aconvb[8];
  FFT(AB, aconvb, 1, 8, -1);
  for(int i = 0 ; i < 8 ; i++)</pre>
    aconvb[i] = aconvb[i] / 8;
  for(int i = 0 ; i < 8 ; i++)</pre>
    printf("%7.21f%7.21f", aconvb[i].a, aconvb[i].b);
 printf("\n");
  for(int i = 0 ; i < 8 ; i++)</pre>
    cpx aconvbi(0,0);
    for (int j = 0 ; j < 8 ; j++)
      aconvbi = aconvbi + a[j] * b[(8 + i - j) % 8];
    printf("%7.21f%7.21f", aconvbi.a, aconvbi.b);
 printf("\n");
 return 0;
}
```

Simplex.cc 17/34

```
//
          c -- an n-dimensional vector
          x -- a vector where the optimal solution will be stored
// OUTPUT: value of the optimal solution (infinity if unbounded
           above, nan if infeasible)
//
// To use this code, create an LPSolver object with A, b, and c as
// arguments. Then, call Solve(x).
#include <iostream>
#include <iomanip>
#include <vector>
#include <cmath>
#include <limits>
using namespace std;
typedef long double DOUBLE;
typedef vector<DOUBLE> VD;
typedef vector<VD> VVD;
typedef vector<int> VI;
const DOUBLE EPS = 1e-9;
struct LPSolver {
 int m, n;
 VI B, N;
 VVD D;
  LPSolver(const VVD &A, const VD &b, const VD &c) :
    m(b.size()), n(c.size()), N(n+1), B(m), D(m+2, VD(n+2)) {
    for (int i = 0; i < m; i++) for (int j = 0; j < n; j++) D[i][j] = A[i][j];</pre>
    for (int i = 0; i < m; i++) { B[i] = n+i; D[i][n] = -1; D[i][n+1] =
b[i]; }
    for (int j = 0; j < n; j++) { N[j] = j; D[m][j] = -c[j]; }
    N[n] = -1; D[m+1][n] = 1;
  }
  void Pivot(int r, int s) {
    for (int i = 0; i < m+2; i++) if (i != r)</pre>
      for (int j = 0; j < n+2; j++) if (j != s)</pre>
        D[i][j] = D[r][j] * D[i][s] / D[r][s];
    for (int j = 0; j < n+2; j++) if (j != s) D[r][j] /= D[r][s];</pre>
    for (int i = 0; i < m+2; i++) if (i != r) D[i][s] /= -D[r][s];</pre>
    D[r][s] = 1.0 / D[r][s];
    swap(B[r], N[s]);
 bool Simplex(int phase) {
    int x = phase == 1 ? m+1 : m;
    while (true) {
      int s = -1;
      for (int j = 0; j <= n; j++) {</pre>
       if (phase == 2 && N[j] == -1) continue;
       if (s == -1 || D[x][j] < D[x][s] || D[x][j] == D[x][s] && N[j] < N[s])
s = j;
```

```
if (D[x][s] >= -EPS) return true;
      int r = -1;
      for (int i = 0; i < m; i++) {</pre>
       if (D[i][s] <= 0) continue;</pre>
        if (r == -1 || D[i][n+1] / D[i][s] < D[r][n+1] / D[r][s] ||
            D[i][n+1] / D[i][s] == D[r][n+1] / D[r][s] && B[i] < B[r]) r = i;
      if (r == -1) return false;
      Pivot(r, s);
    }
  }
  DOUBLE Solve(VD &x) {
    int r = 0;
    for (int i = 1; i < m; i++) if (D[i][n+1] < D[r][n+1]) r = i;</pre>
    if (D[r][n+1] \le -EPS) {
      Pivot(r, n);
      if (!Simplex(1) || D[m+1][n+1] < -EPS) return</pre>
-numeric limits<DOUBLE>::infinity();
      for (int i = 0; i < m; i++) if (B[i] == -1) {</pre>
        int s = -1;
        for (int j = 0; j <= n; j++)</pre>
         if (s == -1 || D[i][j] < D[i][s] || D[i][j] == D[i][s] && N[j] <
N[s]) s = j;
       Pivot(i, s);
    }
    if (!Simplex(2)) return numeric limits<DOUBLE>::infinity();
    x = VD(n);
    for (int i = 0; i < m; i++) if (B[i] < n) x[B[i]] = D[i][n+1];</pre>
    return D[m] [n+1];
  }
};
int main() {
  const int m = 4;
  const int n = 3;
  DOUBLE A[m][n] = {
    \{ 6, -1, 0 \},
    \{-1, -5, 0\},
    { 1, 5, 1 },
    \{-1, -5, -1\}
  };
  DOUBLE b[m] = \{ 10, -4, 5, -5 \};
  DOUBLE c[n] = \{ 1, -1, 0 \};
 VVD A(m);
 VD b(b, b+m);
  VD c(c, c+n);
  for (int i = 0; i < m; i++) A[i] = VD( A[i], A[i] + n);</pre>
  LPSolver solver(A, b, c);
  VD x;
  DOUBLE value = solver.Solve(x);
```

```
cerr << "VALUE: "<< value << endl;
cerr << "SOLUTION:";
for (size_t i = 0; i < x.size(); i++) cerr << " " << x[i];
cerr << endl;
return 0;
}</pre>
```

FastDijkstra.cc 18/34

```
// Implementation of Dijkstra's algorithm using adjacency lists
// and priority queue for efficiency.
// Running time: O(|E| \log |V|)
#include <queue>
#include <stdio.h>
using namespace std;
const int INF = 2000000000;
typedef pair<int, int> PII;
int main(){
  int N, s, t;
  scanf ("%d%d%d", &N, &s, &t);
 vector<vector<PII> > edges(N);
  for (int i = 0; i < N; i++) {</pre>
    int M;
    scanf ("%d", &M);
    for (int j = 0; j < M; j++) {
     int vertex, dist;
     scanf ("%d%d", &vertex, &dist);
      edges[i].push back (make pair (dist, vertex)); // note order of
arguments here
   }
  }
  // use priority queue in which top element has the "smallest" priority
 priority queue<PII, vector<PII>, greater<PII> > Q;
  vector<int> dist(N, INF), dad(N, -1);
  Q.push (make pair (0, s));
  dist[s] = 0;
  while (!Q.empty()){
    PII p = Q.top();
    if (p.second == t) break;
    Q.pop();
    int here = p.second;
    for (vector<PII>::iterator it=edges[here].begin(); it!=edges[here].end();
it++) {
```

```
if (dist[here] + it->first < dist[it->second]) {
    dist[it->second] = dist[here] + it->first;
    dad[it->second] = here;
    Q.push (make_pair (dist[it->second], it->second));
    }
}

printf ("%d\n", dist[t]);
if (dist[t] < INF)
    for(int i=t;i!=-1;i=dad[i])
    printf ("%d%c", i, (i==s?'\n':' '));

return 0;
}</pre>
```

SCC.cc 19/34

```
#include<memory.h>
struct edge{int e, nxt;};
int V, E;
edge e[MAXE], er[MAXE];
int sp[MAXV], spr[MAXV];
int group_cnt, group_num[MAXV];
bool v[MAXV];
int stk[MAXV];
void fill forward(int x)
  int i;
 v[x]=true;
 for(i=sp[x];i;i=e[i].nxt) if(!v[e[i].e]) fill forward(e[i].e);
  stk[++stk[0]]=x;
void fill backward(int x)
{
  int i;
 v[x] = false;
  group num[x]=group cnt;
  for(i=spr[x];i;i=er[i].nxt) if(v[er[i].e]) fill backward(er[i].e);
void add edge(int v1, int v2) //add edge v1->v2
 e [++E].e=v2; e [E].nxt=sp [v1]; sp [v1]=E;
  er[ E].e=v1; er[E].nxt=spr[v2]; spr[v2]=E;
void SCC()
 int i;
 stk[0]=0;
 memset(v, false, sizeof(v));
 for(i=1;i<=V;i++) if(!v[i]) fill_forward(i);</pre>
  group cnt=0;
  for(i=stk[0];i>=1;i--) if(v[stk[i]]){group cnt++; fill backward(stk[i]);}
```

}

EulerianPath.cc 20/34

```
struct Edge;
typedef list<Edge>::iterator iter;
struct Edge
       int next vertex;
       iter reverse edge;
       Edge(int next vertex)
               :next vertex(next vertex)
};
const int max_vertices = ;
int num vertices;
list<Edge> adj[max vertices];
                                    // adjacency list
vector<int> path;
void find_path(int v)
       while(adj[v].size() > 0)
               int vn = adj[v].front().next vertex;
               adj[vn].erase(adj[v].front().reverse edge);
               adj[v].pop front();
               find path(vn);
       path.push back(v);
}
void add_edge(int a, int b)
       adj[a].push_front(Edge(b));
       iter ita = adj[a].begin();
       adj[b].push front(Edge(a));
       iter itb = adj[b].begin();
       ita->reverse edge = itb;
       itb->reverse edge = ita;
}
```

SuffixArray.cc 21/34

```
// Suffix array construction in O(L \log^2 L) time. Routine for // computing the length of the longest common prefix of any two
```

```
// suffixes in O(log L) time.
// INPUT:
            string s
//
// OUTPUT: array suffix[] such that suffix[i] = index (from 0 to L-1)
//
            of substring s[i...L-1] in the list of sorted suffixes.
            That is, if we take the inverse of the permutation suffix[],
//
            we get the actual suffix array.
//
#include <vector>
#include <iostream>
#include <string>
using namespace std;
struct SuffixArray {
 const int L;
 string s;
 vector<vector<int> > P;
 vector<pair<int,int>,int> > M;
  SuffixArray(const string &s) : L(s.length()), s(s), P(1, vector<int>(L, 0)),
M(L) {
    for (int i = 0; i < L; i++) P[0][i] = int(s[i]);</pre>
    for (int skip = 1, level = 1; skip < L; skip *= 2, level++) {</pre>
      P.push back(vector<int>(L, 0));
      for (int i = 0; i < L; i++)</pre>
       M[i] = make pair(make pair(P[level-1][i], i + skip < L ? P[level-1][i
+ \text{ skip}] : -1000), i);
      sort(M.begin(), M.end());
      for (int i = 0; i < L; i++)</pre>
        P[level][M[i].second] = (i > 0 && M[i].first == M[i-1].first) ?
P[level][M[i-1].second] : i;
    }
  }
  vector<int> GetSuffixArray() { return P.back(); }
  // returns the length of the longest common prefix of s[i...L-1] and
s[j...L-1]
  int LongestCommonPrefix(int i, int j) {
    int len = 0;
    if (i == j) return L - i;
    for (int k = P.size() - 1; k >= 0 && i < L && j < L; k--) {</pre>
      if (P[k][i] == P[k][j]) {
       i += 1 << k;
       j += 1 << k;
       len += 1 << k;
      }
    return len;
  }
} ;
int main() {
  // bobocel is the 0'th suffix
```

```
// obocel is the 5'th suffix
// bocel is the 1'st suffix
// ocel is the 6'th suffix
// cel is the 2'nd suffix
// el is the 3'rd suffix
// l is the 4'th suffix
SuffixArray suffix("bobocel");
vector<int> v = suffix.GetSuffixArray();

// Expected output: 0 5 1 6 2 3 4
// 2
for (int i = 0; i < v.size(); i++) cout << v[i] << " ";
cout << endl;
cout << suffix.LongestCommonPrefix(0, 2) << endl;
}</pre>
```

BIT.cc 22/34

```
#include <iostream>
using namespace std;
#define LOGSZ 17
int tree[(1<<LOGSZ)+1];</pre>
int N = (1 << LOGSZ);
// add v to value at x
void set(int x, int v) {
 while (x \le N)
   tree[x] += v;
    x += (x & -x);
 }
}
// get cumulative sum up to and including x
int get(int x) {
  int res = 0;
  while(x) {
   res += tree[x];
   x = (x \& -x);
 return res;
// get largest value with cumulative sum less than or equal to x;
// for smallest, pass x-1 and add 1 to result
int getind(int x) {
  int idx = 0, mask = N;
  while (mask && idx < N) {</pre>
    int t = idx + mask;
    if(x \ge tree[t]) {
      idx = t;
      x -= tree[t];
```

UnionFind.cc 23/34

```
//union-find set: the vector/array contains the parent of each node
int find(vector <int>& C, int x) {return (C[x]==x) ? x : C[x]=find(C, C[x]);}
//C++
int find(int x) {return (C[x]==x) ?x:C[x]=find(C[x]);} //C
```

KDTree.cc 24/34

```
// A straightforward, but probably sub-optimal KD-tree implmentation that's
// probably good enough for most things (current it's a 2D-tree)
//
// - constructs from n points in O(n lg^2 n) time
// - handles nearest-neighbor query in O(lg n) if points are well
distributed
// - worst case for nearest-neighbor may be linear in pathological case
// Sonny Chan, Stanford University, April 2009
// -----
#include <iostream>
#include <vector>
#include <limits>
#include <cstdlib>
using namespace std;
// number type for coordinates, and its maximum value
typedef long long ntype;
const ntype sentry = numeric limits<ntype>::max();
// point structure for 2D-tree, can be extended to 3D
struct point {
   ntype x, y;
   point(ntype xx = 0, ntype yy = 0) : x(xx), y(yy) {}
};
bool operator==(const point &a, const point &b)
   return a.x == b.x && a.y == b.y;
// sorts points on x-coordinate
```

```
bool on x(const point &a, const point &b)
    return a.x < b.x;</pre>
}
// sorts points on y-coordinate
bool on y(const point &a, const point &b)
    return a.y < b.y;</pre>
}
// squared distance between points
ntype pdist2(const point &a, const point &b)
    ntype dx = a.x-b.x, dy = a.y-b.y;
    return dx*dx + dy*dy;
}
// bounding box for a set of points
struct bbox
    ntype x0, x1, y0, y1;
    bbox() : x0(sentry), x1(-sentry), y0(sentry), y1(-sentry) {}
    // computes bounding box from a bunch of points
    void compute(const vector<point> &v) {
        for (int i = 0; i < v.size(); ++i) {</pre>
            x0 = min(x0, v[i].x); x1 = max(x1, v[i].x);
                                   y1 = max(y1, v[i].y);
            y0 = min(y0, v[i].y);
        }
    }
    // squared distance between a point and this bbox, 0 if inside
    ntype distance(const point &p) {
        if (p.x < x0) {
                                return pdist2(point(x0, y0), p);
            if (p.y < y0)
            else if (p.y > y1) return pdist2(point(x0, y1), p);
                                return pdist2(point(x0, p.y), p);
        else if (p.x > x1) {
                                return pdist2(point(x1, y0), p);
            if (p.y < y0)
            else if (p.y > y1) return pdist2(point(x1, y1), p);
            else
                                 return pdist2(point(x1, p.y), p);
        else {
            if (p.y < y0)
                                return pdist2(point(p.x, y0), p);
            else if (p.y > y1) return pdist2(point(p.x, y1), p);
                                return 0;
            else
        }
    }
};
// stores a single node of the kd-tree, either internal or leaf
struct kdnode
```

```
bool leaf;
                   // true if this is a leaf node (has one point)
                    // the single point of this is a leaf
    point pt;
                    // bounding box for set of points in children
   bbox bound;
    kdnode *first, *second; // two children of this kd-node
    kdnode() : leaf(false), first(0), second(0) {}
    ~kdnode() { if (first) delete first; if (second) delete second; }
    // intersect a point with this node (returns squared distance)
    ntype intersect(const point &p) {
        return bound.distance(p);
    // recursively builds a kd-tree from a given cloud of points
    void construct(vector<point> &vp)
        // compute bounding box for points at this node
        bound.compute(vp);
        // if we're down to one point, then we're a leaf node
        if (vp.size() == 1) {
            leaf = true;
            pt = vp[0];
        else {
            // split on x if the bbox is wider than high (not best
heuristic...)
            if (bound.x1-bound.x0 >= bound.y1-bound.y0)
                sort(vp.begin(), vp.end(), on x);
            // otherwise split on y-coordinate
            else
                sort(vp.begin(), vp.end(), on y);
            // divide by taking half the array for each child
            // (not best performance if many duplicates in the middle)
            int half = vp.size()/2;
            vector<point> vl(vp.begin(), vp.begin()+half);
            vector<point> vr(vp.begin()+half, vp.end());
            first = new kdnode(); first->construct(vl);
            second = new kdnode(); second->construct(vr);
        }
    }
};
// simple kd-tree class to hold the tree and handle queries
struct kdtree
    kdnode *root;
    // constructs a kd-tree from a points (copied here, as it sorts them)
    kdtree(const vector<point> &vp) {
        vector<point> v(vp.begin(), vp.end());
        root = new kdnode();
        root->construct(v);
```

```
~kdtree() { delete root; }
    // recursive search method returns squared distance to nearest point
   ntype search(kdnode *node, const point &p)
       if (node->leaf) {
           // commented special case tells a point not to find itself
             if (p == node->pt) return sentry;
             else
               return pdist2(p, node->pt);
       ntype bfirst = node->first->intersect(p);
       ntype bsecond = node->second->intersect(p);
        // choose the side with the closest bounding box to search first
        // (note that the other side is also searched if needed)
       if (bfirst < bsecond) {</pre>
           ntype best = search(node->first, p);
           if (bsecond < best)</pre>
               best = min(best, search(node->second, p));
           return best;
        }
       else {
           ntype best = search(node->second, p);
           if (bfirst < best)</pre>
               best = min(best, search(node->first, p));
           return best;
       }
   }
    // squared distance to the nearest
   ntype nearest(const point &p) {
       return search(root, p);
};
// -----
// some basic test code here
int main()
    // generate some random points for a kd-tree
   vector<point> vp;
    for (int i = 0; i < 100000; ++i) {</pre>
       vp.push back(point(rand()%100000, rand()%100000));
   kdtree tree(vp);
   // query some points
   for (int i = 0; i < 10; ++i) {</pre>
       point g(rand()%100000, rand()%100000);
       cout << "Closest squared distance to (" << q.x << ", " << q.y << ")"
            << " is " << tree.nearest(q) << endl;
    }
```

SegmentTreeLazy.java 25/34

```
public class SegmentTreeRangeUpdate {
       public long[] leaf;
       public long[] update;
       public int origSize;
       public SegmentTreeRangeUpdate(int[] list) {
               origSize = list.length;
                leaf = new long[4*list.length];
                update = new long[4*list.length];
               build(1,0,list.length-1,list);
        public void build(int curr, int begin, int end, int[] list) {
                if(begin == end)
                       leaf[curr] = list[begin];
                else
                       int mid = (begin+end)/2;
                       build(2 * curr, begin, mid, list);
                       build(2 * curr + 1, mid+1, end, list);
                       leaf[curr] = leaf[2*curr] + leaf[2*curr+1];
                }
       public void update(int begin, int end, int val)
                update(1,0,origSize-1,begin,end,val);
       public void update(int curr, int tBegin, int tEnd, int begin, int
end, int val)
                if (tBegin >= begin && tEnd <= end)</pre>
                       update[curr] += val;
                else
                        leaf[curr] += (Math.min(end,tEnd)-
Math.max(begin,tBegin)+1) * val;
                        int mid = (tBegin+tEnd)/2;
                       if (mid >= begin && tBegin <= end)</pre>
                               update(2*curr, tBegin, mid, begin, end, val);
                       if(tEnd >= begin && mid+1 <= end)</pre>
                               update(2*curr+1, mid+1, tEnd, begin, end, val);
                }
        public long query(int begin, int end) {
                return query(1,0,origSize-1,begin,end);
       public long query (int curr, int tBegin, int tEnd, int begin, int end)
                if(tBegin >= begin && tEnd <= end)</pre>
                        if(update[curr] != 0) {
                               leaf[curr] += (tEnd-tBegin+1) * update[curr];
                               if(2*curr < update.length){</pre>
```

```
update[2*curr] += update[curr];
                                        update[2*curr+1] += update[curr];
                                update[curr] = 0;
                        return leaf[curr];
                else
                        leaf[curr] += (tEnd-tBegin+1) * update[curr];
                        if(2*curr < update.length){</pre>
                                update[2*curr] += update[curr];
                                update[2*curr+1] += update[curr];
                        update[curr] = 0;
                        int mid = (tBegin+tEnd)/2;
                        long ret = 0;
                        if (mid >= begin && tBegin <= end)</pre>
                                ret += query(2*curr, tBegin, mid, begin, end);
                        if(tEnd >= begin && mid+1 <= end)</pre>
                                ret += query(2*curr+1, mid+1, tEnd, begin,
end);
                        return ret;
        }
}
```

LCA.cc 26/34

```
const int max nodes, log max nodes;
int num nodes, log num nodes, root;
vector<int> children[max nodes];
                                     // children[i] contains the children of
node i
int A[max nodes][log max nodes+1];
                                     // A[i][j] is the 2^j-th ancestor of
node i, or -1 if that ancestor does not exist
int L[max nodes];
                                      // L[i] is the distance between node i
and the root
// floor of the binary logarithm of n
int lb(unsigned int n)
{
    if(n==0)
       return -1;
    int p = 0;
    if (n >= 1 << 16) \{ n >>= 16; p += 16; \}
   if (n >= 1 << 8) { n >>= 8; p += 8; }
   if (n >= 1 << 4) \{ n >>= 4; p += 4; \}
   if (n >= 1 << 2) { n >>= 2; p += 2; }
   if (n >= 1 << 1)
                                p += 1; 
   return p;
}
void DFS(int i, int 1)
{
```

```
L[i] = 1;
    for(int j = 0; j < children[i].size(); j++)</pre>
        DFS(children[i][j], l+1);
}
int LCA(int p, int q)
    // ensure node p is at least as deep as node q
    if(L[p] < L[q])
       swap(p, q);
    // "binary search" for the ancestor of node p situated on the same level
as q
    for(int i = log num nodes; i >= 0; i--)
        if(L[p] - (1 << i) >= L[q])
            p = A[p][i];
    if(p == q)
        return p;
    // "binary search" for the LCA
    for(int i = log num nodes; i >= 0; i--)
        if (A[p][i] != -1 && A[p][i] != A[q][i])
        {
            p = A[p][i];
            q = A[q][i];
   return A[p][0];
}
int main(int argc,char* argv[])
    // read num nodes, the total number of nodes
    log num nodes=lb(num nodes);
    for(int i = 0; i < num nodes; i++)</pre>
        int p;
        // read p, the parent of node i or -1 if node i is the root
       A[i][0] = p;
        if (p != -1)
            children[p].push back(i);
        else
           root = i;
    }
    // precompute A using dynamic programming
    for(int j = 1; j <= log num nodes; j++)</pre>
        for(int i = 0; i < num nodes; i++)</pre>
            if(A[i][j-1] != -1)
                A[i][j] = A[A[i][j-1]][j-1];
            else
               A[i][j] = -1;
```

```
// precompute L
DFS(root, 0);
return 0;
```

LongestIncreasingSubsequence.cc 27/34

```
// Given a list of numbers of length n, this routine extracts a
// longest increasing subsequence.
//
// Running time: O(n log n)
//
     INPUT: a vector of integers
     OUTPUT: a vector containing the longest increasing subsequence
#include <iostream>
#include <vector>
#include <algorithm>
using namespace std;
typedef vector<int> VI;
typedef pair<int, int> PII;
typedef vector<PII> VPII;
#define STRICTLY INCREASIG
VI LongestIncreasingSubsequence(VI v) {
 VPII best;
 VI dad(v.size(), -1);
  for (int i = 0; i < v.size(); i++) {</pre>
#ifdef STRICTLY INCREASIG
    PII item = make pair(v[i], 0);
    VPII::iterator it = lower bound(best.begin(), best.end(), item);
    item.second = i;
#else
    PII item = make pair(v[i], i);
    VPII::iterator it = upper bound(best.begin(), best.end(), item);
#endif
    if (it == best.end()) {
      dad[i] = (best.size() == 0 ? -1 : best.back().second);
      best.push back(item);
    } else {
      dad[i] = dad[it->second];
      *it = item;
  }
  VI ret;
  for (int i = best.back().second; i >= 0; i = dad[i])
```

```
ret.push_back(v[i]);
reverse(ret.begin(), ret.end());
return ret;
```

Dates.cc 28/34

```
// Routines for performing computations on dates. In these routines,
// months are expressed as integers from 1 to 12, days are expressed
// as integers from 1 to 31, and years are expressed as 4-digit
// integers.
#include <iostream>
#include <string>
using namespace std;
string dayOfWeek[] = {"Mon", "Tue", "Wed", "Thu", "Fri", "Sat", "Sun"};
// converts Gregorian date to integer (Julian day number)
int dateToInt (int m, int d, int y) {
  return
    1461 * (y + 4800 + (m - 14) / 12) / 4 +
    367 * (m - 2 - (m - 14) / 12 * 12) / 12 -
    3 * ((y + 4900 + (m - 14) / 12) / 100) / 4 +
    d - 32075;
}
// converts integer (Julian day number) to Gregorian date: month/day/year
void intToDate (int jd, int &m, int &d, int &y) {
  int x, n, i, j;
 x = jd + 68569;
  n = 4 * x / 146097;
  x = (146097 * n + 3) / 4;
  i = (4000 * (x + 1)) / 1461001;
  x = 1461 * i / 4 - 31;
  j = 80 * x / 2447;
 d = x - 2447 * j / 80;
 x = i / 11;
 m = j + 2 - 12 * x;
  y = 100 * (n - 49) + i + x;
// converts integer (Julian day number) to day of week
string intToDay (int jd) {
 return dayOfWeek[jd % 7];
int main (int argc, char **argv) {
 int jd = dateToInt (3, 24, 2004);
  int m, d, y;
  intToDate (jd, m, d, y);
```

LogLan.java 29/34

```
// Code which demonstrates the use of Java's regular expression libraries.
// This is a solution for
//
    Loglan: a logical language
// http://acm.uva.es/p/v1/134.html
// In this problem, we are given a regular language, whose rules can be
// inferred directly from the code. For each sentence in the input, we must
// determine whether the sentence matches the regular expression or not. The
// code consists of (1) building the regular expression (which is fairly
// complex) and (2) using the regex to match sentences.
import java.util.*;
import java.util.regex.*;
public class LogLan {
    public static String BuildRegex () {
       String space = " +";
       String A = "([aeiou])";
       String C = "([a-z&&[^aeiou]])";
       String MOD = "(g" + A + ")";
       String BA = "(b" + A + ")";
       String DA = "(d" + A + ")";
       String LA = "(1" + A + ")";
       String NAM = "([a-z]*" + C + ")";
       String PREDA = "(" + C + C + A + C + A + "|" + C + A + C + C + A +
")";
       String predstring = "(" + PREDA + "(" + space + PREDA + ")*)";
       String predname = "(" + LA + space + predstring + "|" + NAM + ")";
       String preds = "(" + predstring + "(" + space + A + space + predstring
       String predclaim = "(" + predname + space + BA + space + preds + "|" +
DA + space +
            preds + ")";
       String verbpred = "(" + MOD + space + predstring + ")";
       String statement = "(" + predname + space + verbpred + space +
predname + "|" +
```

```
predname + space + verbpred + ")";
       String sentence = "(" + statement + "|" + predclaim + ")";
       return "^" + sentence + "$";
    }
   public static void main (String args[]) {
       String regex = BuildRegex();
       Pattern pattern = Pattern.compile (regex);
       Scanner s = new Scanner(System.in);
       while (true) {
            // In this problem, each sentence consists of multiple lines,
where the last
           // line is terminated by a period. The code below reads lines
until
           // encountering a line whose final character is a '.'. Note the
use of
                  s.length() to get length of string
            //
                  s.charAt() to extract characters from a Java string
            //
                  s.trim() to remove whitespace from the beginning and end of
Java string
            // Other useful String manipulation methods include
                  s.compareTo(t) < 0 if s < t, lexicographically
                  s.indexOf("apple") returns index of first occurrence of
            //
"apple" in s
            //
                  s.lastIndexOf("apple") returns index of last occurrence of
"apple" in s
                  s.replace(c,d) replaces occurrences of character c with d
                  s.startsWith("apple) returns (s.indexOf("apple") == 0)
            //
                  s.toLowerCase() / s.toUpperCase() returns a new
lower/uppercased string
            //
            //
                  Integer.parseInt(s) converts s to an integer (32-bit)
            //
                  Long.parseLong(s) converts s to a long (64-bit)
                  Double.parseDouble(s) converts s to a double
           String sentence = "";
           while (true) {
               sentence = (sentence + " " + s.nextLine()).trim();
               if (sentence.equals("#")) return;
               if (sentence.charAt(sentence.length()-1) == '.') break;
            }
            // now, we remove the period, and match the regular expression
            String removed period = sentence.substring(0, sentence.length()-
1).trim();
           if (pattern.matcher (removed period).find()) {
               System.out.println ("Good");
            } else {
```

```
System.out.println ("Bad!");
}
}
```

Primes.cc 30/34

```
// O(sqrt(x)) Exhaustive Primality Test
#include <cmath>
#define EPS 1e-7
typedef long long LL;
bool IsPrimeSlow (LL x)
  if(x<=1) return false;</pre>
  if(x<=3) return true;</pre>
  if (!(x%2) || !(x%3)) return false;
  LL s=(LL) (sqrt((double)(x))+EPS);
  for(LL i=5;i<=s;i+=6)</pre>
    if (!(x%i) || !(x%(i+2))) return false;
  return true;
// Primes less than 1000:
        2
              3
                     5
                                 11
                                        13
                                              17
                                                     19
                                                           23
                                                                  29
                                                                        31
                                                                               37
//
                                                     71
//
       41
             43
                    47
                           53
                                 59
                                        61
                                              67
                                                           73
                                                                  79
                                                                        83
                                                                               89
//
       97
             101
                   103
                          107
                                109
                                       113
                                             127
                                                    131
                                                          137
                                                                 139
                                                                       149
                                                                              151
//
      157
             163
                   167
                         173
                                179
                                       181
                                             191
                                                    193
                                                          197
                                                                 199
                                                                       211
                                                                              223
//
                   233
                                                    263
      227
            229
                          239
                                241
                                       251
                                             257
                                                          269
                                                                 271
                                                                       277
                                                                              281
//
      283
            293
                   307
                                313
                          311
                                       317
                                             331
                                                    337
                                                          347
                                                                 349
                                                                       353
                                                                              359
//
      367
             373
                   379
                          383
                                389
                                       397
                                             401
                                                    409
                                                          419
                                                                 421
                                                                       431
                                                                              433
//
      439
             443
                   449
                          457
                                461
                                       463
                                             467
                                                    479
                                                          487
                                                                 491
                                                                       499
                                                                              503
//
      509
             521
                   523
                          541
                                547
                                       557
                                             563
                                                    569
                                                          571
                                                                 577
                                                                       587
                                                                              593
//
      599
                   607
                          613
                                617
                                       619
                                                    641
                                                                 647
                                                                       653
             601
                                             631
                                                          643
                                                                              659
//
      661
             673
                   677
                          683
                                691
                                       701
                                             709
                                                    719
                                                          727
                                                                 733
                                                                       739
                                                                              743
//
      751
             757
                   761
                          769
                                773
                                       787
                                             797
                                                    809
                                                          811
                                                                 821
                                                                       823
                                                                              827
//
      829
             839
                   853
                          857
                                859
                                       863
                                             877
                                                    881
                                                          883
                                                                 887
                                                                       907
                                                                              911
      919
             929
                   937
                          941
                                947
                                       953
                                             967
                                                    971
                                                          977
                                                                 983
                                                                       991
                                                                              997
// Other primes:
      The largest prime smaller than 10 is 7.
//
      The largest prime smaller than 100 is 97.
//
      The largest prime smaller than 1000 is 997.
//
      The largest prime smaller than 10000 is 9973.
//
      The largest prime smaller than 100000 is 99991.
//
      The largest prime smaller than 1000000 is 999983.
//
      The largest prime smaller than 10000000 is 9999991.
//
      The largest prime smaller than 100000000 is 99999989.
//
      The largest prime smaller than 1000000000 is 999999937.
//
      The largest prime smaller than 1000000000 is 9999999967.
//
      The largest prime smaller than 10000000000 is 9999999977.
      The largest prime smaller than 100000000000 is 999999999999.
//
      The largest prime smaller than 100000000000 is 999999999971.
```

IO.cpp 31/34

```
#include <iostream>
#include <iomanip>
using namespace std;
int main()
    // Ouput a specific number of digits past the decimal point,
    // in this case 5
    cout.setf(ios::fixed); cout << setprecision(5);</pre>
    cout << 100.0/7.0 << endl;
    cout.unsetf(ios::fixed);
    // Output the decimal point and trailing zeros
    cout.setf(ios::showpoint);
    cout << 100.0 << endl;
    cout.unsetf(ios::showpoint);
    // Output a '+' before positive values
    cout.setf(ios::showpos);
    cout << 100 << " " << -100 << endl;
    cout.unsetf(ios::showpos);
    // Output numerical values in hexadecimal
    cout << hex << 100 << " " << 1000 << " " << 10000 << dec << endl;
}
```

KMP.cpp 32/34

```
/*
Searches for the string w in the string s (of length k). Returns the
0-based index of the first match (k if no match is found). Algorithm
runs in O(k) time.
*/
#include <iostream>
#include <string>
#include <vector>
using namespace std;
```

```
typedef vector<int> VI;
void buildTable(string& w, VI& t)
 t = VI(w.length());
 int i = 2, j = 0;
 t[0] = -1; t[1] = 0;
 while(i < w.length())</pre>
    if(w[i-1] == w[j]) { t[i] = j+1; i++; j++; }
    else if(j > 0) j = t[j];
   else { t[i] = 0; i++; }
}
int KMP(string& s, string& w)
  int m = 0, i = 0;
 VI t;
 buildTable(w, t);
  while (m+i < s.length())</pre>
    if(w[i] == s[m+i])
    {
     i++;
     if(i == w.length()) return m;
    }
    else
    m += i-t[i];
     if(i > 0) i = t[i];
 return s.length();
int main()
 string a = (string) "The example above illustrates the general technique for
assembling "+
   "the table with a minimum of fuss. The principle is that of the overall
search: "+
   "most of the work was already done in getting to the current position, so
very "+
   "little needs to be done in leaving it. The only minor complication is
that the "+
    "logic which is correct late in the string erroneously gives non-proper "+
    "substrings at the beginning. This necessitates some initialization
code.";
 string b = "table";
  int p = KMP(a, b);
  cout << p << ": " << a.substr(p, b.length()) << " " << b << endl;</pre>
```

}

LatLong.cpp 33/34

```
Converts from rectangular coordinates to latitude/longitude and vice
versa. Uses degrees (not radians).
#include <iostream>
#include <cmath>
using namespace std;
struct 11
 double r, lat, lon;
struct rect
 double x, y, z;
};
11 convert(rect& P)
 11 Q;
 Q.r = sqrt(P.x*P.x+P.y*P.y+P.z*P.z);
 Q.lat = 180/M PI*asin(P.z/Q.r);
 Q.lon = 180/M PI*acos(P.x/sqrt(P.x*P.x+P.y*P.y));
  return Q;
rect convert(ll& Q)
 rect P;
 P.x = Q.r*cos(Q.lon*M PI/180)*cos(Q.lat*M PI/180);
 P.y = Q.r*sin(Q.lon*M PI/180)*cos(Q.lat*M PI/180);
 P.z = Q.r*sin(Q.lat*M PI/180);
 return P;
}
int main()
  rect A;
 11 B;
 A.x = -1.0; A.y = 2.0; A.z = -3.0;
  B = convert(A);
  cout << B.r << " " << B.lat << " " << B.lon << endl;</pre>
```

```
A = convert(B);
cout << A.x << " " << A.y << " " << A.z << endl;
}</pre>
```

EmacsSettings.txt 34/34

Generated by GNU enscript 1.6.1.