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AI1110 Assignment 1

AI21BTECH11001

ICSE Grade 10 2014 paper

Question 3:

(a) Without using trigonometric tables, evaluate $\sin^2 34^\circ + \sin^2 56^\circ + 2 \tan 18^\circ \tan 72^\circ - \cot^2 30^\circ$ [3]

Solution:

$$= \sin^2 34^\circ + \sin^2 56^\circ + 2 \tan 18^\circ \tan 72^\circ - \cot^2 30^\circ$$
(1)

$$\sin^2 56^\circ = \sin^2(90^\circ - 34^\circ) \tag{2}$$

$$\implies \sin^2 56^\circ = \cos^2(56^\circ) \tag{3}$$

$$2\tan 18^{\circ} \tan 72^{\circ} = 2\tan 18^{\circ} \tan(90 - 18)^{\circ}$$
(4)

$$\implies 2 \tan 18^{\circ} \tan 72^{\circ} = 2 \tan 18^{\circ} \cot 18^{\circ} \tag{5}$$

$$= \sin^2 34^\circ + \cos^2 34^\circ + 2 \tan 18^\circ \cot 18^\circ - \cot^2 30^\circ$$
(6)

$$= 1 + 2 \times \tan 18^{\circ} \times \frac{1}{\tan 18^{\circ}} - (\sqrt{3})^{2}$$
 (7)

$$=1+2-3=0$$
 (8)