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# Errata: A Quantum Computation Workbook

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# Postulates of Quantum Mechanics

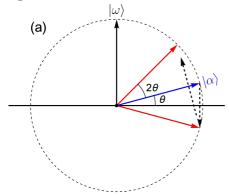
**Problem 1.10 (a), p. 30** The words "first" and "second" in the statements must be exchanged ( $p_2$  should also be replaced with  $p_1$  to be consistent with the rest subquestions). The correct statement should read as

What is the probability  $p_0$  to find the *second* qubit in  $|0\rangle$  (regardless of the *first* qubit)? Similarly, what is the probability  $p_1$  to find the *second* qubit in the state  $|1\rangle$ ?

# Quantum Algorithms

**Fig. 4.4b, p. 179** "... with respect to  $\omega$  ..."  $\rightarrow$  "... with respect to  $|v\rangle$  ..."

**Fig. 4.5a, p. 182**  $\theta, \theta/2 \rightarrow 2\theta, \theta$ , respectively. Here is the correct figure for Fig. 4.5a:



Section 4.4, p. 161, below Eq. (4.64) "... performing the transformation  $\hat{U}$  repeatedly depending on the value y on the native register."  $\rightarrow$  "... performing the transformation  $\hat{U}$  repeatedly depending on value x on the native register."

**Problem 4.1 (a)** "Classically (...), ..."  $\rightarrow$  "Show that classically (...), ...".

# Quantum Decoherence

- Section 5.1 In several places, "Zender" must be corrected to "Zehnder".
- Section 5.1, p. 191, the last line "In the blue arm, photon passes through ..."  $\rightarrow$  "In the red arm, photon passes through ...".
- Section 5.1, p. 194, below Eq. (5.6) "Whence the photon detection probabilities ..."  $\rightarrow$  "Hence the photon detection probabilities...".
- Fig. 5.4, p. 208, line 3 of the caption "... the success probability is 1/4 ..."  $\rightarrow$  "... the success probability is  $1/d^2$  for  $d = \dim \mathcal{V}$  ...".
- **Section 5.2, p. 209, line 1** "... a success probability of 1/4 ..."  $\rightarrow$  "... a success probability of  $1/d^2$  for  $d = \dim \mathcal{V}$  ...".
- Section 5.2, p. 209, line 10 from top "... a success probability of 1/4 ..."  $\rightarrow$  "... a success probability of  $1/d^2$  ...".
- Section 5.3, p. 216, line 8 "...probabilities  $\mathcal{F}_m(\hat{\rho})$ " must reads as "...probabilities  $\text{Tr}\left[\mathcal{F}_m(\hat{\rho})\right]$ ".
- Section 5.4, Eq. (5.99) It should read as

$$\hat{G} = \frac{1}{2} \sum_{\mu > 0} \hat{L}_{\mu}^{\dagger} \hat{L}_{\mu} \,.$$

Section 5.4, Eq. (5.147) It should read as

$$\frac{d\hat{\rho}}{dt} = \cdots.$$

- Section 5.5, the first sentence, p. 234 "..., who close (or different) ..."  $\rightarrow$  "..., how close (or different) ...".
- Section 5.5, p. 236, just below Eq. (5.164) "... the canonical norm associate with ..."  $\rightarrow$  "... the canonical norm associated with ...".

- Section 5.5, p. 237, just below Eq. (5.177) "... traceless Hermitian operators  $(a_0)$  ..."  $\rightarrow$  "... traceless Hermitian operators  $(a_0 = 0)$  ...".
- Section 5.5, p. 244, the first line "associate with a POVM ..."  $\rightarrow$  "associated with a POVM ...".
- Section 5.5, p. 247, below Eq. (5.209) "... of two vectors normalized vectors ..."  $\rightarrow$  "... of two normalized vectors ...".
- Section 5.5, p. 248, below Eq. (5.215) "... to note that  $\hat{\rho}$  as two eigenvalues ..."  $\rightarrow$  "... to note that  $\hat{\rho}$  has two eigenvalues ...".
- Sectoin 5.5, p. 249, Eq. (5.224) It should reads

$$\cdots \geq \left| \left( \left\langle \Psi \right| \otimes \left\langle \epsilon_0 \right| \right) \hat{U} \hat{U}^\dagger \left( \left| \Phi \right\rangle \otimes \left| \epsilon_0 \right\rangle \right) \right| = \cdots.$$

Problem 5.4, p. 252, Eq.(5.234)  $\gamma_1 \rightarrow \gamma_{\phi}$ 

# Quantum Error-Correction Codes

Section 6.3, p. 288. Eq. (6.75)

$$\hat{U}(|0\rangle \otimes |\alpha\rangle) = |0\rangle \otimes |\alpha_0\rangle + |1\rangle \otimes \hat{A} |\alpha_1\rangle = \cdots$$

must be changed to

$$\hat{U}(|0\rangle \otimes |\alpha\rangle) = |0\rangle \otimes |\alpha_0\rangle + |1\rangle \otimes \hat{A} |\alpha_0\rangle = \cdots.$$

Section 6.4, p. 298, above Eq. (6.101) "whence"  $\rightarrow$  "hence".

#### Appendix A

# Linear Algebra

- **Appendix A.1, p. 350, Definition 5.3** "... there exists a solution ..."  $\rightarrow$  "... there exists a non-trivial solution ..."
- **Appendix A.1, p. 351, above Eq. (A.5)** "Whence u is orthogonal ..."  $\rightarrow$  "Hence u is orthogonal ...".
- Appendix A.4, p. 364, above Eq. (A.55) "Whence,  $\hat{A} \geq 0$ ."  $\rightarrow$  "Hence,  $\hat{A} \geq 0$ ."

#### Appendix B

## Superoperators

Appendix B.1, p. 377, Eq. (B.6)  $\hat{S}^x \rightarrow \hat{S}^{\mu}$ .

Appendix B.2, below Exercise B.4

- "The following theorem confirms that any supermap ..." to "The following theorem confirms that any completely positive supermap ...".
- "... find a more compact ..."  $\rightarrow$  "... find more compact ...".

Appendix B.2, between Eqs. (B.30) and (B.31)

- $\{v_i\} \rightarrow \{|v_i\rangle\}$
- $|w_k\rangle \to \{|w_k\rangle\}$

Appendix B.4, p. 391, just below Eq. (B.53) "we have"  $\rightarrow$  "We have".

**Appendix B.4, p. 392, Eq. (B.56)**  $|\Psi\rangle\langle\Psi|$  should be replaced by  $|\Phi\rangle\langle\Phi|$ .

Appendix B.4, p. 393, the second last line "Whence, transposition ..."  $\rightarrow$  "Hence, transposition ...".

### Appendix F

## **Solutions**

Problem 6.7, p. 422, the display equation between (F.58) and (F.59)  $\hat{W}$  must be replaced with  $\hat{P}'''$ , i.e.,

$$\cdots (\hat{Z} \otimes \hat{W}) \cdots \rightarrow \cdots (\hat{Z} \otimes \hat{P}''') \cdots$$