

vulture_population_matrix.R

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```
# Matrix Population Models for White-backed Vultures

# useful link http://www.mbr-pwrc.usgs.gov/workshops/uf2016/

# clean everything first
rm(list=ls())

# load required packages
library(popbio)
library(diagram)

## Loading required package: shape

# fecundity calculation, (Gauthier & Lebreton (2004) Population models for Greater Snow Geese)
bp <- 0.85 # breeding propensity
cs <- 1 # clutch size
hs <- 0.75 # hatching success
fs <- 0.6 # fledging success
fecundity <- bp * (cs/2) * hs * fs # divide by 2 to get females only

# KRUGER

fsKr <- 0.42 # first year survival
jsKr <- 0.8193305 # juvenile survival Kruger
ssKr <- 0.8885506 # subadult survival Kruger
asKr <- 1.0 # adult survival Kruger

# survival this year is multiplied by fecundity next year because in this model
# the birds have to survive the year before they become breeders i.e. from 4 years old to
# breeding age at 5 years old

# for Kruger

ssfKr <- ssKr * fecundity
asfKr <- asKr * fecundity

# create the matrix for Kruger
MKr <- c(0,0,0,0,ssfKr,asfKr,
        fsKr,0,0,0,0,0,
        0,jsKr,0,0,0,0,
        0,0,jsKr,0,0,0,
        0,0,0,ssKr,0,0,
        0,0,0,0,ssKr,asKr
)
MKr <- matrix((MKr), ncol=6, byrow = TRUE)
colnames(MKr) <- c("babies", "1yr olds", "2yr olds", "3yr olds", "4yr olds", "5yr olds")
MKr

##      babies  1yr olds  2yr olds  3yr olds  4yr olds  5yr olds
```

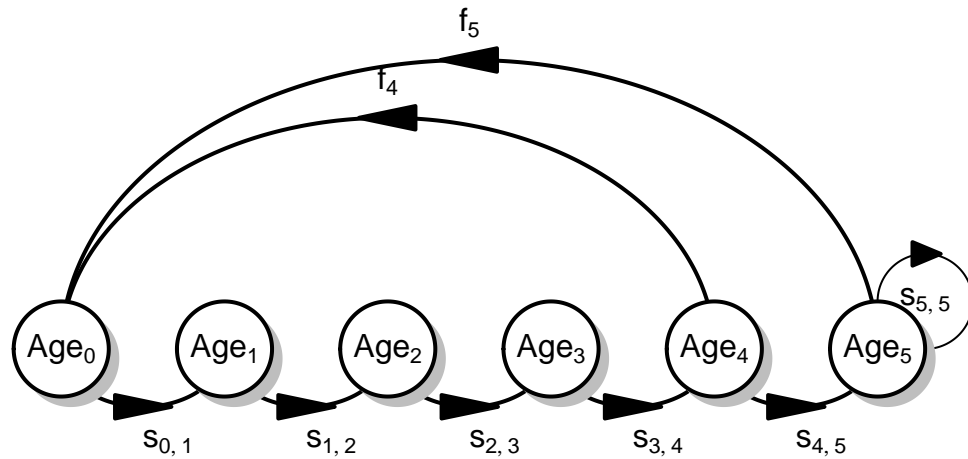
```
## [1,] 0.00 0.0000000 0.0000000 0.0000000 0.1699353 0.19125
## [2,] 0.42 0.0000000 0.0000000 0.0000000 0.0000000 0.00000
## [3,] 0.00 0.8193305 0.0000000 0.0000000 0.0000000 0.00000
## [4,] 0.00 0.0000000 0.8193305 0.0000000 0.0000000 0.00000
## [5,] 0.00 0.0000000 0.0000000 0.8885506 0.0000000 0.00000
## [6,] 0.00 0.0000000 0.0000000 0.0000000 0.8885506 1.00000

# the process looks like the diagram with the nodes representing the age classes
# Create population matrix
#
par(mfrow=c(1,1))

Numgenerations <- 6
DiffMat <- matrix(data = 0, nrow = Numgenerations, ncol = Numgenerations)
AA <- as.data.frame(DiffMat)
AA[[1,5]] <- "f[4]"
AA[[1,6]] <- "f[5]"
#
AA[[2,1]] <- "s[list(0,1)]"
AA[[3,2]] <- "s[list(1,2)]"
AA[[4,3]] <- "s[list(2,3)]"
AA[[5,4]] <- "s[list(3,4)]"
AA[[6,5]] <- "s[list(4,5)]"
AA[[6,6]] <- "s[list(5,5)]"

#
name <- c(expression(Age[0]), expression(Age[1]), expression(Age[2]),
           expression(Age[3]), expression(Age[4]), expression(Age[5]))
#
plotmat(A = AA, pos = 6, curve = 0.7, name = name, lwd = 2,
        arr.len = 0.6, arr.width = 0.25, my = -0.2,
        box.size = 0.05, arr.type = "triangle", dtext = 0.95,
        main = "Age-structured population model",
        relsize=0.97)
```

Age-structured population model



```
# Population sizes at each age from Kruger
```

```
# Murn estimates 904 pairs of breeding adults
```

```
# Assume an additional 0.3 immature and non-breeding birds per pair
```

```
# Remember, we're only modelling females
```

```
additionalPopKr <- 904 * 0.3
```

```
totalPopKr <- 904*2 + additionalPopKr # = Murn's estimate
```

```
# divide additional population among the 5 non-adult categories
```

```
# (Note: do we want some of these included among the adults as adult aged non-breeders?)
```

```
additionalPopKr / 5 / 2
```

```
## [1] 27.12
```

```
nKR<-c(27, 27, 27, 27, 27, 904)
```

```
nKR<-matrix (nKR, ncol=1)
```

```
nKR
```

```
##      [,1]
```

```
## [1,] 27
```

```
## [2,] 27
```

```
## [3,] 27
```

```
## [4,] 27
```

```
## [5,] 27
```

```
## [6,] 904
```

```
# previous function is wrapped up into pop.projection
```

```
popModelKr <- pop.projection(MKr,nKR,iterations=10)
```

```
# Calculate population growth rate and other demographic parameters from a projection matrix model
# using matrix algebra
eigen.analysis(MKr, zero=TRUE)
```

```
## $lambda1
## [1] 1.036838
##
## $stable.stage
## [1] 0.13470442 0.05456579 0.04311902 0.03407354 0.02920039 0.70433684
##
## $sensitivities
##      babies    1yr olds    2yr olds    3yr olds    4yr olds    5yr olds
## [1,] 0.00000000 0.00000000 0.00000000 0.00000000 0.006743367 0.1626554
## [2,] 0.07679472 0.00000000 0.00000000 0.00000000 0.000000000 0.00000000
## [3,] 0.00000000 0.03936602 0.00000000 0.00000000 0.000000000 0.00000000
## [4,] 0.00000000 0.00000000 0.03936602 0.00000000 0.000000000 0.00000000
## [5,] 0.00000000 0.00000000 0.00000000 0.03629932 0.000000000 0.00000000
## [6,] 0.00000000 0.00000000 0.00000000 0.00000000 0.035009652 0.8444608
##
## $elasticities
##      babies    1yr olds    2yr olds    3yr olds    4yr olds    5yr olds
## [1,] 0.00000000 0.00000000 0.00000000 0.00000000 0.001105223 0.03000262
## [2,] 0.03110785 0.00000000 0.00000000 0.00000000 0.000000000 0.00000000
## [3,] 0.00000000 0.03110785 0.00000000 0.00000000 0.000000000 0.00000000
## [4,] 0.00000000 0.00000000 0.03110785 0.00000000 0.000000000 0.00000000
## [5,] 0.00000000 0.00000000 0.00000000 0.03110785 0.000000000 0.00000000
## [6,] 0.00000000 0.00000000 0.00000000 0.00000000 0.030002624 0.81445814
##
## $repro.value
## [1] 1.000000 2.468661 3.124014 3.953344 4.613103 5.191716
##
## $damping.ratio
## [1] 2.158824
```

```
#          KZN
```

```
fsKZN <- 0.42 # first year survival
jsKZN <- 0.8601882 # juvenile survival KZN
ssKZN <- 0.5134050 # subadult survival KZN
asKZN <- 0.5672604 # adult survival KZN
```

```
# survival this year is multiplied by fecundity next year because in this model
# the birds have to survive the year before they become breeders i.e. from 4 years old to
# breeding age at 5 years old
```

```
# for KZN
```

```
ssfKZN <- ssKZN * fecundity
asfKZN <- asKZN * fecundity
```

```
# create the matrix for KZN
```

```
MKZN <- c(0,0,0,0,ssfKZN,asfKZN,
          fsKZN,0,0,0,0,0,
          0,jsKZN,0,0,0,0,
          0,0,jsKZN,0,0,0,
```

```

0,0,0,ssKZN,0,0,
0,0,0,0,ssKZN,asKZN
)
MKZN <- matrix ((MKZN), ncol=6, byrow = TRUE)
colnames(MKZN) <- c("babies", "1yr olds", "2yr olds", "3yr olds", "4yr olds", "5yr olds")
MKZN

```

```

##      babies  1yr olds  2yr olds 3yr olds  4yr olds  5yr olds
## [1,]    0.00 0.0000000 0.0000000 0.0000000 0.09818871 0.1084886
## [2,]    0.42 0.0000000 0.0000000 0.0000000 0.00000000 0.0000000
## [3,]    0.00 0.8601882 0.0000000 0.0000000 0.00000000 0.0000000
## [4,]    0.00 0.0000000 0.8601882 0.0000000 0.00000000 0.0000000
## [5,]    0.00 0.0000000 0.0000000 0.513405 0.00000000 0.0000000
## [6,]    0.00 0.0000000 0.0000000 0.0000000 0.51340500 0.5672604

```

```

# Population sizes at each age from KZN

```

```

# Rushworth estimates 319 pairs of breeding adults
# Assume an additional 0.3 immature and non-breeding birds per pair
# Remember, we're only modelling females
additionalPopKZN <- 319 * 0.3
totalPopKZN <- 319*2 + additionalPopKZN # < Rushworth's estimate
# divide additional population among the 5 non-adult categories
# (Note: do we want some of these included among the adults as adult aged non-breeders?)
additionalPopKZN / 5 / 2

```

```

## [1] 9.57

```

```

# this value is too low to reach the estimated 900 birds, instead we subtract the breeding population
# from the total pop estimate and divide the remainder up among the other 5 age categories
# Rushworth assumes there are between 800 and 900 birds in total in KZN, taking the 900 value
(900-319*2)/5/2

```

```

## [1] 26.2

```

```

nKZN<-c(26, 26, 26, 26, 26, 319)
nKZN<-matrix (nKZN, ncol=1)
nKZN

```

```

##      [,1]
## [1,]    26
## [2,]    26
## [3,]    26
## [4,]    26
## [5,]    26
## [6,]   319

```

```

# pop.projection function
popModelKZN <- pop.projection(MKZN,nKZN,iterations=10)

```

```

# Calculate population growth rate and other demographic parameters from a projection matrix model
# using matrix algebra
eigen.analysis(MKZN, zero=TRUE)

```

```

## $lambda1
## [1] 0.6532752
##

```

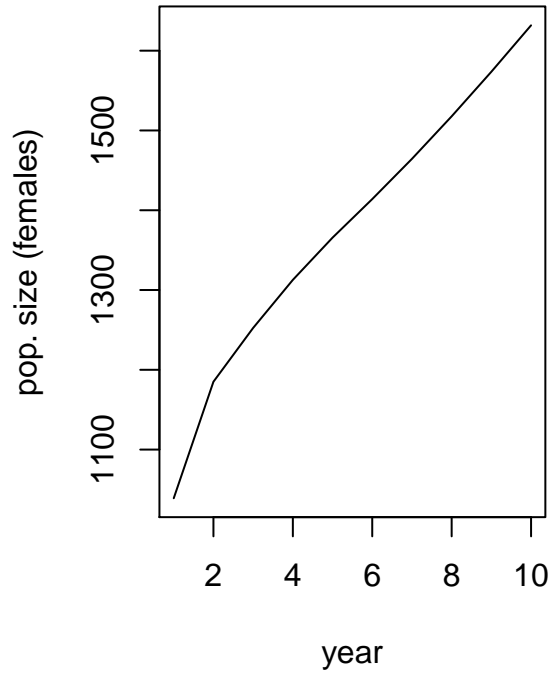
```

## $stable.stage
## [1] 0.10299820 0.06621902 0.08719269 0.11480938 0.09022800 0.53855270
##
## $sensitivities
##      babies    1yr olds    2yr olds    3yr olds    4yr olds    5yr olds
## [1,] 0.0000000 0.00000000 0.00000000 0.00000000 0.07555167 0.4509527
## [2,] 0.1341465 0.00000000 0.00000000 0.00000000 0.00000000 0.0000000
## [3,] 0.0000000 0.06549906 0.00000000 0.00000000 0.00000000 0.0000000
## [4,] 0.0000000 0.00000000 0.06549906 0.00000000 0.00000000 0.0000000
## [5,] 0.0000000 0.00000000 0.00000000 0.1097409 0.00000000 0.0000000
## [6,] 0.0000000 0.00000000 0.00000000 0.00000000 0.09529163 0.5687765
##
## $elasticities
##      babies    1yr olds    2yr olds    3yr olds    4yr olds    5yr olds
## [1,] 0.00000000 0.00000000 0.00000000 0.00000000 0.01135558 0.07488911
## [2,] 0.08624469 0.00000000 0.00000000 0.00000000 0.00000000 0.0000000
## [3,] 0.00000000 0.08624469 0.00000000 0.00000000 0.00000000 0.0000000
## [4,] 0.00000000 0.00000000 0.08624469 0.00000000 0.00000000 0.0000000
## [5,] 0.00000000 0.00000000 0.00000000 0.08624469 0.00000000 0.0000000
## [6,] 0.00000000 0.00000000 0.00000000 0.00000000 0.07488911 0.49388741
##
## $repro.value
## [1] 1.0000000 1.5554171 1.1812711 0.8971236 1.1415327 1.2612777
##
## $damping.ratio
## [1] 1.542428

# Plot the data
# create panel plot to show the population trends of both populations side by side
par(mfrow=c(1,2))
plot(popModelKr$pop.sizes, type="l", xlab = "year", ylab = "pop. size (females)", main = "Kruger")
plot(popModelKZN$pop.sizes, type="l", xlab = "year", ylab = "pop. size (females)", main = "KZN")

```

Kruger



KZN

