

# Diffie-Hellman Key Exchange (DH Algorithm)

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- first public-key type scheme proposed by Diffie & Hellman in 1976
- a practical method for public exchange of a secret key
- used in a number of commercial products

# Diffie-Hellman Key Exchange

- a public-key distribution scheme
  - establish a common key known only to the two participants

两个用户安全的交换一个密钥  
以便于以后的信息加密

- security depends on the difficulty of computing discrete logarithms

依赖于计算离散对数的难度

# Diffie-Hellman Key Exchange Algorithm

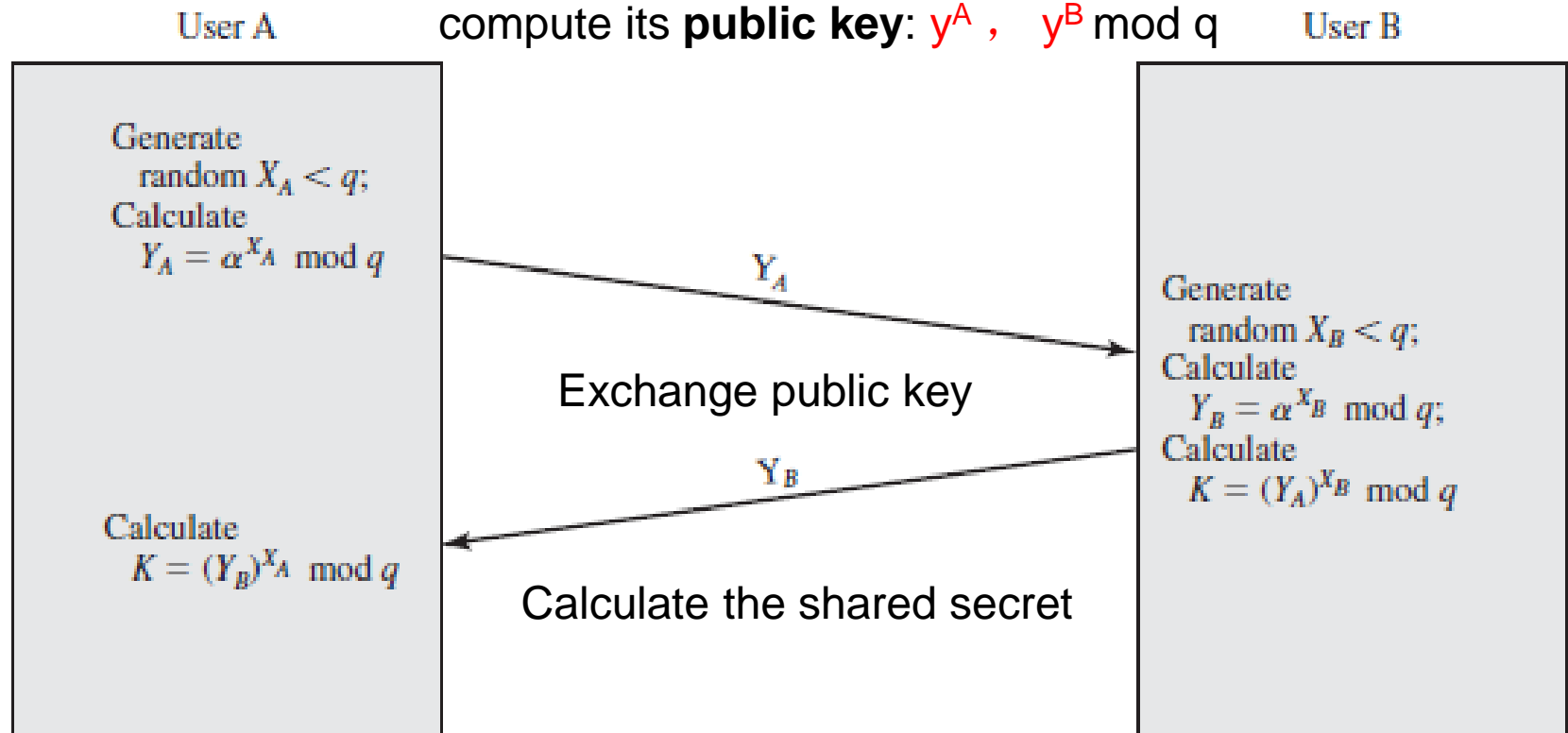
users agree on global parameters:

$q$ ,  $a$

each user generates its key

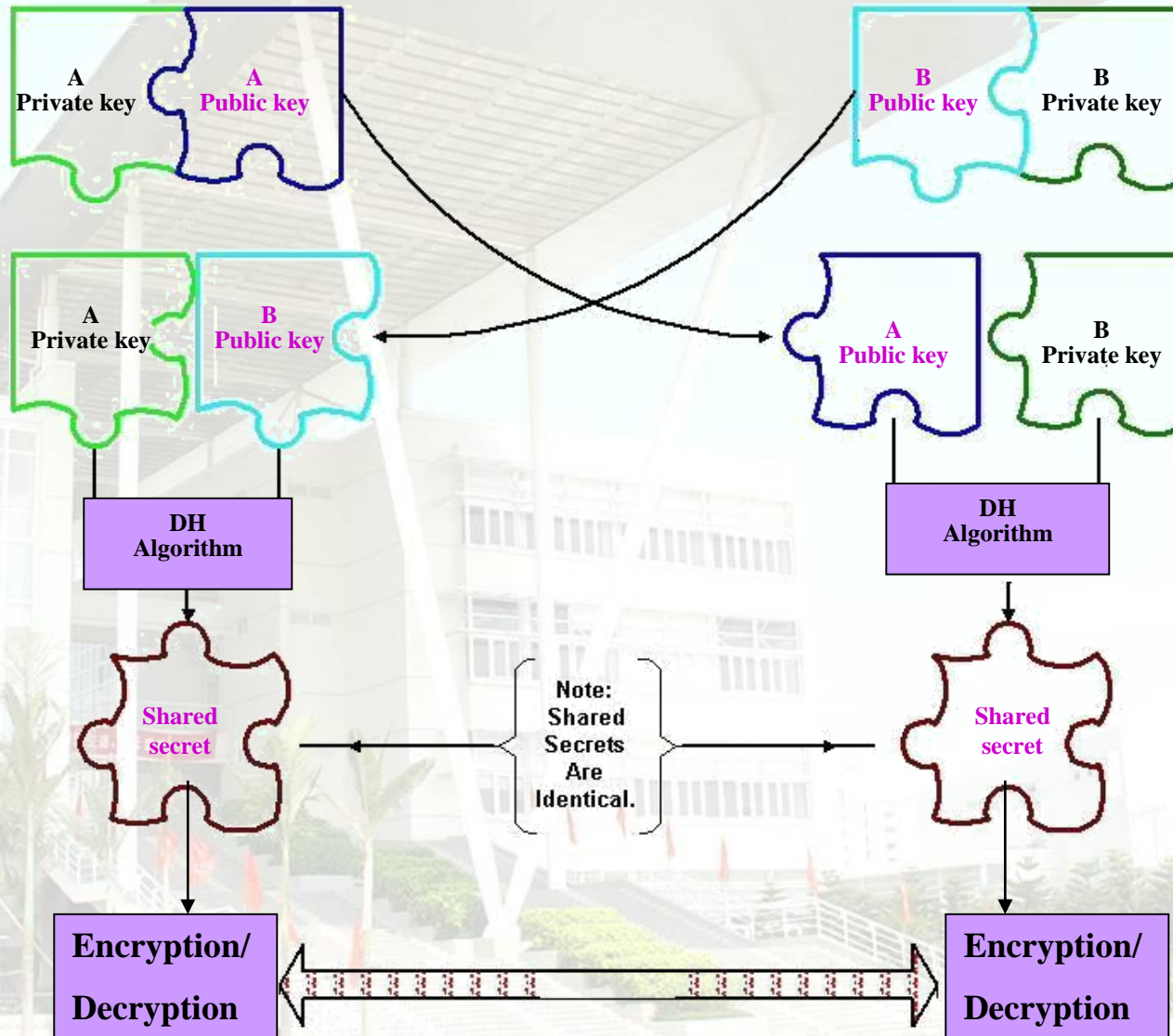
chooses a secret key :  $x^A$ ,  $x^B < q$

compute its **public key**:  $y^A$ ,  $y^B \bmod q$



# Diffie-Hellman Algorithm

Diffie-Hellman Key Exchange





# Diffie-Hellman Key Exchange

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shared secret for users A & B is K:

$$\begin{aligned} K &= y_A^{x_B} \bmod q \\ &= (a^{x_A} \bmod q)^{x_B} \bmod q \\ &= (a^{x_A})^{x_B} \bmod q \\ &= (a^{x_B})^{x_A} \bmod q \\ &= y_B^{x_A} \text{ (which A can compute)} \end{aligned}$$





Alice



Bob

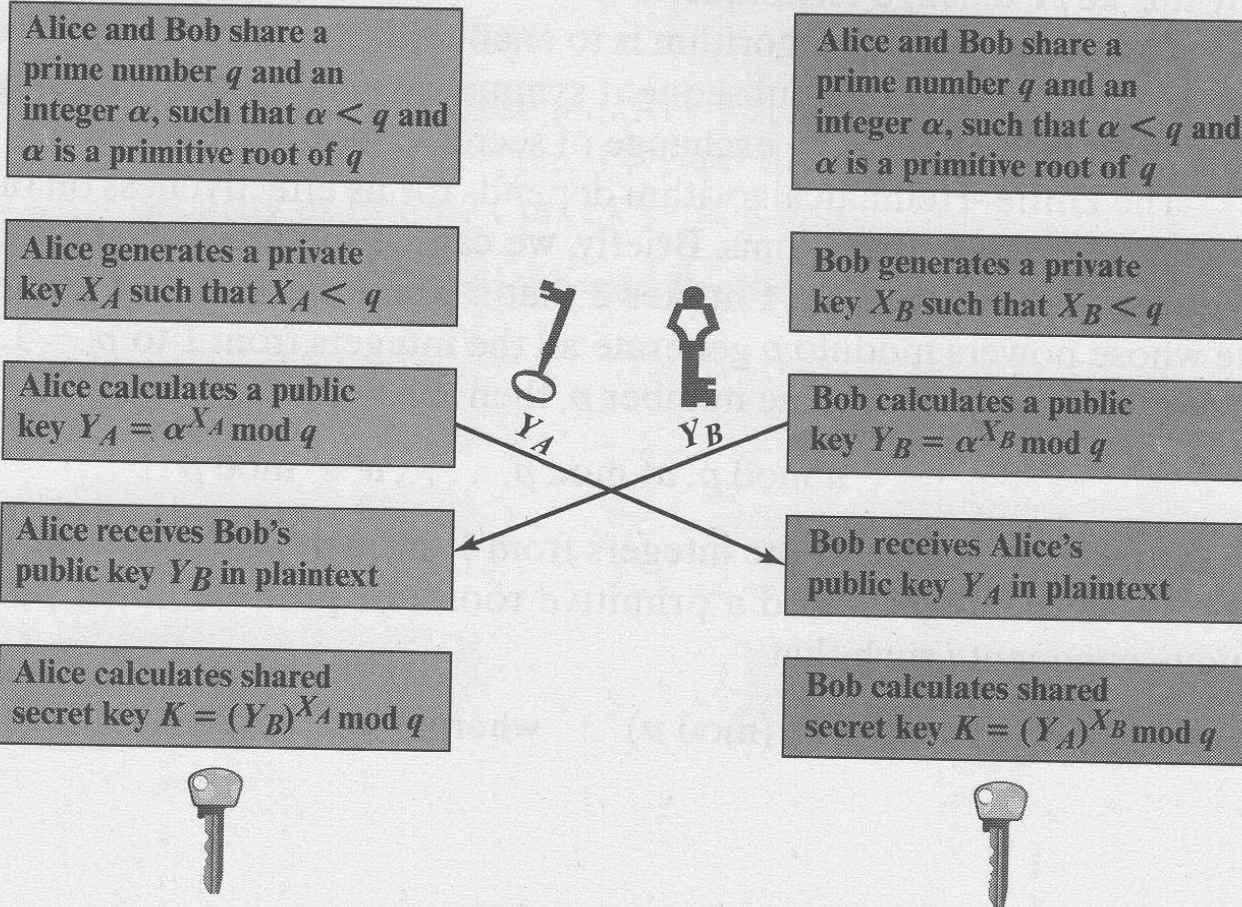


Figure 10.1 The Diffie-Hellman Key Exchange



# Diffie-Hellman Example

users A & B who wish to swap keys:

➤ agree on prime  $q=353$  and  $a=3$

✓ **select random secret keys:**

A chooses  $x_A=97$ , B chooses  $x_B=233$

➤ compute respective public keys:

$$y_A = 3^{97} \bmod 353 = 40 \quad (\text{A})$$

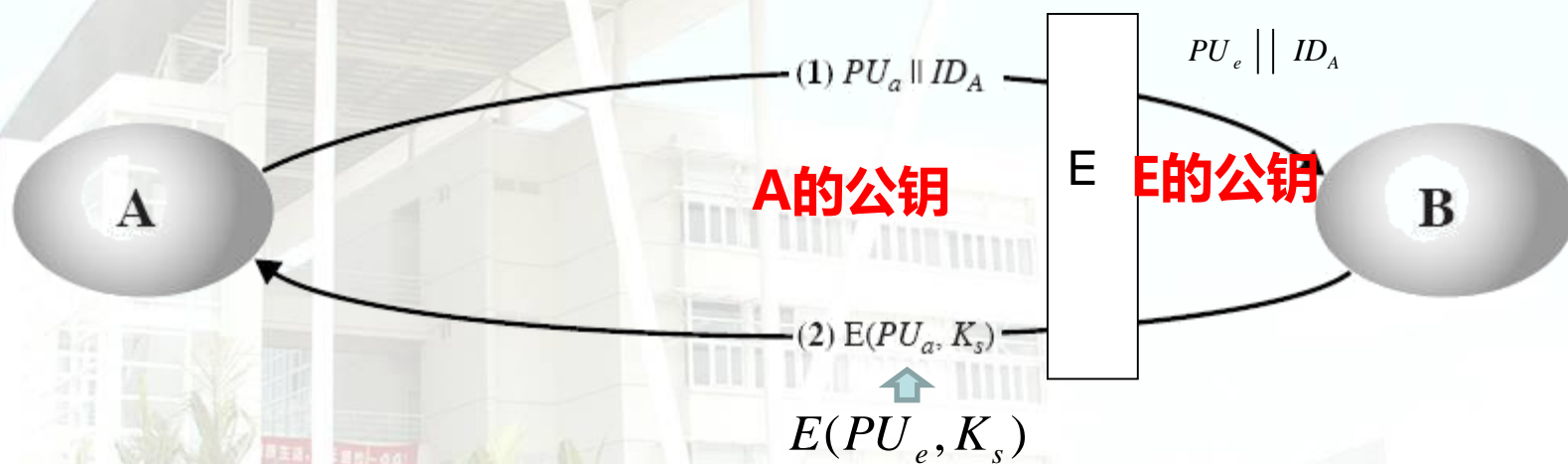
$$y_B = 3^{233} \bmod 353 = 248 \quad (\text{B})$$

➤ compute shared secret as:

$$K_{AB} = y_B^{x_A} \bmod 353 = 248^{97} = 160 \quad (\text{A})$$

$$K_{AB} = y_A^{x_B} \bmod 353 = 40^{233} = 160 \quad (\text{B})$$

# The-man-in-the-middle 中间人攻击

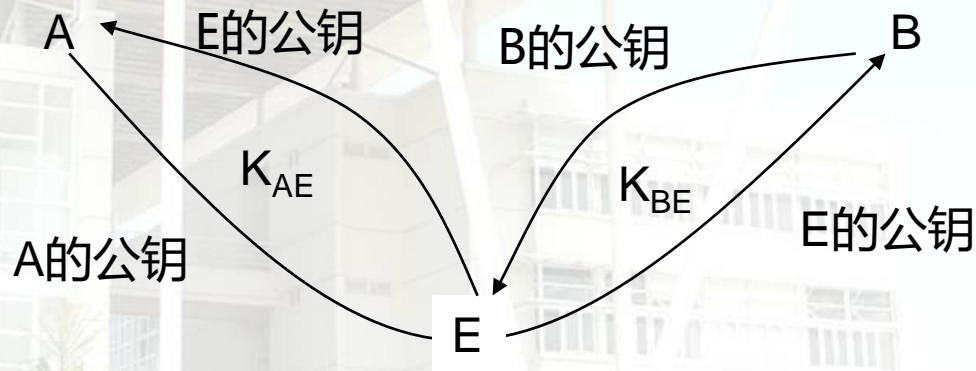


需验明正身!!!!



# Key Exchange

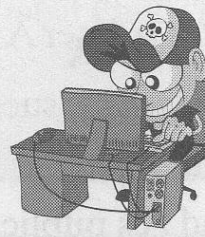
- vulnerable to The-man-in-the-middle Attack  
中间人攻击



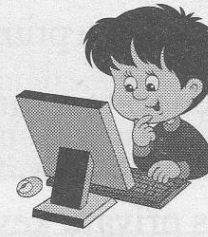
- authentication of the keys is needed  
(需验明正身!!!!)



Alice



Darth



Bob

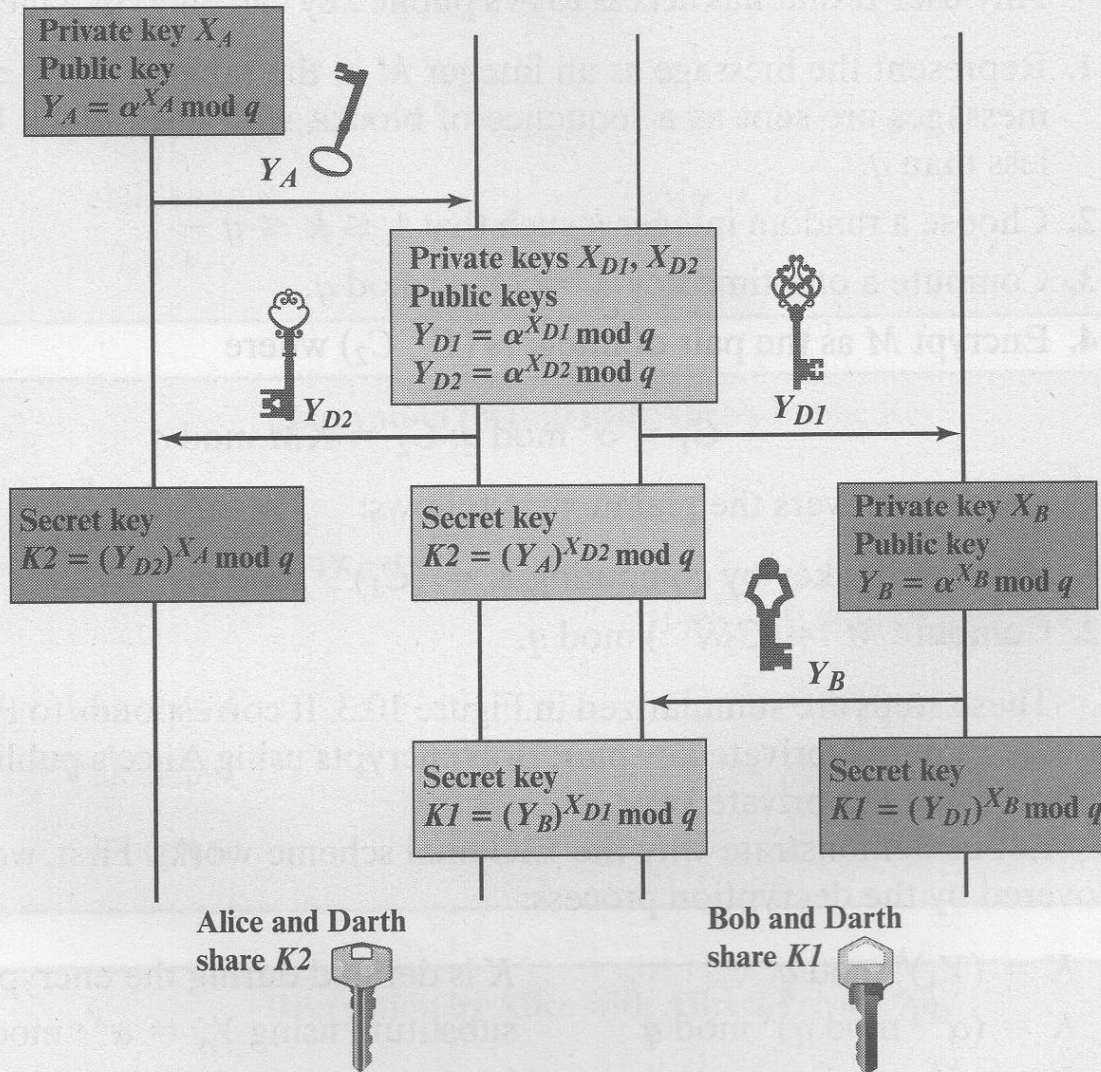


Figure 10.2 Man-in-the-Middle Attack