



Algorithm: Insertion Sort





Insertion Sort



Key Aspects:

- In-place comparison sort.
- The algorithm divides the list into two portions: sorted and unsorted.
- Selects the minimum element and “inserts it” at the right position in the sorted portion of the list.
- Inefficient for large lists.
- Efficient for small or mostly sorted lists.

**The list is
sorted in
ascending
order**

Algorithm:

- The sorted portion of the list initially contains one element (at index 0).
- Select the first element of the unsorted portion of the list.
- Insert this element at the right position in the sorted portion of the list.
- To do this, you might need to “move” to the right all the elements that are greater than the element that is being inserted.
- Expand the sorted portion.
- Repeat these steps until the process is completed. The final output is a sorted list.

Time Complexity:

- Worst-Case Time Complexity: Quadratic $O(n^2)$
- Average-Case Time Complexity: Quadratic $O(n^2)$
- Best-Case Time Complexity: Linear $O(n)$

**Insertion Sort
=
Insert the
elements one by one**

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Insertion Sort



Code:

```
def insertion_sort(lst):
    # For every element in the list (except the first one).
    for i in range(1, len(lst)):
        # Select the first element of the unsorted portion of the list.
        elem_selected = lst[i]

        # Check the elements in the sorted portion
        # and move them one index to the right if they
        # are greater than the element selected.
        while i > 0 and elem_selected < lst[i-1]:
            lst[i] = lst[i-1]
            i -= 1

        # Insert the element where it belongs.
        lst[i] = elem_selected
```

Example:

```
>>> insertion_sort([5, 1, 3])
```

=====> Starting Insertion Sort

---> Outer loop. Iteration #1 (i = 1)

Sorted portion: [5]

Unsorted portion: [1, 3]

We need to find the correct spot for: 1.

1 is the first element in the unsorted portion.

Now let's compare 1 with the elements of the sorted portion.

Let's find where it belongs...

-> Inner loop

Is the element selected 1 smaller than 5?

Yes, it is! So we need to move 5 to the right to make room for 1

Moving 5 from index 0 to index 1 (see below)

Old list: [5, 1, 3]

New list: [5, 5, 3]

See how 5 is now at index 1

Bingo!

We've found the right location for 1: index 0

The list is now: [1, 5, 3]

---> Outer loop. Iteration #2 (i = 2)

Sorted portion: [1, 5]

Unsorted portion: [3]

We need to find the correct spot for: 3.

3 is the first element in the unsorted portion.

Now let's compare 3 with the elements of the sorted portion.

Let's find where it belongs...

-> Inner loop

Is the element selected 3 smaller than 5?

Yes, it is! So we need to move 5 to the right to make room for 3

Moving 5 from index 1 to index 2 (see below)

Old list: [1, 5, 3]

New list: [1, 5, 5]

See how 5 is now at index 2

Is the element selected (3) smaller than 1?

No, it isn't! We need to stay where we are, at index 1.

The element 3 should be there.

Bingo!

We've found the right location for 3: index 1

The list is now: [1, 3, 5]

The list is now sorted!





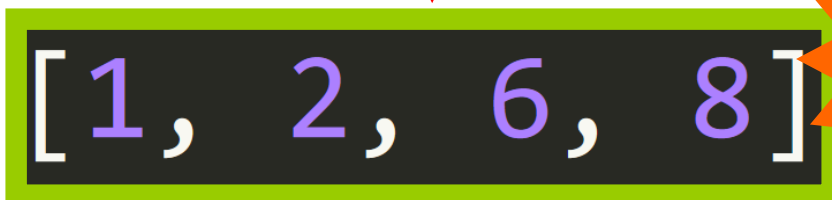
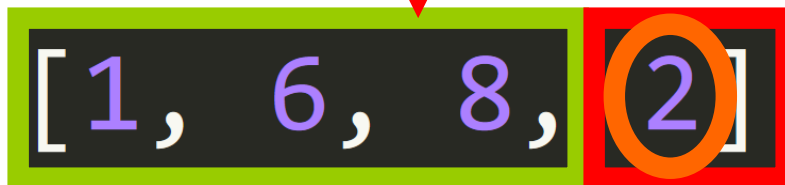
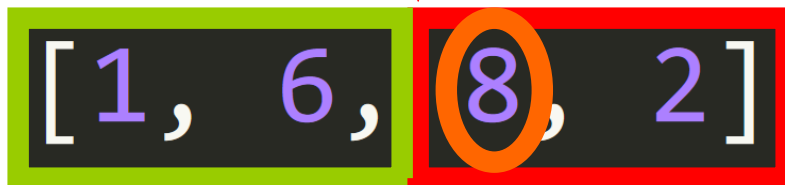
Insertion Sort



Example: `>>> insertion_sort([6, 1, 8, 2])`



sorted unsorted element



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Insertion Sort



Example:

```
>>> insertion_sort([6, 1, 8, 2])
```

```
=====> Starting Insertion Sort
```

```
---> Outer loop. Iteration #1 (i = 1)
```

```
Sorted portion: [6]
```

```
Unsorted portion: [1, 8, 2]
```

We need to find the correct spot for: 1.

1 is the first element in the unsorted portion.

Now let's compare 1 with the elements of the sorted portion.

Let's find where it belongs...

-> Inner loop

Is the element selected 1 smaller than 6?

Yes, it is! So we need to move 6 to the right to make room for 1

Moving 6 from index 0 to index 1 (see below)

Old list: [6, 1, 8, 2]

New list: [6, 6, 8, 2]

See how 6 is now at index 1

Bingo!

We've found the right location for 1: index 0

The list is now: [1, 6, 8, 2]





Insertion Sort



Example:

```
---> Outer loop. Iteration #2 (i = 2)
Sorted portion: [1, 6]
Unsorted portion: [8, 2]
```

```
We need to find the correct spot for: 8.
8 is the first element in the unsorted portion.
Now let's compare 8 with the elements of the sorted portion.
Let's find where it belongs...
```

```
Is the element selected (8) smaller than 6?
No, it isn't! We need to stay where we are, at index 2.
The element 8 should be there.
```

```
Bingo!
We've found the right location for 8: index 2
The list is now: [1, 6, 8, 2]
```

```
---> Outer loop. Iteration #3 (i = 3)
Sorted portion: [1, 6, 8]
Unsorted portion: [2]
```

```
We need to find the correct spot for: 2.
2 is the first element in the unsorted portion.
Now let's compare 2 with the elements of the sorted portion.
Let's find where it belongs...
```

```
-> Inner loop
Is the element selected 2 smaller than 8?
Yes, it is! So we need to move 8 to the right to make room for 2
Moving 8 from index 2 to index 3 (see below)
Old list: [1, 6, 8, 2]
New list: [1, 6, 8, 8]
See how 8 is now at index 3
```

```
-> Inner loop
Is the element selected 2 smaller than 6?
Yes, it is! So we need to move 6 to the right to make room for 2
Moving 6 from index 1 to index 2 (see below)
Old list: [1, 6, 8, 8]
New list: [1, 6, 6, 8]
See how 6 is now at index 2
```

```
Is the element selected (2) smaller than 1?
No, it isn't! We need to stay where we are, at index 1.
The element 2 should be there.
```

```
Bingo!
We've found the right location for 2: index 1
The list is now: [1, 2, 6, 8]
The list is now sorted!
```

