# Hanwen\_Zhang\_a2\_p1

October 6, 2022

```
[]:|import IPython
     from google.colab import files
     from IPython.display import Image
[]: uploaded = files.upload()
    <IPython.core.display.HTML object>
    Saving 00125v.jpg to 00125v (1).jpg
    Saving 00149v.jpg to 00149v (1).jpg
    Saving 00153v.jpg to 00153v (1).jpg
    Saving 00351v.jpg to 00351v (1).jpg
    Saving 00398v.jpg to 00398v (1).jpg
    Saving 01112v.jpg to 01112v (1).jpg
[]: uploaded = files.upload()
    <IPython.core.display.HTML object>
    Saving 01047u.tif to 01047u.tif
    Saving 01657u.tif to 01657u.tif
    Saving 01861a.tif to 01861a.tif
```

### 1 3 color channels alignment using FFT and gaussian sharpen filter

```
[]: import time
  from PIL import Image, ImageChops
  import numpy as np
  import math
  import matplotlib.pyplot as plt
  import cv2 as cv

def crop(img):
    # get the width and height of the img and crop it
    w, h = img.shape
    img=img[int(w*0.075):int(w-w*0.075),int(h*0.075):int(h-h*0.075)]
    return img
```

```
def sharpen(img):
  #sharpen image by using gaussian filter
  #blurred_img = gaussian_filter(img, 3)
  #filter_blurred_img = gaussian_filter(blurred_img, 1)
  \#alpha = 30
  #sharpened = blurred_img + alpha * (blurred_img - filter_blurred_img)
 kernel = np.array([[-1,-1,-1], [-1,9,-1], [-1,-1,-1]])
  sharpened = cv.filter2D(img, -1, kernel)
  return sharpened
def displacement(a, b):
  #sharpen input images by using gaussian filter
 a = sharpen(a)
 b = sharpen(b)
 height, width = a.shape
 dt = a.dtype # data type
  # FFT
 G_a = np.fft.fft2(a)
 G_b = np.fft.fft2(b)
 conj_b = np.ma.conjugate(G_b)
 R = G a*conj b
 R /= np.absolute(R)
 r = np.fft.fftshift(np.fft.ifft2(R).real)
  # Get result and Interpolation
 DY, DX = np.unravel_index(r.argmax(), r.shape)
 return round(abs(width/2 - DX)), round(abs(height/2 - DY))
  \#abs(width/2-sDX), abs(height/2-sDY)
def horizontal_shift(img, n):
  return np.roll(img, n, axis=1)
def vertical_shift(img, n):
 return np.roll(img, n, axis=0)
# aligns images using horizontal and vertical shift
def align(A, d):
 return horizontal_shift(vertical_shift(A, d[1]), d[0])
def colorize(file):
 # Count the running time
 start_time = time.time()
  # Open the image and convert it to an array
```

```
imname = file
org_img = cv.imread
img=cv.imread(imname)
img = cv.cvtColor(img, cv.COLOR_BGR2GRAY)
# Divid the height of the image array into 1/3
height = np.floor(img.shape[0] / 3.0).astype(np.int)
b = img[ : height]
g = img[height : 2 * height]
r = img[2 * height : 3 * height]
# Crop B, G, R image from the original image
blue = crop(b)
green = crop(g)
red = crop(r)
dis_green = displacement(blue, green)
dis_red = displacement(blue, red)
print("dx dy of green")
print(dis_green)
print("dx dy of red")
print(dis_red)
# Align original images relative to rescaled image displacement
new_green = align(green, [dis_green[0], dis_green[1]])
new_red = align(red, [dis_red[0], dis_red[1]])
# Convert to color image
img = (np.dstack((new_red, new_green, blue)))
if file.split('.')[1] == 'jpg':
  img = img.astype(np.uint8)
elif file.split('.')[1] == 'tif':
  img = (img).astype(np.uint8)
# Crop the image to remove the black border
img = img[int(img.shape[0]*0.05):int(img.shape[0]-img.shape[0]*0.05),int(img.shape[0]*0.05)
\Rightarrowshape[1]*0.05):int(img.shape[1]-img.shape[1]*0.05)]
colorized = Image.fromarray(img)
saveName = file.split('.')[0] + '.jpeg'
colorized.save(saveName)
plt.figure()
plt.imshow(colorized)
# Print the running time
```

```
print("Runtime: %.5s seconds" % (time.time() - start_time))
[]: file = "00125v.jpg"
     colorize(file)
     file = "00149v.jpg"
     colorize(file)
     file = "00153v.jpg"
     colorize(file)
     file = "00351v.jpg"
     colorize(file)
     file = "00398v.jpg"
     colorize(file)
     file = "01112v.jpg"
     colorize(file)
    /usr/local/lib/python3.7/dist-packages/ipykernel_launcher.py:66:
    DeprecationWarning: `np.int` is a deprecated alias for the builtin `int`. To
    silence this warning, use `int` by itself. Doing this will not modify any
    behavior and is safe. When replacing `np.int`, you may wish to use e.g.
    `np.int64` or `np.int32` to specify the precision. If you wish to review your
    current use, check the release note link for additional information.
    Deprecated in NumPy 1.20; for more details and guidance:
    https://numpy.org/devdocs/release/1.20.0-notes.html#deprecations
    dx dy of green
    (2, 5)
    dx dy of red
    (1, 10)
    Runtime: 0.087 seconds
    dx dy of green
    (2, 4)
    dx dy of red
    (2, 9)
    Runtime: 0.072 seconds
    dx dy of green
    (2, 7)
    dx dy of red
    (4, 14)
    Runtime: 0.080 seconds
    dx dy of green
    (0, 4)
    dx dy of red
    (0, 13)
    Runtime: 0.092 seconds
    dx dy of green
    (3, 5)
    dx dy of red
    (4, 11)
```

Runtime: 0.073 seconds

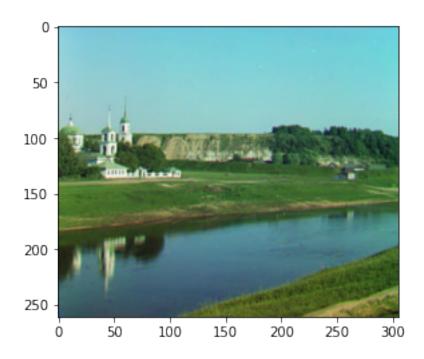
dx dy of green

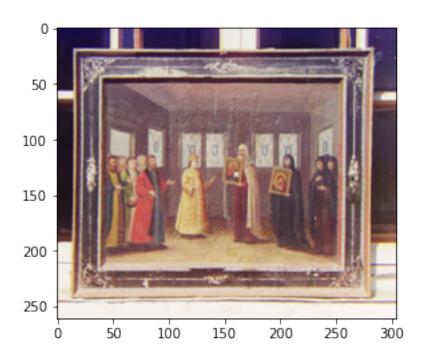
(0, 0)

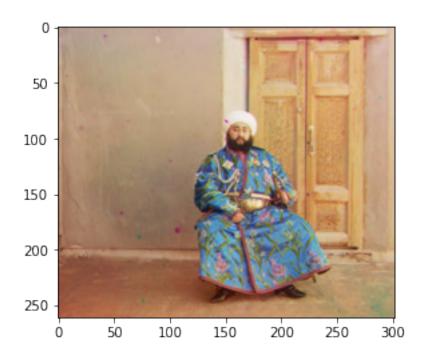
dx dy of red

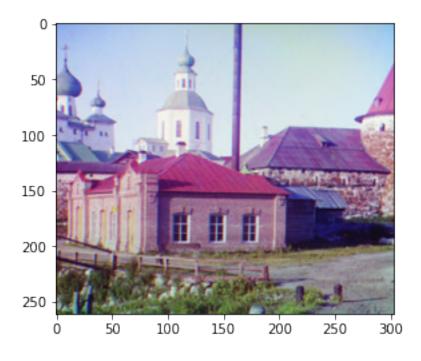
(1, 5)

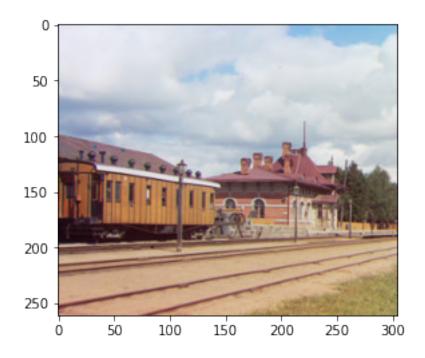
Runtime: 0.079 seconds













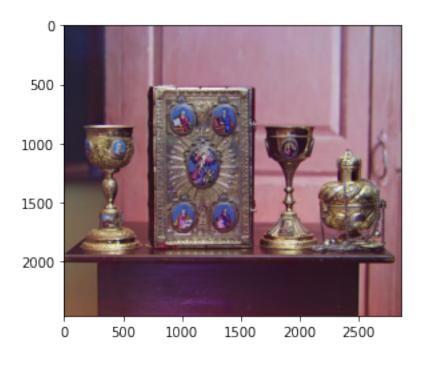
```
[]: file = "01047u.tif"
  colorize(file)
  file = "01657u.tif"
  colorize(file)
```

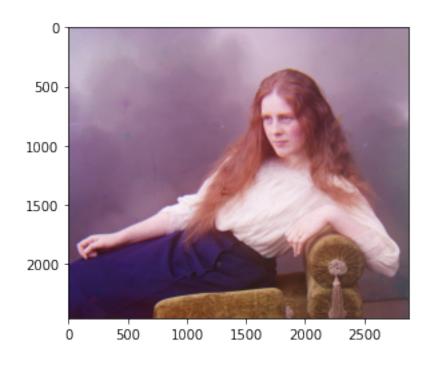
```
file = "01861a.tif"
colorize(file)
```

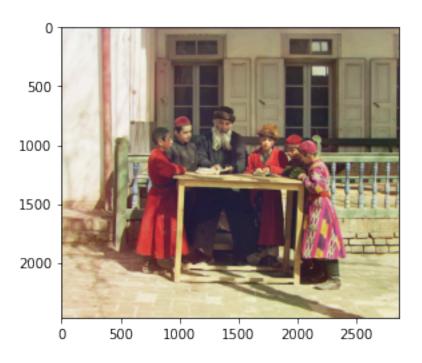
/usr/local/lib/python3.7/dist-packages/ipykernel\_launcher.py:66:
DeprecationWarning: `np.int` is a deprecated alias for the builtin `int`. To silence this warning, use `int` by itself. Doing this will not modify any behavior and is safe. When replacing `np.int`, you may wish to use e.g. `np.int64` or `np.int32` to specify the precision. If you wish to review your current use, check the release note link for additional information.
Deprecated in NumPy 1.20; for more details and guidance:
https://numpy.org/devdocs/release/1.20.0-notes.html#deprecations

dx dy of green
(19, 24)
dx dy of red
(32, 70)
Runtime: 7.925 seconds
dx dy of green
(9, 56)
dx dy of red
(13, 120)
Runtime: 6.852 seconds
dx dy of green
(39, 70)
dx dy of red
(63, 146)

Runtime: 6.711 seconds







#### 2 Plot the inverse fourier for unsharpened images

```
[]: def crop(img):
       # get the width and height of the img and crop it
      w, h = img.shape
       img=img[int(w*0.075):int(w-w*0.075),int(h*0.075):int(h-h*0.075)]
      return img
     def inverse_fourier(a, b):
      height, width = a.shape
      dt = a.dtype # data type
       # FFT
      G_a = np.fft.fft2(a)
      G_b = np.fft.fft2(b)
      conj_b = np.ma.conjugate(G_b)
      R = G_a*conj_b
      r = np.fft.fftshift(np.fft.ifft2(R).real)
     def horizontal_shift(img, n):
      return np.roll(img, n, axis=1)
     def vertical_shift(img, n):
      return np.roll(img, n, axis=0)
     # aligns images using horizontal and vertical shift
     def align(A, d):
      return horizontal_shift(vertical_shift(A, d[1]), d[0])
     def plot_unsharpen_inverse_fourier(file):
       # Open the image and convert it to an array
       imname = file
      org_img = cv.imread
       img=cv.imread(imname)
       img = cv.cvtColor(img, cv.COLOR_BGR2GRAY)
       # Divid the height of the image array into 1/3
      height = np.floor(img.shape[0] / 3.0).astype(np.int)
      b = img[ : height]
      g = img[height : 2 * height]
      r = img[2 * height : 3 * height]
       # Crop B, G, R image from the original image
      blue = crop(b)
       green = crop(g)
       red = crop(r)
```

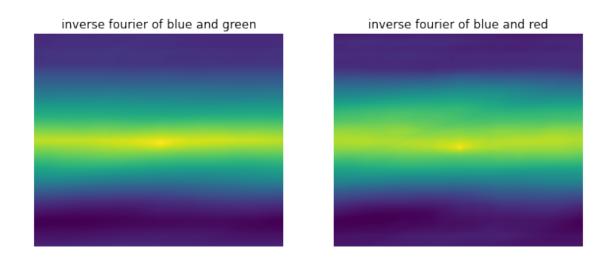
```
inver_b_g = inverse_fourier(blue, green)
inver_b_r = inverse_fourier(blue, red)

saveName = file.split('.')[0] + '_unsharpen_inver_fourier.jpeg'

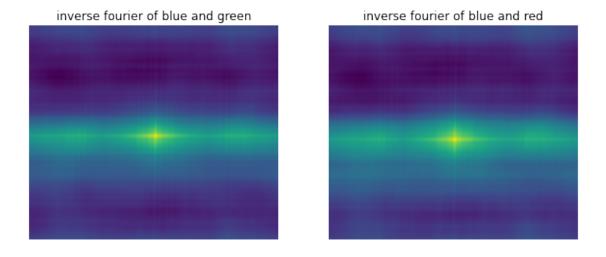
fig = plt.figure(figsize=(10, 7))
fig.add_subplot(1, 2, 1)
plt.imshow(inver_b_g)
plt.axis('off')
plt.title("inverse fourier of blue and green")
fig.add_subplot(1, 2, 2)
# showing image
plt.imshow(inver_b_r)
plt.axis('off')
plt.title("inverse fourier of blue and red")
fig.suptitle('Inverse Fourier for unsharpened images')
plt.savefig(saveName)
```

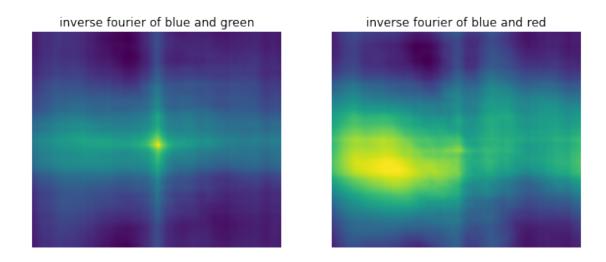
```
[]: file = "00125v.jpg"
     plot_unsharpen_inverse_fourier(file)
     file = "00149v.jpg"
     plot_unsharpen_inverse_fourier(file)
     file = "00153v.jpg"
     plot_unsharpen_inverse_fourier(file)
     file = "00351v.jpg"
     plot_unsharpen_inverse_fourier(file)
     file = "00398v.jpg"
     plot_unsharpen_inverse_fourier(file)
     file = "01112v.jpg"
     plot_unsharpen_inverse_fourier(file)
     file = "01047u.tif"
     plot unsharpen inverse fourier(file)
     file = "01657u.tif"
     plot_unsharpen_inverse_fourier(file)
     file = "01861a.tif"
     plot_unsharpen_inverse_fourier(file)
```

/usr/local/lib/python3.7/dist-packages/ipykernel\_launcher.py:36:
DeprecationWarning: `np.int` is a deprecated alias for the builtin `int`. To silence this warning, use `int` by itself. Doing this will not modify any behavior and is safe. When replacing `np.int`, you may wish to use e.g. `np.int64` or `np.int32` to specify the precision. If you wish to review your current use, check the release note link for additional information.
Deprecated in NumPy 1.20; for more details and guidance:
https://numpy.org/devdocs/release/1.20.0-notes.html#deprecations

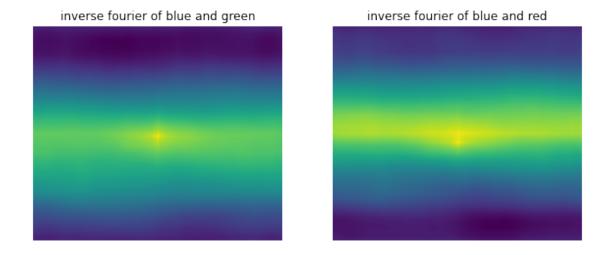


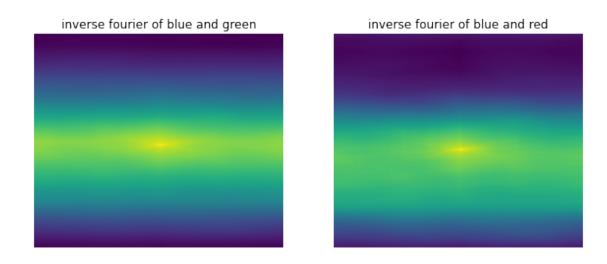
Inverse Fourier for unsharpened images



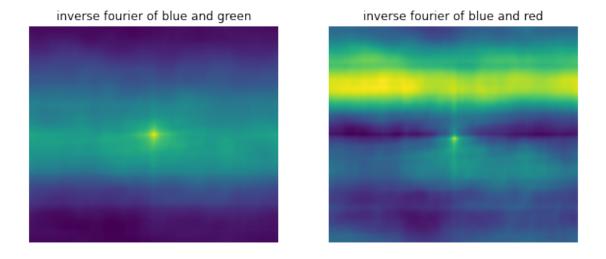


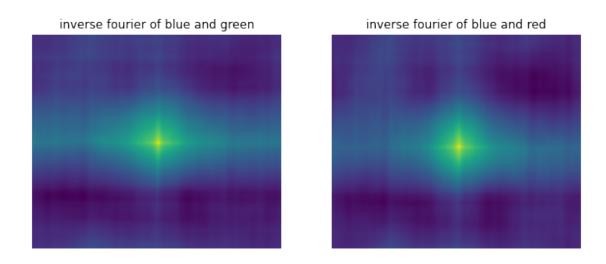
Inverse Fourier for unsharpened images



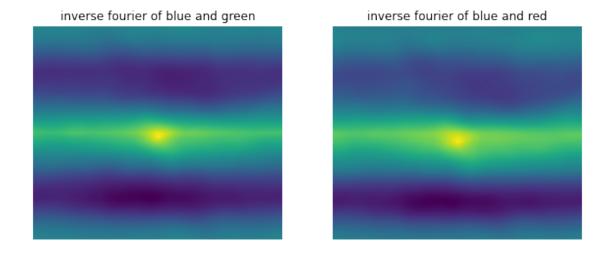


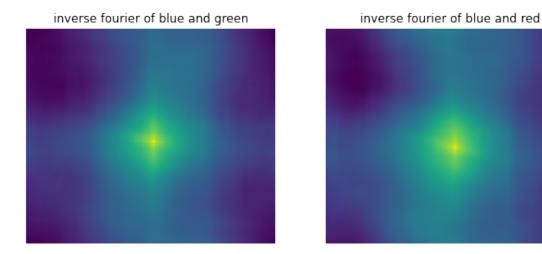
Inverse Fourier for unsharpened images





Inverse Fourier for unsharpened images





## 3 Plot the inverse Fourier for sharpened images

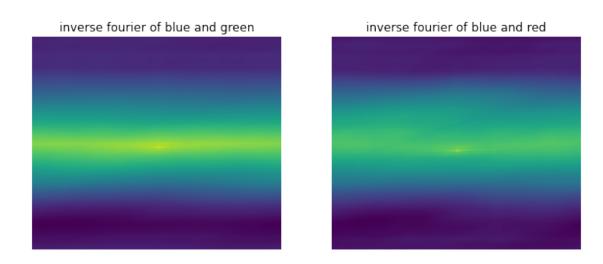
```
[]: def crop(img):
       # get the width and height of the img and crop it
      w, h = img.shape
       img=img[int(w*0.075):int(w-w*0.075),int(h*0.075):int(h-h*0.075)]
      return img
     def sharpen(img):
      #sharpen image by using gaussian filter
       #blurred_img = gaussian_filter(img, 3)
       #filter_blurred_img = gaussian_filter(blurred_img, 1)
       \#alpha = 30
       #sharpened = blurred_img + alpha * (blurred_img - filter_blurred_img)
      kernel = np.array([[-1,-1,-1], [-1,9,-1], [-1,-1,-1]])
      sharpened = cv.filter2D(img, -1, kernel)
      return sharpened
     def inverse_fourier(a, b):
       #sharpen input images by using gaussian filter
       a = sharpen(a)
       b = sharpen(b)
```

```
height, width = a.shape
  dt = a.dtype # data type
  # FFT
  G_a = np.fft.fft2(a)
 G_b = np.fft.fft2(b)
 conj_b = np.ma.conjugate(G_b)
 R = G_a*conj_b
 r = np.fft.fftshift(np.fft.ifft2(R).real)
 return r
def horizontal_shift(img, n):
 return np.roll(img, n, axis=1)
def vertical_shift(img, n):
 return np.roll(img, n, axis=0)
# aligns images using horizontal and vertical shift
def align(A, d):
 return horizontal_shift(vertical_shift(A, d[1]), d[0])
def plot_sharpened_inverse_fourier(file):
  # Open the image and convert it to an array
 imname = file
  org_img = cv.imread
  img=cv.imread(imname)
  img = cv.cvtColor(img, cv.COLOR_BGR2GRAY)
  # Divid the height of the image array into 1/3
 height = np.floor(img.shape[0] / 3.0).astype(np.int)
 b = img[ : height]
  g = img[height : 2 * height]
 r = img[2 * height : 3 * height]
  # Crop B, G, R image from the original image
 blue = crop(b)
  green = crop(g)
 red = crop(r)
  inver_b_g = inverse_fourier(blue, green)
  inver_b_r = inverse_fourier(blue, red)
  saveName = file.split('.')[0] + '_sharpened_inver_fourier.jpeg'
  fig = plt.figure(figsize=(10, 7))
  fig.add_subplot(1, 2, 1)
  plt.imshow(inver_b_g)
```

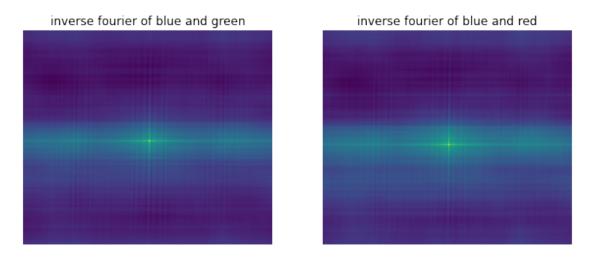
```
plt.axis('off')
plt.title("inverse fourier of blue and green")
fig.add_subplot(1, 2, 2)
# showing image
plt.imshow(inver_b_r)
plt.axis('off')
plt.title("inverse fourier of blue and red")
fig.suptitle('Inverse Fourier for sharpened images')
plt.savefig(saveName)
```

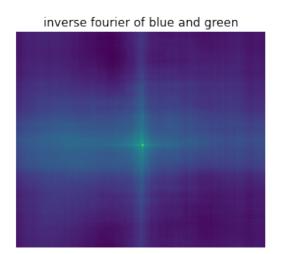
```
[]: file = "00125v.jpg"
     plot_sharpened_inverse_fourier(file)
     file = "00149v.jpg"
     plot_sharpened_inverse_fourier(file)
     file = "00153v.jpg"
     plot_sharpened_inverse_fourier(file)
     file = "00351v.jpg"
     plot_sharpened_inverse_fourier(file)
     file = "00398v.jpg"
     plot_sharpened_inverse_fourier(file)
     file = "01112v.jpg"
     plot_sharpened_inverse_fourier(file)
     file = "01047u.tif"
     plot_sharpened_inverse_fourier(file)
     file = "01657u.tif"
     plot_sharpened_inverse_fourier(file)
     file = "01861a.tif"
     plot_sharpened_inverse_fourier(file)
```

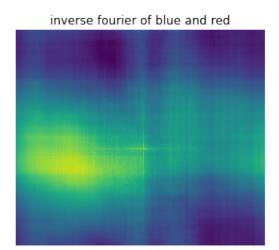
/usr/local/lib/python3.7/dist-packages/ipykernel\_launcher.py:51:
DeprecationWarning: `np.int` is a deprecated alias for the builtin `int`. To silence this warning, use `int` by itself. Doing this will not modify any behavior and is safe. When replacing `np.int`, you may wish to use e.g. `np.int64` or `np.int32` to specify the precision. If you wish to review your current use, check the release note link for additional information.
Deprecated in NumPy 1.20; for more details and guidance: https://numpy.org/devdocs/release/1.20.0-notes.html#deprecations

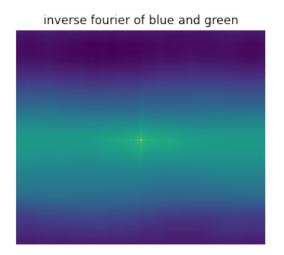


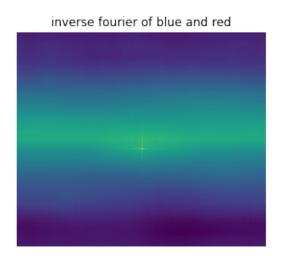
Inverse Fourier for sharpened images

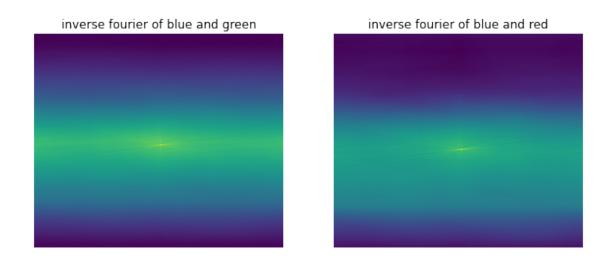




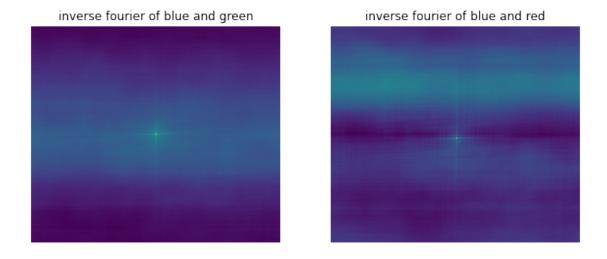


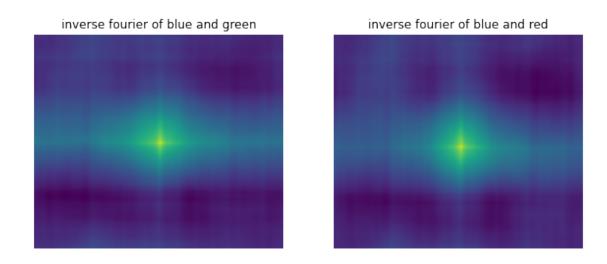






Inverse Fourier for sharpened images





Inverse Fourier for sharpened images

