Qubits (Quantum Bits)

In[0]:= << Q3`

How to refer to qubits

A collection of qubits are referred to by choosing a symbol, say, S.

```
In[0]:= Let[Qubit, S]
```

The Pauli X operator acting on different qubits.

```
In[0]:= S[1, 1]
         S[2, 1]
         S[3, 1]
Out[0]=
         S_1^X
Out[0]=
         S_2^X
Out[0]=
 In[o]:= S"X" // InputForm
Out[•]//InputForm=
         S[1, 1]
 In[0]:= S[1, 2, 1]
         S[2, 2, 1]
Out[0]=
         S_{1,2}^{X}
Out[0]=
         S_{2,2}^{X}
```

Various operators acting on the same qubit.

```
In[•]:= S[1, 0]
             S[1, 1]
             S[1, 2]
             S[1, 3]
             S[1, 4]
             S[1, 5]
             S[1, 6]
             S[1, 7]
             S[1, 8]
             S[1, 9]
Out[0]=
             S_1^0
Out[0]=
             S_1^X
Out[0]=
             \mathsf{S}_1^\mathsf{Y}
Out[0]=
             S_1^Z
Out[•]=
             S_1^+
Out[0]=
             \mathsf{S}_{\mathsf{1}}^{\scriptscriptstyle{-}}
Out[•]=
             \mathsf{S}_1^\mathsf{H}
Out[0]=
             S_1^S
Out[0]=
             S_1^T
Out[•]=
             \mathsf{S}_1^\mathsf{F}
```

Summary

The relation between the last flavor index and the corresponding operators.

```
In[\circ]:= Thread[Range[0, 9] \rightarrow S[1, Range[0, 9]]] // TableForm
Out[•]//TableForm=
              0\,\to\,S_1^0
              1 \to S_1^\chi
              2\,\to\,S_1^Y
              3\,\to\,S_1^Z
              4\,\rightarrow\,S_1^{\scriptscriptstyle +}
              5\,\to\,S_1^-
              6 \, \to \, S_1^H
              7\,\to\,S_1^S
              8 \, \to \, S_1^T
              9 \, \to \, S_1^F
```

Conventional notations for the Pauli-like operators acting on qubits.

```
In[o]:= Thread[S[1, Range[0, 9]] → PauliForm[S[1, Range[0, 9]]]] // TableForm
Out[•]//TableForm=
            S_1^0 \to \textbf{I}
            S_1^X \to X
            S_1^Y \to Y
            S_1^Z \to Z
            S_1^{\scriptscriptstyle +} \to X^{\scriptscriptstyle +}
            S_1^- \to X^-
            S_1^H \to H
            S_1^S \to S
            S_1^T \to T
            S_1^F \to F
```

Special flavor index \$

The qubit itself is referred to by putting the special flavor index \$ in the last slot of index.

```
In[0]:= S[1, $]
         S[2, $]
Out[•]=
         S_1
Out[0]=
         S_2
  In[•]:= S<sub>2</sub> // InputForm
Out[o]//InputForm=
         S[2, $]
 In[0]:= S[1, 2, $]
         S[2, 2, $]
Out[0]=
         S_{1,2}
Out[0]=
         S_{2,2}
```

Collective reference to several operators on the same qubit

```
In[0]:= Let[Qubit, S]
        In many cases, we need to deal with all Pauli operators on a particular qubit S[2,$].
 In[0]:= {S[2, 1], S[2, 2], S[2, 3]}
Out[0]=
        \{S_2^X, S_2^Y, S_2^Z\}
```

```
In[=]:= S[2, All]
Out[=]=
\left\{S_{2}^{X}, S_{2}^{Y}, S_{2}^{Z}\right\}
```

If you want to include the identity operator, then this is the way.

```
\label{eq:out} \begin{split} &\inf\{*\,\,J\!:=\,\,S[2,\,Full]\\ &\text{Out}\{*\,\,J\!:=\,\, \Big\{\,S_2^0\,,\,\,S_2^\chi\,,\,\,S_2^\gamma\,,\,\,S_2^\chi\,\Big\} \end{split}
```

What about this?

```
In[*]:= S[2, \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}]
Out[*]:= \{S_2^0, S_2^X, S_2^Y, S_2^Z, S_2^+, S_2^-, S_2^H, S_2^S, S_2^T, S_2^F\}
In[*]:= S[2, Range[0, 9]]
Out[*]:= \{S_2^0, S_2^X, S_2^Y, S_2^Z, S_2^+, S_2^-, S_2^H, S_2^S, S_2^T, S_2^F\}
```

Collective reference to many qubits

```
In[0]:= Let[Qubit, S]
```

Sometimes, we also need to deal with many qubits.

```
In[\circ]:= S[\{1, 2, 3, 4\}, \$]

Out[\oldsymbol{\sigma}]= \{S_1, S_2, S_3, S_4\}
```

The same Pauli X operator on many qubits?

```
In[\circ]:= S[\{1, 2, 3, 4\}, 1]
Out[\circ]=
\left\{S_1^X, S_2^X, S_3^X, S_4^X\right\}
```

Summary

Function

```
Let[Qubit,S]

S[1,$]

S[1,1], S[1,2], S[2,3], ...

S[1,All], S[1,Full], S[1,{1,2,3,4,...}]

S[{1,2,3,4,...},1]
```

■ Range

Related Links

■ Tutorial: "Quick Quantum Computing with Q3"