













Aerofoil Optimisation

A Report Submitted To the CFD Competition as a Part of the 6th International Conference on Computational Methods in Engineering and Health Sciences (ICCMEH 2023)

by

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2 Abstract

To gain an insight into the problem parameters, a parametric sweep was conducted in Ansys Fluent. The design points to be optimised were identified using the results thus obtained. A genetic algorithm was coded and employed by coupling MATLAB and XFOIL. The optimised airfoil thus achieved was then subjected to a parametric sweep to verify the conformance to the problem parameters.















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5 List of Symbols and Abbreviations

Symbol	Description	Symbol	Description	
CFD	Computational Fluid	α	Angle of Attack	
	Dynamics			
DaFOAM	Discrete Adjoint with	MATLAB	Matrix Laboratory	
	OpenFOAM			
y/c	Thickness to Chord Ratio	ρ	Density	
a	Speed of Sound	U_{∞}	Freestream Velocity	
M	Mach Number	M_{∞}	Freestream Mach Number	
μ	Dynamic Viscosity	μ_{∞}	Freestream Dynamic	
			Viscosity	
CST	Class Shape Transformation	h	Altitude	
t	Maximum Thickness	Yair	Isentropic Expansion Factor	
m	Position of Maximum	T	Temperature	
	Thickness			
p	Chordwise Position of	P	Pressure	
	Maximum Ordinate			
M_{air}	Molecular Mass of Air	K	Number of Aerofoils to	
			be Generated in the First	
			Iteration	
AR	Aspect Ratio	C_n	n th CST Coefficient	
P_n	n th PARSEC Coefficient	N	Number of Generations	
C_L	Coefficient of Lift	C_D	Coefficient of Drag	















6 Problem Description and Introduction

6.1 Problem Statement

The main aim of the project was to meet the constraints specified by the competition guidelines. Hence efforts were undertaken to optimise the NACA 4412 aerofoil for operation at 36,000 ft in the subsonic regime (below Mach 0.8). Further, several other constraints had to be met, namely,

- * Minimum L/D of 15
- * AoA (α) between 2° and 5°
- * Minimum C_l between 0.6 and 1.2
- * Maximum thickness y/c = 15%
- * Manufacturing constraints

6.2 Introduction

A multi-faceted approach was taken to solving the given problem. A mesh validation study was conducted to verify the quality of the mesh by comparing the values found in the reference [1]. A parametric sweep was carried out in Ansys Fluent to evaluate the scope of the problem. Based on this, an optimisation using CST coefficients was conducted by integrating MATLAB with XFOIL. This was achieved using a genetic algorithm whose details are outlined in the following section. The optimised aerofoil thus achieved was subjected to a parametric sweep to validate and compile the resulting aerofoil's characteristics. The results were compiled, and a report was formulated using LATEX.

7 Methodology

7.1 Aerofoil Characteristics According to Mach Number

Initially, the optimum aerofoil characteristics were studied according to Mach number, and the following study was conducted.

Table 7.1: Aerofoil Characteristics According to Mach Number

Mach Number	Characteristics
Mach 0.1 to Mach 0.5	At low Mach numbers (subsonic), aerofoil shapes are typically characterised by gentle curvature on the upper surface and a relatively flat lower surface. The camber (curvature) of the aerofoil provides lift while minimising drag. The thickness of the aerofoil may be relatively higher to generate more lift at low
	speeds.















Mach 0.6	Similar characteristics to Mach 0.5 but slightly thinner aerofoils are more efficient.	
Mach 0.7	Transitional Mach number, aerofoils with a moderate thickness and slightly increased curvature on the upper surface work well.	
Mach 0.8	Aerofoils designed for transonic flight, like supercritical aerofoils, become more relevant in this regime.	

7.2 Approach

Several software were considered to optimise the aerofoil to meet the mission requirements. These included SU2, CB2, DaFOAM and COMSOL. These are outlined in the flow chart below. The OpenFOAM-based jacobian free discrete adjoint method (DaFOAM) was abandoned due to the fact that a shape constraint couldn't be implemented in the existing architecture of the solver. Dr Ping He, the original author of the solver, confirmed this. Similarly, CB2 and SU2 were also abandoned due to the shape constraint.

Figure 7.1: Outline of the Approach

7.3 Operating Conditions

The operating conditions for the study are as given below,

Table 7.2: Operating Conditions

Parameter	Value	Parameter	Value
h	36,000 ft	M_{air}	28.97 kg/mol
Pair	22729.31 Pa	$ ho_{air}$	$0.36 kg/m^3$
T_{air}	216.83 K	a_{∞}	295.19 m/s
μ_{∞}	$1.825 \times 10^{-5} \text{ Pa} \cdot \text{S}$	Yair	1.4















7.4 Aerofoil Generation

The NACA 4412 aerofoil was generated using the standard equations mentioned in reference [2]. The thickness distribution of the aerofoil is given by,

$$\pm y_t = \frac{t}{0.20} (0.29090\sqrt{x} - 0.12600x - 0.35160x^2 + 0.28430x^3 - 0.10150x^4)$$
 (7.1)

Further, the mean camber line was obtained using the equations,

The forward of maximum ordinate is given by,

$$y_c = \frac{m}{p^2} (2px - x^2) \tag{7.2}$$

and the aft of maximum ordinate is given by,

$$y_c = \frac{m}{(1-p)^2}(1-2p) + 2px - x^2 \tag{7.3}$$

The slope of the above equations was used to obtain θ . This was then utilised to get the x and y coordinates of the upper and lower surfaces of the aerofoil using the following equations.

The upper surface of the aerofoil is given by,

$$x_u = x - y_t \cdot \sin\theta \tag{7.4}$$

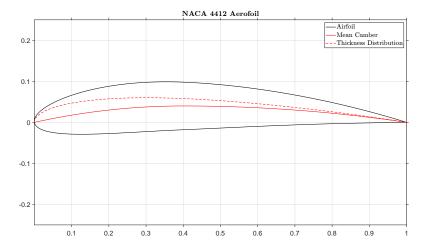
$$y_u = y_c + y_t \cdot \cos\theta \tag{7.5}$$

The lower surface of the aerofoil is given by,

$$x_l = x + y_t \cdot \sin\theta \tag{7.6}$$

$$y_l = y_c - y_t \cdot \cos\theta \tag{7.7}$$

Figure 7.2: NACA 4412 Aerofoil

















7.5 Mesh Validation Study and Parametric Sweep

A C-type mesh was created for the base aerofoil. The mesh Metrics are given below. A mesh validation study was conducted for $\alpha = 0$ and Reynolds number 5.9 x 10^6 , using the k- ω SST turbulence model. The results obtained were compared with those outlined in reference [1], and an error of less than 5% was achieved (3.1%). After which, a parametric sweep was done by varying α and u_{∞} in order to obtain a s comprehensive understanding of the problem parameters.

Figure 7.3: Generated Mesh

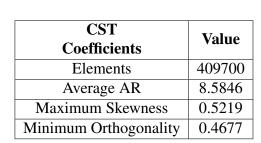
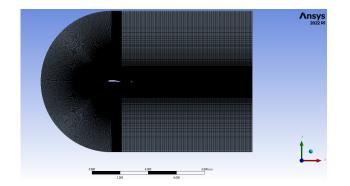


Table 7.3: Mesh Metrics



7.6 CST and PARSEC

The Class Shape Transformation (see reference [3]) and the PARSEC parametrisation techniques were utilised to optimise the aerofoil. The CST and PARSEC coefficients of the NACA 4412 aerofoil are as follows,

Figure 7.4: Class Shape Transformation

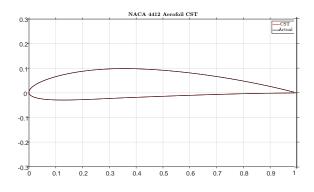


Figure 7.5: PARSEC

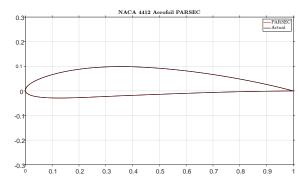
















Figure 7.6: Class Shape Transformation

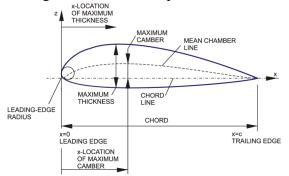


Image Source - Research Gate

Figure 7.7: PARSEC

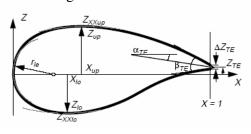


Image Source - Research Gate

Table 7.4: CST Coefficients

Table 7.5: PARSEC Coefficients

PARSEC PARSEC

Value
0.2142
0.2881
0.2395
0.2881
-0.1328
-0.0112
-0.0469
0.0018

PARSEC Coefficients	Value	PARSEC Coefficients	Value
P_1	0.0230	P_7	0.0289
P_2	0.0092	P_8	0.8868
P_3	0.3589	P_9	$-1.0116e^{-4}$
P_4	0.0986	P_{10}	$-8.9585e^{-5}$
P_5	-0.7270	P_{11}	7.9002
P_6	0.1255	P_{12}	16.7892

7.7 Genetic Algorithm

A genetic algorithm was chosen due to its efficiency in finding the global optimum solution. It was also chosen due to its ability to solve complex problems and parallel capabilities.

Initially, the CST and PARSEC coefficients were varied according to the standard limits and limits approximated based on different speed regimes (refer to section 7.1). Based on these limits, an array of aerofoils were generated. These aerofoils were arranged in decreasing order of their L/D ratios. The fittest aerofoils were chosen based on their transcendence probabilities.

Based on the crossover and the mutation probabilities, the parameters were crossed and mutated. This process was carried out for multiple generations. Finally, the fittest aerofoil was then chosen. After running the genetic algorithm using both CST and PARSEC coefficients, it was decided to finalise the CST parametrisation technique due to its efficiency.















Figure 7.8: Flowchart

Genetic Algorithm Vary CST Generate and PARSEC Aerofoil Based on Number of Generations Coefficients Calculate C_I, Cd C_I/Cd Sorting & Choosing Crossover Mutation Fittest Aerofoil

Table 7.6: Genetic Algorithm Specifications

Parameter	Value
K	30
Crossover Probability	75%
Transcendence Probability	5%
Mutation Probability	20%
Generations (N)	40

7.8 Verification

A C-type mesh was used for the verification of the optimised aerofoil. The mesh metrics are given below. A parametric analysis was carried out based on the k- ω SST turbulence model for the specified operating conditions.

Figure 7.9: Generated Mesh Using Optimised Aerofoil

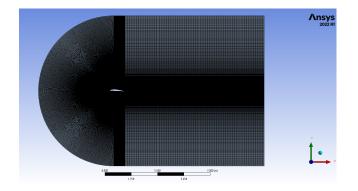


Table 7.7: Mesh Metrics

CST	Value	
Coefficients		
Elements	409700	
Average AR	8.6141	
Maximum Skewness	0.6911	
Minimum Orthogonality	0.4677	











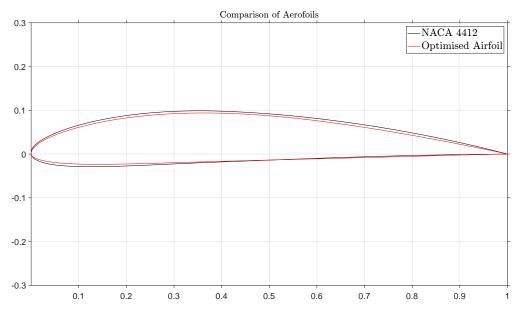




8 Results

The optimised aerofoil is plotted below,

Figure 8.1: Optimised Aerofoil



The following results were obtained after running a parametric sweep on the averaged angle of attack of 3.5° in Ansys Fluent.

Variation of C_L at $\alpha = 3.5^{\circ}$ 0.81 NACA 4412 optimised 0.8 0.79 0.78 Coefficient of Lift (C_L) 0.77 0.76 0.75 0.74 0.73 0.72 0.71 0.2 0.3 0.6 0.8

Mach Number

Figure 8.2: Coefficient of Lift C_L















Figure 8.3: Coefficient of Drag C_D

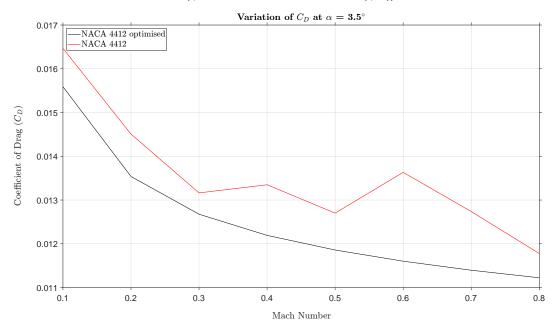


Figure 8.4: L/D Ratio

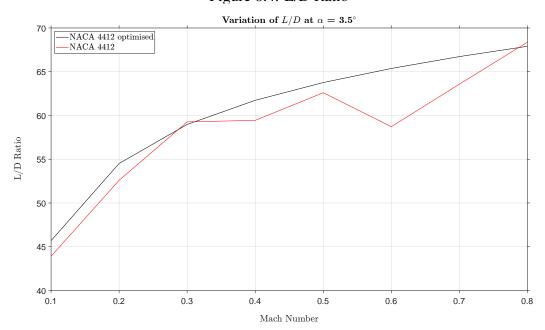










Figure 8.6: Drag



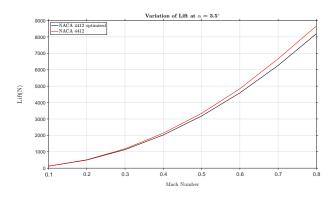


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Drag(N)



Figure 8.5: Lift



Variation of Drag at $\alpha=3.5^\circ$

9 Conclusions

The results obtained at the end of the study conform to the problem parameters, and satisfactory results have been achieved.

10 References

- [1] Albert E. Von Doenhoff and Ira Abott, "Theory of Wing Sections: Including a Summary of Airfoil Data", 1949
- [2] Brenda M. Kulfan, "A Universal Parametric Geometry Representation Method "CST" ", June 18, 2012
- [3] Pramudita Satria Palar, "Short note on CST method for Airfoil Parameterization (MATLAB Code included)", https://pramsatriapalar.wordpress.com/2013/06/15/short-note-on-cst-method-for-airfoil-parameterization-matlab-code-included/, June 15, 2013
- [4] Sean Wu, "Airfoil Optimization using Xfoil and PARSEC geometric parametrization, March 22, 2015
- [5] Johannes Achleitner, Mirko Hornung, Kai Rohde-Barandenburger "Airfoil Optimization with CST-Parametrization for (un-)conventional demands", July 2018
- [6] Wenping Song, Zhong-Hua Han, Jianhua Xu "Aerodynamic optimization design of airfoil based on CST parameterization method", October 2013