

Mastering Terra Mystica: Super-human Strategy in AI

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Abstract

In this paper, we explore and compare multiple algorithms for solving the complex strategy game of Terra Mystica, thereafter abbreviated as TM. Previous work in the area of super-human game-play using AI has proven effective, with recent break-throughs for generic algorithms in games such as Go, Chess, and Shogi [?]. We directly apply these breakthroughs to a novel state-representation of TM by combining multiple techniques to create an AI capable of rivaling human players. Specifically, we present initial results of applying AlphaZero to this state-representation, and analyze the strategies developed, their strengths and weakness. We call this modified algorithm with our novel state-representation AlphaTM. In the end, we discuss the success and short-comings of this method by comparing against multiple baselines and typical human scores.

In this progress report, we describe in detail the algorithms and models which we will be using to tackle our proposed problem. For reference, please refer to our previously submitted proposal, which defines and covers the scope of what we wish to achieve.

This paper focuses almost exclusively on describing in detail the methods we've implemented for attempting to achieve our results, as well as very preliminary experimental results we've achieved.

Furthermore, the paper proposes further modification which need to be made, as well as next steps and experiments to be run.

1. Background and Overview

We provide a brief discussion of our task in this section. For more detail, refer to our previously submitted proposal.

Our task involves developing the infrastructure, framework, and models required to achieve super-human level game-play in the game of Terra Mystica (TM) [?], without any of its expansions¹. TM is a fully-deterministic, turn-based, strategy board game (though an online implementation exists). The only randomness arises from pregame set-up, such as players selecting different Factions², different set of end-round bonus tiles being selected, as well as other minutia which we discussed in our proposal.

TM is typically played between 2-5 players, though we focused exclusively on the 2-player version of the game.

¹There are multiple expansions, most which consists of adding different Factions to the game or extending the TM Game Map. We hope to have the time to explore handling these expansions, but do not make this part of our goal

²A Faction essentially restricts each Player to particular areas of the map, as well as to special actions and cost functions for building

2. Deep Q-Learning Methods for Terra Mystica

Existing open-source AIs for TM are based on combination of sophisticated search techniques (such as depth-limited, alpha-beta search, domain-specific adaptations, and handcrafted evaluation functions refined by expert human players). Most of these AIs fail to play at a competitive level against human players. The space of open-source AIs is relatively small, mainly due to the newness of TM.

2.1. Alpha Zero for TM

In this section, we describe the main methods we use for training our agent. In particular, we place heavy emphasis on the methods described by AlphaGo[?], AlphaGoZero, [?], and AlphaZero [?] with pertinent modifications made for our specific problem domain.

Our main method will be a modification of the Alpha Zero [?] algorithm which was described in detail. We chose this algorithm over the methods described for Alpha Go [?] for two main reasons:

1. The Alpha Zero algorithm is a zero-knowledge reinforcement learning algorithm. This is well-suited for our purposes, given that we can perfectly simulate gameplay.
2. The Alpha Zero algorithm is a simplification over the dual-network architecture used for AlphaGo.

As such, our goal is to demonstrate and develop a slightly modified general-purpose reinforcement learning algorithm which can achieve super-human performance tabula-rasa on TM.

2.1.1 TM Specific Challenges

We first introduce some of the TM-specific challenges our algorithm must overcome.

1. Unlike the game of Go, the rules of TM are **not** translationally invariant. The rules of

TM are position-dependent – the most obvious way of seeing this is that each terrain-tile and patterns of terrains are different, making certain actions impossible from certain positions (or extremely costly). This is not particularly well-suited for the weight-sharing structure of Convolutional Neural Networks.

2. Unlike the game of Go, the rules for TM are asymmetric. We can, again, trivially see this by noting that the board game board itself **2** has little symmetry.
3. The game-board is not easily quantizable to exploit positional advantages. Unlike games where the AlphaZero algorithm has been previously applied (such as Go/Shogi/Chess), the TM map is not rectangular. In fact, each “position” has **6** neighbors, which is not easily representable in matrix form for CNNs.
4. The action space is significantly more complex and hierarchical, with multiple possible “mini”-games being played. Unlike other games where similar approaches have been applied, this action-space is extremely complex. To see this, we detail the action-spaces for other games below.
 - (a) The initial DQN approach for Atari games had an output action space of dimension 18 (though some games had only 4 possible actions, the maximum number of actions was 18 and this was represented simply as a 18-dimensional vector representing a softmax probability distribution).
 - (b) For Go, the output actions space was similar to a $19 \times 19 + 1$ probability distribution over the locations on which to place a stone.
 - (c) Even for Chess and Shogi, the action space similarly consisted of all legal destinations of all player’s pieces on

the board. While this is very expansive and more similar to what we expect for TM, TM nonetheless has additional complexity in that some actions are inherently hierarchical. You must first decide if you want to build, then decide **where** to build, and finally decide **what** to build. This involves defining an output actions-space which is significantly more complex than anything we’ve seen in the literature. For comparison, in [?] the output space consists of a stack of planes of $8 \times 8 \times 73$. Each of the 64 positions identifies a piece to be moved, with the 73 associated layers identifying exactly *how* the piece will be moved. As can be seen, this is essentially a two-level decision tree (select piece followed by selecting how to move the piece). In TM, the action-space is far more varied.

5. The next challenge is that TM is not a binary win-lose situation, as is the case in Go. Instead, we must seek to maximize our score *relative* to other players. Additionally, in TM, there is always the possibility of a tie.
6. Another challenge present in TM not present in other stated games is the fact that there exist a limited number of resources in the game. Each player has a limited number of workers/priests/coin with which a sequence of actions must be selected.
7. Furthermore, TM is now a multi-player game (not two-player). For our purposes, however, we leave exploring this problem to later research. We focus exclusively on a game between two fixed factions (Engineers and Halflings).

2.2. Input Representation

Unless otherwise specified, we leave the training and search algorithm large unmodified from

those presented in [?] and [?]. We will describe the algorithm, nonetheless, in detail in subsequent sections. For now, we focus on presenting the input representation of our game state.

2.2.1 The Game Board

We begin by noting that the TM GameBoard 2 is naturally represented as 13×9 hexagonal grid. As mentioned in the challenges section, this presents a unique problem since for each intuitive “tile”, we have 6 rather than the 4 (as in Go, Chess, and Shogi). Furthermore, unlike chess where a natural dilation of the convolution will cover additional tangent spots equally (expanding to 8), the hexagonal nature makes TM particularly interesting.

However, a particular peculiarity of TM is that we can think of each “row” of tiles as being shifted by “half” a tile, thereby becoming “neighbors”. With this approach, we chose to instead represent the TM board as a 9×26 grid, where each tile is horizontally doubled. Our terrain representation of the map then begins as a $9 \times 26 \times 8$ stack of layers. Each layer is a binary encoding of the terrain-type for each tile. The 7 main types are {PLAIN, SWAMP, LAKE, FOREST, MOUNTAIN, WASTELAND, DESERT}. It is a possible action to “terra-form” any of these tiles into any of the other available tiles, therefore why we must maintain all 7 of them as part of our configuration. The 8-th layer actually remains constant throughout the game, as this layer represents the water-ways and cannot be modified. Note that even-row (B, D, F, H) are padded at columns 0 and 25 with WATER tiles.

The next feature which we tackle is the representation of the structures which can be built on each terrain tile. As part of the rules of TM, a structure can only exist on a terrain which corresponds to its player’s terrain. As such, for each tile we only need to consider the 5 possible structures, {DWELLING, TRADING POST, SANCTUARY, TEMPLE, STRONGHOLD}. We en-

code these as an additional five-layers in our grid. Our representation is now a $9 \times 26 \times 13$ stack.

We now proceed to add a set of constant layers. First, to represent each of the 5 special-actions, we add 6-constant layers which will be either 0 or 1 signifying whether a particular action is available (0) or take (1). This gives us a $9 \times 26 \times 19$ representation.

To represent the scoring tiles (of which there are 8), we add 8×6 constant layers (either all 1 or all 0) indicating their presence in each of the 6 rounds. This gives us a $9 \times 26 \times 75$ stack.

For favor tiles, there are 12 distinct favor tiles. We add 12 layers each specifying the number of favor tiles remaining. This gives use $9 \times 26 \times 87$.

For the bonus tiles, we add 9 constant layers. These 9 layers specify which favor tiles were selected for this game (only $P + 3$ cards are ever in play). This gives us a game-board representation which is of size $9 \times 26 \times 96$

2.2.2 Player Representation and Resource Limitations

We now introduce another particularity of TM, which is the fact that **each** player has a different amount of **resources** which must be handled with care. This is something which is not treated in other games, since the resource limitation does not exist in Go, Chess, or Shogi (other than those fully encoded by the state of the board).

With that in-mind, we move to the task of encoding each player. To be fully generic, we scale this representation with the number of players playing the game, in our case, $P = 2$.

To do this, for each player, we add constant layers specifying: (1) number of workers, (2) number of priests, (3) number of coins, (4) power in bowl I, (5) power in bowl II, (6) power in bowl III, (7) the cost to terraform, (8) shipping distance, (9-12) positions in each of the 4 cult tracks, (13-17) number of building built of each type, (18) current score, (19) next round worker income, (20) next round priest income, (21) next round coin in-

come, (22) next round power income, (23) number of available bridges. This gives us a total of $23P$ additional layers required to specify information about the player resources.

Next, we consider representing the location of bridges. We add P layers, each corresponding to each player, in a fixed order. The each layer is a bit representing the existence/absence of a bridge at a particular location. This gives us $24P$ layers.

We’ve already considered the positions of the player in the cult-track. The only thing left is the tiles which the player may have. We add $9+10+5$ layers to each player. The first 9 specify which bonus card the player currently holds. The next 10 specify which favor tiles the player currently owns. And the last 5 specify how many town tiles of each type the player currently holds. This gives use an additional $24P$ layers.

We end with a complete stack of dimension $9 \times 26 \times 24P$ to represent P players.

2.2.3 Putting it All Together

Finally, we add 14 layers to specify which of the 14 possible factions the neural network should play as. This gives us an input representation of size $9 \times 26 \times (48P + 110)$. See Table 1 which places this into context. In our case, this becomes $9 \times 26 \times 206$

2.3. Action Space Representation

Terra Mystica is a complex game, where actions are significantly varied. In fact, it is not immediately obvious how to even represent all of the possible actions. We provide a brief overview here of our approach.

In general, there are 8 possible actions in TM which are, generally speaking, quite distinct. In general, we output all possible actions and assign a probability. Illegal actions are removed by setting their probabilities to zero and re-normalizing the remaining actions. Actions are considered legal as long as they can be legally performed during that turn (ie, a player can and will burn

power/workers/etc. in order to perform the required action. We could technically add additional actions for each of these possibilities, but this vastly increases the complexity.

1. Terra Form and Build: This action consists of (1) selecting a location (2) selecting a terrain to terraform to (if any) and (3) optionally selecting to build. We can represent this process as a vector of size $9 \times 13 \times (7 \times 2)$. The 9×13 is selecting a location, while the first 7 layers the probability of terraforming into one of the 7 terrains and **not** building, and the last 7 the probability of terraforming into each of the 7 terrains and building.
2. Advancing on the Shipping Track: The player may choose to advance on the shipping track. This consists of a single additional value encoding the probability of advancement.
3. : Lowering Spade Exchange Rate: The player may choose to advance on the spade track. This consists of a single additional value encoding the probability of choosing to advance on the spade track.
4. Upgrading a Structure: This action consists of (1) selecting a location, (2) selecting which structure to upgrade to. Depending on the location and existing structure, some actions may be illegal. We can represent this process as a vector of size $9 \times 13 \times 4$ specifying which location as well as the requested upgrade to the structure (DWELLING to TRADING POST, TRADING POST to STRONG HOLD, TRADING POST to TEMPLE, or TEMPLE to SANCTUARY).

Note that when a structure is built, it's possible for the opponents to trade victory points for power. While this is an interesting aspect of the game, we ignore for our purposes and assume players will never choose to take additional power.

5. Send A Priest to the Order of A Cult: In this action, the player chooses to send his or her priest to one of four possible cults. Additionally, the player must determine if he wants to send his priest to advance 3, 2 or 1 spaces – some of which maybe illegal moves. We can represent this simply as a 4×3 vector of probabilities.
6. Take a Board Power Action: There are 6 available power actions on the board. We represent this as a 6×1 vector indicating which power action the player wishes to take. Actions can only be taken once per round.
7. Take a Special Action: There are multiple possible “special” actions a player may choose to take. For example, there's a (1) spade bonus tile, (2) cult favor tile as well as special action allowed by the faction (3). As such, we output a 3×1 vector in this case for each of the above mentioned actions, many of which may be illegal.
8. Pass: The player may choose to pass. If the first to pass, the player will become the first to go next round. For this action, the player must also choose which bonus tile to take. There are 9 possible bonus tiles (some which won't be available, either because they were never in play or because the other players have taken them). As such, we represent this action by a 9×1 vector.
9. Miscellaneous: At any point during gameplay for this player, it may become the case that a town is founded. For each player round, we also output a 5×1 vector of probabilities specifying which town tile to take in the event this has occurred. These probabilities are normalized independently of the other actions, as they are not exclusive, though most of the time they will be ignored since towns are founded relatively rarely (two or three times per game).

2.3.1 Concluding Remarks for Action Space Representation

As described above, this leads to a relatively complex action-space representation. In fact, we'll end-up outputting a $9 \times 13 \times 18 + 4 \times 3 + 20 + 5$. We summarize the action-space representation in Table 2 and provide a few other methods for reference.

2.4. Deep Q-Learning with MCTS Algorithm and Modifications

In this section, we present our main algorithm and the modifications we've made so far to make it better suited for our state-space and action-space. We describe in detail the algorithm for completeness, despite the algorithm remaining mostly the same as that used in [?] and presented in detail in [?].

2.4.1 Major Modifications

The main modifications to the algorithm are mostly performed on the architecture of the neural network.

1. We extend the concept of introduced in [?] of "dual" heads to "multi-head" thereby providing us with multiple differing final processing steps.
2. We modify the output and input dimensions accordingly.

2.4.2 Overview of Approach

We make use of a deep neural network (architecture described in Section 2.4.3) $(\mathbf{p}, \mathbf{m}, v) = f_{\theta}(s)$ with parameters θ , state-representations s , as described in Section 2.2, output action-space *textbf{fp}*, as described in Section 2.3, additional action-information as \mathbf{m} as described in Section 2.3.1, and a scalar value v that estimates the expected output z from position s $v \approx \mathbb{E}[z \mid s]$. The values from this neural network are then

used to guide MCTS, and the resulting move-probabilities and game output are used to iteratively update the weights for the network.

2.4.3 Neural Network Architecture

We first describe the architecture of our neural network. The input is a $9 \times 26 \times 206$ image stack as described in Section 2.2.3. Note that unlike other games, our representation includes no temporal-information ($T = 1$), both for computational efficiency and due to the fact that the game is fully encoded with the current state.

The input features s_t are processed by a residual tower which consists of a single convolutional block followed by 19 residual blocks, as per [?]. The first convolutional block consists of 256 filters of kernel size 3×3 with stride 1, batch normalization, and a ReLU non-linearity.

Each residual block applies the following modules, in sequence, to its input. A convolution of 256 filters of kernel size 3×3 with stride 1, batch-normalization, and a ReLU non-linearity, followed by a second convolution of 256 filters of kernel size 3×3 with stride 1, and batch-normalization. The input is then added to this, a ReLU applied, and the final output taken as input for the next block. See Figure 1 for a reference.

The output of the residual tower is passed into multiple separate 'heads' for computing the policy, value, and miscellaneous information. The heads in charge of computing the policy apply the following modules, which we guess at given that the AlphaZero Paper [?] does not discuss in detail how the heads are modified to handle the final values.

For the policy, we have one head that applies a convolution of 64 filters with kernel size 2×2 with stride 2 along the horizontal direction, reducing our map to $9 \times 13 \times 64$. This convolution is followed by batch normalization, a ReLU non-linearity.

We then split this head into two further heads. We then apply an FC layer which outputs a vector

of $9 \times 13 \times 18 + 32$ which we interpret as discussed in Section 2.3, representing the mutually exclusive possible actions that a player can take.

For the second part, we apply a further convolution with 1 filter of size 1×1 , reducing our input to 9×13 . This is followed by a batch-normalization layer followed by a ReLU. We then apply a FC layer further producing a probability distribution over a 5×1 vector.

For the value head, we apply a convolution of 32 filters of kernel size 1×1 with stride 1 to the, followed by batch normalization and a ReLU unit. We follow this with an FC to 264 units, a ReLU, another FC to a scalar, and a tanh nonlinearity to output a scalar in the range $[-1, 1]$.

3. Preliminary Results

Given the complexity of the problem we're facing, the majority of the work has been spent developing the reinforcement learning pipeline with an implementation of MCTS. For reference, we present the results we've achieved with approximately 2 days of training on our local GPU. We note that the score achieved by our AI is significantly worse than that achieved from our baseline AIs. See Table 5 for overview of our results in the two factions described previously.

Preliminary analysis of the game play reveals that our AI appears to be learning little, if anything. Actions are frequently being selected in a non-sensible fashion, and it's often the case that actions with high probabilities are in fact illegal actions.

To be honest, we likely have a bug in our implementation. It will require more work to obtain good results.

4. Task Definition

Our proposal involves developing the infrastructure, framework, and models required to achieve super-human level game-play in the game of Terra Mystica (TM). The game of TM involves very-little luck, and is entirely based on

strategy (similar to Chess, Go, and other games which have recently broken to novel Reinforcement Learning such Deep Q-Learning and Monte-Carlo Tree Search as a form of Policy Improvement [?] [?]). In fact, any random component to the game comes only from the initial configuration of the map and the initial reward structure, which is selected at random during typical game-play.

TM is a game played between 2-5 players. For our research, we focus mostly on the adversarial 2-player version of the game. We do this mostly for computational efficiency, though for each algorithm we present, we discuss briefly strategies for generalizing them to multiple players.

TM is a fully-deterministic game whose complexity arises from the large branching factor and a large number of possible actions A_t from a given state, S_t . There is further complexity caused by the way in which actions can interact, discussed further in Section 4.1.

4.1. Input/Output Of System

In order to understand the inputs and outputs of our system, the game of TM must be fully understood. We lay out the important aspects of a given state below, according to the standard rules [?].

The game of TM consists of a terrain board that's split into 9×13 terrain tiles. The board is fixed, but each terrain tile can be terra-formed (changed) into any of the 7 distinct terrains (plus water, which cannot be modified). Players can only expand onto terrain which belongs to them. Furthermore, TM also has a mini-game which consists of a Cult-Board where individual players can choose to move up in each of the cult-tracks throughout game-play.

The initial state of the game consists of players selecting initial starting positions for their original dwellings.

At each timestep, the player has a certain amount of resources, consisting of Workers, Priests, Power, and Coin. The player also has an associated number of VPs.

Throughout the game, the goal of each player is to accumulate as many VPs as possible. The player with the highest number of VPs at the end of the game is the winner.

From the definition above, the main emphasis of our system is the task of taking a single state representation S_t at a particular time-step, and outputting an action to take to continue game-play for the current player. As such, the input of our system consists of the following information, fully representative of the state of the game:

1. Current terrain configuration. The terrain configuration consists of multiple pieces of information. For each terrain tile, we will receive as input:

- (a) The current color of the tile. This gives us information not only about which player currently controls the terrain, but also which terrains can be expanded into.
- (b) The current level of development for the terrain. For the state of development, we note that each terrain tile can be one of (1) UNDEVELOPED, (2) DWELLING, (3) TRADING_POST, (4) SANCTUARY, or (5) STRONGHOLD.
- (c) The current end-of-round bonus as well as future end-of-round bonus tiles.
- (d) Which special actions are currently available for use.

2. For each player, we also receive the following information.

- (a) Current level of shipping ability, Current level of spade ability, the current number of VPs that the player has.
- (b) The current number of towns the player has (as well as which town is owned), The current number of worker available to the player, the current number of

coins available to the player, the current number of LV1, LV2, and LV3 power tokens.

- (c) The current number of priests available to the player.
- (d) Which bonus tiles are currently owned by the player.
- (e) The amount of income the player currently produces. This is simply the power, coins, priests, and worker income for the player.

The above is an incomplete enumeration of the input to our algorithm, and has not yet been fully formalized. However, in general, the input to the algorithm is a complete definition of the game state at a particular turn. Note that Terra Mystica *does not* have any dependencies in previous moves, and is completely Markovian. As such, modeling the game as an MDP is fully realizable, and is simply a question of incorporating all the features of the state.

4.2. Output and Evaluation Metrics

For a given state, the output of our algorithm will consist of an action which the player can take to continue to the next state of the game. Actions in TM are quite varied, and we do not fully enumerate them here. In general, however, there are eight possible actions:

- 1. Convert and build.
- 2. Advance on the shipping ability.
- 3. Advance on the spade ability.
- 4. Upgrade a building.
- 5. Sacrifice a priest and move up on the cult track.
- 6. Claim a special action from the board.
- 7. Some other special ability (varies by class)

8. Pass and end the current turn.

We will evaluate our agents using the standard simulator. The main metric for evaluation will be the maximum score achieved by our agent in self-play when winning, as well as the maximum score achieved against a set of human competitors.

5. Infrastructure

An open-source simulator for the game of TM already exists and is written in TM [?]. We’ve currently converted this open-source simulator into Python and can run locally, simulating gameplay. For our baselines, we’ve taken the built-in AI agents as baselines (which tend to perform relatively poorly). For our oracles, we’ve instead taken the approach of analyzing a large database of game data available online.

5.1. Model and Approaches

Developing an AI agent that can play well will be extremely challenging. Even current heuristic-based agents have difficulty scoring positions. The state-action space for TM is extremely large. Games typically have trees that are ≥ 50 moves deep (per player) and which have a branching factor of > 10 .

We can approach this game as a typical min-max search-problem. Simple approaches would simply be depth-limited alpha-beta pruning similar to what we used in PacMan. These approaches can be tweaked for efficiency, and are essentially what the current AIs use.

Further improvement can be made to these approaches by attempting to improve on the *Eval* functions.

However, the main contribution of this paper will be to apply more novel approaches to a custom state-space representation of the game. In fact, we will be attempting to apply Q-Learning – specifically DQNs (as per [?], [?], and [?]).

6. Baselines

For the base-lines, we have quite a few options. Using the simulator that’s been converted into Python, we already have multiple AI agents that have been developed and can be played against. We can use these as the lowest bound for the base-lines, since even the strongest-AI agents so far struggle to complete against average TM players. We summarize the results for these agents in Table 1.

7. Oracle

For an Oracle, we have two options. Even the current state-of the art AI in TM does not come close to beating average TM players. However, there is a large collection of online games that have been played by humans [?]. From these statistics, we can derive the following-upper bounds.

7.1. Competitive Player Oracle

Our oracle will therefore consists of the scores achieved by expert players. We’ve summarized this data in Table 4, broken down by faction. We look only at the two-player scenario, as this is the one on which our algorithm focuses.

8. Appendices

<i>Domain</i>	<i>Input Dimensions</i>	<i>Total Size</i>
Atari 2600	84 x 84 x 4	28,224
Go	19 x 19 x 17	6,137
Chess	8 x 8 x 119	7,616
Shogi	9 x 9 x 362	29,322
Terra Mystica	9 x 26 x 206	48,204
ImageNet	224x224x1	50,176

Table 1. Comparison of input sizes for different domain of both games. For reference, typical CNN domain of ImageNet is also included.

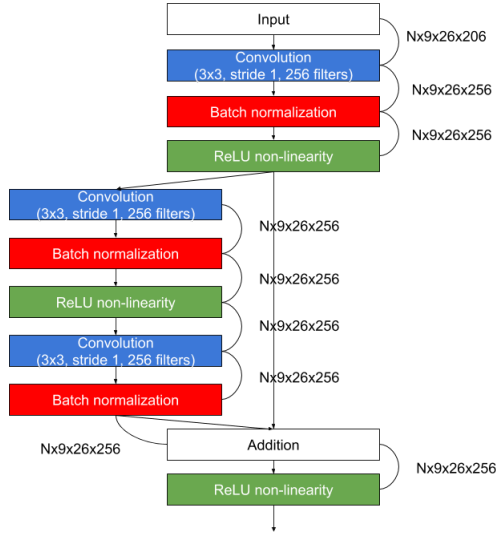


Figure 1. Architecture Diagram for shared processing of the state space features. An initial convolution block is used to standardize the number of features, which is then followed by 18 residual blocks.

Domain	Input Dimensions	Total Size
Atari 2600	18 x 1	18
Go	19 x 19 + 1	362
Chess	8 x 8 x 73	4,672
Shogi	9 x 9 x 139	11,259
Terra Mystica	9 x 13 x 18 + 4x3 + 25	2,143
ImageNet	1000x1	1000

Table 2. Comparison of action space sizes for different domain of both games. For ImageNet, we consider the class-distribution the actions-space

Average Human Score (2p)		
Faction	Average Score	Sampled Games
Halfing	133.32	2227
Engineers	127.72	1543

Table 3. Average human scores by faction for a two-player TM games online.

Simulated Self-Play Average Scores		
Faction	Average Score	Sampled Games
Halfing	92.21	1000
Engineers	77.12	1000

Table 4. Self-play easy AI agent: AI Level5 from [?]

Simulated Self-Play Average Scores		
Faction	Average Score ³	Training Iterations
Halfing	32.11	10,000
Engineers	34.12	10,000

Table 5. Our Self-Play AI after 10,000 training iterations, with average score over final 1000 games.



Figure 2. The Terra Mystica Game Board and Its Representation



Figure 3. The Terra Mystica Cult Track

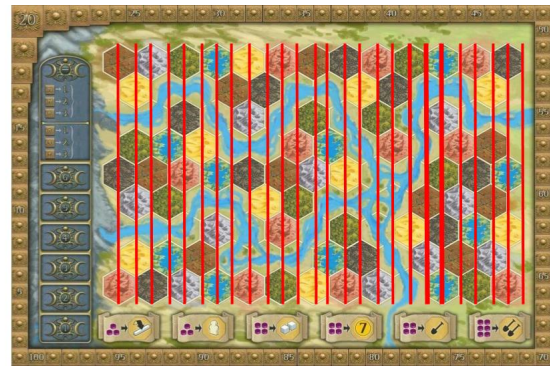


Figure 4. The Terra Mystica Board Representation