

Algorithm

Quicksort

Code Walkthrough

`partition()`





Quicksort

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```



Quicksort



[7, 2, 8, 1, 0, 3, 5]

[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

```
[7, 2, 8, 1, 0, 3, 5]
```

[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

```
a = [7, 2, 8, 1, 0, 3, 5]  
quicksort(a, 0, len(a)-1)
```

```
quicksort(a, 0, len(a)-1)
```

```
[7, 2, 8, 1, 0, 3, 5]
```

[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
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        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

```
[7, 2, 8, 1, 0, 3, 5]
```

```
[0] [1] [2] [3] [4] [5] [6]
```

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

```
quicksort(a, 0, len(a)-1)
```



[7, 2, 8, 1, 0, 3, 5]

[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)



[7, 2, 8, 1, 0, 3, 5]

[0]

[1]

[2]

[3]

[4]

[5]

[6]



partition(lst, 0, 6)

pivot = 5

i = -1

j = 0

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

[7, 2, 8, 1, 0, 3, 5]

[0]

[1]

[2]

[3]

[4]

[5]

[6]



pivot = 5

i = -1

j = 0

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

7 <= 5?

No!

[7, 2, 8, 1, 0, 3, 5]

[0]

[1]

[2]

[3]

[4]

[5]

[6]



pivot = 5

i = -1

j = 1

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

2 <= 5?

Yes!

[7, 2, 8, 1, 0, 3, 5]

[0]



[1]



[2]

[3]

[4]

[5]

[6]

pivot = 5

i = 0

j = 1

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

2 <= 5?
Yes!

[2, 7, 8, 1, 0, 3, 5]

[0]



[1]



[2]

[3]

[4]

[5]

[6]

pivot = 5

i = 0

j = 1

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

[2, 7, 8, 1, 0, 3, 5]

[0]



[1]

[2]



[3]

[4]

[5]

[6]

pivot = 5

i = 0

j = 2

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

[2, 7, 8, 1, 0, 3, 5]

[0]



[1]

[2]



[3]

[4]

[5]

[6]

pivot = 5

i = 0

j = 2

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

8 <= 5?

No!

[2, 7, 8, 1, 0, 3, 5]

[0]

[1]

[2]

[3]

[4]

[5]

[6]



pivot = 5

i = 0

j = 3

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

1 <= 5?
Yes!

[2, 7, 8, 1, 0, 3, 5]

[0]

[1]

[2]

[3]

[4]

[5]

[6]



pivot = 5

i = 1

j = 3

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```



`[0]`

`[1]`

`[2]`

`[3]`

`[4]`

`[5]`

`[6]`



pivot = 5

i = 1

j = 3

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

[2, 1, 8, 7, 0, 3, 5]

[0]

[1]

[2]

[3]

[4]

[5]

[6]



pivot = 5

i = 1

j = 4

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

0 <= 5?
Yes!

[2, 1, 8, 7, 0, 3, 5]

[0]

[1]

[2]

[3]

[4]

[5]

[6]



pivot = 5

i = 2

j = 4

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

[2, 1, 8, 7, 0, 3, 5]

[0]

[1]

[2]

[3]

[4]

[5]

[6]



pivot = 5

i = 2

j = 4

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

[2, 1, 0, 7, 8, 3, 5]

[0]

[1]

[2]

[3]

[4]

[5]

[6]



pivot = 5

i = 2

j = 4

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

[2, 1, 0, 7, 8, 3, 5]

[0]

[1]

[2]

[3]

[4]

[5]

[6]



pivot = 5

i = 2

j = 5

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

3 <= 5?
Yes!

[2, 1, 0, 7, 8, 3, 5]

[0]

[1]

[2]

[3]

[4]

[5]

[6]



pivot = 5

i = 3

j = 5

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```


[2, 1, 0, 7, 8, 3, 5]

[0]

[1]

[2]

[3]

[4]

[5]

[6]



pivot = 5

i = 3

j = 5

```
def partition(lst, low, high):  
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    for j in range(low, high):  
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            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

[2, 1, 0, 7, 8, 3, 5]

[0]

[1]

[2]

[3]

[4]

[5]

[6]



pivot = 5

i = 3

j = 5

```
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[2, 1, 0, 3, 8, 7, 5]

[0]

[1]

[2]

[3]

[4]

[5]

[6]



pivot = 5

i = 3

j = 5

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            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

[2, 1, 0, 3, 8, 7, 5]

[0]

[1]

[2]

[3]

[4]

[5]

[6]



Stop

pivot = 5

i = 3

j = 5

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
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[2, 1, 0, 3, 8, 7, 5]

[0]

[1]

[2]

[3]

[4]

[5]

[6]



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    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

[2, 1, 0, 3, 8, 7, 5]

[0]

[1]

[2]

[3]

[4]

[5]

[6]



pivot = 5

i = 3

j = 5

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            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

[2, 1, 0, 3, 5, 7, 8]

[0]

[1]

[2]

[3]

[4]

[5]

[6]



pivot = 5

i = 3

j = 5

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

return 4

```
quicksort(a, 0, len(a)-1)
```

2	1	0	3	5	7	8
[0]	[1]	[2]	[3]	[4]	[5]	[6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

4

2	1	0	3	5	7	8
[0]	[1]	[2]	[3]	[4]	[5]	[6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

```
quicksort(a, 0, len(a)-1)
```



```
quicksort(lst, 0, 3)
```

2	1	0	3	5	7	8
[0]	[1]	[2]	[3]	[4]	[5]	[6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

```
quicksort(a, 0, len(a)-1)
```



<waiting recursive call>

```
quicksort(lst, 0, 3)
```

2	1	0	3	5	7	8
[0]	[1]	[2]	[3]	[4]	[5]	[6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

```
quicksort(a, 0, len(a)-1)
```



<waiting recursive call>

```
quicksort(lst, 0, 3)
```

[2, 1, 0, 3, 5, 7, 8]
[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

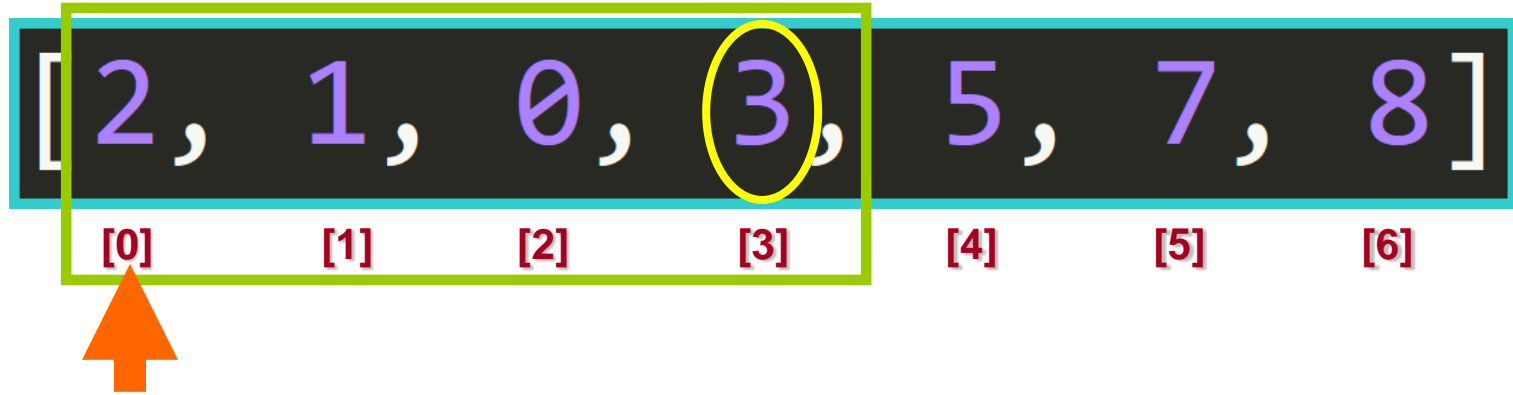
quicksort(a, 0, len(a)-1)



<waiting recursive call>

quicksort(lst, 0, 3)



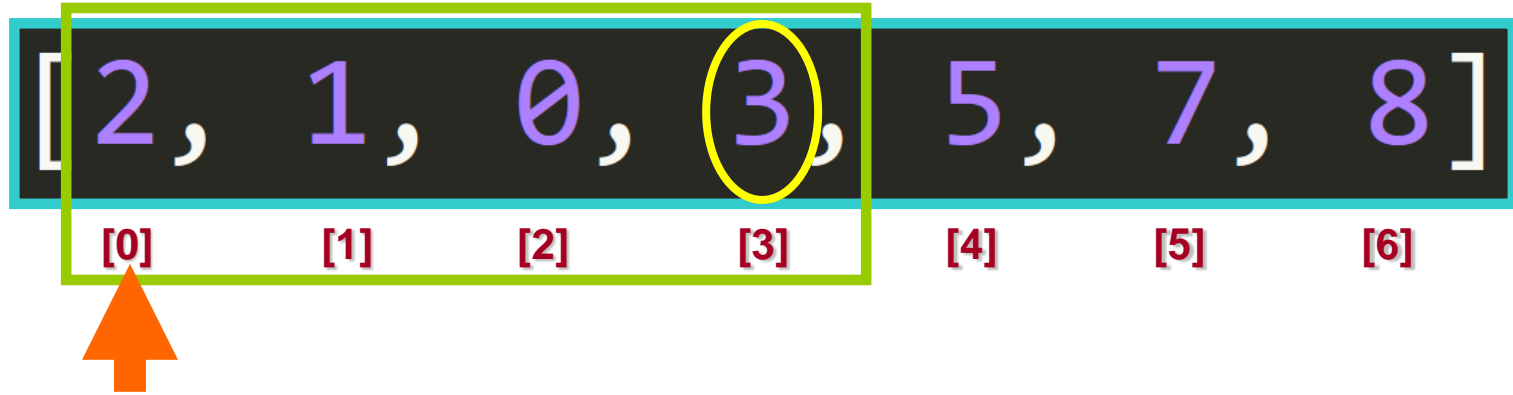


pivot = 3

i = -1

j = 0

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```



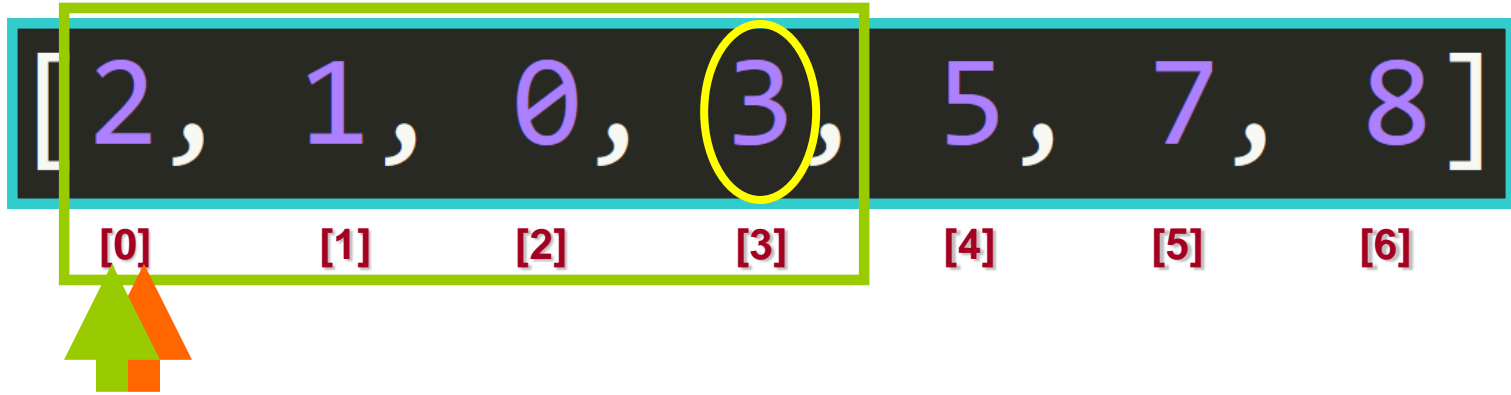
pivot = 3

i = -1

j = 0

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

2 <= 3?
Yes!

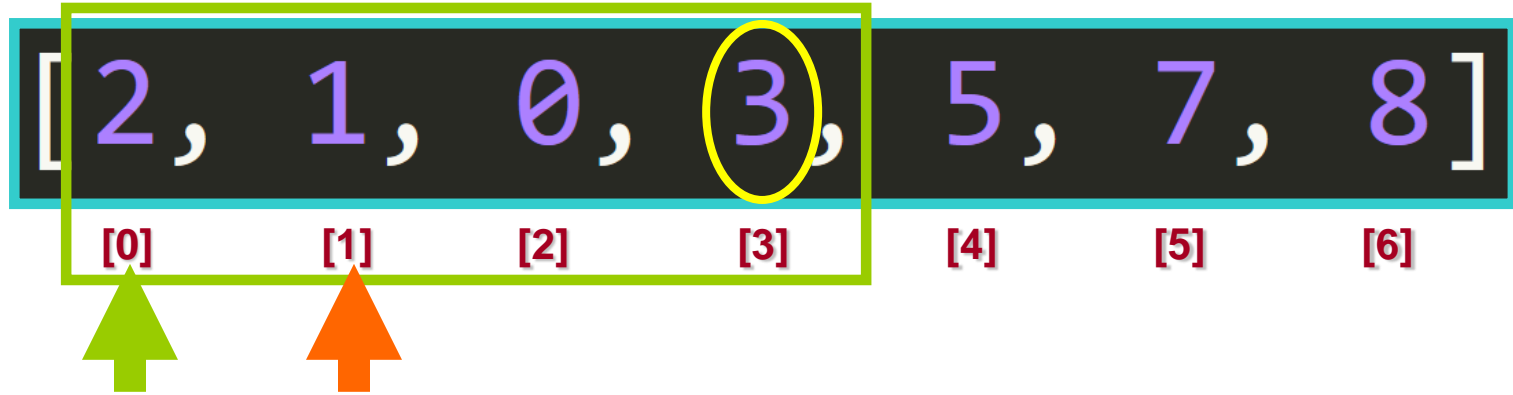


pivot = 3

i = 0

j = 0

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```



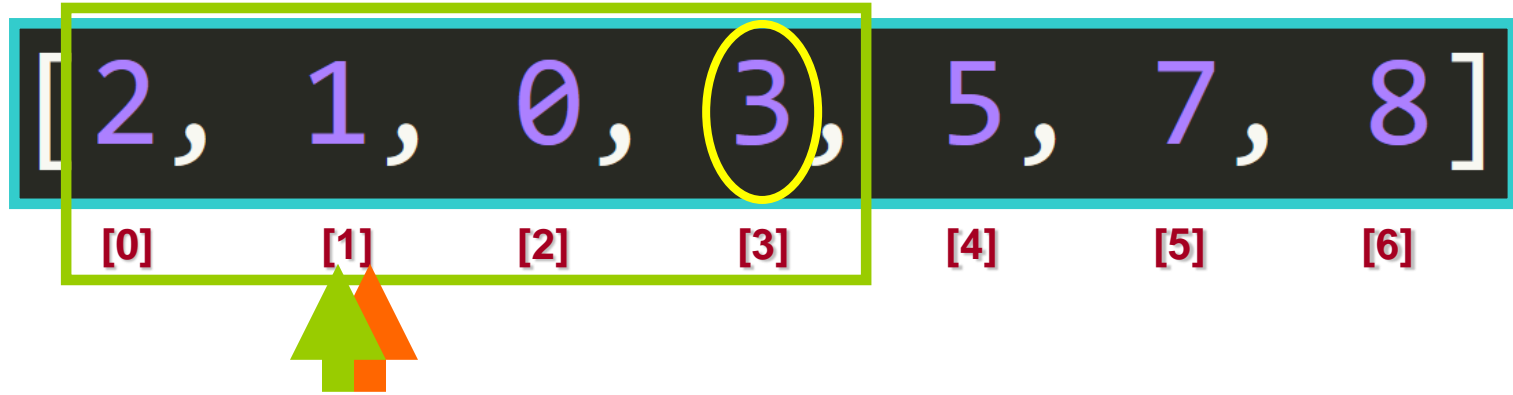
pivot = 3

i = 0

j = 1

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

1 <= 3?
Yes!

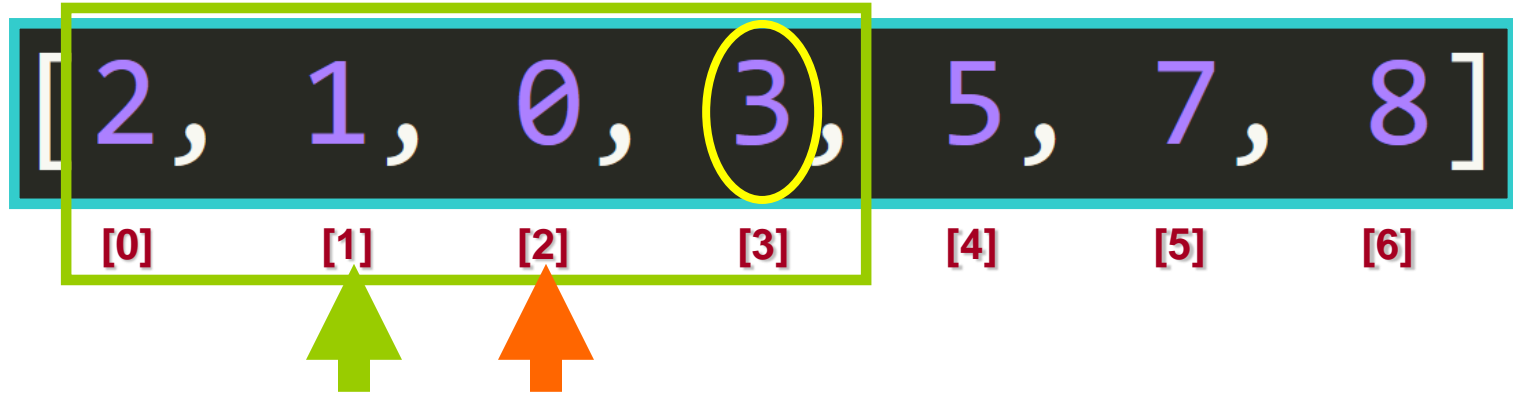


pivot = 3

i = 1

j = 1

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```



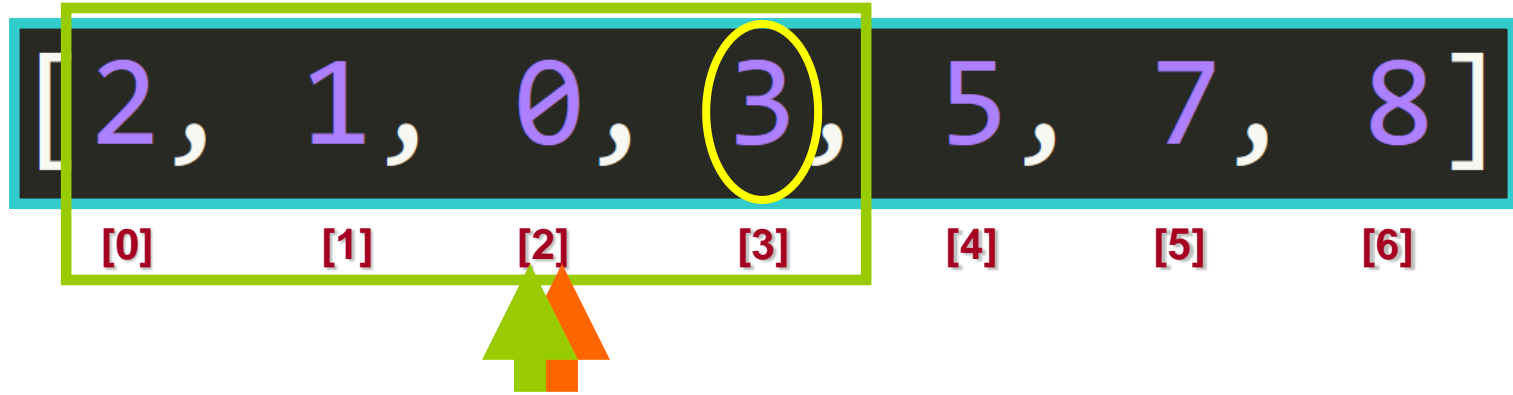
pivot = 3

i = 1

j = 2

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

0 <= 3?
Yes!

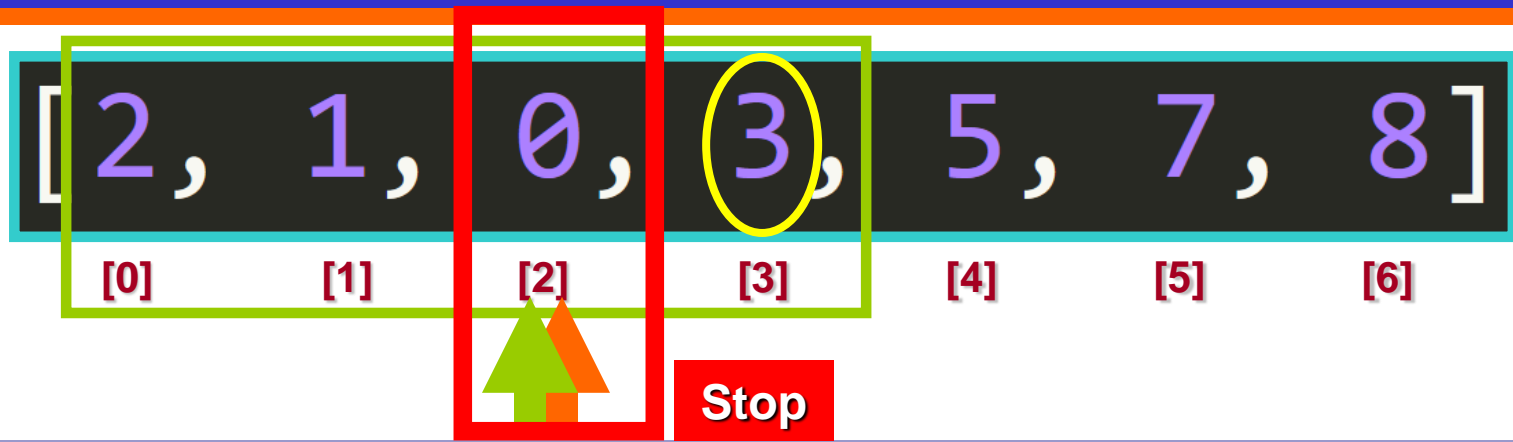


pivot = 3

i = 1

j = 2

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

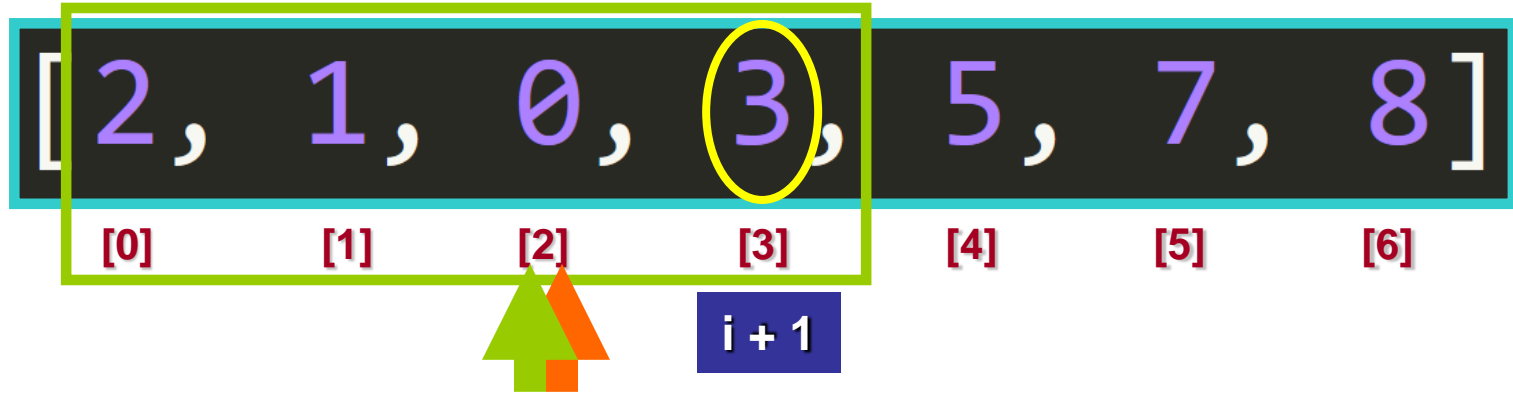


pivot = 3

i = 1

j = 2

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

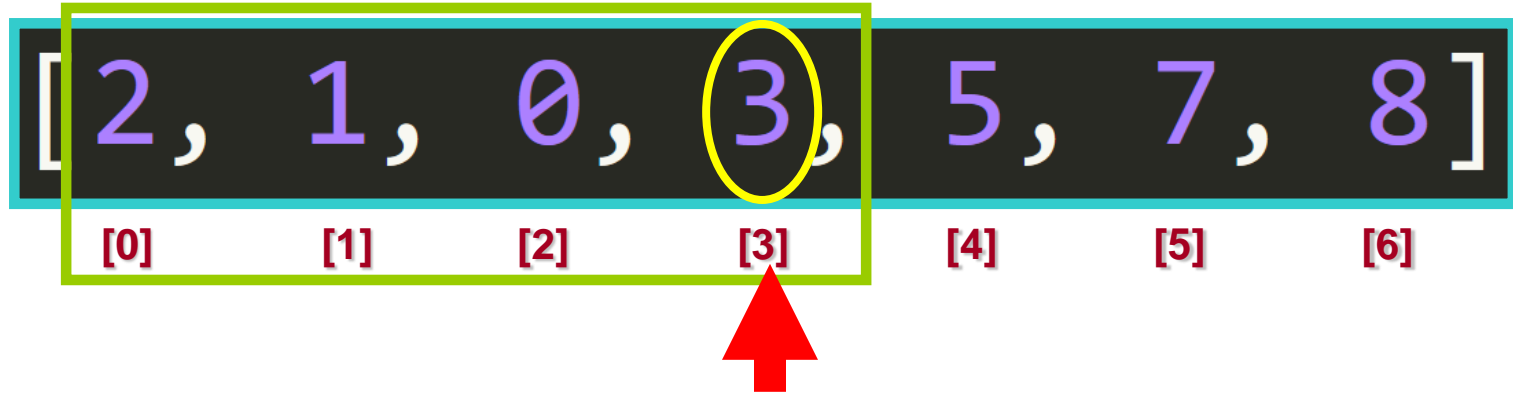


pivot = 3

i = 1

j = 2

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```



pivot = 3

i = 1

j = 2

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

return 3

[2, 1, 0, 3, 5, 7, 8]
[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)



[2, 1, 0, 3, 5, 7, 8]
[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)

<waiting recursive call>

quicksort(lst, 0, 2)

[2, 1, 0, 3, 5, 7, 8]
[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

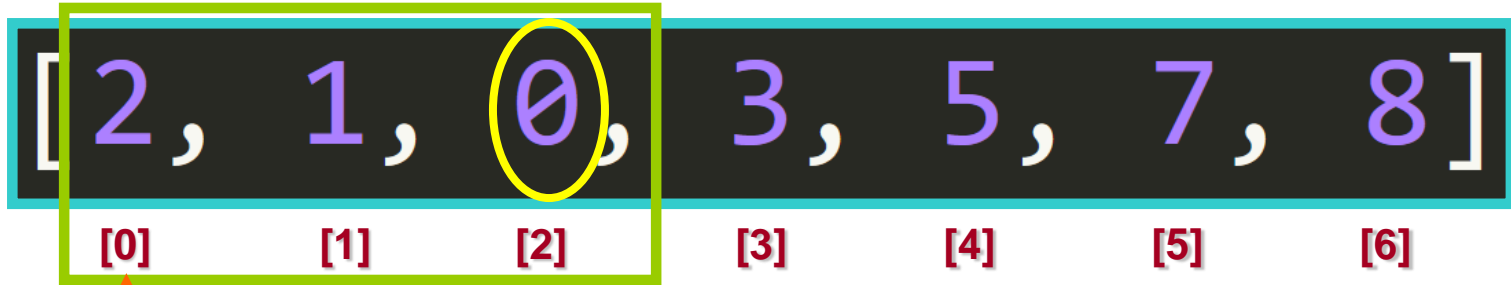
quicksort(lst, 0, 3)

<waiting recursive call>

quicksort(lst, 0, 2)



Partition...

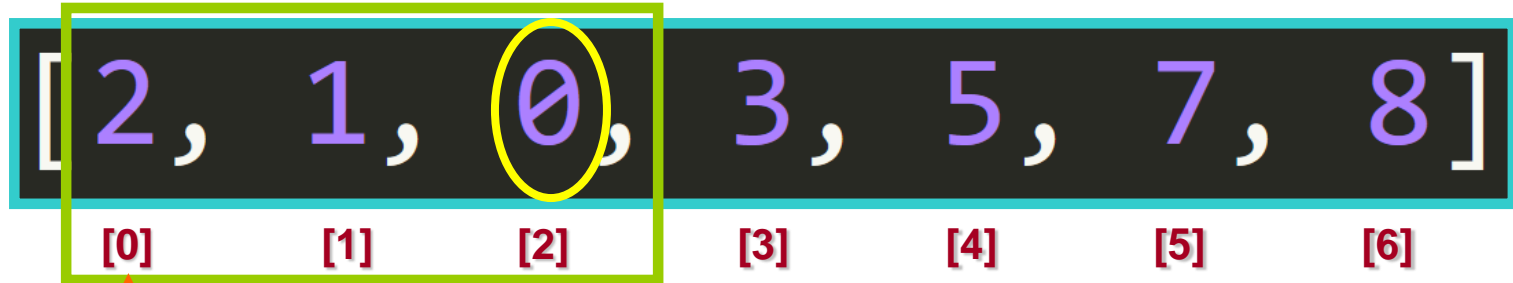


pivot = 0

i = -1

j = 0

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```



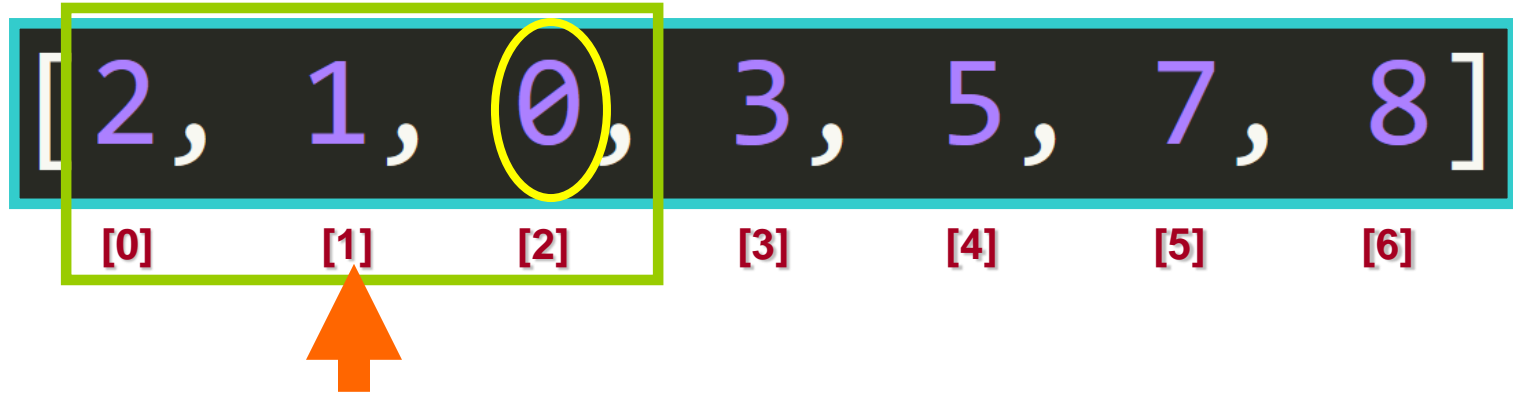
pivot = 0

i = -1

j = 0

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

2 <= 0?
No!

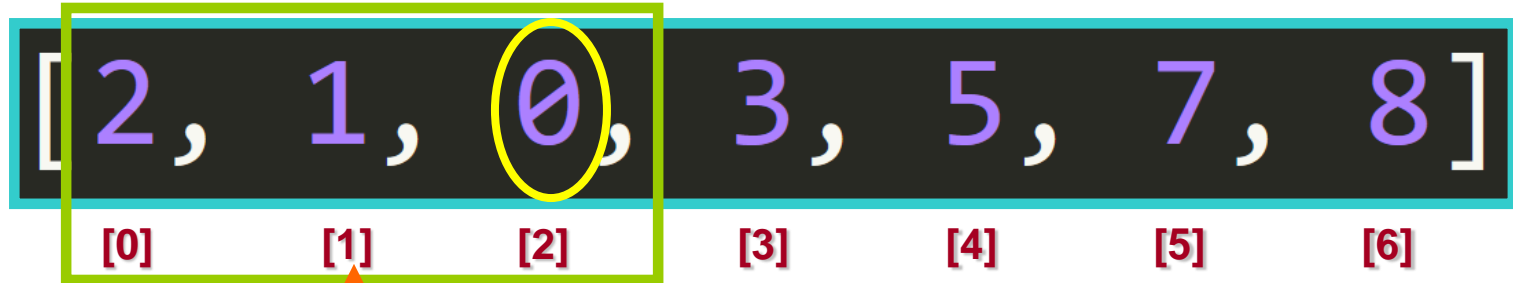


pivot = 0

i = -1

j = 1

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```



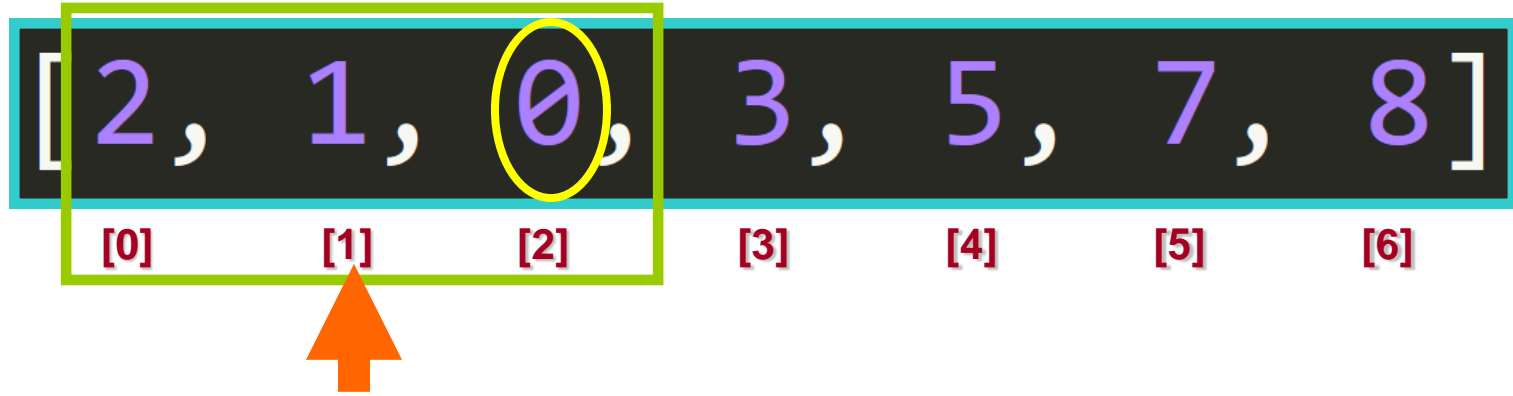
pivot = 0

i = -1

j = 1

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

1 <= 0?
No!



pivot = 0

i = -1

j = 1

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```



pivot = 0

i = -1

j = 1

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```



pivot = 0

i = -1

j = 1

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```


[0, 1, 2, 3, 5, 7, 8]

[0]

[1]

[2]

[3]

[4]

[5]

[6]

pivot = 0

i = -1

j = 1

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

return 0

[0, 1, 2, 3, 5, 7, 8]
[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)

<waiting recursive call>

quicksort(lst, 0, 2)

0

[0, 1, 2, 3, 5, 7, 8]
[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)

<waiting recursive call>

quicksort(lst, 0, 2)

<waiting recursive call>

quicksort(lst, 0, -1)

Stop!

[0, 1, 2, 3, 5, 7, 8]
[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)

<waiting recursive call>

quicksort(lst, 0, 2)

quicksort(lst, 0, -1)

quicksort(lst, 1, 2)

Partition...

[0, 1, 2, 3, 5, 7, 8]
[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)

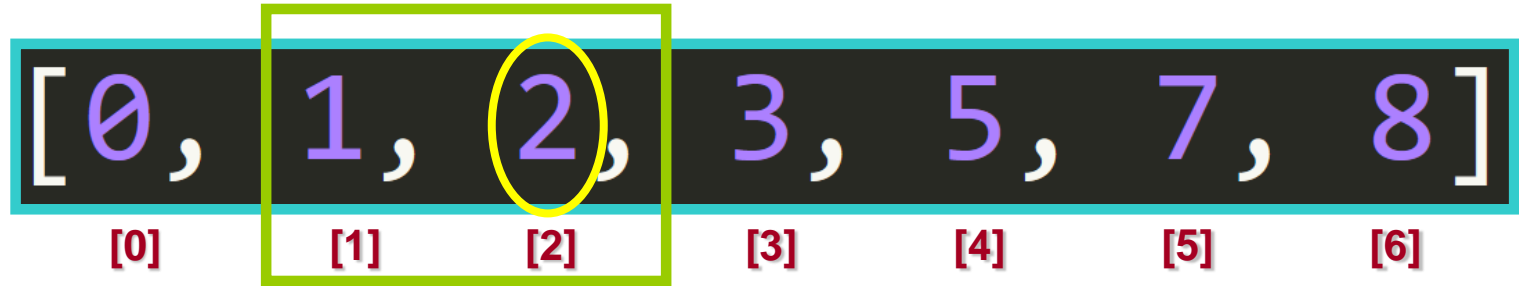
<waiting recursive call>

quicksort(lst, 0, 2)

quicksort(lst, 0, -1)

quicksort(lst, 1, 2)

Partition...

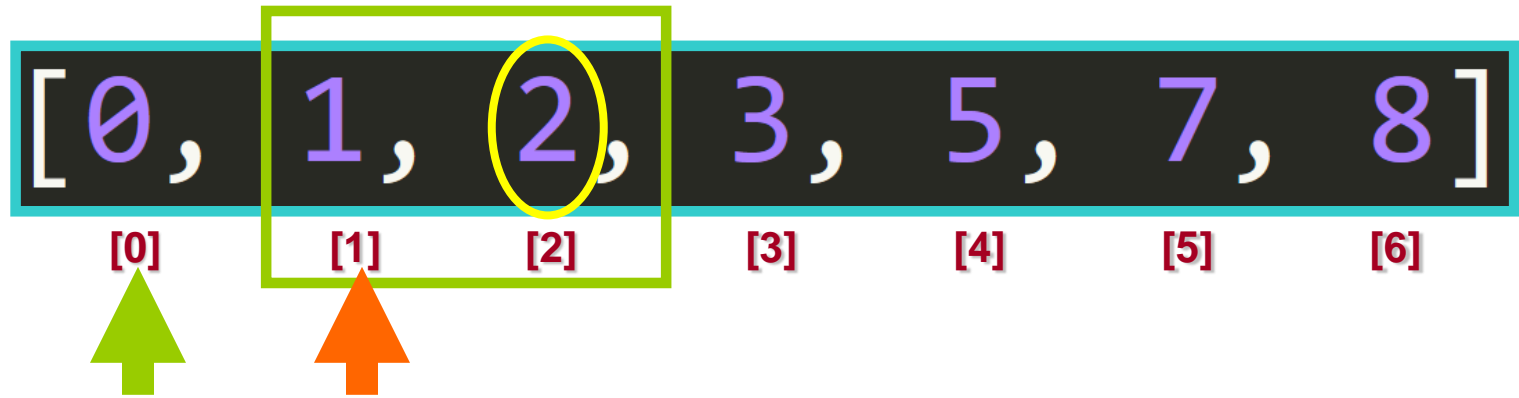


pivot = 0

i = 0

j = 1

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```



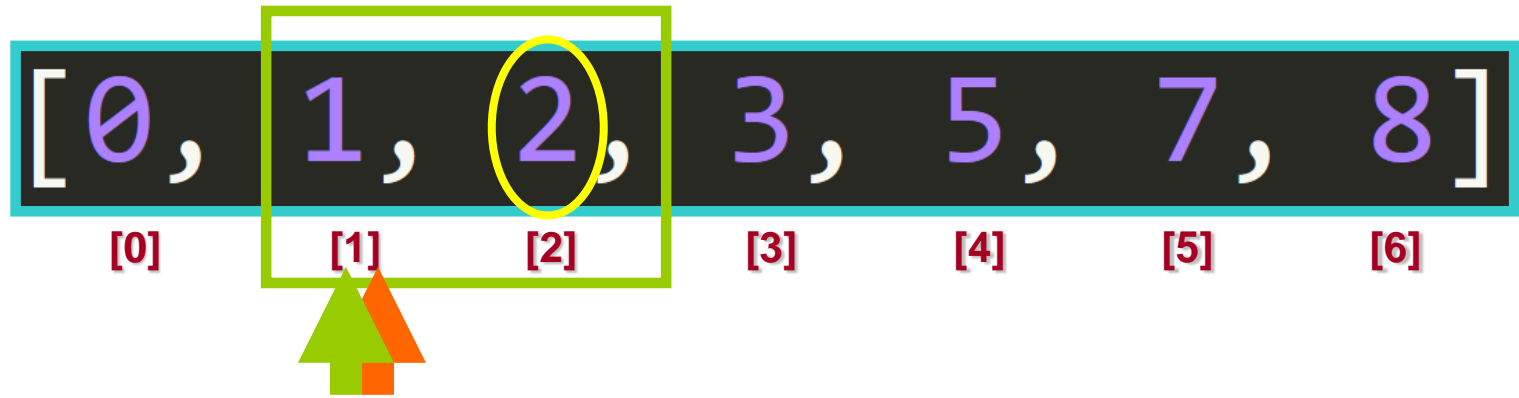
pivot = 0

i = 0

j = 1

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

1 <= 2?
Yes!



pivot = 0

i = 0

j = 1

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

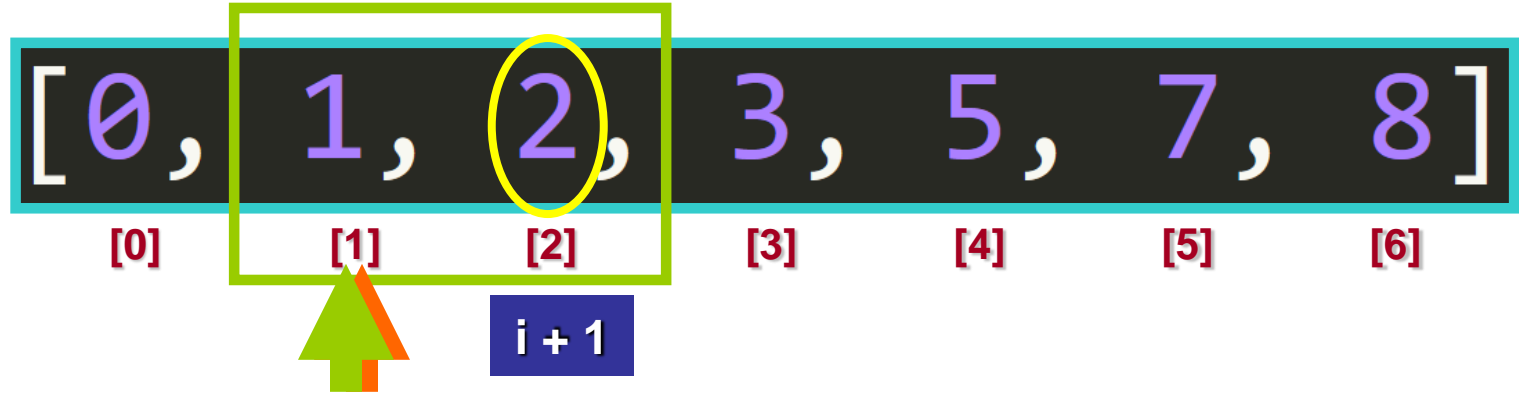



pivot = 0

i = 0

j = 1

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```



pivot = 0

i = 0

j = 1

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

[0, 1, 2, 3, 5, 7, 8]

[0] [1] [2] [3] [4] [5] [6]



pivot = 0

i = 0

j = 1

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

return 2

[0, 1, 2, 3, 5, 7, 8]
[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)

<waiting recursive call>

quicksort(lst, 0, 2)

quicksort(lst, 0, -1)

quicksort(lst, 1, 2)

quicksort(lst, 1, 1)

Stop!

[0, 1, 2, 3, 5, 7, 8]
[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)

<waiting recursive call>

quicksort(lst, 0, 2)

quicksort(lst, 0, -1)

quicksort(lst, 1, 2)

quicksort(lst, 1, 1)

quicksort(lst, 3, 2)

Stop!

[0, 1, 2, 3, 5, 7, 8]

[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)

quicksort(lst, 0, 2)

quicksort(lst, 4, 3)

Stop!

[0]	[1]	[2]	[3]	[4]	[5]	[6]
0	1	2	3	5	7	8

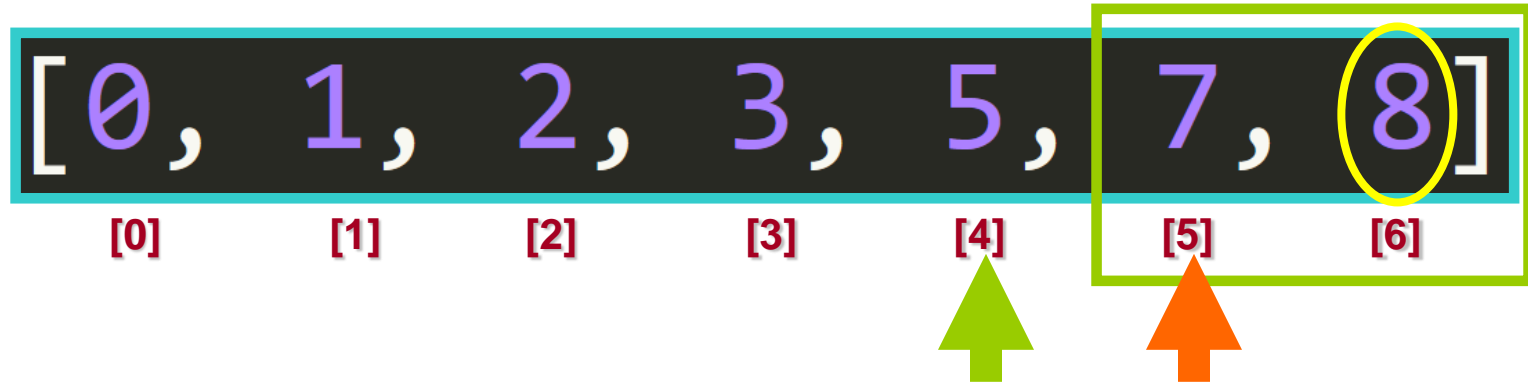
```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

quicksort(lst, 0, 3)

quicksort(lst, 5, 6)



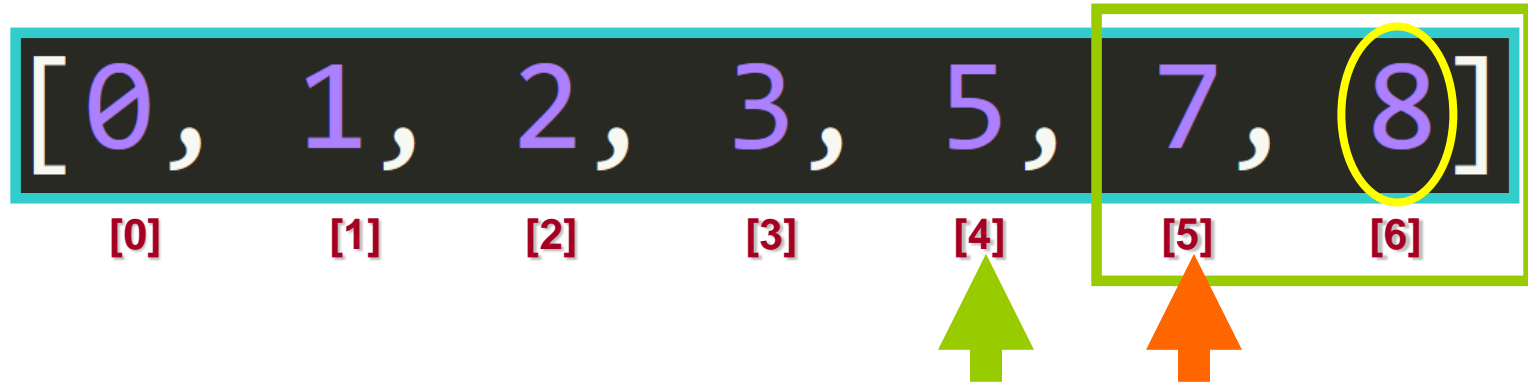


pivot = 8

i = 4

j = 5

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

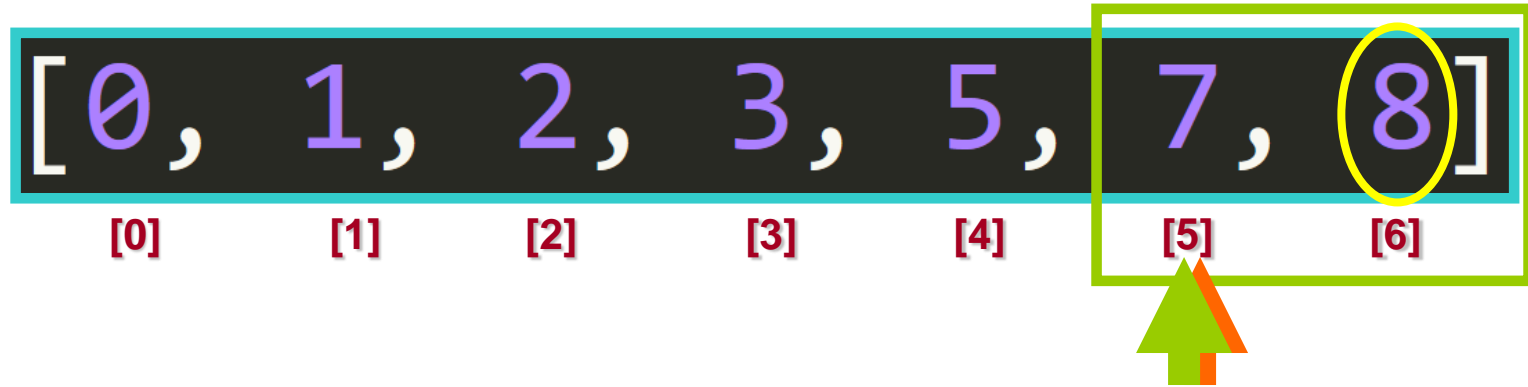
pivot = 8

i = 4

j = 5

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

7 <= 8?
Yes!

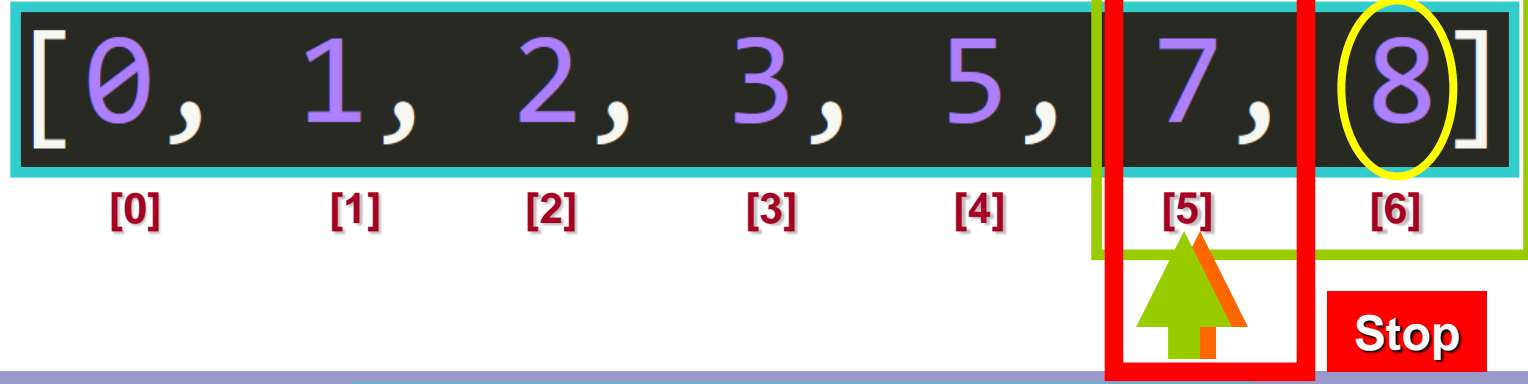


pivot = 8

i = 5

j = 5

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

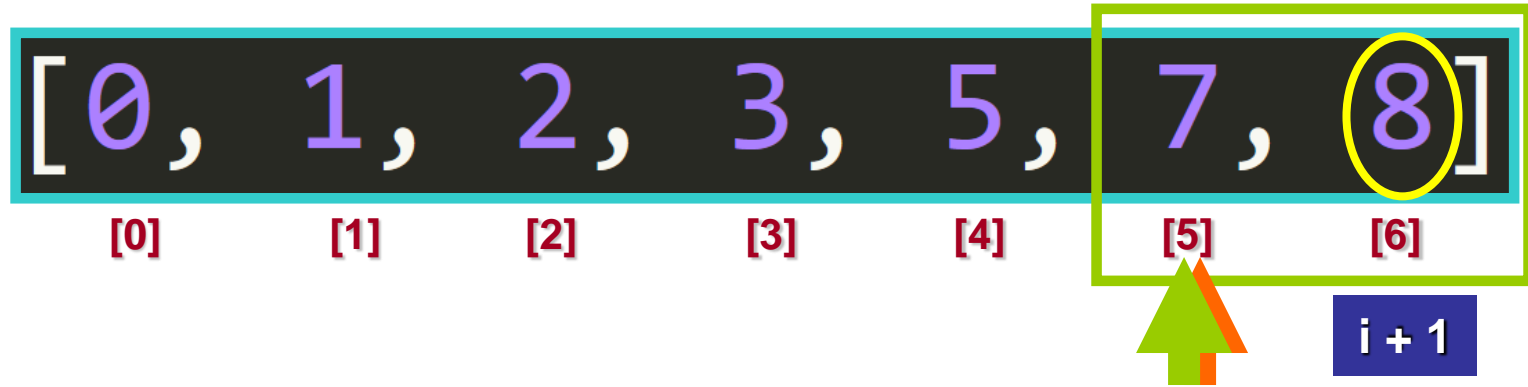


pivot = 8

i = 5

j = 5

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

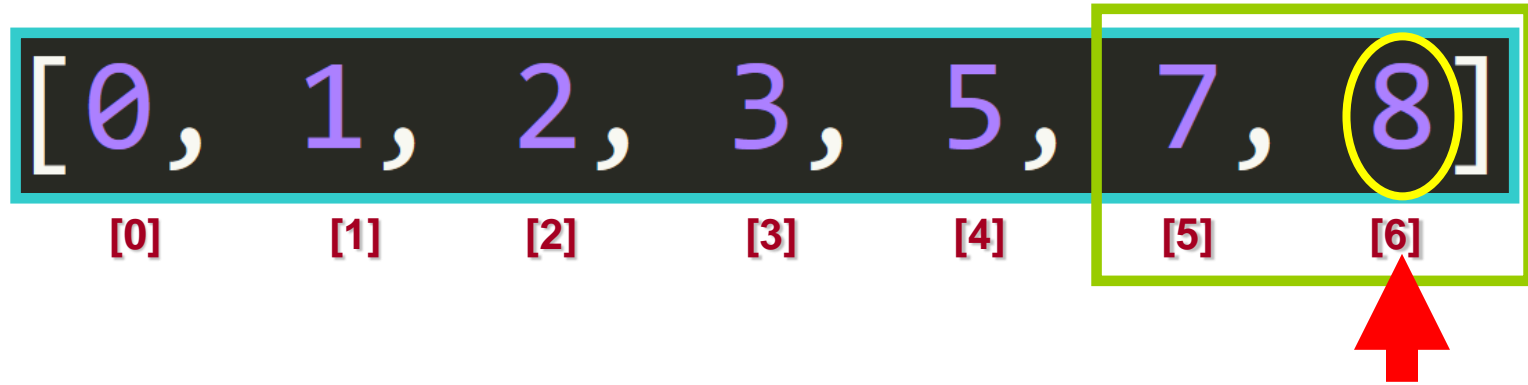


pivot = 8

i = 5

j = 5

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```



pivot = 8

i = 5

j = 5

```
def partition(lst, low, high):  
    pivot = lst[high]  
  
    i = low - 1  
  
    for j in range(low, high):  
        if lst[j] <= pivot:  
            i += 1  
            lst[i], lst[j] = lst[j], lst[i]  
  
    lst[i+1], lst[high] = lst[high], lst[i+1]  
    return i+1
```

return 6

[0, 1, 2, 3, 5, 7, 8]

[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

quicksort(lst, 0, 3)

quicksort(lst, 5, 6)

quicksort(lst, 5, 5)

Stop!

[0, 1, 2, 3, 5, 7, 8]

[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

quicksort(lst, 0, 3)

quicksort(lst, 5, 6)

quicksort(lst, 5, 5)

quicksort(lst, 7, 6)

Stop!



Quicksort

[0, 1, 2, 3, 5, 7, 8]

Sorted!

1 $f([7, 2, 8, 1, 0, 3, 5], 0, 6)$
After partition: $[2, 1, 0, 3, 5, 7, 8]$

2 $f([2, 1, 0, 3, 5, 7, 8], 0, 3)$
After partition: $[2, 1, 0, 3, 5, 7, 8]$

9 $f([0, 1, 2, 3, 5, 7, 8], 5, 6)$
After partition: $[0, 1, 2, 3, 5, 7, 8]$

3 $f([2, 1, 0, 3, 5, 7, 8], 0, 2)$
After partition: $[0, 1, 2, 3, 5, 7, 8]$

8 $f([0, 1, 2, 3, 5, 7, 8], 4, 3)$
After partition: $[0, 1, 2, 3, 5, 7, 8]$

10 $f([0, 1, 2, 3, 5, 7, 8], 5, 5)$
Not a valid interval

11 $f([0, 1, 2, 3, 5, 7, 8], 7, 6)$
Not a valid interval

4 Not a valid interval
5 $f([0, 1, 2, 3, 5, 7, 8], 1, 2)$
After partition: $[0, 1, 2, 3, 5, 7, 8]$

6 $f([0, 1, 2, 3, 5, 7, 8], 1, 1)$ Not a valid interval
7 $f([0, 1, 2, 3, 5, 7, 8], 3, 2)$ Not a valid interval

Note: for illustration purposes, f = quicksort



To the Details

