

# 3 Lambda expressions

# This chapter covers

- ▶ Lambdas in a nutshell
- ▶ Where and how to use lambdas
- ▶ The execute-around pattern
- ▶ Functional interfaces, type inference
- ▶ Method references
- ▶ Composing

## 3.1 Lambdas in a nutshell

- ▶ A *lambda expression*
  - ▶ a **concise** representation of an **anonymous function** that can be passed around.
- ▶ Using a lambda expression you can create a custom **Comparator** object in a more concise way.

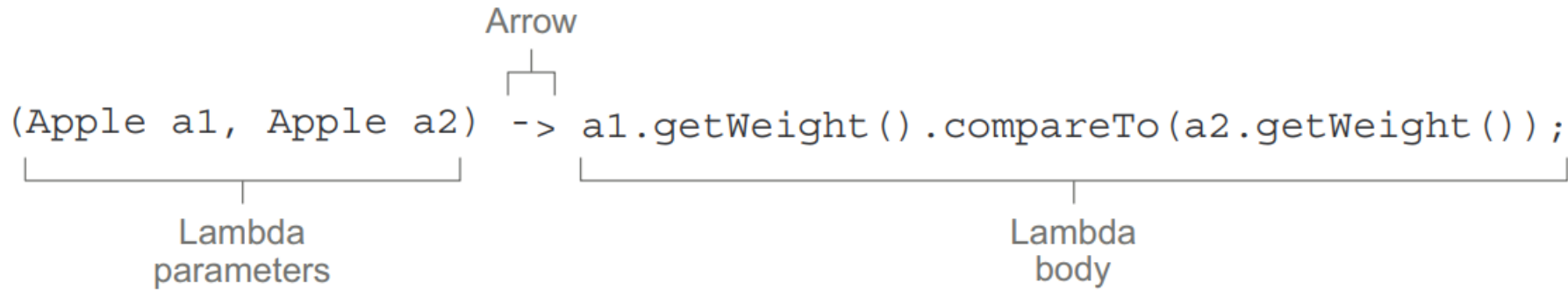
Before:

```
Comparator<Apple> byWeight = new Comparator<Apple>() {  
    public int compare(Apple a1, Apple a2) {  
        return a1.getWeight().compareTo(a2.getWeight());  
    }  
};
```

After (with lambda expressions):

```
Comparator<Apple> byWeight =  
    (Apple a1, Apple a2) -> a1.getWeight().compareTo(a2.getWeight());
```

The lambda we just showed you has three parts, as shown in figure 3.1:



**Figure 3.1** A lambda expression is composed of parameters, an arrow, and a body.

- *A list of parameters*
- *An arrow*
- *The body of the lambda*

### Listing 3.1 Valid lambda expressions in Java 8

```
(String s) -> s.length()  
(Apple a) -> a.getWeight() > 150  
(int x, int y) -> {  
    System.out.println("Result:");  
    System.out.println(x + y);  
}
```

Takes one parameter of type **String** and returns an **int**.  
It has no return statement as return is implied.

Takes one parameter of type **Apple** and returns a  
**boolean** (whether the apple is heavier than 150 g).

Takes two parameters of type **int** and returns no value  
(void return). Its body contains two statements.

```
() -> 42
```

```
(Apple a1, Apple a2) -> a1.getWeight().compareTo(a2.getWeight())
```

Takes two parameters of type **Apple** and returns an  
**int** representing the comparison of their weights

Takes no parameter  
and returns the **int** 42

**Table 3.1** Examples of lambdas

Use case	Examples of lambdas
A boolean expression	<code>(List&lt;String&gt; list) -&gt; list.isEmpty()</code>
Creating objects	<code>() -&gt; new Apple(10)</code>
Consuming from an object	<code>(Apple a) -&gt; {     System.out.println(a.getWeight()); }</code>
Select/extract from an object	<code>(String s) -&gt; s.length()</code>
Combine two values	<code>(int a, int b) -&gt; a * b</code>
Compare two objects	<code>(Apple a1, Apple a2) -&gt; a1.getWeight().compareTo(a2.getWeight())</code>

## 3.2 Where and how to use lambdas

- ▶ `List<Apple> greenApples =  
    filter(inventory, (Apple a) -> GREEN.equals(a.getColor()));`  
`Predicate<T>`
- ▶ Where exactly can you use lambdas?  
Ans: You can use a lambda expression in the context of  
`a functional interface`.



# Functional Interface

- ▶ 

```
public interface Predicate<T> {  
    boolean test (T t);  
}
```
- ▶ a functional interface
  - ▶ an interface that specifies exactly **one abstract method**.
  - ▶ Now a functional interface can have **many default methods**.
- ▶ What can you do with functional interfaces?
  - ▶ Lambda expression let you provide the implementation of the abstract method of a functional interface directly in line.
  - ▶ Treat the whole expression as **an instance of a functional interface**.

```
public interface Comparator<T> {    ← java.util.Comparator
    int compare(T o1, T o2);
}
public interface Runnable {        ← java.lang.Runnable
    void run();
}
public interface ActionListener extends EventListener { ← java.awt.event.ActionListener
    void actionPerformed(ActionEvent e);
}
public interface Callable<V> {      ← java.util.concurrent.Callable
    V call() throws Exception;
}
public interface PrivilegedAction<T> { ← java.security.PrivilegedAction
    T run();
}
```

Runnable is a functional interface defining only one abstract method, run:

```
Runnable r1 = () -> System.out.println("Hello World 1");  
Runnable r2 = new Runnable() {  
    public void run() {  
        System.out.println("Hello World 2");  
    }  
};  
public static void process(Runnable r) {  
    r.run();  
}  
process(r1);  
process(r2);  
process(() -> System.out.println("Hello World 3"));
```

← **Uses a lambda**

← **Uses an anonymous class**

← **Prints "Hello World 1"**

← **Prints "Hello World 2"**

← **Prints "Hello World 3" with a lambda passed directly**

# Function descriptor

- ▶ The signature of the abstract method of the functional interface describes the signature of the lambda expression. We call this abstract method a *functional descriptor*.
- ▶ `() -> void`  
`(Apple, Apple) -> int`
- ▶ A lambda expression can be
  - ▶ assigned to a variable
  - ▶ passed to a method expecting a functional interface as an argument

```
public void process(Runnable r) {  
    r.run();  
}  
process(() -> System.out.println("This is awesome!!"));
```

## Lambdas and void method invocation

Although this may feel weird, the following lambda expression is valid:

```
process(() -> System.out.println("This is awesome"));
```

After all, `System.out.println` returns `void` so this is clearly not an expression! Why don't we have to enclose the body with curly braces like this?

```
process(() -> { System.out.println("This is awesome"); });
```

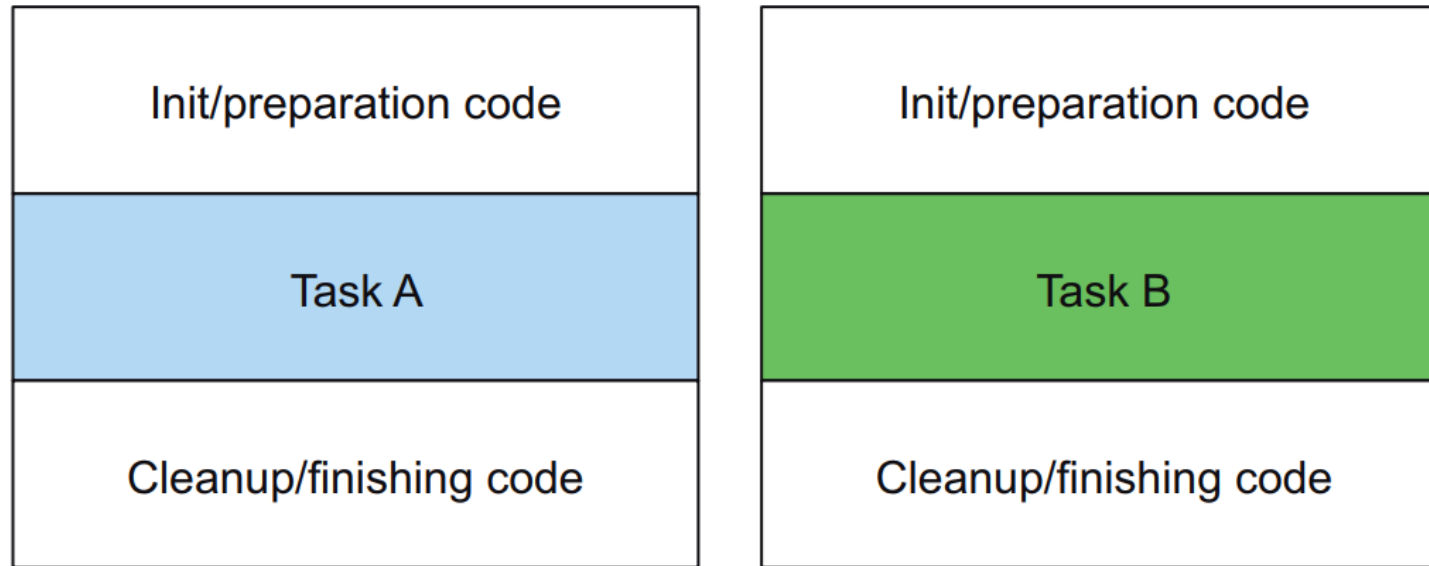
It turns out that there's a special rule for a void method invocation defined in the Java Language Specification. You don't have to enclose a single void method invocation in braces.

## 3.3 Putting Lambdas into practice: the execute-around pattern

- ▶ the *execute-around* pattern
  - ▶ **Setup** phase -> Code doing the processing -> **Cleanup** phase
- ▶ Read the next slide.
  - ▶ This code is limited to read only the first line of the file.
  - ▶ You need to parameterize the behavior of `processFile`.

```
public String processFile() throws IOException {  
    try (BufferedReader br =  
        new BufferedReader(new FileReader("data.txt"))) {  
        return br.readLine();  
    }  
}
```

← This is the line that does useful work.




**Figure 3.2** Tasks A and B are surrounded by boilerplate code responsible for preparation/cleanup.

- ▶ Step 1: Remember behavior parameterization
  - ▶ String result  
= processFile( (BufferedReader br) -> br.readLine() + br.readLine() );
- ▶ Step 2: Use functional interfaces to pass behaviors.
  - ▶ @FunctionalInterface  
public interface BufferedReaderProcessor {  
 String process(BufferedReader b) throws IOException;  
}  
public String processFile(BufferedReaderProcessor p) throws IOException {  
 ...  
}



### ► Step 3: Execute a behavior!

```
public String processFile(BufferedReaderProcessor p) throws IOException {  
    try (BufferedReader br =  
        new BufferedReader(new FileReader("data.txt"))) {  
        return p.process(br);  
    }  
}
```



**Processes the  
BufferedReader object**

### ► Step 4: Pass lambdas

The following shows processing one line:

```
String oneLine =  
    processFile((BufferedReader br) -> br.readLine());
```

The following shows processing two lines:

```
String twoLines =  
    processFile((BufferedReader br) -> br.readLine() + br.readLine());
```

<pre>public String <b>processFile</b>() throws IOException {     try (BufferedReader br =         new BufferedReader(new FileReader("data.txt"))){         return br.readLine();     } }</pre>	1
<pre>public interface <b>BufferedReaderProcessor</b> {     String process(BufferedReader b) throws IOException; }  public String processFile(<b>BufferedReaderProcessor</b> p) throws IOException {     ... }</pre>	2
<pre>public String <b>processFile</b>(<b>BufferedReaderProcessor</b> p) throws IOException {     try (BufferedReader br =         new BufferedReader(new FileReader("data.txt"))){         return p.process(br);     } }</pre>	3
<pre>String oneLine = <b>processFile</b>((BufferedReader br) -&gt;     br.readLine());  String twoLines = <b>processFile</b>((BufferedReader br) -&gt;     br.readLine + br.readLine());</pre>	4

Figure 3.3 Four-step process to apply the execute-around pattern

## 3.4 Using functional interfaces

- ▶ Comparable, Runnable, and Callable functional interfaces.
- ▶ java.util.function package
  - ▶ Predicate
    - ▶ java.util.function.Predicate<T>
  - ▶ Consumer
    - ▶ java.util.function.Consumer<T>
  - ▶ Function
    - ▶ java.util.function.Function<T, R>
  - ▶ Supplier
    - ▶ java.util.function.Supplier<T>

# Predicate

## Listing 3.2 Working with a Predicate

```
@FunctionalInterface
public interface Predicate<T> {
    boolean test(T t);
}

public <T> List<T> filter(List<T> list, Predicate<T> p) {
    List<T> results = new ArrayList<>();
    for(T t: list) {
        if(p.test(t)) {
            results.add(t);
        }
    }
    return results;
}

Predicate<String> nonEmptyStringPredicate = (String s) -> !s.isEmpty();
List<String> nonEmpty = filter(listOfStrings, nonEmptyStringPredicate);
```

# Consumer

## Listing 3.3 Working with a Consumer

```
@FunctionalInterface
public interface Consumer<T> {
    void accept(T t);
}

public <T> void forEach(List<T> list, Consumer<T> c) {
    for(T t: list) {
        c.accept(t);
    }
}

forEach(
    Arrays.asList(1,2,3,4,5),
    (Integer i) -> System.out.println(i)
);
```

**The lambda is the implementation  
of the accept method from  
Consumer.**

# Function

## Listing 3.4 Working with a Function

```
@FunctionalInterface
public interface Function<T, R> {
    R apply(T t);
}

public <T, R> List<R> map(List<T> list, Function<T, R> f) {
    List<R> result = new ArrayList<>();
    for(T t: list) {
        result.add(f.apply(t));
    }
    return result;
}

// [7, 2, 6]
List<Integer> l = map(
    Arrays.asList("lambdas", "in", "action"),
    (String s) -> s.length()
);
```

**Implements  
the apply  
method of  
Function**



- ▶ Every Java type is either a **reference type** (for example, Byte, Integer, Object, List) or a **primitive type** (for example, int, double, byte, char).
- ▶ But **generic parameters** (for example, the T in Consumer<T>) can be bound only to **reference type**.
- ▶ Boxing vs. Unboxing
- ▶ Java 8 added a specialized version of the functional interface.
  - ▶ **IntPredicate** vs **Predicate<Integer>**
  - ▶ **DoublePredicate**, **IntConsumer**, **LongBinaryOperator**, **IntFunction**
  - ▶ **ToIntFunction<T>**, **IntToDoubleFunction**, and so on.

```
public interface IntPredicate {  
    boolean test(int t);  
}
```

```
IntPredicate evenNumbers = (int i) -> i % 2 == 0;
```

```
evenNumbers.test(1000);
```

```
Predicate<Integer> oddNumbers = (Integer i) -> i % 2 != 0;
```

```
oddNumbers.test(1000);
```

True (no boxing)

False (boxing)



**Table 3.2 Common functional interfaces added in Java 8**

Functional interface	Predicate<T>	Consumer<T>
Predicate<T>	T -> boolean	IntPredicate, LongPredicate, DoublePredicate
Consumer<T>	T -> void	IntConsumer, LongConsumer, DoubleConsumer
Function<T, R>	T -> R	IntFunction<R>, IntToDoubleFunction, IntToLongFunction, LongFunction<R>, LongToDoubleFunction, LongToIntFunction, DoubleFunction<R>, DoubleToIntFunction, DoubleToLongFunction, ToIntFunction<T>, ToDoubleFunction<T>, ToLongFunction<T>

Supplier<T>	() -> T	BooleanSupplier, IntSupplier, LongSupplier, DoubleSupplier
UnaryOperator<T>	T -> T	IntUnaryOperator, LongUnaryOperator, DoubleUnaryOperator
BinaryOperator<T>	(T, T) -> T	IntBinaryOperator, LongBinaryOperator, DoubleBinaryOperator
BiPredicate<T, U>	(T, U) -> boolean	
BiConsumer<T, U>	(T, U) -> void	ObjIntConsumer<T>, ObjLongConsumer<T>, ObjDoubleConsumer<T>
BiFunction<T, U, R>	(T, U) -> R	ToIntBiFunction<T, U>, ToLongBiFunction<T, U>, ToDoubleBiFunction<T, U>

**Table 3.3 Examples of lambdas with functional interfaces**

Use case	Example of lambda	Matching functional interface
A boolean expression	<code>(List&lt;String&gt; list) -&gt; list.isEmpty()</code>	<code>Predicate&lt;List&lt;String&gt;&gt;</code>
Creating objects	<code>() -&gt; new Apple(10)</code>	<code>Supplier&lt;Apple&gt;</code>
Consuming from an object	<code>(Apple a) -&gt; System.out.println(a.getWeight())</code>	<code>Consumer&lt;Apple&gt;</code>
Select/extract from an object	<code>(String s) -&gt; s.length()</code>	<code>Function&lt;String, Integer&gt;</code> or <code>ToIntFunction&lt;String&gt;</code>
Combine two values	<code>(int a, int b) -&gt; a * b</code>	<code>IntBinaryOperator</code>
Compare two objects	<code>(Apple a1, Apple a2) -&gt; a1.getWeight().compareTo(a2.getWeight())</code>	<code>Comparator&lt;Apple&gt;</code> or <code>BiFunction&lt;Apple, Apple, Integer&gt;</code> or <code>ToIntBiFunction&lt;Apple, Apple&gt;</code>

## 3.5 Type checking, type inference, and restrictions

- ▶ The type of a lambda is deduced from **the context** in which the lambda is used.
  - ▶ **a method parameter** that it is passed to
  - ▶ **a local variable** that it is assigned to
- ▶ *target type*

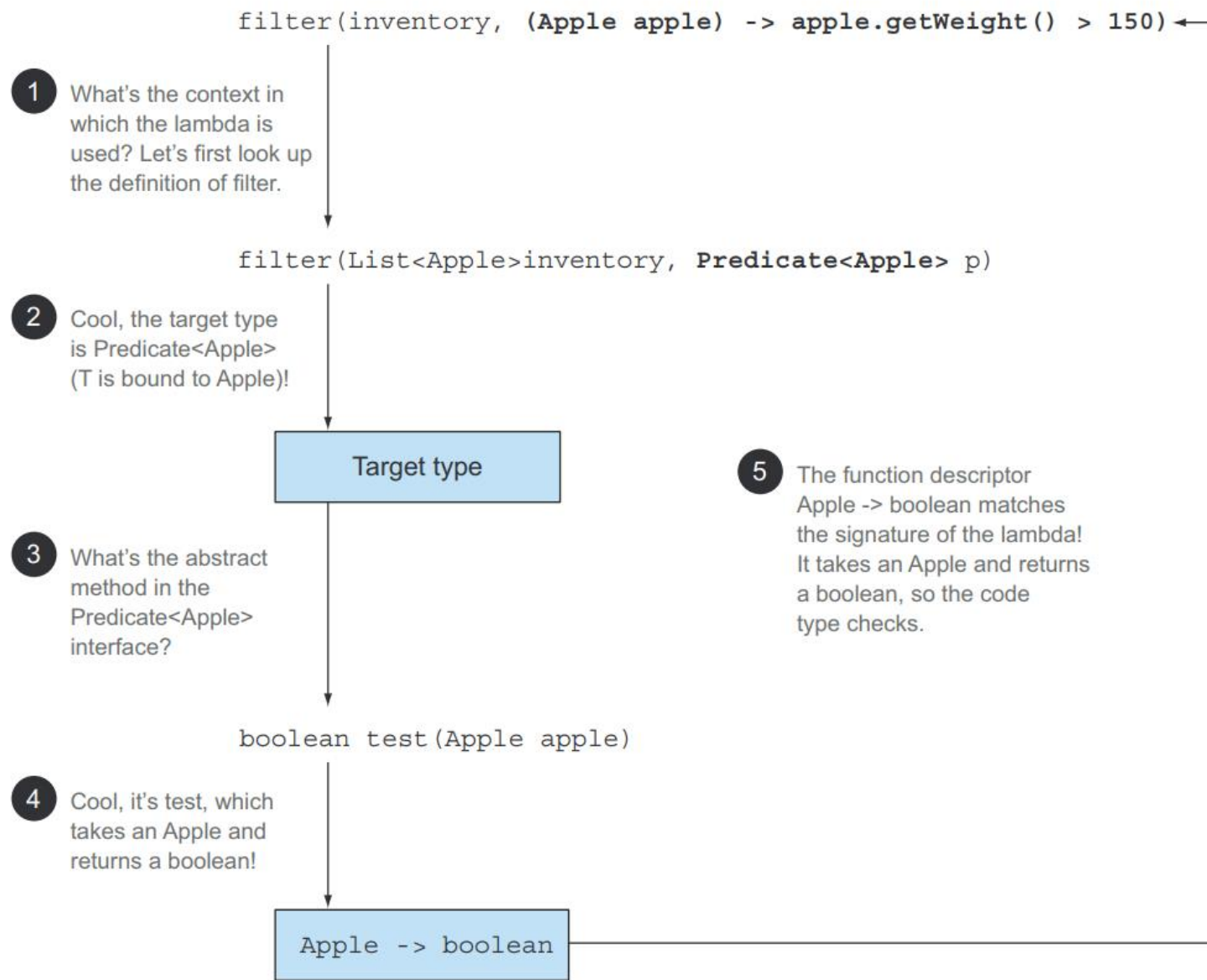


Figure 3.4 Deconstructing the type-checking process of a lambda expression

# Same lambda, different functional interface

- ▶ `Callable<Integer> c = () -> 42;`  
`PrivilegedAction<Integer> p = () -> 42;`
- ▶ `Comparator<Apple> c1 =`  
    `(Apple a1, Apple a2) -> a1.getWeight().compareTo(a2.getWeight());`  
`ToIntBiFunction<Apple, Apple> c2 =`  
    `(Apple a1, Apple a2) -> a1.getWeight().compareTo(a2.getWeight());`  
`BiFunction<Apple, Apple, Integer> c3 =`  
    `(Apple a1, Apple a2) -> a1.getWeight().compareTo(a2.getWeight());`

# Type Inference

- ▶ The Java compiler deduces what functional interface to associate with a lambda expression from **its surrounding context** (**the target type**), meaning it can also deduce **an appropriate signature** for the lambda because **the functional descriptor** is available through the target type.

```
List<Apple> greenApples =  
    filter(inventory, apple -> GREEN.equals(apple.getColor()));
```

No explicit type on  
the parameter apple

The benefits of code readability are more noticeable with lambda expressions that have several parameters. For example, here's how to create a Comparator object:

```
Comparator<Apple> c =  
    (Apple a1, Apple a2) -> a1.getWeight().compareTo(a2.getWeight());  
Comparator<Apple> c =  
    (a1, a2) -> a1.getWeight().compareTo(a2.getWeight());
```

Without type inference

With type inference

# Using Local Variables

All the lambda expressions we've shown so far used only their arguments inside their body. But **lambda expressions are also allowed to use *free variables* (variables that aren't the parameters and are defined in an outer scope) like anonymous classes can.** They're called ***capturing lambdas***. For example, the following lambda captures the variable `portNumber`:

```
int portNumber = 1337;  
Runnable r = () -> System.out.println(portNumber);
```

Nonetheless, there's a small twist. There are some restrictions on what you can do with these variables. **Lambdas are allowed to capture (to reference in their bodies) instance variables and static variables without restrictions. But when local variables are captured, they have to be explicitly declared `final` or be effectively `final`.** Lambda expressions can capture local variables that are assigned to only once. (Note: capturing an instance variable can be seen as capturing the final local variable `this`.) For



```
int portNumber = 1337;  
Runnable r = () -> System.out.println(portNumber);  
portNumber = 31337;
```



**Error: local variable  
portNumber is not final  
or effectively final.**

## 3.6 Method references

- ▶ **Method references** can be seen as **shorthand for lambdas** calling only a specific method.
- ▶ Indeed, a method reference lets you create a lambda expression from an existing method implementation.
- ▶ You can think of method reference as **syntactic sugar** for lambdas that refer only to a single method.

Before:

```
inventory.sort((Apple a1, Apple a2)
a1.getWeight().compareTo(a2.getWeight()));
```

After (using a method reference and `java.util.Comparator.comparing`):

```
inventory.sort(comparing(Apple::getWeight));
```

← **Your first method  
reference**

**Table 3.4** Examples of lambdas and method reference equivalents

Lambda	Method reference equivalent
<code>(Apple apple) -&gt; apple.getWeight()</code>	<code>Apple::getWeight</code>
<code>() -&gt; Thread.currentThread().dumpStack()</code>	<code>Thread.currentThread()::dumpStack</code>
<code>(str, i) -&gt; str.substring(i)</code>	<code>String::substring</code>
<code>(String s) -&gt; System.out.println(s)</code>	<code>System.out::println</code>
<code>(String s) -&gt; this.isValidName(s)</code>	<code>this::isValidName</code>

# Recipe for Constructing Method References

There are three main kinds of method references:

- 1 A method reference to a *static method* (for example, the method `parseInt` of `Integer`, written `Integer::parseInt`)
- 2 A method reference to an instance method of an arbitrary type (for example, the method `length` of a `String`, written `String::length`)
- 3 A method reference to an *instance method of an existing object or expression* (for example, suppose you have a local variable `expensiveTransaction` that holds an object of type `Transaction`, which supports an instance method `getValue`; you can write `expensiveTransaction::getValue`)

- For example, say you defined a helper method `isValidName`:

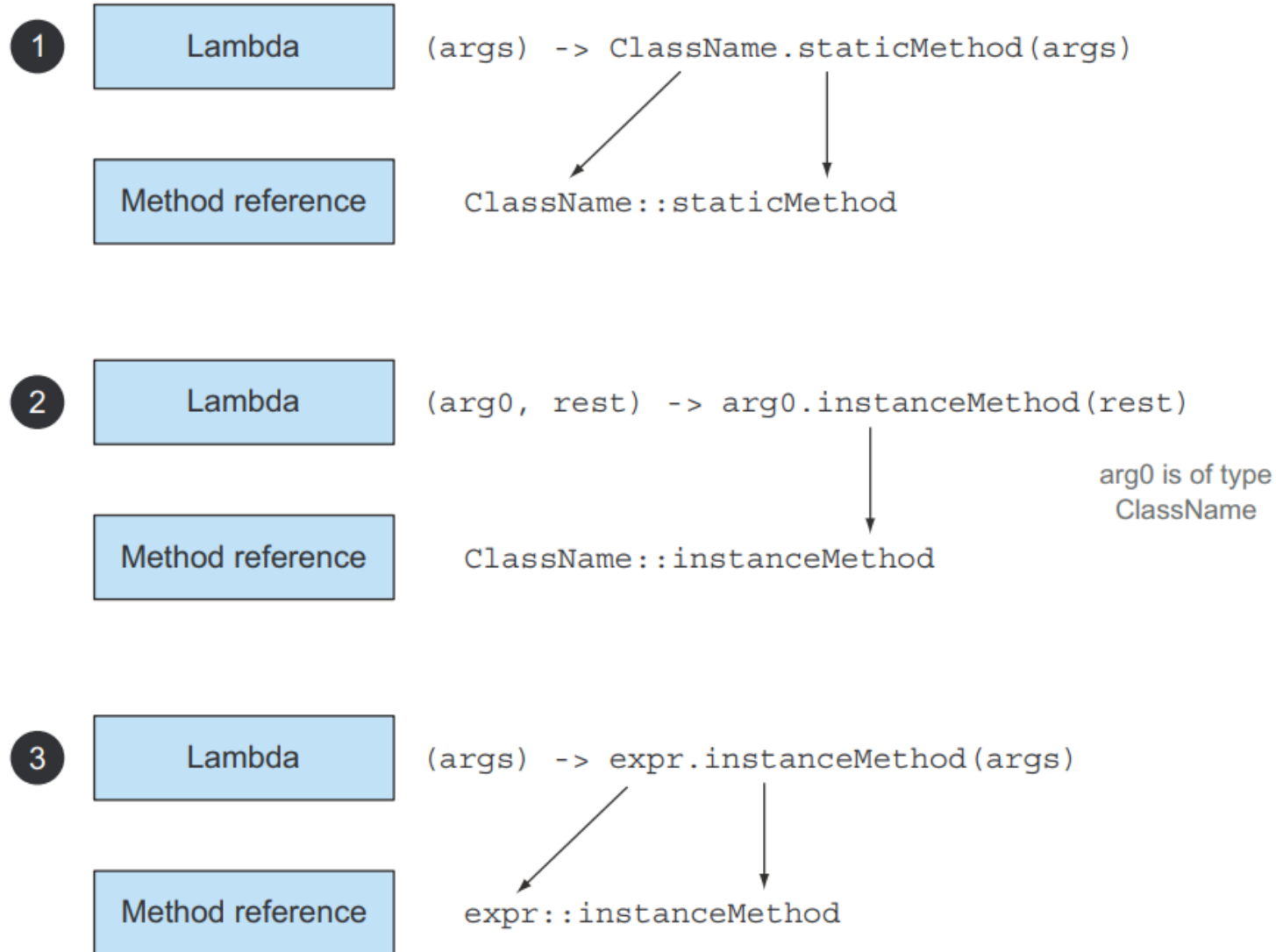
```
private boolean isValidName(String string) {  
    return Character.isUpperCase(string.charAt(0));  
}
```

You can now pass this method around in the context of a `Predicate<String>` using a method reference:

```
filter(words, this::isValidName)
```

- ```
List<String> str = Arrays.asList("a", "b", "A", "B");  
str.sort((s1, s2) -> s1.compareToIgnoreCase(s2));
```

```
List<String> str = Arrays.asList("a", "b", "A", "B");  
str.sort(String::compareToIgnoreCase);
```



**Figure 3.5** Recipes for constructing method references for three different types of lambda expressions

# Constructor References

- You can create a reference to an existing constructor using its name and the keyword new as follows: `ClassName::new`.

For example, suppose there's a zero-argument constructor. This fits the signature `() -> Apple` of `Supplier`; you can do the following:

```
Supplier<Apple> c1 = Apple::new;  
Apple a1 = c1.get();
```

Constructor reference to the default `Apple()` constructor

Calling `Supplier`'s `get` method produces a new `Apple`.

which is equivalent to

```
Supplier<Apple> c1 = () -> new Apple();  
Apple a1 = c1.get();
```

Lambda expression to create an `Apple` using the default constructor

Calling `Supplier`'s `get` method produces a new `Apple`.

- If you have a constructor with signature `Apple(Integer weight)`, it fits the signature of the Function interface, so you can do this

```
Function<Integer, Apple> c2 = Apple::new;  
Apple a2 = c2.apply(110);
```

Calling Function's apply method with a given weight produces an Apple.

Constructor reference to Apple (Integer weight)

which is equivalent to

```
Function<Integer, Apple> c2 = (weight) -> new Apple(weight);  
Apple a2 = c2.apply(110);
```

Lambda expression to create an Apple with a given weight

Calling Function's apply method with a given weight produces a new Apple object.



In the following code, each element of a `List` of `Integer`s is passed to the constructor of `Apple` using a similar `map` method we defined earlier, resulting in a `List` of apples with various weights:

```
List<Integer> weights = Arrays.asList(7, 3, 4, 10);
List<Apple> apples = map(weights, Apple::new);
public List<Apple> map(List<Integer> list, Function<Integer, Apple> f) {
    List<Apple> result = new ArrayList<>();
    for(Integer i: list) {
        result.add(f.apply(i));
    }
    return result;
}
```

**Passing a constructor  
reference to the map method**

- If you have a two-argument constructor, `Apple (Color color, Integer weight)`, it fits the signature of the **BiFunction** interface, so you can do this:

```
BiFunction<Color, Integer, Apple> c3 = Apple::new;  
Apple a3 = c3.apply(GREEN, 110);
```

Constructor reference to `Apple (Color color, Integer weight)`

BiFunction's `apply` method with a given color and weight produces a new `Apple` object.

which is equivalent to

```
BiFunction<String, Integer, Apple> c3 =  
    (color, weight) -> new Apple(color, weight);  
Apple a3 = c3.apply(GREEN, 110);
```

Lambda expression to create an `Apple` with a given color and weight

BiFunction's `apply` method with a given color and weight produces a new `Apple` object.

- Use a **Map** to associate constructors with a string value. Create a method **giveMeFruit** that, given a **String** and an **Integer**, can create different types of fruits with different weights, as follows:

```
static Map<String, Function<Integer, Fruit>> map = new HashMap<>();
static {
    map.put("apple", Apple::new);
    map.put("orange", Orange::new);
    // etc...
}
public static Fruit giveMeFruit(String fruit, Integer weight){
    return map.get(fruit.toLowerCase())
        .apply(weight);
}
```

**Get a Function<Integer, Fruit> from the map**

**Function's apply method with an Integer weight parameter creates the requested Fruit.**

## 3.7 Putting lambdas and method references into practice

- ▶ Behavior Parameterization, anonymous classes, lambda expressions, and method references.

- ▶ Step 1: Pass code

```
void sort(Comparator<? super E> c);
```

```
public class AppleComparator implements Comparator<Apple> {  
    public int compare(Apple a1, Apple a2) {  
        return a1.getWeight().compareTo(a2.getWeight());  
    }  
}  
inventory.sort(new AppleComparator());
```

## ► Step 2: Use an anonymous class

```
inventory.sort(new Comparator<Apple>() {  
    public int compare(Apple a1, Apple a2) {  
        return a1.getWeight().compareTo(a2.getWeight());  
    }  
});
```

## ► Step 3: Use lambda expressions

```
inventory.sort((Apple a1, Apple a2)  
    -> a1.getWeight().compareTo(a2.getWeight())  
);
```

```
inventory.sort((a1, a2) -> a1.getWeight().compareTo(a2.getWeight()));
```

- ▶ Comparator includes a static helper method called `comparing` that takes a Function extracting a Comparable key and produces a Comparator object.

```
Comparator<Apple> c = Comparator.comparing((Apple a) -> a.getWeight());
```

You can now rewrite your solution in a slightly more compact form:

```
import static java.util.Comparator.comparing;  
inventory.sort(comparing(apple -> apple.getWeight()));
```

- ▶ Step 4: Use method references

```
inventory.sort(comparing(Apple::getWeight));
```

## 3.8 Useful methods to compose lambda expressions

- ▶ Many functional interfaces such as **Comparator**, **Function**, and **Predicate** that are used to pass lambda expressions provide methods that allow **composition**.
- ▶ *Composing Comparators*
  - ▶ **Reversed Order**
    - ▶ `inventory.sort(comparing(Apple::getWeight).reversed());`
  - ▶ **Chaining Comparators**

```
inventory.sort (comparing(Apple::getWeight)  
                .reversed()  
                .thenComparing(Apple::getCountry));
```

Sorts by decreasing weight

Sorts further by country when  
two apples have same weight

## ► *Composing Predicate*

### ► *negate, and, and or.*

```
Predicate<Apple> notRedApple = redApple.negate();
```

Produces the negation of the existing Predicate object redApple

You may want to combine two lambdas to say that an apple is both red and heavy with the and method:

```
Predicate<Apple> redAndHeavyApple =  
redApple.and(apple -> apple.getWeight() > 150);
```

Chains two predicates to produce another Predicate object

```
Predicate<Apple> redAndHeavyAppleOrGreen =  
redApple.and(apple -> apple.getWeight() > 150)  
.or(apple -> GREEN.equals(a.getColor()));
```

Chains three predicates to construct a more complex Predicate object



## ► Composing Functions

### ► andThen and compose

```
Function<Integer, Integer> f = x -> x + 1;  
Function<Integer, Integer> g = x -> x * 2;  
Function<Integer, Integer> h = f.andThen(g);  
int result = h.apply(1);
```

In mathematics  
you'd write  $g(f(x))$   
or  $(g \circ f)(x)$ .

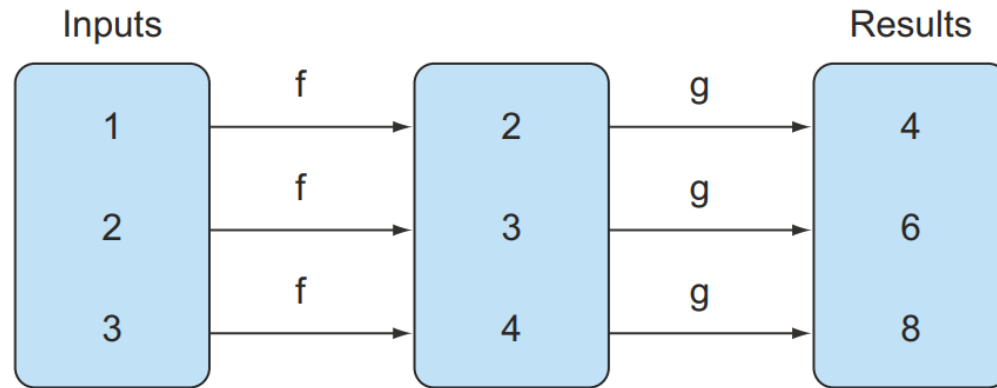
← This returns 4.

```
Function<Integer, Integer> f = x -> x + 1;  
Function<Integer, Integer> g = x -> x * 2;  
Function<Integer, Integer> h = f.compose(g);  
int result = h.apply(1);
```

In mathematics  
you'd write  $f(g(x))$   
or  $(f \circ g)(x)$ .

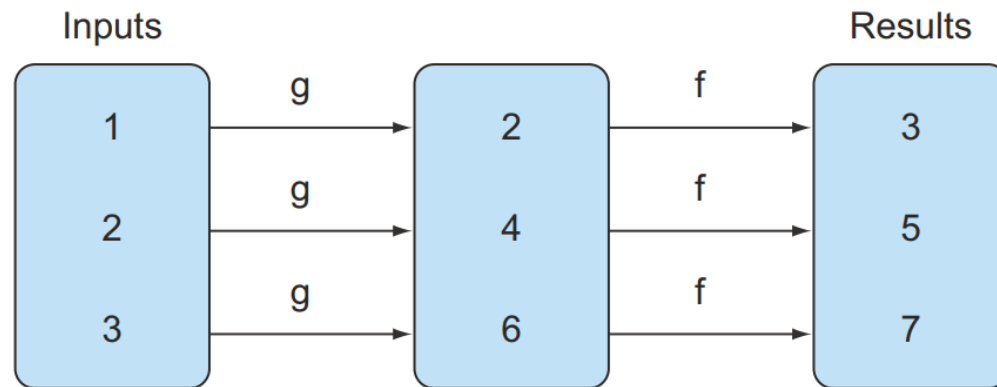
← This returns 3.

`f.andThen(g)`



```
Function<Integer, Integer> f = x -> x + 1;  
Function<Integer, Integer> g = x -> x * 2;
```

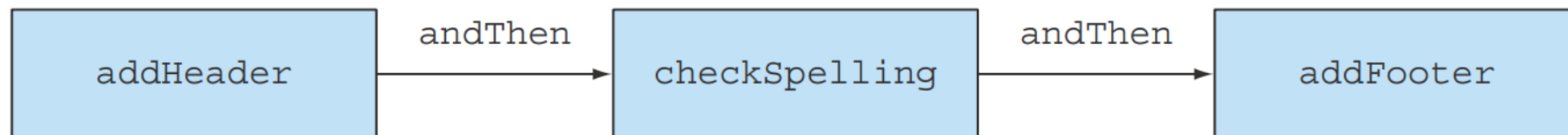
`f.compose(g)`



**Figure 3.6** Using `andThen` versus `compose`

```
Function<String, String> addHeader = Letter::addHeader;  
Function<String, String> transformationPipeline  
    = addHeader.andThen(Letter::checkSpelling)  
      .andThen(Letter::addFooter);
```

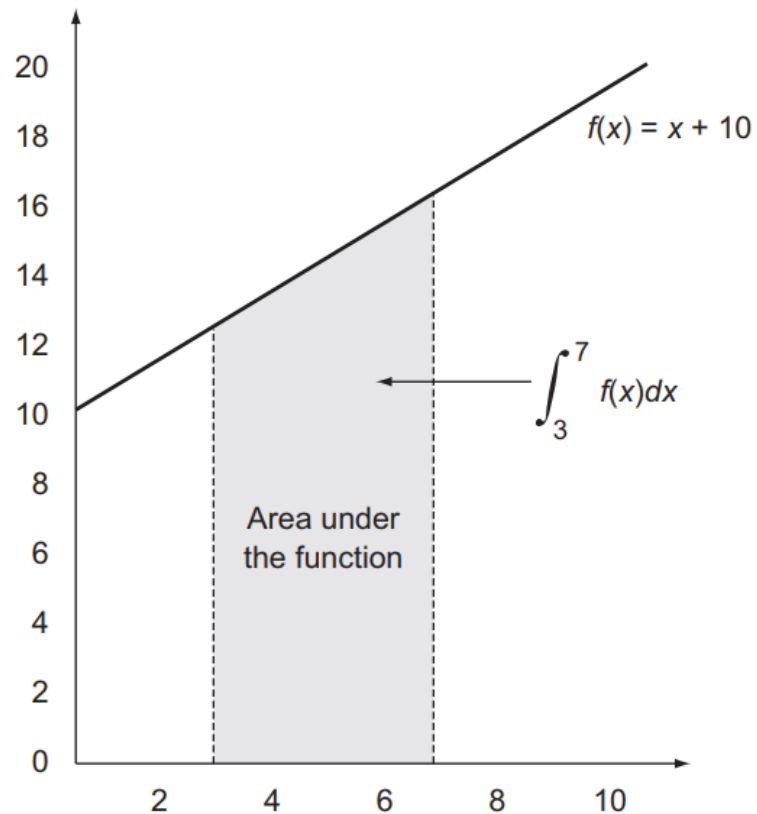
### Transformation pipeline



**Figure 3.7** A transformation pipeline using `andThen`

## 3.9 Similar ideas from mathematics

- ▶  $f(x) = x + 10$
- ▶  $\int_3^7 f(x)dx$  or  $\int_3^7 (x + 10)dx$



`integrate(f, 3, 7)`  
`integrate(x + 10, 3, 7)`

`integrate((double x) -> x + 10, 3, 7)`  
`Integrate(C::f, 3, 7)`

**Figure 3.8** Area under the function  
 $f(x) = x + 10$  for  $x$  from 3 to 7

```
public double integrate((double -> double) f, double a, double b) {  
    return (f(a) + f(b)) * (b - a) / 2.0  
}
```

**Incorrect Java code!** (You can't write functions as you do in mathematics.)

But because lambda expressions can be used only in a context expecting a functional interface (in this case, `DoubleFunction`<sup>4</sup>), you have to write it the following way:

```
public double integrate(DoubleFunction<Double> f, double a, double b) {  
    return (f.apply(a) + f.apply(b)) * (b - a) / 2.0;  
}
```

or using `DoubleUnaryOperator`, which also avoids boxing the result:

```
public double integrate(DoubleUnaryOperator f, double a, double b) {  
    return (f.applyAsDouble(a) + f.applyAsDouble(b)) * (b - a) / 2.0;  
}
```