# CS224N Assignment 1: Exploring Word Vectors (25 Points)

### Due 4:30pm, Tue Jan 19

Welcome to CS224N!

Before you start, make sure you read the README.txt in the same directory as this notebook for important setup information. A lot of code is provided in this notebook, and we highly encourage you to read and understand it as part of the learning:)

If you aren't super familiar with Python, Numpy, or Matplotlib, we recommend you check out the review session on Friday. The session will be recorded and the material will be made available on our website. The CS231N Python/Numpy tutorial is also a great resource.

**Assignment Notes:** Please make sure to save the notebook as you go along. Submission Instructions are located at the bottom of the notebook.

```
In [75]:
         # All Import Statements Defined Here
         # Note: Do not add to this list.
         import sys
         assert sys.version info[0]==3
         assert sys.version info[1] >= 5
         from gensim.models import KeyedVectors
         from gensim.test.utils import datapath
         import pprint
         import matplotlib.pyplot as plt
         plt.rcParams['figure.figsize'] = [10, 5]
         import nltk
         nltk.download('reuters')
         from nltk.corpus import reuters
         import numpy as np
         import random
         import scipy as sp
         from sklearn.decomposition import TruncatedSVD
         from sklearn.decomposition import PCA
         START TOKEN = '<START>'
         END TOKEN = '<END>'
         np.random.seed(0)
         random.seed(0)
```

```
[nltk_data] Downloading package reuters to
[nltk_data] /Users/kangjunseo/nltk_data...
[nltk_data] Package reuters is already up-to-date!
```

## **Word Vectors**

Word Vectors are often used as a fundamental component for downstream NLP tasks, e.g. question answering, text generation, translation, etc., so it is important to build some intuitions as to their strengths and weaknesses. Here, you will explore two types of word vectors: those derived from *co-occurrence matrices*, and those derived via *GloVe*.

**Note on Terminology:** The terms "word vectors" and "word embeddings" are often used interchangeably. The term "embedding" refers to the fact that we are encoding aspects of a word's meaning in a lower dimensional space. As Wikipedia states, "conceptually it involves a mathematical embedding from a space with one dimension per word to a continuous vector space with a much lower dimension".

## Part 1: Count-Based Word Vectors (10 points)

Most word vector models start from the following idea:

You shall know a word by the company it keeps (Firth, J. R. 1957:11)

Many word vector implementations are driven by the idea that similar words, i.e., (near) synonyms, will be used in similar contexts. As a result, similar words will often be spoken or written along with a shared subset of words, i.e., contexts. By examining these contexts, we can try to develop embeddings for our words. With this intuition in mind, many "old school" approaches to constructing word vectors relied on word counts. Here we elaborate upon one of those strategies, *co-occurrence matrices* (for more information, see here or here).

#### Co-Occurrence

A co-occurrence matrix counts how often things co-occur in some environment. Given some word  $w_i$  occurring in the document, we consider the *context window* surrounding  $w_i$ . Supposing our fixed window size is n, then this is the n preceding and n subsequent words in that document, i.e. words  $w_{i-n} \ldots w_{i-1}$  and  $w_{i+1} \ldots w_{i+n}$ . We build a *co-occurrence matrix* M, which is a symmetric word-by-word matrix in which  $M_{ij}$  is the number of times  $w_i$  appears inside  $w_i$ 's window among all documents.

#### **Example: Co-Occurrence with Fixed Window of n=1:**

Document 1: "all that glitters is not gold"

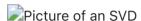
Document 2: "all is well that ends well"

*	<start></start>	all	that	glitters	is	not	gold	well	ends	<end></end>
<start></start>	0	2	0	0	0	0	0	0	0	0
all	2	0	1	0	1	0	0	0	0	0
that	0	1	0	1	0	0	0	1	1	0
glitters	0	0	1	0	1	0	0	0	0	0
is	0	1	0	1	0	1	0	1	0	0
not	0	0	0	0	1	0	1	0	0	0
gold	0	0	0	0	0	1	0	0	0	1

*	<start></start>	all	that	glitters	is	not	gold	well	ends	<end></end>	
well	0	0	1	0	1	0	0	0	1	1	
ends	0	0	1	0	0	0	0	1	0	0	
<end></end>	0	0	0	0	0	0	1	1	0	0	

**Note:** In NLP, we often add <START> and <END> tokens to represent the beginning and end of sentences, paragraphs or documents. In thise case we imagine <START> and <END> tokens encapsulating each document, e.g., " <START> All that glitters is not gold <END> ", and include these tokens in our co-occurrence counts.

The rows (or columns) of this matrix provide one type of word vectors (those based on word-word co-occurrence), but the vectors will be large in general (linear in the number of distinct words in a corpus). Thus, our next step is to run dimensionality reduction. In particular, we will run SVD (Singular Value Decomposition), which is a kind of generalized PCA (Principal Components Analysis) to select the top k principal components. Here's a visualization of dimensionality reduction with SVD. In this picture our co-occurrence matrix is k with k rows corresponding to k words. We obtain a full matrix decomposition, with the singular values ordered in the diagonal k matrix, and our new, shorter length-k word vectors in k.



This reduced-dimensionality co-occurrence representation preserves semantic relationships between words, e.g. *doctor* and *hospital* will be closer than *doctor* and *dog*.

**Notes:** If you can barely remember what an eigenvalue is, here's a slow, friendly introduction to SVD. If you want to learn more thoroughly about PCA or SVD, feel free to check out lectures 7, 8, and 9 of CS168. These course notes provide a great high-level treatment of these general purpose algorithms. Though, for the purpose of this class, you only need to know how to extract the k-dimensional embeddings by utilizing pre-programmed implementations of these algorithms from the numpy, scipy, or sklearn python packages. In practice, it is challenging to apply full SVD to large corpora because of the memory needed to perform PCA or SVD. However, if you only want the top k vector components for relatively small k – known as Truncated SVD — then there are reasonably scalable techniques to compute those iteratively.

## Plotting Co-Occurrence Word Embeddings

Here, we will be using the Reuters (business and financial news) corpus. If you haven't run the import cell at the top of this page, please run it now (click it and press SHIFT-RETURN). The corpus consists of 10,788 news documents totaling 1.3 million words. These documents span 90 categories and are split into train and test. For more details, please see <a href="https://www.nltk.org/book/ch02.html">https://www.nltk.org/book/ch02.html</a>. We provide a read\_corpus function below that pulls out only articles from the "crude" (i.e. news articles about oil, gas, etc.) category. The function also adds <START> and <END> tokens to each of the documents, and lowercases words. You do **not** have to perform any other kind of pre-processing.

Let's have a look what these documents are like....

```
In [77]:
         reuters corpus = read corpus()
          pprint.pprint(reuters_corpus[:3], compact=True, width=100)
         [['<START>', 'japan', 'to', 'revise', 'long', '-', 'term', 'energy', 'demand',
         'downwards', 'the',
           'ministry', 'of', 'international', 'trade', 'and', 'industry', '(', 'miti',
         ')', 'will', 'revise',
           'its', 'long', '-', 'term', 'energy', 'supply', '/', 'demand', 'outlook', 'b
         y', 'august', 'to',
           'meet', 'a', 'forecast', 'downtrend', 'in', 'japanese', 'energy', 'demand',
         ',', 'ministry',
           'officials', 'said', '.', 'miti', 'is', 'expected', 'to', 'lower', 'the', 'p
         rojection', 'for',
           'primary', 'energy', 'supplies', 'in', 'the', 'year', '2000', 'to', '550',
         'mln', 'kilolitres',
                'kl', ')', 'from', '600', 'mln', ',', 'they', 'said', '.', 'the', 'deci
         sion', 'follows',
           'the', 'emergence', 'of', 'structural', 'changes', 'in', 'japanese', 'indust
         ry', 'following',
           'the', 'rise', 'in', 'the', 'value', 'of', 'the', 'yen', 'and', 'a', 'declin
         e', 'in', 'domestic',
           'electric', 'power', 'demand', '.', 'miti', 'is', 'planning', 'to', 'work',
         'out', 'a', 'revised',
           'energy', 'supply', '/', 'demand', 'outlook', 'through', 'deliberations', 'o
         f', 'committee',
            'meetings', 'of', 'the', 'agency', 'of', 'natural', 'resources', 'and', 'ene
         rgy', ',', 'the',
           'officials', 'said', '.', 'they', 'said', 'miti', 'will', 'also', 'review',
         'the', 'breakdown',
           'of', 'energy', 'supply', 'sources', ',', 'including', 'oil', ',', 'nuclea
         r', ',', 'coal', 'and',
           'natural', 'gas', '.', 'nuclear', 'energy', 'provided', 'the', 'bulk', 'of',
         'japan', "'", 's',
           'electric', 'power', 'in', 'the', 'fiscal', 'year', 'ended', 'march', '31',
         ',', 'supplying',
           'an', 'estimated', '27', 'pct', 'on', 'a', 'kilowatt', '/', 'hour', 'basis',
         ',', 'followed',
           'by', 'oil', '(', '23', 'pct', ')', 'and', 'liquefied', 'natural', 'gas',
         '(', '21', 'pct', '),',
           'they', 'noted', '.', '<END>'],
          ['<START>', 'energy', '/', 'u', '.', 's', '.', 'petrochemical', 'industry',
         'cheap', 'oil',
           'feedstocks', ',', 'the', 'weakened', 'u', '.', 's', '.', 'dollar', 'and',
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'utilization', 'rate', 'approaching', '90', 'pct', 'will', 'propel', 'the',
'streamlined', 'u',
  '.', 's', '.', 'petrochemical', 'industry', 'to', 'record', 'profits', 'thi
s', 'year', ',',
  'with', 'growth', 'expected', 'through', 'at', 'least', '1990', ',', 'majo
r', 'company',
  'executives', 'predicted', '.', 'this', 'bullish', 'outlook', 'for', 'chemic
al', 'manufacturing',
  'and', 'an', 'industrywide', 'move', 'to', 'shed', 'unrelated', 'businesse
s', 'has', 'prompted',
  'gaf', 'corp', '&', 'lt', ';', 'gaf', '>,', 'privately', '-', 'held', 'cai
n', 'chemical', 'inc',
  ',', 'and', 'other', 'firms', 'to', 'aggressively', 'seek', 'acquisitions',
'of', 'petrochemical',
  'plants', '.', 'oil', 'companies', 'such', 'as', 'ashland', 'oil', 'inc',
'&', 'lt', ';', 'ash',
  '>,', 'the', 'kentucky', '-', 'based', 'oil', 'refiner', 'and', 'marketer',
',', 'are', 'also',
  shopping', 'for', 'money', '-', 'making', 'petrochemical', 'businesses', 't
o', 'buy', '.', '"',
  'i', 'see', 'us', 'poised', 'at', 'the', 'threshold', 'of', 'a', 'golden',
'period', ',"', 'said',
  'paul', 'oreffice', ',', 'chairman', 'of', 'giant', 'dow', 'chemical', 'co',
'&', 'lt', ';',
  'dow', '>,', 'adding', ',', '"', 'there', "'", 's', 'no', 'major', 'plant',
'capacity', 'being',
  'added', 'around', 'the', 'world', 'now', '.', 'the', 'whole', 'game', 'is',
'bringing', 'out',
  'new', 'products', 'and', 'improving', 'the', 'old', 'ones', '."', 'analyst
s', 'say', 'the',
  'chemical', 'industry', "'", 's', 'biggest', 'customers', ',', 'automobile',
'manufacturers',
  'and', 'home', 'builders', 'that', 'use', 'a', 'lot', 'of', 'paints', 'and',
'plastics', ',',
  'are', 'expected', 'to', 'buy', 'quantities', 'this', 'year', '.', 'u', '.',
's', '.',
  'petrochemical', 'plants', 'are', 'currently', 'operating', 'at', 'about',
'90', 'pct',
  'capacity', ',', 'reflecting', 'tighter', 'supply', 'that', 'could', 'hike',
'product', 'prices',
  'by', '30', 'to', '40', 'pct', 'this', 'year', ',', 'said', 'john', 'doshe
r', ',', 'managing',
  'director', 'of', 'pace', 'consultants', 'inc', 'of', 'houston', '.', 'deman
d', 'for', 'some',
  'products', 'such', 'as', 'styrene', 'could', 'push', 'profit', 'margins',
'up', 'by', 'as',
  'much', 'as', '300', 'pct', ',', 'he', 'said', '.', 'oreffice', ',', 'speaki
ng', 'at', 'a',
  'meeting', 'of', 'chemical', 'engineers', 'in', 'houston', ',', 'said', 'do
w', 'would', 'easily',
  'top', 'the', '741', 'mln', 'dlrs', 'it', 'earned', 'last', 'year', 'and',
'predicted', 'it',
  'would', 'have', 'the', 'best', 'year', 'in', 'its', 'history', '.', 'in',
'1985', ',', 'when',
  'oil', 'prices', 'were', 'still', 'above', '25', 'dlrs', 'a', 'barrel', 'an
d', 'chemical',
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'exports', 'were', 'adversely', 'affected', 'by', 'the', 'strong', 'u', '.',
's', '.', 'dollar',
      'dow', 'had', 'profits', 'of', '58', 'mln', 'dlrs', '.', '"', 'i', 'bel
ieve', 'the',
  'entire', 'chemical', 'industry', 'is', 'headed', 'for', 'a', 'record', 'yea
r', 'or', 'close',
  'to', 'it', ',"', 'oreffice', 'said', '.', 'gaf', 'chairman', 'samuel', 'hey
man', 'estimated',
  'that', 'the', 'u', '.', 's', '.', 'chemical', 'industry', 'would', 'repor
t', 'a', '20', 'pct',
  'gain', 'in', 'profits', 'during', '1987', '.', 'last', 'year', ',', 'the',
'domestic',
  'industry', 'earned', 'a', 'total', 'of', '13', 'billion', 'dlrs', ',', 'a',
'54', 'pct', 'leap',
  'from', '1985', '.', 'the', 'turn', 'in', 'the', 'fortunes', 'of', 'the', 'o
nce', '-', 'sickly',
  'chemical', 'industry', 'has', 'been', 'brought', 'about', 'by', 'a', 'combi
nation', 'of', 'luck',
  'and', 'planning', ',', 'said', 'pace', "'", 's', 'john', 'dosher', '.', 'do
sher', 'said', 'last',
  'year', "'", 's', 'fall', 'in', 'oil', 'prices', 'made', 'feedstocks', 'dram
atically', 'cheaper',
  'and', 'at', 'the', 'same', 'time', 'the', 'american', 'dollar', 'was', 'wea
kening', 'against',
  'foreign', 'currencies', '.', 'that', 'helped', 'boost', 'u', '.', 's', '.',
'chemical',
  'exports', '.', 'also', 'helping', 'to', 'bring', 'supply', 'and', 'demand',
'into', 'balance',
  'has', 'been', 'the', 'gradual', 'market', 'absorption', 'of', 'the', 'extr
a', 'chemical',
  'manufacturing', 'capacity', 'created', 'by', 'middle', 'eastern', 'oil', 'p
roducers', 'in',
  'the', 'early', '1980s', '.', 'finally', ',', 'virtually', 'all', 'major',
'u', '.', 's', '.',
  'chemical', 'manufacturers', 'have', 'embarked', 'on', 'an', 'extensive', 'c
orporate',
  'restructuring', 'program', 'to', 'mothball', 'inefficient', 'plants', ',',
'trim', 'the',
  'payroll', 'and', 'eliminate', 'unrelated', 'businesses', '.', 'the', 'restr
ucturing', 'touched',
  'off', 'a', 'flurry', 'of', 'friendly', 'and', 'hostile', 'takeover', 'attem
pts', '.', 'gaf', ',',
  'which', 'made', 'an', 'unsuccessful', 'attempt', 'in', '1985', 'to', 'acqui
re', 'union',
  'carbide', 'corp', '&', 'lt', ';', 'uk', '>,', 'recently', 'offered', 'thre
e', 'billion', 'dlrs',
  'for', 'borg', 'warner', 'corp', '&', 'lt', ';', 'bor', '>,', 'a', 'chicag
o', 'manufacturer',
  'of', 'plastics', 'and', 'chemicals', '.', 'another', 'industry', 'powerhous
e', ',', 'w', '.',
  'r', '.', 'grace', '&', 'lt', ';', 'gra', '>', 'has', 'divested', 'its', 're
tailing', ',',
  'restaurant', 'and', 'fertilizer', 'businesses', 'to', 'raise', 'cash', 'fo
r', 'chemical'
  'acquisitions', '.', 'but', 'some', 'experts', 'worry', 'that', 'the', 'chem
ical', 'industry',
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'may', 'be', 'headed', 'for', 'trouble', 'if', 'companies', 'continue', 'tur
ning', 'their',
  'back', 'on', 'the', 'manufacturing', 'of', 'staple', 'petrochemical', 'comm
odities', ',', 'such',
  'as', 'ethylene', ',', 'in', 'favor', 'of', 'more', 'profitable', 'specialt
y', 'chemicals',
  'that', 'are', 'custom', '-', 'designed', 'for', 'a', 'small', 'group', 'o
f', 'buyers', '.', '"',
  'companies', 'like', 'dupont', '&', 'lt', ';', 'dd', '>', 'and', 'monsanto',
'co', '&', 'lt', ';',
  'mtc', '>', 'spent', 'the', 'past', 'two', 'or', 'three', 'years', 'trying',
'to', 'get', 'out',
  'of', 'the', 'commodity', 'chemical', 'business', 'in', 'reaction', 'to', 'h
ow', 'badly', 'the',
  'market', 'had', 'deteriorated', ',"', 'dosher', 'said', '.', '"', 'but',
'i', 'think', 'they',
  'will', 'eventually', 'kill', 'the', 'margins', 'on', 'the', 'profitable',
'chemicals', 'in',
  'the', 'niche', 'market', '."', 'some', 'top', 'chemical', 'executives', 'sh
are', 'the',
  'concern', '.', '"', 'the', 'challenge', 'for', 'our', 'industry', 'is', 't
o', 'keep', 'from',
  'getting', 'carried', 'away', 'and', 'repeating', 'past', 'mistakes', ',"',
'qaf', "'", 's',
  'heyman', 'cautioned', '.', '"', 'the', 'shift', 'from', 'commodity', 'chemi
cals', 'may', 'be',
  'ill', '-', 'advised', '.', 'specialty', 'businesses', 'do', 'not', 'stay',
'special', 'long',
  '."', 'houston', '-', 'based', 'cain', 'chemical', ',', 'created', 'this',
'month', 'by', 'the',
  'sterling', 'investment', 'banking', 'group', ',', 'believes', 'it', 'can',
'generate', '700',
  'mln', 'dlrs', 'in', 'annual', 'sales', 'by', 'bucking', 'the', 'industry',
'trend', '.',
  'chairman', 'gordon', 'cain', ',', 'who', 'previously', 'led', 'a', 'leverag
ed', 'buyout', 'of',
  'dupont', "'", 's', 'conoco', 'inc', "'", 's', 'chemical', 'business', ',',
      'spent', '1',
  '.', '1', 'billion', 'dlrs', 'since', 'january', 'to', 'buy', 'seven', 'petr
ochemical', 'plants',
  'along', 'the', 'texas', 'gulf', 'coast', '.', 'the', 'plants', 'produce',
'only', 'basic',
  'commodity', 'petrochemicals', 'that', 'are', 'the', 'building', 'blocks',
'of', 'specialty',
  'products', '.', '"', 'this', 'kind', 'of', 'commodity', 'chemical', 'busine
ss', 'will', 'never',
  'be', 'a', 'glamorous', ',', 'high', '-', 'margin', 'business', ',"', 'cai
n', 'said', ',',
  'adding', 'that', 'demand', 'is', 'expected', 'to', 'grow', 'by', 'about',
'three', 'pct',
  'annually', '.', 'garo', 'armen', ',', 'an', 'analyst', 'with', 'dean', 'wit
ter', 'reynolds', ',',
  'said', 'chemical', 'makers', 'have', 'also', 'benefitted', 'by', 'increasin
g', 'demand', 'for',
  'plastics', 'as', 'prices', 'become', 'more', 'competitive', 'with', 'alumin
um', ',', 'wood',
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'and', 'steel', 'products', '.', 'armen', 'estimated', 'the', 'upturn', 'i
n', 'the', 'chemical',
  'business', 'could', 'last', 'as', 'long', 'as', 'four', 'or', 'five', 'year
s', ',', 'provided',
  'the', 'u', '.', 's', '.', 'economy', 'continues', 'its', 'modest', 'rate',
'of', 'growth', '.',
  '<END>'],
 ['<START>', 'turkey', 'calls', 'for', 'dialogue', 'to', 'solve', 'dispute',
'turkey', 'said',
  'today', 'its', 'disputes', 'with', 'greece', ',', 'including', 'rights', 'o
n', 'the',
  'continental', 'shelf', 'in', 'the', 'aegean', 'sea', ',', 'should', 'be',
'solved', 'through',
  'negotiations', '.', 'a', 'foreign', 'ministry', 'statement', 'said', 'the',
'latest', 'crisis',
  'between', 'the', 'two', 'nato', 'members', 'stemmed', 'from', 'the', 'conti
nental', 'shelf',
  'dispute', 'and', 'an', 'agreement', 'on', 'this', 'issue', 'would', 'effec
t', 'the', 'security',
  ',', 'economy', 'and', 'other', 'rights', 'of', 'both', 'countries', '.',
'"', 'as', 'the',
  'issue', 'is', 'basicly', 'political', ',', 'a', 'solution', 'can', 'only',
'be', 'found', 'by',
  'bilateral', 'negotiations', ',"', 'the', 'statement', 'said', '.', 'greec
e', 'has', 'repeatedly',
  'said', 'the', 'issue', 'was', 'legal', 'and', 'could', 'be', 'solved', 'a
t', 'the',
  'international', 'court', 'of', 'justice', '.', 'the', 'two', 'countries',
'approached', 'armed',
  'confrontation', 'last', 'month', 'after', 'greece', 'announced', 'it', 'pla
nned', 'oil',
  'exploration', 'work', 'in', 'the', 'aegean', 'and', 'turkey', 'said', 'it',
'would', 'also',
  'search', 'for', 'oil', '.', 'a', 'face', '-', 'off', 'was', 'averted', 'whe
n', 'turkey',
  'confined', 'its', 'research', 'to', 'territorrial', 'waters', '.', '"', 'th
e', 'latest',
  'crises', 'created', 'an', 'historic', 'opportunity', 'to', 'solve', 'the',
'disputes', 'between',
  'the', 'two', 'countries', ',"', 'the', 'foreign', 'ministry', 'statement',
'said', '.', 'turkey',
  "'", 's', 'ambassador', 'in', 'athens', ',', 'nazmi', 'akiman', ',', 'was',
'due', 'to', 'meet',
  'prime', 'minister', 'andreas', 'papandreou', 'today', 'for', 'the', 'gree
k', 'reply', 'to', 'a',
  'message', 'sent', 'last', 'week', 'by', 'turkish', 'prime', 'minister', 'tu
rgut', 'ozal', '.',
  'the', 'contents', 'of', 'the', 'message', 'were', 'not', 'disclosed', '.',
'<END>']]
```

## Question 1.1: Implement distinct\_words [code] (2 points)

Write a method to work out the distinct words (word types) that occur in the corpus. You can do this with for loops, but it's more efficient to do it with Python list comprehensions. In

particular, this may be useful to flatten a list of lists. If you're not familiar with Python list comprehensions in general, here's more information.

Your returned corpus\_words should be sorted. You can use python's sorted function for this.

You may find it useful to use Python sets to remove duplicate words.

```
In [78]:
        def distinct words(corpus):
             """ Determine a list of distinct words for the corpus.
                Params:
                    corpus (list of list of strings): corpus of
        documents
                Return:
                    corpus words (list of strings): sorted list of
        distinct words across the corpus
                    num corpus words (integer): number of distinct
        words across the corpus
            corpus words = []
            num corpus words = -1
            # -----
            # Write your implementation here.
            corpus words = sorted(set([y for x in corpus for y in
        set(x)))
            num corpus words = len(corpus words)
            return corpus words, num corpus words
```

```
In [79]:
       # -----
        # Run this sanity check
        # Note that this not an exhaustive check for correctness.
        # -----
        # Define toy corpus
        test corpus = ["{} All that glitters isn't gold
        {}".format(START_TOKEN, END_TOKEN).split(" "), "{} All's well
        that ends well {}".format(START TOKEN, END TOKEN).split(" ")]
        test corpus words, num corpus words =
        distinct words(test corpus)
        # Correct answers
        ans_test_corpus_words = sorted([START_TOKEN, "All", "ends",
        "that", "gold", "All's", "glitters", "isn't", "well",
        END TOKEN])
        ans num corpus words = len(ans test corpus words)
        # Test correct number of words
        assert(num corpus words == ans num corpus words), "Incorrect
        number of distinct words. Correct: {}. Yours:
        {}".format(ans num corpus words, num corpus words)
        # Test correct words
```

```
assert (test_corpus_words == ans_test_corpus_words), "Incorrect
corpus_words.\nCorrect: {}\nYours:
{}".format(str(ans_test_corpus_words), str(test_corpus_words))

# Print Success
print ("-" * 80)
print("Passed All Tests!")
print ("-" * 80)
```

```
---
Passed All Tests!
```

## Question 1.2: Implement compute\_co\_occurrence\_matrix [code] (3 points)

Write a method that constructs a co-occurrence matrix for a certain window-size n (with a default of 4), considering words n before and n after the word in the center of the window. Here, we start to use <code>numpy</code> (<code>np</code>) to represent vectors, matrices, and tensors. If you're not familiar with NumPy, there's a NumPy tutorial in the second half of this cs231n Python <code>NumPy</code> tutorial.

```
In [80]:
        def compute co occurrence matrix(corpus, window size=4):
             """ Compute co-occurrence matrix for the given corpus and
         window size (default of 4).
                 Note: Each word in a document should be at the center
         of a window. Words near edges will have a smaller
                       number of co-occurring words.
                       For example, if we take the document "<START> All
         that glitters is not gold <END>" with window size of 4,
                       "All" will co-occur with "<START>", "that",
         "glitters", "is", and "not".
                 Params:
                     corpus (list of list of strings): corpus of
         documents
                     window size (int): size of context window
                 Return:
                     M (a symmetric numpy matrix of shape (number of
         unique words in the corpus , number of unique words in the
         corpus)):
                         Co-occurence matrix of word counts.
                         The ordering of the words in the rows/columns
         should be the same as the ordering of the words given by the
         distinct words function.
                     word2ind (dict): dictionary that maps word to index
         (i.e. row/column number) for matrix M.
            words, num_words = distinct_words(corpus)
             M = None
             word2ind = {}
```

```
In [81]:
        # -----
        # Run this sanity check
        # Note that this is not an exhaustive check for correctness.
        # Define toy corpus and get student's co-occurrence matrix
        test corpus = ["{} All that glitters isn't gold
        {}".format(START_TOKEN, END_TOKEN).split(" "), "{} All's well
        that ends well {}".format(START TOKEN, END TOKEN).split(" ")]
        M test, word2ind test =
        compute co occurrence matrix(test corpus, window size=1)
        # Correct M and word2ind
        M test ans = np.array(
            [[0., 0., 0., 0., 0., 0., 1., 0., 0., 1.,],
             [0., 0., 1., 1., 0., 0., 0., 0., 0., 0., 0., ],
             [0., 1., 0., 0., 0., 0., 0., 1., 0.,],
             [0., 1., 0., 0., 0., 0., 0., 0., 1.,],
             [0., 0., 0., 0., 0., 0., 0., 0., 1., 1.,],
             [0., 0., 0., 0., 0., 0., 1., 1., 0.,],
             [1., 0., 0., 0., 0., 0., 1., 0., 0., ],
             [0., 0., 0., 0., 0., 1., 1., 0., 0., 0.,],
             [0., 0., 1., 0., 1., 1., 0., 0., 0., 1.,],
             [1., 0., 0., 1., 1., 0., 0., 0., 1., 0.,]]
        ans_test_corpus_words = sorted([START TOKEN, "All", "ends",
        "that", "gold", "All's", "glitters", "isn't", "well",
        END TOKEN])
        word2ind ans = dict(zip(ans test corpus words,
        range(len(ans_test_corpus_words))))
        # Test correct word2ind
        assert (word2ind ans == word2ind_test), "Your word2ind is
        incorrect:\nCorrect: {}\nYours: {}".format(word2ind ans,
        word2ind test)
        # Test correct M shape
        assert (M test.shape == M test ans.shape), "M matrix has
        incorrect shape.\nCorrect: {}\nYours: {}".format(M_test.shape,
```

```
M test ans.shape)
# Test correct M values
for w1 in word2ind ans.keys():
    idx1 = word2ind ans[w1]
    for w2 in word2ind ans.keys():
        idx2 = word2ind ans[w2]
        student = M test[idx1, idx2]
        correct = M test ans[idx1, idx2]
        if student != correct:
            print("Correct M:")
            print(M test ans)
            print("Your M: ")
            print(M test)
            raise AssertionError("Incorrect count at index ({}),
{})=({}, {}) in matrix M. Yours has {} but should have
{}.".format(idx1, idx2, w1, w2, student, correct))
# Print Success
print ("-" * 80)
print("Passed All Tests!")
print ("-" * 80)
```

```
--
Passed All Tests!
```

## Question 1.3: Implement reduce\_to\_k\_dim [code] (1 point)

Construct a method that performs dimensionality reduction on the matrix to produce k-dimensional embeddings. Use SVD to take the top k components and produce a new matrix of k-dimensional embeddings.

**Note:** All of numpy, scipy, and scikit-learn (sklearn) provide *some* implementation of SVD, but only scipy and sklearn provide an implementation of Truncated SVD, and only sklearn provides an efficient randomized algorithm for calculating large-scale Truncated SVD. So please use sklearn.decomposition.TruncatedSVD.

```
In [82]:
        def reduce to k dim(M, k=2):
             """ Reduce a co-occurence count matrix of dimensionality
         (num corpus words, num corpus words)
                 to a matrix of dimensionality (num corpus words, k)
         using the following SVD function from Scikit-Learn:
                     - http://scikit-
         learn.org/stable/modules/generated/sklearn.decomposition.Truncated
                 Params:
                     M (numpy matrix of shape (number of unique words in
         the corpus , number of unique words in the corpus)): co-
         occurence matrix of word counts
                     k (int): embedding size of each word after
         dimension reduction
                 Return:
                     M_reduced (numpy matrix of shape (number of corpus
```

```
words, k)): matrix of k-dimensioal word embeddings.
                   In terms of the SVD from math class, this
actually returns U * S
   n iters = 10
                  # Use this parameter in your call to
`TruncatedSVD`
   M reduced = None
   print("Running Truncated SVD over %i words..." %
(M.shape[0]))
   # -----
   # Write your implementation here.
   SVD = TruncatedSVD(n components=k, n iter=n iters)
   SVD.fit(M)
   M reduced = SVD.transform(M)
   # -----
   print("Done.")
   return M reduced
```

```
In [83]:
        # -----
        # Run this sanity check
        # Note that this is not an exhaustive check for correctness
        # In fact we only check that your M reduced has the right
        dimensions.
        # Define toy corpus and run student code
        test corpus = ["{} All that glitters isn't gold
        {}".format(START_TOKEN, END_TOKEN).split(" "), "{} All's well
        that ends well {}".format(START TOKEN, END TOKEN).split(" ")]
        M_test, word2ind test =
        compute co occurrence matrix(test corpus, window size=1)
        M_test_reduced = reduce_to_k_dim(M_test, k=2)
        # Test proper dimensions
        assert (M test reduced.shape[0] == 10), "M reduced has {} rows;
        should have {}".format(M_test_reduced.shape[0], 10)
        assert (M test reduced.shape[1] == 2), "M reduced has {}
        columns; should have {}".format(M test reduced.shape[1], 2)
        # Print Success
        print ("-" * 80)
        print("Passed All Tests!")
        print ("-" * 80)
```

```
Running Truncated SVD over 10 words...

Done.

---

Passed All Tests!
```

Question 1.4: Implement plot\_embeddings [code] (1 point)

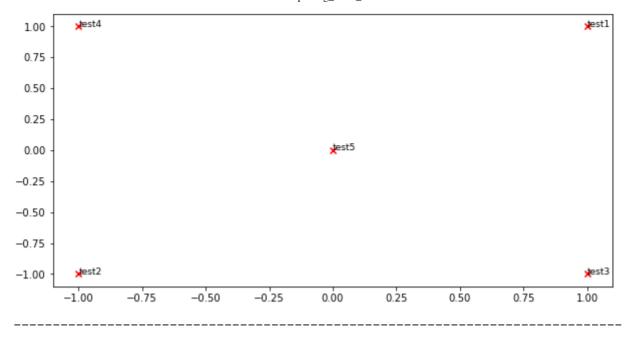
Here you will write a function to plot a set of 2D vectors in 2D space. For graphs, we will use Matplotlib (plt).

For this example, you may find it useful to adapt this code. In the future, a good way to make a plot is to look at the Matplotlib gallery, find a plot that looks somewhat like what you want, and adapt the code they give.

```
In [84]:
        def plot embeddings(M reduced, word2ind, words):
             """ Plot in a scatterplot the embeddings of the words
         specified in the list "words".
                 NOTE: do not plot all the words listed in M reduced /
                 Include a label next to each point.
                 Params:
                     M reduced (numpy matrix of shape (number of unique
         words in the corpus , 2)): matrix of 2-dimensioal word
         embeddings
                     word2ind (dict): dictionary that maps word to
         indices for matrix M
                     words (list of strings): words whose embeddings we
         want to visualize
             # Write your implementation here.
             for i, word in enumerate(words):
                 x, y = M reduced[word2ind[word]][0],
         M reduced[word2ind[word]][1]
                 plt.scatter(x, y, marker='x', color='red')
                 plt.text(x, y, word, fontsize=9)
             plt.show()
```

--

Outputted Plot:



\*\*Test Plot Solution\*\*



### Question 1.5: Co-Occurrence Plot Analysis [written] (3 points)

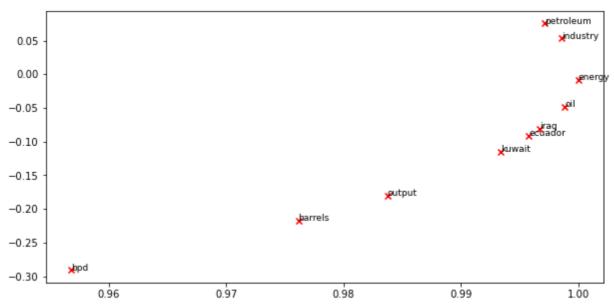
Now we will put together all the parts you have written! We will compute the co-occurrence matrix with fixed window of 4 (the default window size), over the Reuters "crude" (oil) corpus. Then we will use TruncatedSVD to compute 2-dimensional embeddings of each word. TruncatedSVD returns U\*S, so we need to normalize the returned vectors, so that all the vectors will appear around the unit circle (therefore closeness is directional closeness).

Note: The line of code below that does the normalizing uses the NumPy concept of broadcasting. If you don't know about broadcasting, check out Computation on Arrays:

Broadcasting by Jake VanderPlas.

Run the below cell to produce the plot. It'll probably take a few seconds to run. What clusters together in 2-dimensional embedding space? What doesn't cluster together that you might think should have? **Note:** "bpd" stands for "barrels per day" and is a commonly used abbreviation in crude oil topic articles.

Running Truncated SVD over 8185 words...
Done.



#### Write your answer here.

What clusters together in 2-dimensional embedding space?

```
irag, ecuador, kuwait
petroleum, industry
```

What doesn't cluster together that you might think should have?

```
bpd, barrels
oil, energy
```

## Part 2: Prediction-Based Word Vectors (15 points)

As discussed in class, more recently prediction-based word vectors have demonstrated better performance, such as word2vec and GloVe (which also utilizes the benefit of counts). Here, we shall explore the embeddings produced by GloVe. Please revisit the class notes and lecture slides for more details on the word2vec and GloVe algorithms. If you're feeling adventurous, challenge yourself and try reading GloVe's original paper.

Then run the following cells to load the GloVe vectors into memory. **Note**: If this is your first time to run these cells, i.e. download the embedding model, it will take a couple minutes to run. If you've run these cells before, rerunning them will load the model without redownloading it, which will take about 1 to 2 minutes.

```
len(wv_from_bin.vocab.keys()))
    return wv_from_bin
```

```
In [88]: # ------
# Run Cell to Load Word Vectors
# Note: This will take a couple minutes
# ------
wv_from_bin = load_embedding_model()
```

Note: If you are receiving a "reset by peer" error, rerun the cell to restart the download.

#### Reducing dimensionality of Word Embeddings

Let's directly compare the GloVe embeddings to those of the co-occurrence matrix. In order to avoid running out of memory, we will work with a sample of 10000 GloVe vectors instead. Run the following cells to:

- 1. Put 10000 Glove vectors into a matrix M
- 2. Run reduce\_to\_k\_dim (your Truncated SVD function) to reduce the vectors from 200-dimensional to 2-dimensional.

```
In [89]:
         def get matrix of vectors (wv from bin, required words=
         ['barrels', 'bpd', 'ecuador', 'energy', 'industry', 'kuwait', 'oil', 'output', 'petroleum', 'iraq']):
              """ Put the GloVe vectors into a matrix M.
                  Param:
                      wv from bin: KeyedVectors object; the 400000 GloVe
         vectors loaded from file
                  Return:
                      M: numpy matrix shape (num words, 200) containing
         the vectors
                      word2ind: dictionary mapping each word to its row
         number in M
             import random
             words = list(wv from bin.key to index.keys())
             print("Shuffling words ...")
             random.seed(224)
             random.shuffle(words)
             words = words[:10000]
             print("Putting %i words into word2ind and matrix M..." %
         len(words))
             word2ind = \{\}
             M = []
             curInd = 0
              for w in words:
                  try:
                      M.append(wv_from_bin.word_vec(w))
                      word2ind[w] = curInd
                      curInd += 1
                  except KeyError:
                      continue
              for w in required words:
                  if w in words:
                      continue
```

```
# ----
# Run Cell to Reduce 200-Dimensional Word Embeddings to k
Dimensions
# Note: This should be quick to run
# ----
M, word2ind = get_matrix_of_vectors(wv_from_bin)
M_reduced = reduce_to_k_dim(M, k=2)

# Rescale (normalize) the rows to make them each of unit-length
M_lengths = np.linalg.norm(M_reduced, axis=1)
M_reduced_normalized = M_reduced / M_lengths[:, np.newaxis] #
broadcasting
```

```
Shuffling words ...

Putting 10000 words into word2ind and matrix M...

Done.

Running Truncated SVD over 10010 words...

Done.

/opt/anaconda3/envs/cs224n/lib/python3.7/site-packages/ipykernel_launcher.py:2

1: DeprecationWarning: Call to deprecated `word vec` (Use get vector instead).
```

Note: If you are receiving out of memory issues on your local machine, try closing other applications to free more memory on your device. You may want to try restarting your machine so that you can free up extra memory. Then immediately run the jupyter notebook and see if you can load the word vectors properly. If you still have problems with loading the embeddings onto your local machine after this, please go to office

/opt/anaconda3/envs/cs224n/lib/python3.7/site-packages/ipykernel\_launcher.py:3
0: DeprecationWarning: Call to deprecated `word\_vec` (Use get\_vector instead).

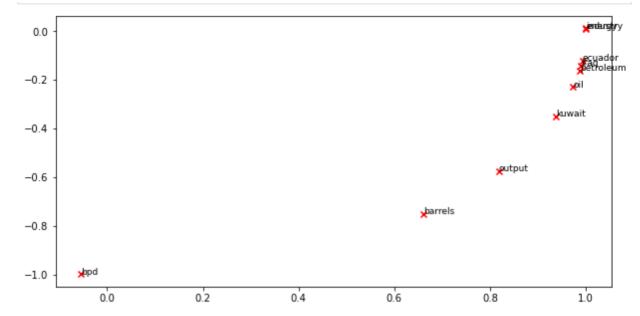
## Question 2.1: GloVe Plot Analysis [written] (3 points)

```
Run the cell below to plot the 2D GloVe embeddings for ['barrels', 'bpd', 'ecuador', 'energy', 'industry', 'kuwait', 'oil', 'output', 'petroleum', 'iraq'].
```

What clusters together in 2-dimensional embedding space? What doesn't cluster together that you think should have? How is the plot different from the one generated earlier from the co-occurrence matrix? What is a possible cause for the difference?

```
In [91]: words = ['barrels', 'bpd', 'ecuador', 'energy', 'industry',
    'kuwait', 'oil', 'output', 'petroleum', 'iraq']
    plot_embeddings(M_reduced_normalized, word2ind, words)
```

hours or contact course staff.



#### Write your answer here.

What clusters together in 2-dimensional embedding space?

```
ecuador, iraq, petroleum energy, industry
```

What doesn't cluster together that you think should have?

```
bpd, barrels
oil, energy
kuwait, ecuador
```

How is the plot different from the one generated earlier from the co-occurrence matrix?

```
clusters are much closer than before but I think accuracy is bit decreased
```

What is a possible cause for the difference?

Glove is the one with more generalized, and the one that used before was more specified

## **Cosine Similarity**

Now that we have word vectors, we need a way to quantify the similarity between individual words, according to these vectors. One such metric is cosine-similarity. We will be using this to find words that are "close" and "far" from one another.

We can think of n-dimensional vectors as points in n-dimensional space. If we take this perspective L1 and L2 Distances help quantify the amount of space "we must travel" to get between these two points. Another approach is to examine the angle between two vectors. From trigonometry we know that:



Instead of computing the actual angle, we can leave the similarity in terms of  $similarity = cos(\Theta)$ . Formally the Cosine Similarity s between two vectors p and q is defined as:

$$s = rac{p \cdot q}{||p||||q||}, ext{ where } s \in [-1,1]$$

## Question 2.2: Words with Multiple Meanings (1.5 points) [code + written]

Polysemes and homonyms are words that have more than one meaning (see this wiki page to learn more about the difference between polysemes and homonyms). Find a word with at least two different meanings such that the top-10 most similar words (according to cosine similarity) contain related words from both meanings. For example, "leaves" has both "go\_away" and "a\_structure\_of\_a\_plant" meaning in the top 10, and "scoop" has both "handed\_waffle\_cone" and "lowdown". You will probably need to try several polysemous or homonymic words before you find one.

Please state the word you discover and the multiple meanings that occur in the top 10. Why do you think many of the polysemous or homonymic words you tried didn't work (i.e. the top-10 most similar words only contain **one** of the meanings of the words)?

**Note**: You should use the wv\_from\_bin.most\_similar(word) function to get the top 10 similar words. This function ranks all other words in the vocabulary with respect to their cosine similarity to the given word. For further assistance, please check the GenSim documentation.

#### Write your answer here.

I found the word 'term' which has 2 meaning of "mean" and "interest". It uses average result of vector, so it's hard to find the second meaning.

### Question 2.3: Synonyms & Antonyms (2 points) [code + written]

When considering Cosine Similarity, it's often more convenient to think of Cosine Distance, which is simply 1 - Cosine Similarity.

Find three words  $(w_1, w_2, w_3)$  where  $w_1$  and  $w_2$  are synonyms and  $w_1$  and  $w_3$  are antonyms, but Cosine Distance  $(w_1, w_3) <$  Cosine Distance  $(w_1, w_2)$ .

As an example,  $w_1$ ="happy" is closer to  $w_3$ ="sad" than to  $w_2$ ="cheerful". Please find a different example that satisfies the above. Once you have found your example, please give a possible explanation for why this counter-intuitive result may have happened.

You should use the the wv\_from\_bin.distance(w1, w2) function here in order to compute the cosine distance between two words. Please see the GenSim documentation for further assistance.

True

#### Write your answer here.

This is because 'man' and 'woman' is used at similar position in the sentence, while 'male' is used at describing animals more often.

## Question 2.4: Analogies with Word Vectors [written] (1.5 points)

Word vectors have been shown to sometimes exhibit the ability to solve analogies.

As an example, for the analogy "man: king:: woman: x" (read: man is to king as woman is to x), what is x?

In the cell below, we show you how to use word vectors to find x using the most\_similar function from the GenSim documentation. The function finds words that are most similar to the words in the positive list and most dissimilar from the words in the negative list (while omitting the input words, which are often the most similar; see this paper). The answer to the analogy will have the highest cosine similarity (largest returned numerical value).

```
('monarch', 0.5889754891395569),

('throne', 0.5775108933448792),

('prince', 0.5750998258590698),

('elizabeth', 0.546359658241272),

('daughter', 0.5399125814437866),

('kingdom', 0.5318052172660828),

('mother', 0.5168542861938477),

('crown', 0.5164473056793213)]
```

Let m, k, w, and x denote the word vectors for man , king , woman , and the answer, respectively. Using **only** vectors m, k, w, and the vector arithmetic operators + and - in your answer, what is the expression in which we are maximizing cosine similarity with x?

Hint: Recall that word vectors are simply multi-dimensional vectors that represent a word. It might help to draw out a 2D example using arbitrary locations of each vector. Where would man and woman lie in the coordinate plane relative to king and the answer?

#### Write your answer here.

```
woman + king - man = queen
w + k - m
```

## Question 2.5: Finding Analogies [code + written] (1.5 points)

Find an example of analogy that holds according to these vectors (i.e. the intended word is ranked top). In your solution please state the full analogy in the form x:y :: a:b. If you believe the analogy is complicated, explain why the analogy holds in one or two sentences.

**Note**: You may have to try many analogies to find one that works!

```
[('actress', 0.8572622537612915),
  ('actresses', 0.6734700798988342),
  ('actors', 0.6297088265419006),
  ('starring', 0.6084522008895874),
  ('starred', 0.5989462733268738),
  ('screenwriter', 0.5959889888763428),
  ('dancer', 0.5881682634353638),
  ('comedian', 0.5791140794754028),
  ('singer', 0.5661861896514893),
  ('married', 0.5574131011962891)]
```

#### Write your answer here.

```
man: woman:: actor: actress
```

## Question 2.6: Incorrect Analogy [code + written] (1.5 points)

Find an example of analogy that does *not* hold according to these vectors. In your solution, state the intended analogy in the form x:y :: a:b, and state the (incorrect) value of b according to the word vectors.

```
# -----
# Write your implementation here.

pprint.pprint(wv_from_bin.most_similar(positive=['second', 'apple'], negative=['first']))
# -------
```

```
[('intel', 0.614384651184082),
  ('iphone', 0.5742251873016357),
  ('microsoft', 0.571113646030426),
  ('ipod', 0.5478871464729309),
  ('ibm', 0.5415121912956238),
  ('macintosh', 0.5324228405952454),
  ('pc', 0.5299952030181885),
  ('ipad', 0.5260148048400879),
  ('google', 0.5142451524734497),
  ('chips', 0.5086367726325989)]
```

#### Write your answer here.

```
first : second :: apple : samsung

I expected samsung, but for global, it seems intel is on
it! lol
```

## Question 2.7: Guided Analysis of Bias in Word Vectors [written] (1 point)

It's important to be cognizant of the biases (gender, race, sexual orientation etc.) implicit in our word embeddings. Bias can be dangerous because it can reinforce stereotypes through applications that employ these models.

Run the cell below, to examine (a) which terms are most similar to "woman" and "worker" and most dissimilar to "man", and (b) which terms are most similar to "man" and "worker" and most dissimilar to "woman". Point out the difference between the list of female-associated words and the list of male-associated words, and explain how it is reflecting gender bias.

```
In [97]: # Run this cell
# Here `positive` indicates the list of words to be similar to
and `negative` indicates the list of words to be
# most dissimilar from.
pprint.pprint(wv_from_bin.most_similar(positive=['woman',
    'worker'], negative=['man']))
print()
pprint.pprint(wv_from_bin.most_similar(positive=['man',
    'worker'], negative=['woman']))

[('employee', 0.6375862956047058),
```

```
('workers', 0.6068919897079468),
```

```
('nurse', 0.5837946534156799),
 ('pregnant', 0.5363885760307312),
 ('mother', 0.5321308970451355),
 ('employer', 0.5127025842666626),
 ('teacher', 0.5099576711654663),
 ('child', 0.5096741318702698),
 ('homemaker', 0.5019455552101135),
 ('nurses', 0.4970572590827942)]
[('workers', 0.611325740814209),
 ('employee', 0.5983109474182129),
('working', 0.5615329742431641),
('laborer', 0.5442320704460144),
 ('unemployed', 0.5368516445159912),
 ('job', 0.5278825759887695),
 ('work', 0.5223963260650635),
 ('mechanic', 0.5088937878608704),
 ('worked', 0.5054520964622498),
 ('factory', 0.49404534697532654)]
```

#### Write your answer here.

- (a) employee, nurse, employer, teacher
- (b) workers, laborer, unemployed, mechanic, factory
- (a) includes some feeling which is not working for using our body, such as 'employer' or 'teacher', while (b) includes 'workers', 'laborer', 'mechanic', 'factory' which seems like fully using their body muscles while doing stuffs.

## Question 2.8: Independent Analysis of Bias in Word Vectors [code + written] (1 point)

Use the most\_similar function to find another case where some bias is exhibited by the vectors. Please briefly explain the example of bias that you discover.

('fund', 0.6202576160430908), ('even', 0.6163768172264099), ('already', 0.607093870639801), ('because', 0.6064628958702087), ('billions', 0.5984749794006348),

```
('now', 0.593262255191803),
('credit', 0.5899507999420166)]

[('funds', 0.6231023073196411),
('cash', 0.5972325801849365),
('donations', 0.5773746967315674),
('taxpayer', 0.5465309023857117),
('proceeds', 0.5427141785621643),
('paying', 0.5338638424873352),
('taxpayers', 0.5338127613067627),
('pay', 0.5333255529403687),
('paid', 0.5251866579055786),
('payments', 0.5181621313095093)]
```

#### Write your answer here.

```
For korea about money, we can see `much`, `billions`, `credit`, and those are a bit possible words. While dprk, we can see `donations`, `taxpayer`, `pay`, and those are a bit negative.
```

### Question 2.9: Thinking About Bias [written] (2 points)

Give one explanation of how bias gets into the word vectors. What is an experiment that you could do to test for or to measure this source of bias?

#### Write your answer here.

Bias makes words' meaning "pre-fixed". We can test these by maybe using regression of some wordvec.

## **Submission Instructions**

- 1. Click the Save button at the top of the Jupyter Notebook.
- 2. Select Cell -> All Output -> Clear. This will clear all the outputs from all cells (but will keep the content of all cells).
- 3. Select Cell -> Run All. This will run all the cells in order, and will take several minutes.
- 4. Once you've rerun everything, select File -> Download as -> PDF via LaTeX (If you have trouble using "PDF via LaTex", you can also save the webpage as pdf. Make sure all your solutions especially the coding parts are displayed in the pdf, it's okay if the provided codes get cut off because lines are not wrapped in code cells).
- 5. Look at the PDF file and make sure all your solutions are there, displayed correctly. The PDF is the only thing your graders will see!
- 6. Submit your PDF on Gradescope.