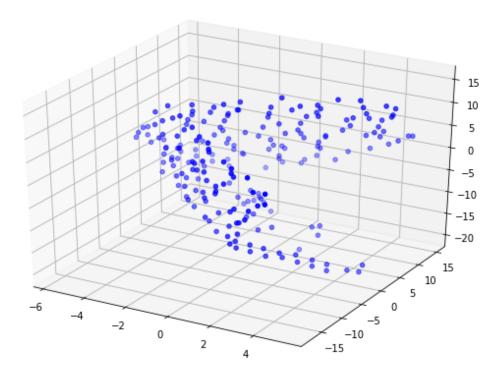
Hanwen_Zhang_a5_p1

December 8, 2022

```
[311]: import pandas as pd
       import numpy as np
       from scipy.linalg import fractional_matrix_power
       import matplotlib.pyplot as plt
       import math
       from PIL import Image
[312]: path = 'measurement_matrix.txt'
       data = np.loadtxt(path, dtype=float)
       m, n = data.shape
      norm_data = np.zeros((m, n))
[313]: from numpy.core.fromnumeric import mean
       for i in range(0, m):
        norm_data[i, :] = data[i, :] - np.mean(data[i, :])
[314]: U, S, V =np.linalg.svd(norm_data)
       U3 = U[:, 0:3]
       S_temp = np.zeros((m, n))
       for i in range(m) :
          for j in range(n) :
               if i == j : S_{temp}[i,j] = S[j]
       W3 = S_{temp}[0:3, 0:3]
       V3 = V[0:3, :]
       M = np.dot(U3, fractional_matrix_power(W3, 0.5))
       S = np.dot(fractional_matrix_power(W3, 0.5), V3)
[315]: # Creating figure
       fig = plt.figure(figsize = (10, 7))
       ax = plt.axes(projection ="3d")
       # Creating plot
       ax.scatter3D(S[2, :], S[1, :], S[0, :], color = "blue")
       # show plot
```

```
plt.show()
```



```
[316]: estimated_D = np.dot(M, S)
    per_frame_residual = np.zeros((int(m/2), 1))

[317]: def sumsqr(test_list):
    return sum(map(lambda i : i * i, test_list))

[318]: estimated_D.shape

[318]: (202, 215)

[319]: estimated_D[50:51, 1]

[319]: array([-118.40707933])

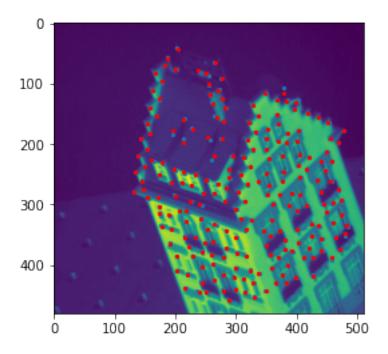
[320]: for i in range(1, int(m/2) + 1):
    for j in range(0, n):
        temp = (estimated_D[2*i-2:2*i, j-1] - norm_data[2*i-2:2*i, j-1]).tolist()
        a = sumsqr(temp)
        b = math.sqrt(a)
```

```
per_frame_residual[i-1, 0] = per_frame_residual[i-1, 0] + b
```

```
[321]: selected_frame = [1,50,100]
```

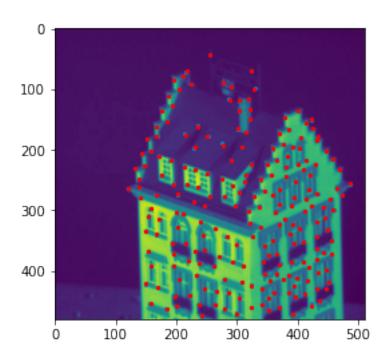
```
index = selected_frame[0]
image_name = 'frame00000' + '{0:03}'.format(index) + '.jpg'
im = plt.imread(image_name)
implot = plt.imshow(im)
plt.scatter(data[2*index-2, :], data[2*index-1, :], s = 5)
plt.scatter(x=(estimated_D[2*index-2, :] + mean(data[2*index-2, :])),
y=estimated_D[2*index-1, :] + mean(data[2*index-1,:]), c='r', s = 5)
```

[322]: <matplotlib.collections.PathCollection at 0x7f8906220580>



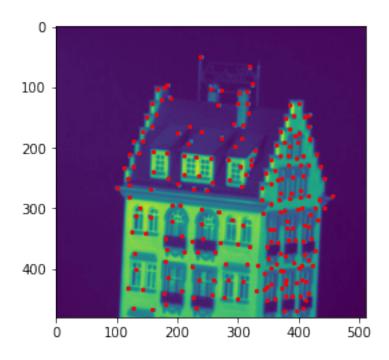
```
index = selected_frame[1]
image_name = 'frame00000' + '{0:03}'.format(index) + '.jpg'
im = plt.imread(image_name)
implot = plt.imshow(im)
plt.scatter(data[2*index-2, :], data[2*index-1, :], s = 5)
plt.scatter(x=(estimated_D[2*index-2, :] + mean(data[2*index-2, :])),
y=estimated_D[2*index-1, :] + mean(data[2*index-1,:]), c='r', s = 5)
```

[323]: <matplotlib.collections.PathCollection at 0x7f8905f87be0>



```
index = selected_frame[2]
image_name = 'frame00000' + '{0:03}'.format(index) + '.jpg'
im = plt.imread(image_name)
implot = plt.imshow(im)
plt.scatter(data[2*index-2, :], data[2*index-1, :], s = 5)
plt.scatter(x=(estimated_D[2*index-2, :] + mean(data[2*index-2, :])),
y=estimated_D[2*index-1, :] + mean(data[2*index-1,:]), c='r', s = 5)
```

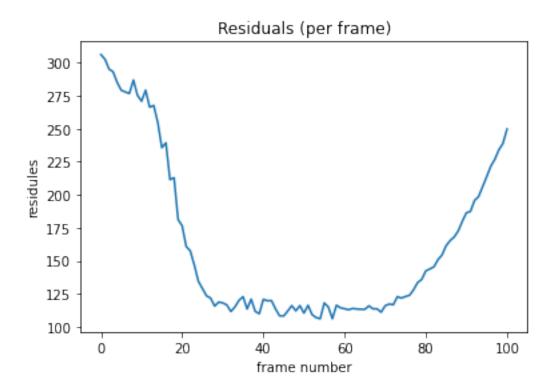
[324]: <matplotlib.collections.PathCollection at 0x7f8906249640>



```
[325]: print('Total residual: {}'.format(sum(per_frame_residual)))

Total residual: [16428.33206303]

[326]: x = per_frame_residual.shape[0]
    x_axis = [i for i in range(x)]
    y_axis = per_frame_residual.tolist()
    plt.plot(x_axis, y_axis)
    plt.title('Residuals (per frame)')
    plt.xlabel('frame number')
    plt.ylabel('residules')
    plt.show()
```



```
[327]: y_axis = per_frame_residual.tolist()
type(y_axis)
```

[327]: list