

# Algorithm

# Quicksort

## Code Walkthrough

`quicksort()`





## Quicksort

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```





## Quicksort



[7, 2, 8, 1, 0, 3, 5]

[0] [1] [2] [3] [4] [5] [6]

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```

```
a = [7, 2, 8, 1, 0, 3, 5]
```

```
quicksort(a, 0, len(a)-1)
```

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quicksort(a, 0, len(a)-1)
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quicksort(a, 0, len(a)-1)
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[7, 2, 8, 1, 0, 3, 5]

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quicksort(a, 0, len(a)-1)





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quicksort(a, 0, len(a)-1)
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```
[2, 1, 0, 3, 5, 7, 8]
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4

2	1	0	3	5	7	8
[0]	[1]	[2]	[3]	[4]	[5]	[6]

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        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

```
quicksort(a, 0, len(a)-1)
```



```
quicksort(lst, 0, 3)
```

2	1	0	3	5	7	8
[0]	[1]	[2]	[3]	[4]	[5]	[6]

```
def quicksort(lst, low, high):  
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        quicksort(lst, pivot_index+1, high)
```

```
quicksort(a, 0, len(a)-1)
```



<waiting recursive call>

```
quicksort(lst, 0, 3)
```

2	1	0	3	5	7	8
[0]	[1]	[2]	[3]	[4]	[5]	[6]

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def quicksort(lst, low, high):  
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quicksort(a, 0, len(a)-1)
```



<waiting recursive call>

```
quicksort(lst, 0, 3)
```

[2, 1, 0, 3, 5, 7, 8]  
[0] [1] [2] [3] [4] [5] [6]

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```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)



[2, 1, 0, 3, 5, 7, 8]  
[0] [1] [2] [3] [4] [5] [6]

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```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)



[ 2, 1, 0, 3, 5, 7, 8 ]  
[0] [1] [2] [3] [4] [5] [6]

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def quicksort(lst, low, high):  
    if low < high:  
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        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)

<waiting recursive call>

quicksort(lst, 0, 2)

[2, 1, 0, 3, 5, 7, 8]  
[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
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```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)

<waiting recursive call>

quicksort(lst, 0, 2)





[0, 1, 2, 3, 5, 7, 8]  
[0] [1] [2] [3] [4] [5] [6]

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        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)

<waiting recursive call>

quicksort(lst, 0, 2)

0

[0, 1, 2, 3, 5, 7, 8]  
[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)

<waiting recursive call>

quicksort(lst, 0, 2)

<waiting recursive call>

quicksort(lst, 0, -1)

**Stop!**

[0, 1, 2, 3, 5, 7, 8]  
[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)

<waiting recursive call>

quicksort(lst, 0, 2)

quicksort(lst, 0, -1)

quicksort(lst, 1, 2)

Partition...

[0, 1, 2, 3, 5, 7, 8]  
[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)

<waiting recursive call>

quicksort(lst, 0, 2)

quicksort(lst, 0, -1)

quicksort(lst, 1, 2)

Partition...

[0, 1, 2, 3, 5, 7, 8]  
[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)

<waiting recursive call>

quicksort(lst, 0, 2)

quicksort(lst, 0, -1)

quicksort(lst, 1, 2)

quicksort(lst, 1, 1)

**Stop!**

[0, 1, 2, 3, 5, 7, 8]  
[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)

<waiting recursive call>

quicksort(lst, 0, 2)

quicksort(lst, 0, -1)

quicksort(lst, 1, 2)

quicksort(lst, 1, 1)

quicksort(lst, 3, 2)

Stop!

[0, 1, 2, 3, 5, 7, 8]

[0] [1] [2] [3] [4] [5] [6]

```
def quicksort(lst, low, high):  
    if low < high:  
        pivot_index = partition(lst, low, high)  
        quicksort(lst, low, pivot_index-1)  
        quicksort(lst, pivot_index+1, high)
```

quicksort(a, 0, len(a)-1)

<waiting recursive call>

quicksort(lst, 0, 3)

quicksort(lst, 0, 2)

quicksort(lst, 4, 3)

**Stop!**

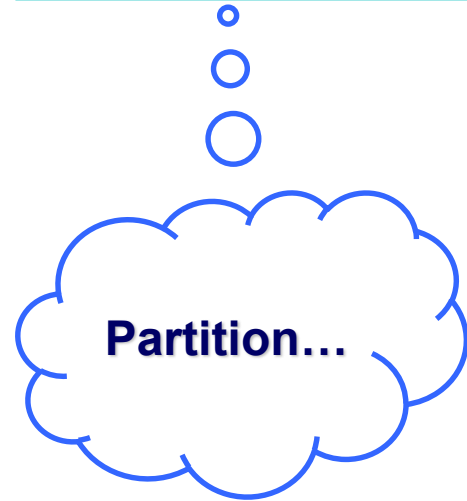
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[0]	[1]	[2]	[3]	[4]	[5]	[6]

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```

quicksort(a, 0, len(a)-1)

quicksort(lst, 0, 3)

quicksort(lst, 5, 6)





[0, 1, 2, 3, 5, 7, 8]

[0] [1] [2] [3] [4] [5] [6]

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        quicksort(lst, low, pivot_index-1)  
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```

quicksort(a, 0, len(a)-1)

quicksort(lst, 0, 3)

quicksort(lst, 5, 6)

quicksort(lst, 5, 5)

**Stop!**

[0, 1, 2, 3, 5, 7, 8]

[0] [1] [2] [3] [4] [5] [6]

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def quicksort(lst, low, high):  
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```

quicksort(a, 0, len(a)-1)

quicksort(lst, 0, 3)

quicksort(lst, 5, 6)

quicksort(lst, 5, 5)

quicksort(lst, 7, 6)

**Stop!**



## Quicksort

[0, 1, 2, 3, 5, 7, 8]

**Sorted!**

1  $f([7, 2, 8, 1, 0, 3, 5], 0, 6)$   
After partition:  $[2, 1, 0, 3, 5, 7, 8]$

2  $f([2, 1, 0, 3, 5, 7, 8], 0, 3)$   
After partition:  $[2, 1, 0, 3, 5, 7, 8]$

9  $f([0, 1, 2, 3, 5, 7, 8], 5, 6)$   
After partition:  $[0, 1, 2, 3, 5, 7, 8]$

3  $f([2, 1, 0, 3, 5, 7, 8], 0, 2)$   
After partition:  $[0, 1, 2, 3, 5, 7, 8]$

8  $f([0, 1, 2, 3, 5, 7, 8], 4, 3)$   
After partition:  $[0, 1, 2, 3, 5, 7, 8]$

10  $f([0, 1, 2, 3, 5, 7, 8], 5, 5)$   
Not a valid interval

11  $f([0, 1, 2, 3, 5, 7, 8], 7, 6)$   
Not a valid interval

4 Not a valid interval  
5  $f([0, 1, 2, 3, 5, 7, 8], 1, 2)$   
After partition:  $[0, 1, 2, 3, 5, 7, 8]$

6  $f([0, 1, 2, 3, 5, 7, 8], 1, 1)$  Not a valid interval  
7  $f([0, 1, 2, 3, 5, 7, 8], 3, 2)$  Not a valid interval

Note: for illustration purposes,  $f$  = quicksort



To partition()

