

SORTING ALGORITHMS

SHELL SORT



Shell sort

- ▶ Another quadratic running time sorting algorithm
- ▶ It is the generalization of the insertion sort
- ▶ Insertion sort → sometimes we have to make lots of shifts / swaps
- ▶ This feature is not so good → that's why shell sort came to be as an enhanced insertion sort
- ▶ The method starts by sorting pairs of elements far apart from each other
- ▶ Then progressively reducing the gap between elements to be compared
- ▶ Starting with far apart elements can move some out-of-place elements into position faster than a simple nearest neighbor exchange

Shell sort

- ▶ Shell sort is heavily dependent on the gap sequence it uses
- ▶ Consider every h -th element in the array
- ▶ Such a subarray is said to be h -sorted
- ▶ We use insertion sort as a subprocedure → the only difference is that we start sorting items far away from each other
- ▶ This rearrangement allows elements to move long distances in the original list → reducing large amounts of disorder quickly

Shell sort

- ▶ Unstable → it changes the relative order of elements with equal value
- ▶ Because it relies heavily on insertion sort → it is also an adaptive algorithm so runs faster on partially sorted input
- ▶ Not so popular algorithm nowadays !!!

Shell sort

```
shellSort(array)
```

```
  for every gap in gaps
```

```
    for i=gap to n
```

```
      temp = array[i]
```

```
      for j=i and j >= gap and array[j-gap] > temp
```

```
        array[j] = array[j-gap]
```

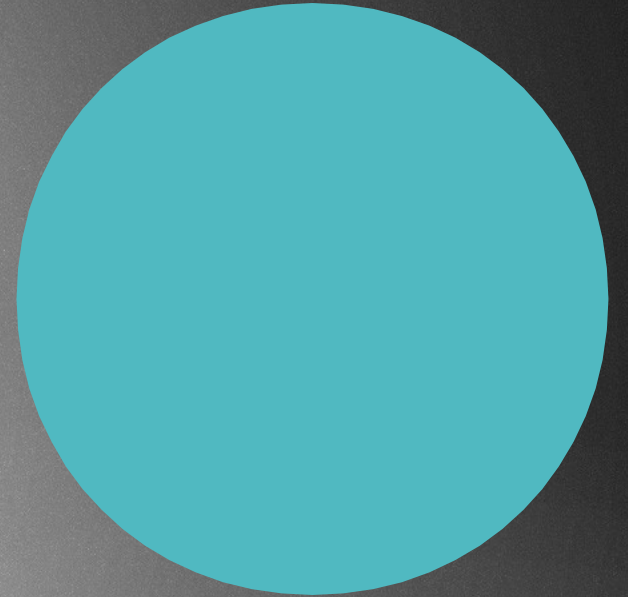
```
        j = j - gap
```

```
      end
```

```
      a[j] = temp
```

```
    end
```

```
  end
```



Shell sort

```
shellSort(array)
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```
  for every gap in gaps
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    for i=gap to n
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      temp = array[i]
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      for j=i and j >= gap and array[j-gap] > temp
```

```
        array[j] = array[j-gap]
```

```
        j = j - gap
```

```
      end
```

```
      a[j] = temp
```

```
    end
```

```
  end
```

We have to define some formula for choosing the gaps: for example at the beginning we consider every **3rd** item ... after that we consider every **2nd** item

Shell sort

```
shellSort(array)
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```
  for every gap in gaps
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    for i=gap to n
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      temp = array[i]
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      for j=i and j >= gap and array[j-gap] > temp
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        array[j] = array[j-gap]
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```
        j = j - gap
```

```
      end
```

```
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```

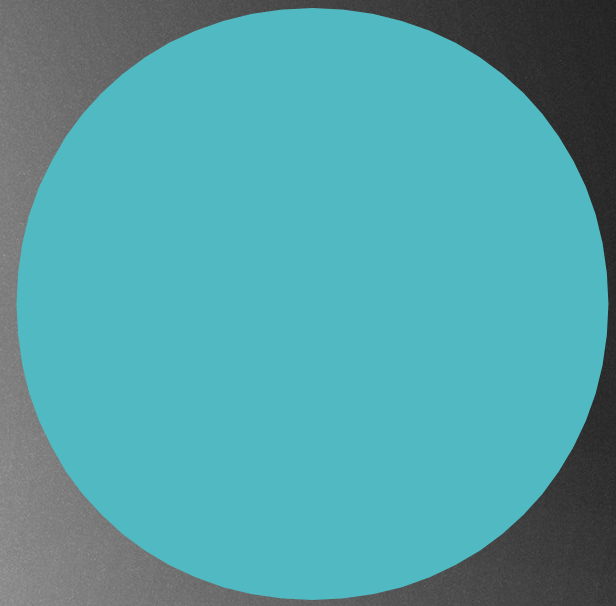
```
    end
```

```
  end
```



Basically we do a simple
insertion sort on the subarray

34	-3	0	2	14	8	-1	24
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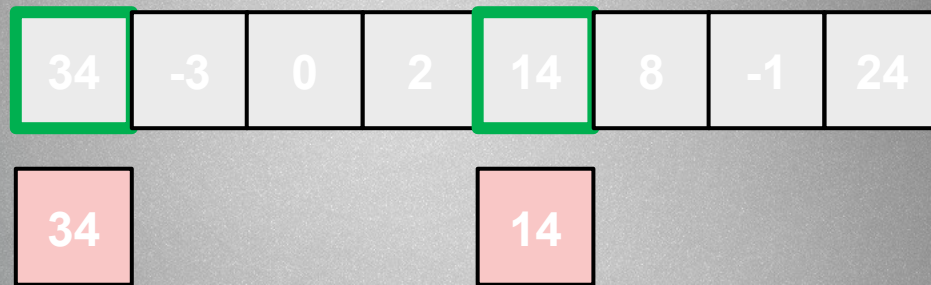


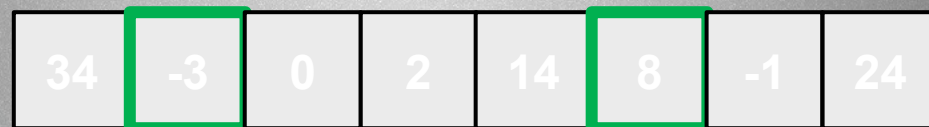
There are a lots of articles and models on how to choose the gaps
to be the most efficient !!!

~ we start at 4 → it means we consider every 4th item and sort them

34	-3	0	2	14	8	-1	24
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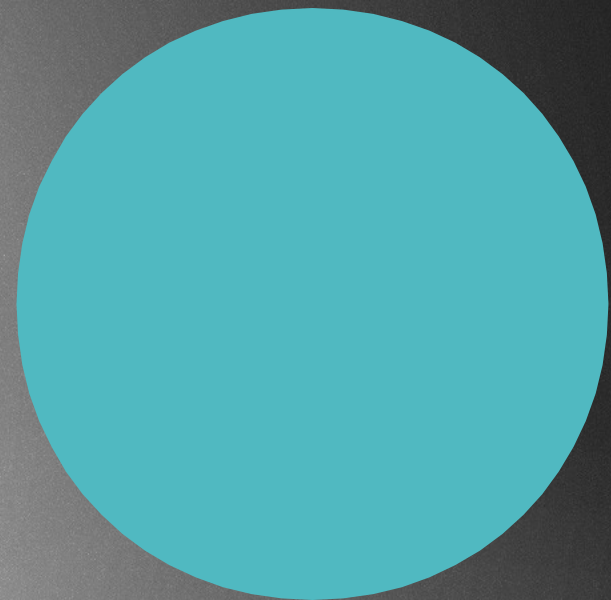
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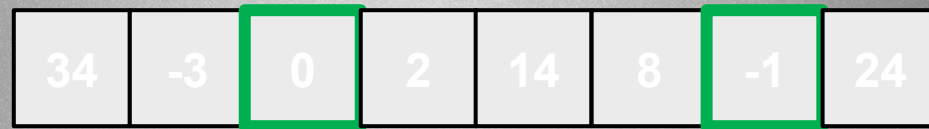
34

14

-3

8





34	-3	0	2	14	8	-1	24
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34

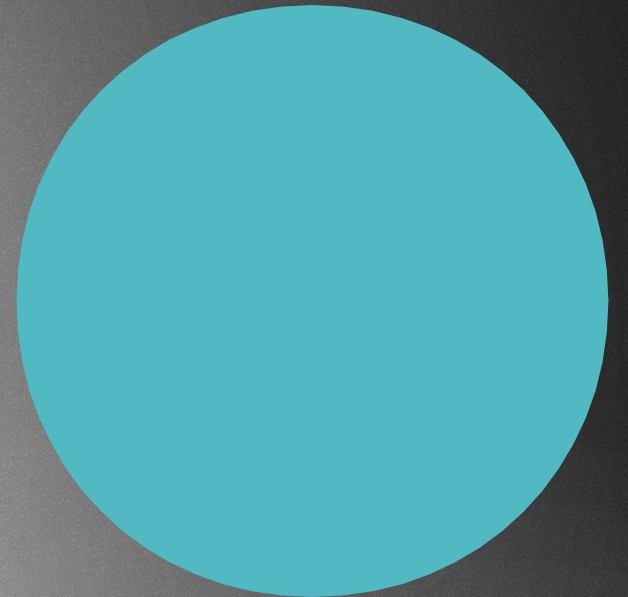
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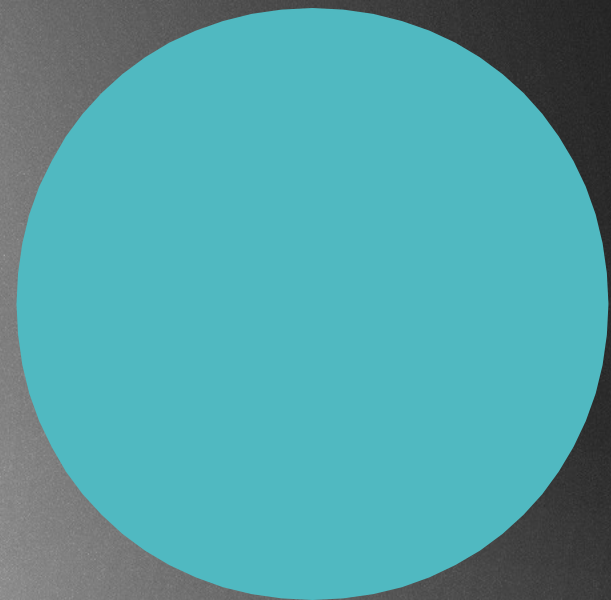
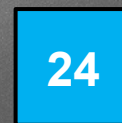
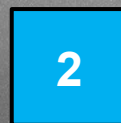
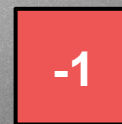
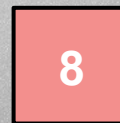
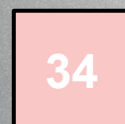
-3

8

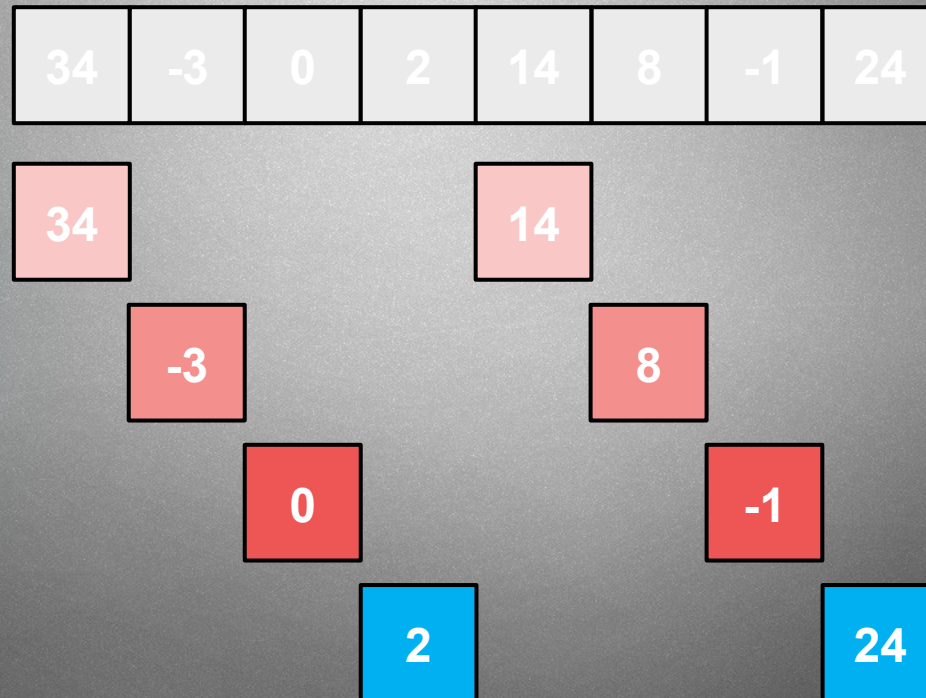
0

-1

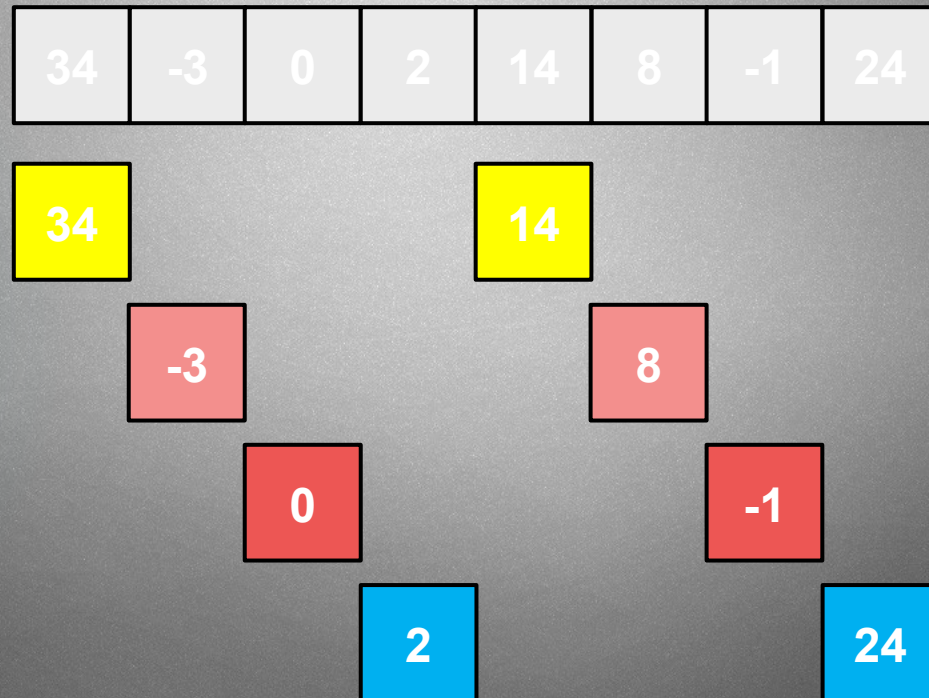




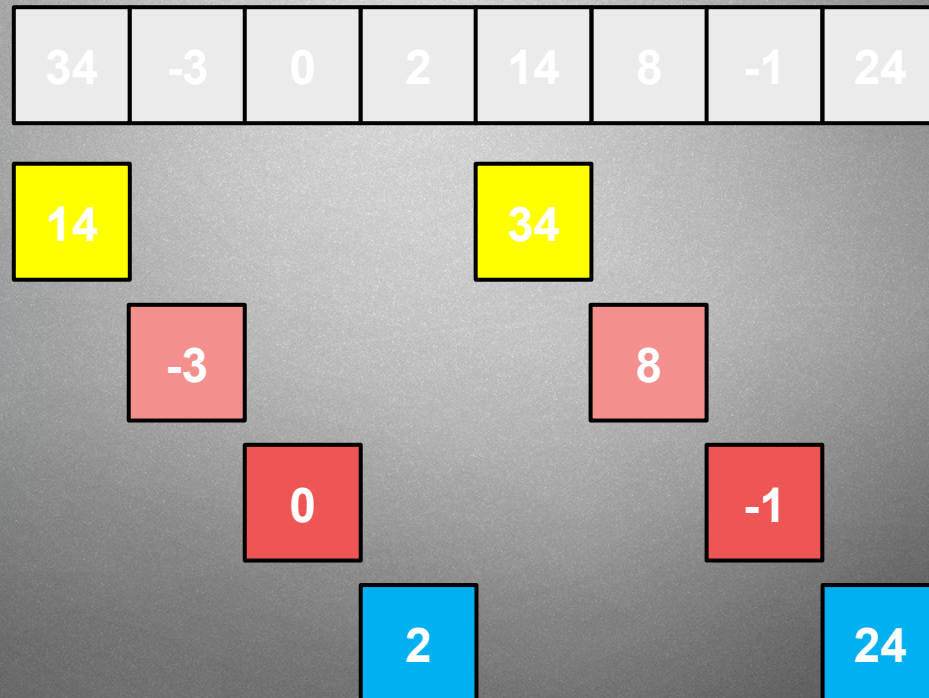
So we have managed to find all the subarrays with gap 4, meaning all the subarrays where the items are 4 units away from each other
~ we have to sort these sublists independently
+ insert them back into the original array



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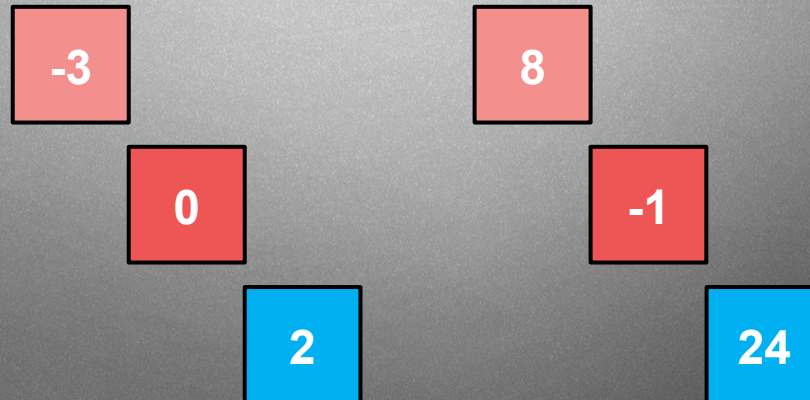


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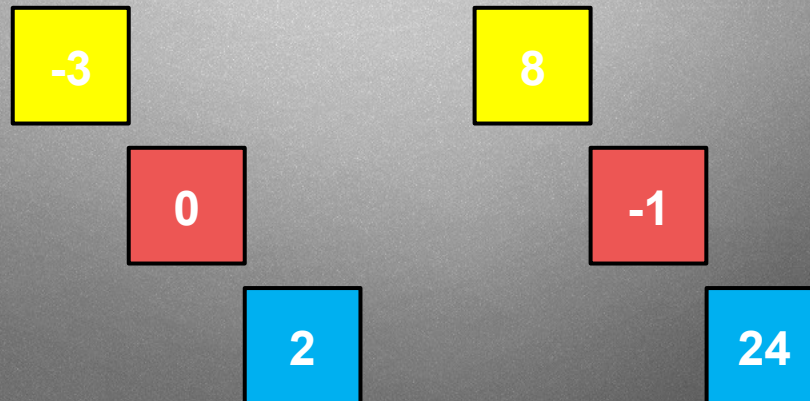
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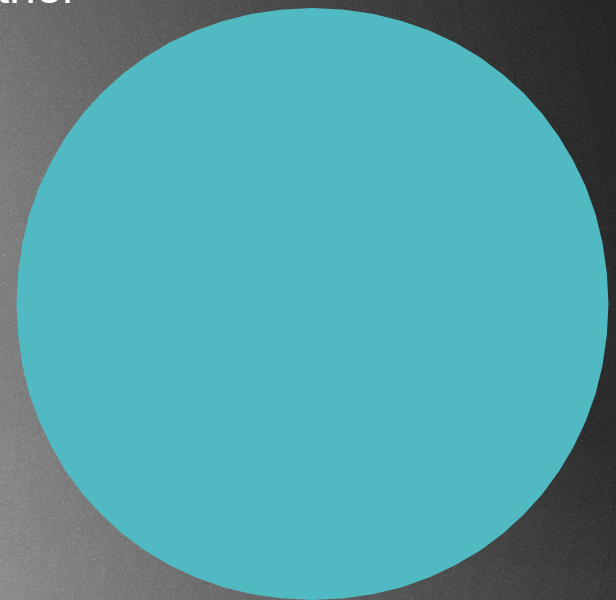
14	-3	0	2	34	8	-1	24
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0

2

-1

24



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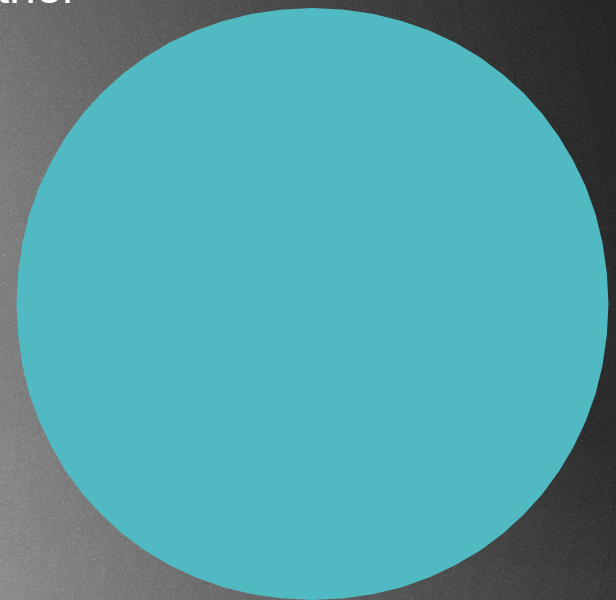
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14	-3	-1	2	34	8	0	24
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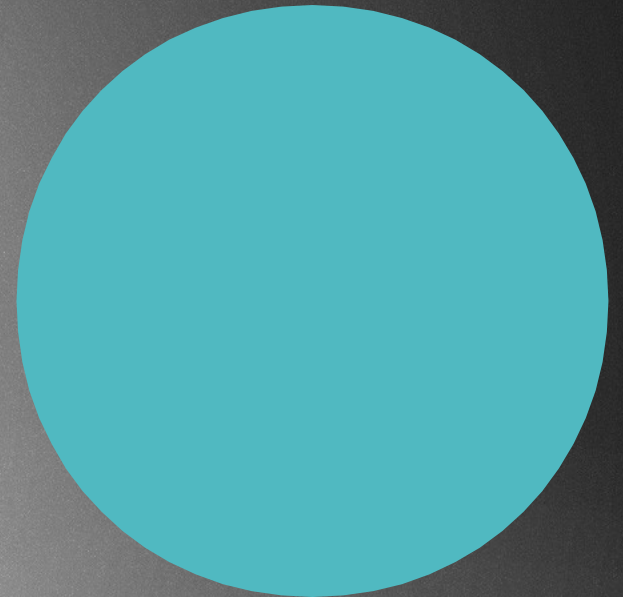
The gap so far was 4 units → lets decrease it to be 3 units

14	-3	-1	2	34	8	0	24
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14	-3	-1	2	34	8	0	24
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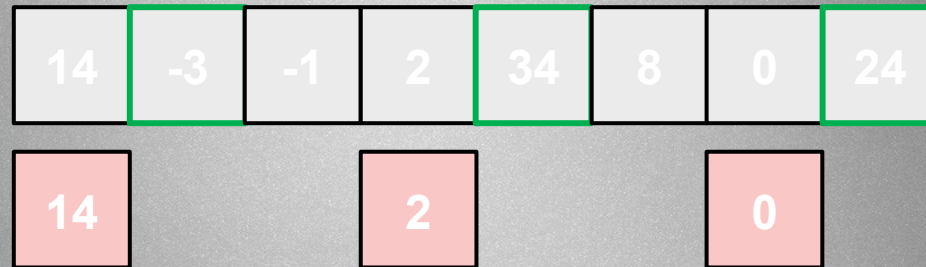


The gap so far was 4 units → lets decrease it to be 3 units

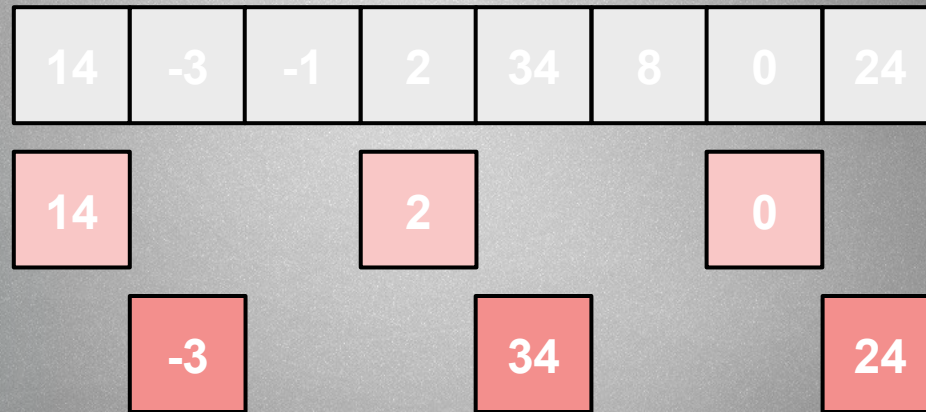
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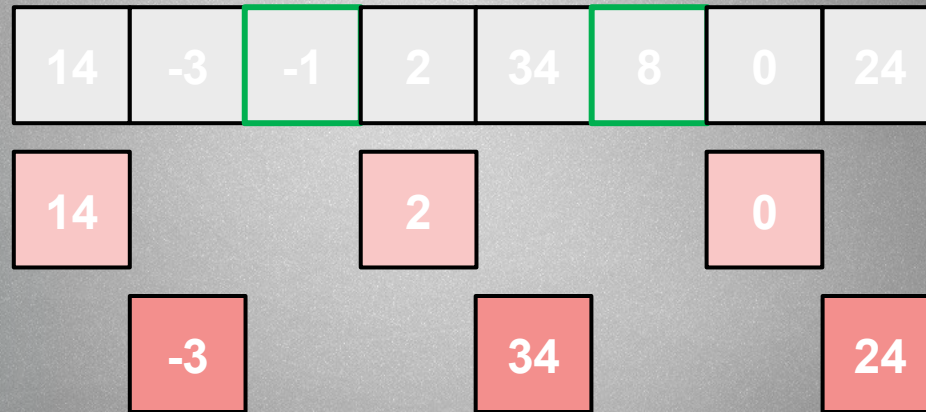
The gap so far was 4 units → lets decrease it to be 3 units



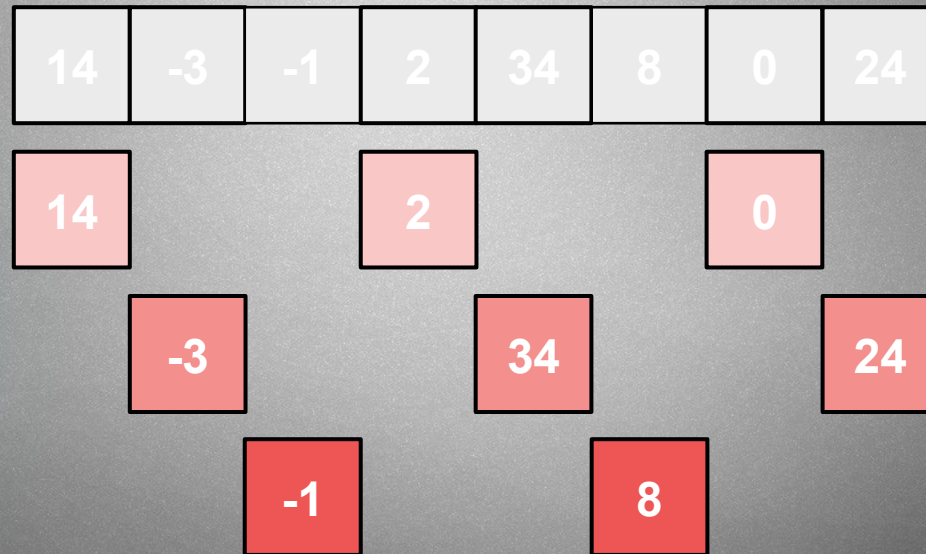
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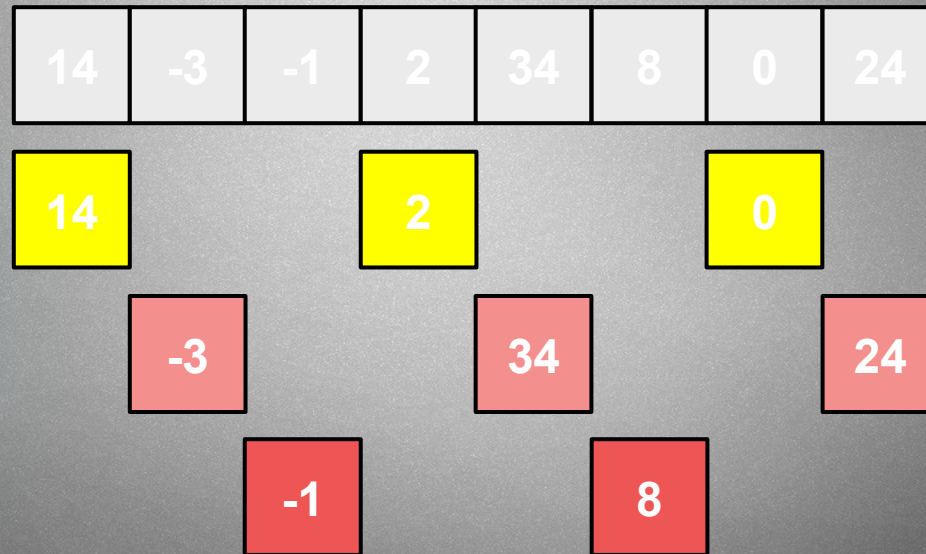
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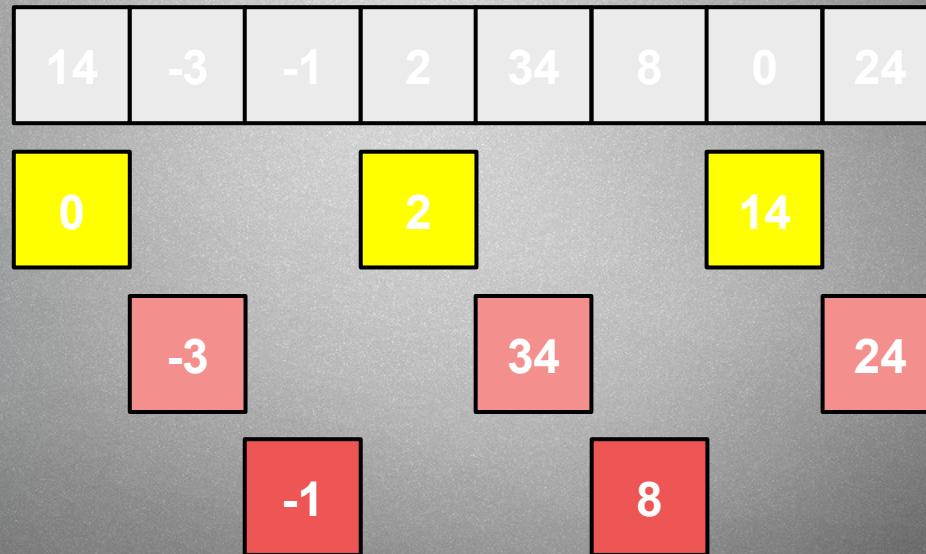
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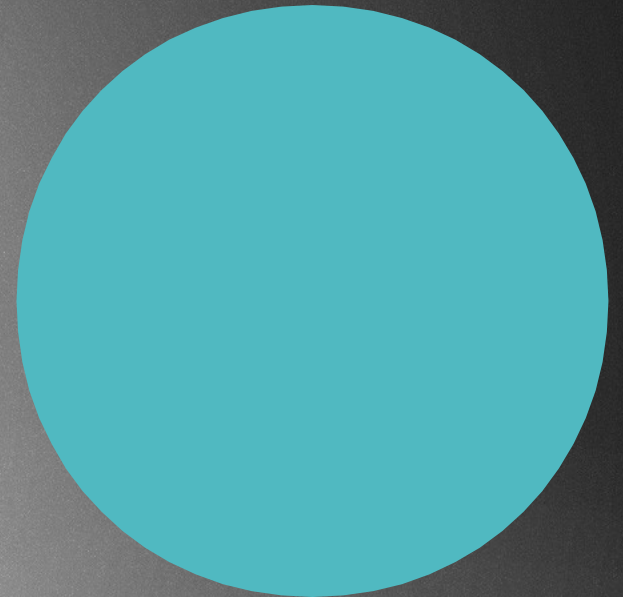
-3

34

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-1

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0	-3	-1	2	34	8	14	24
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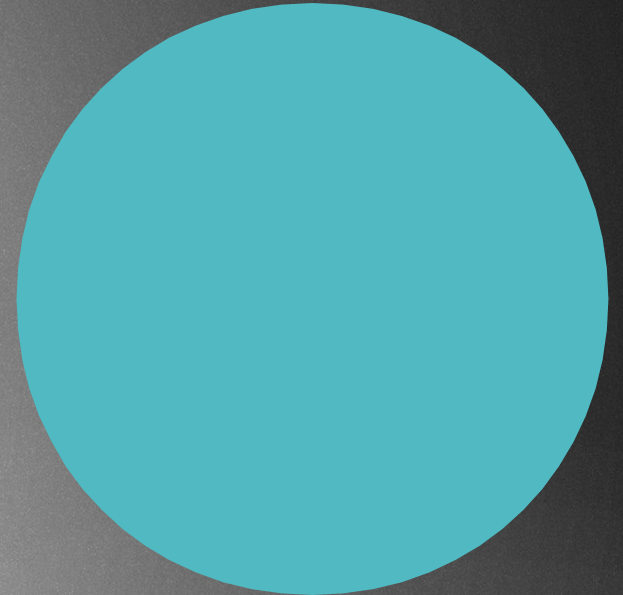
-3

34

24

-1

8



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0	-3	-1	2	34	8	14	24
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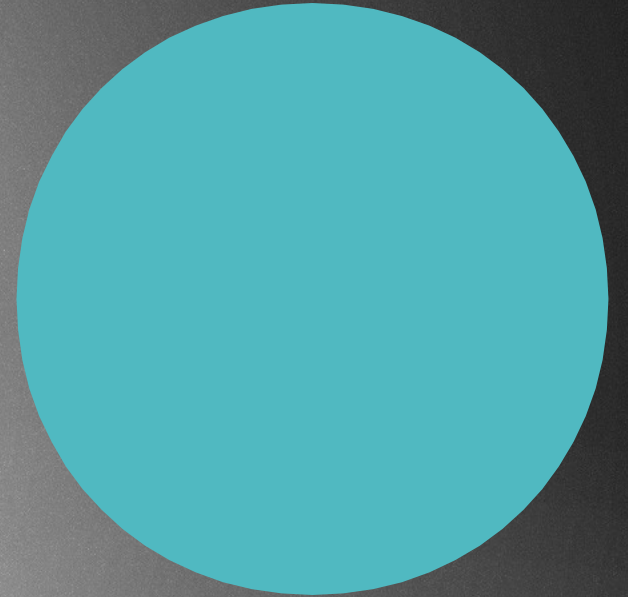
-3

24

34

-1

8



The gap so far was 4 units → lets decrease it to be 3 units

0	-3	-1	2	24	8	14	34
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-1

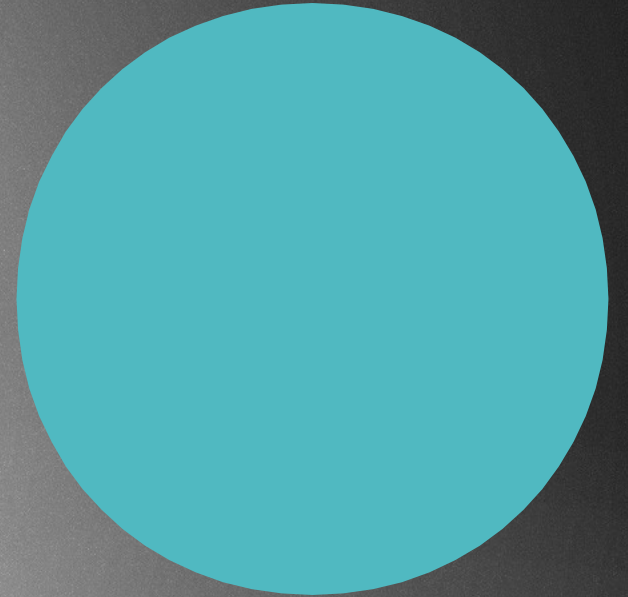
8

The gap so far was 4 units → lets decrease it to be 3 units

0	-3	-1	2	24	8	14	34
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-1

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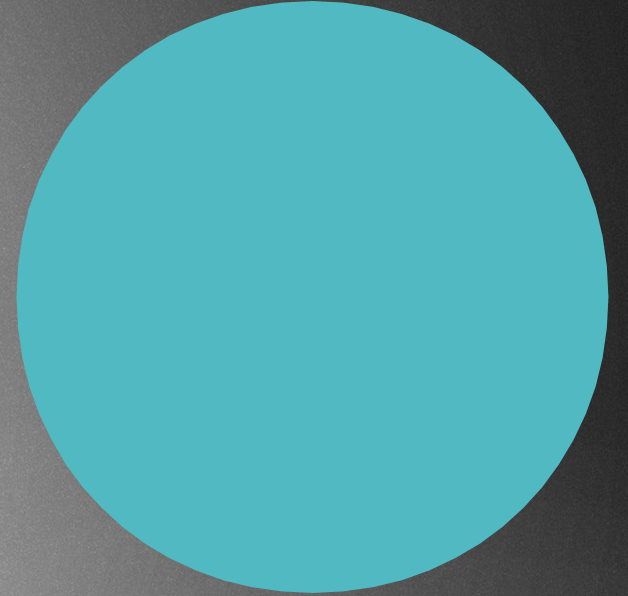


The gap so far was 3 units → lets decrease it to be 1 unit
What does it mean 1 unit? It is basically the insertion sort !!!

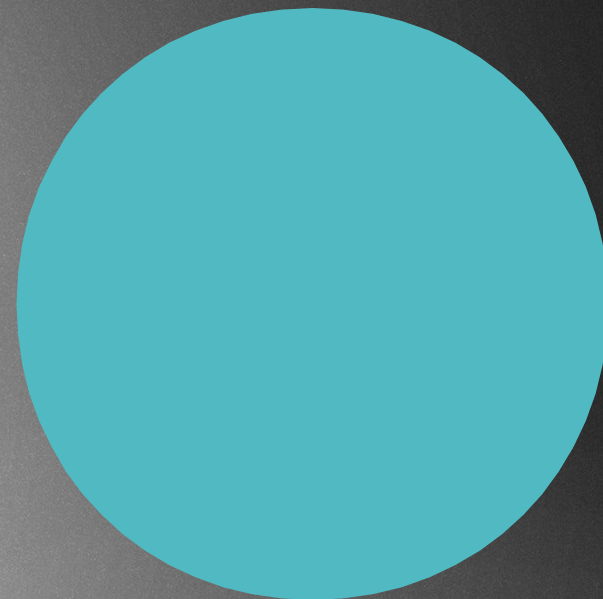
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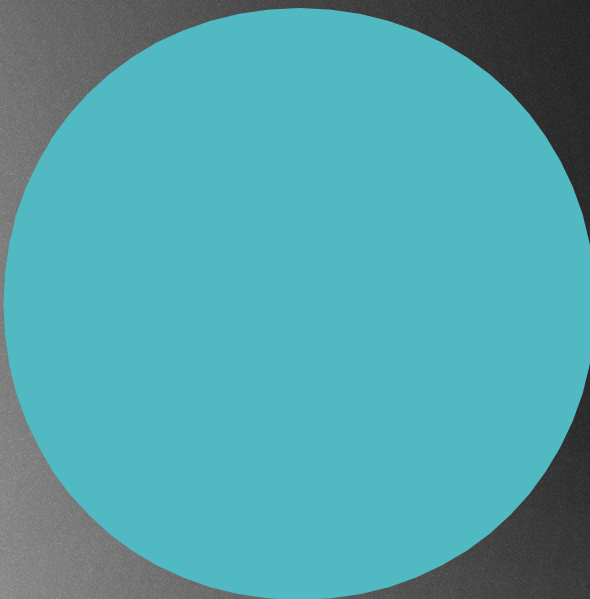
0	-3	-1	2	24	8	14	34
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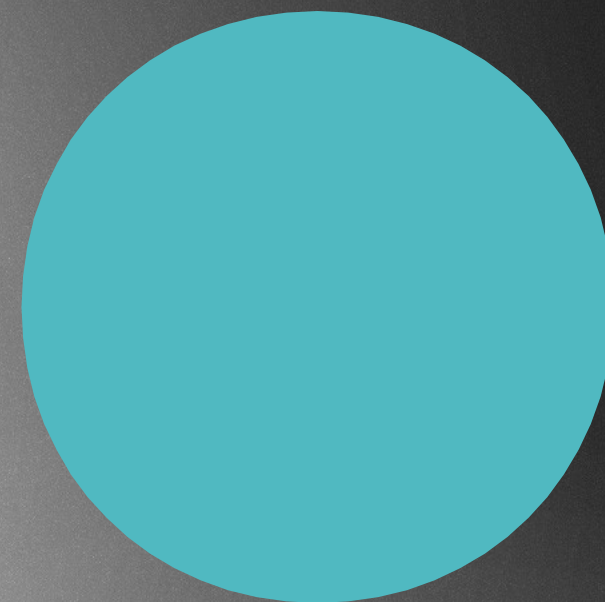
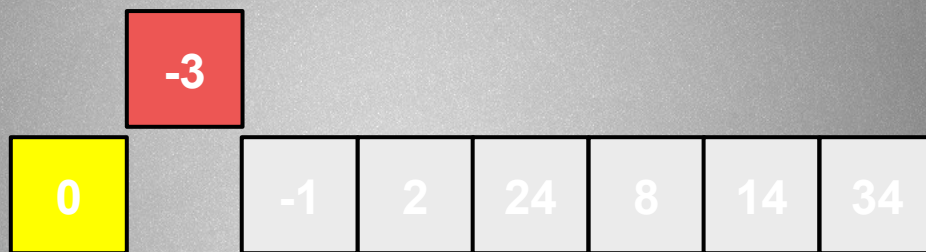
0	-3	-1	2	24	8	14	34
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0	-3	-1	2	24	8	14	34
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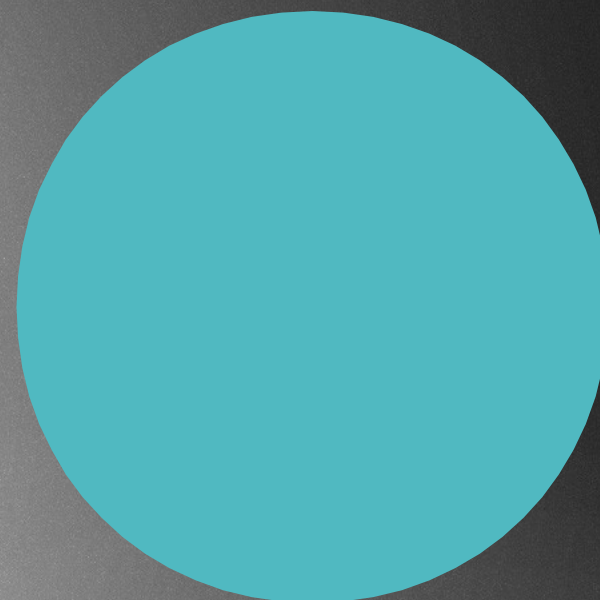




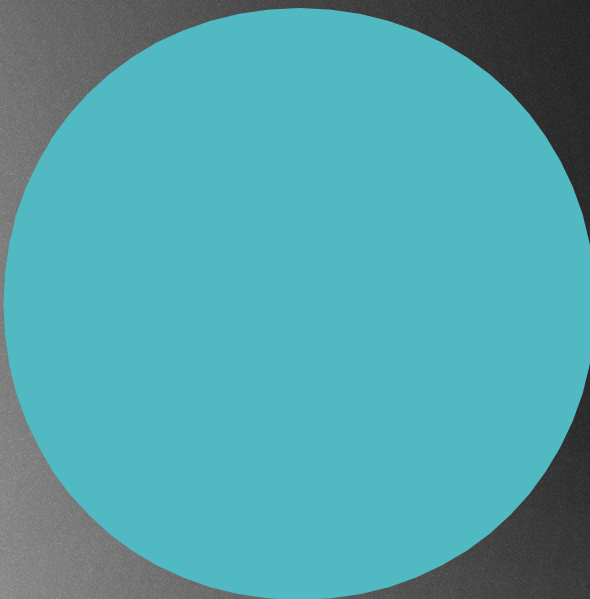




-3						
0	-1	2	24	8	14	34



-3	0	-1	2	24	8	14	34
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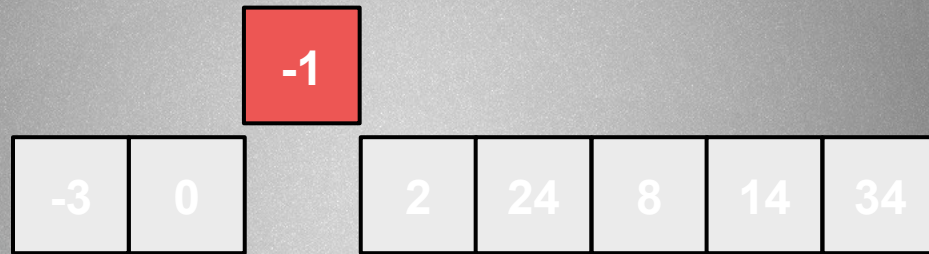


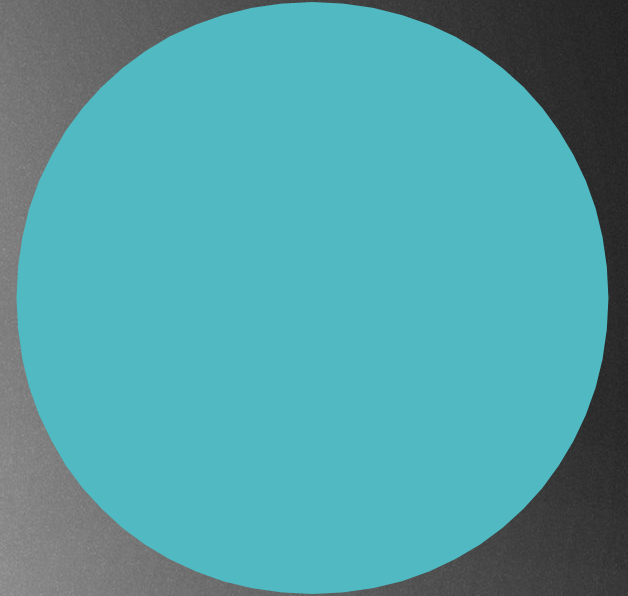
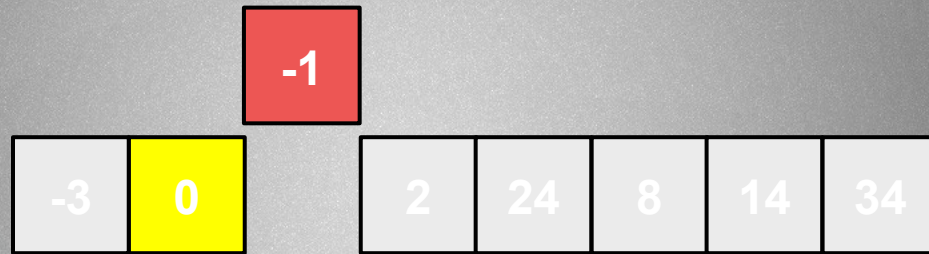
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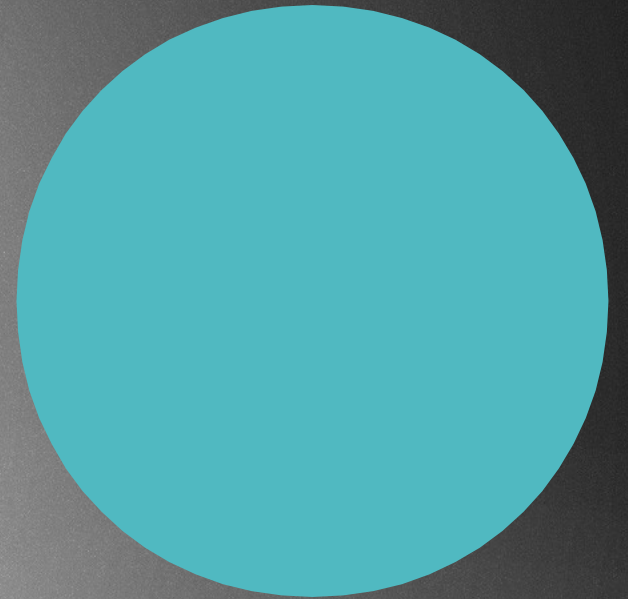
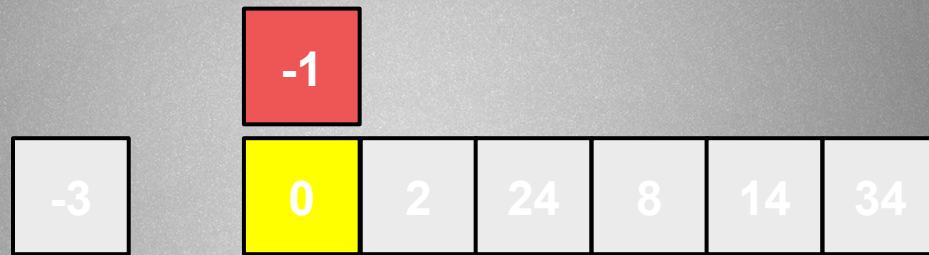


-3	0	-1	2	24	8	14	34
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-3

-1

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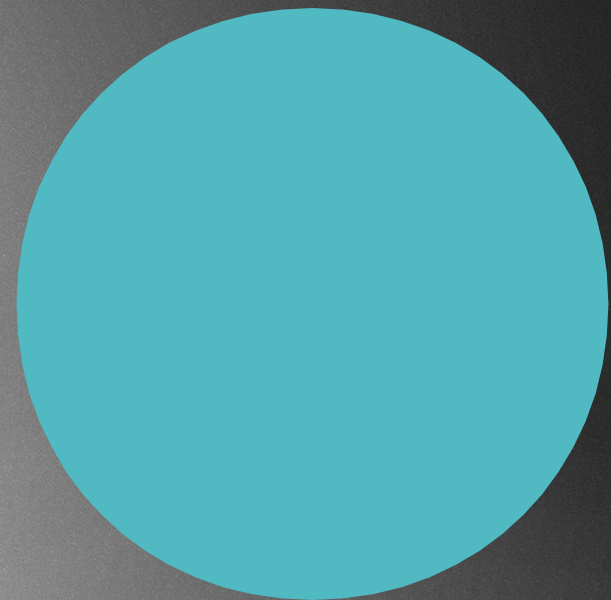
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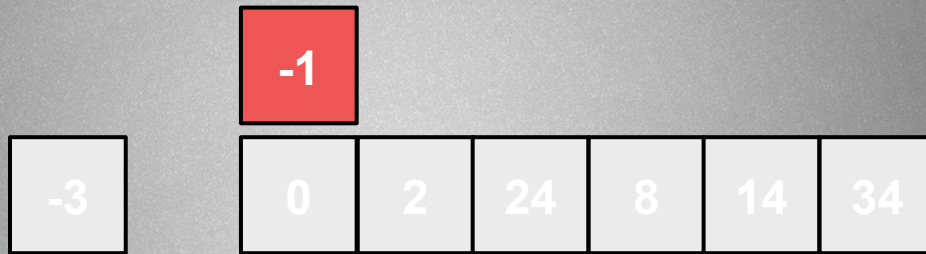
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8

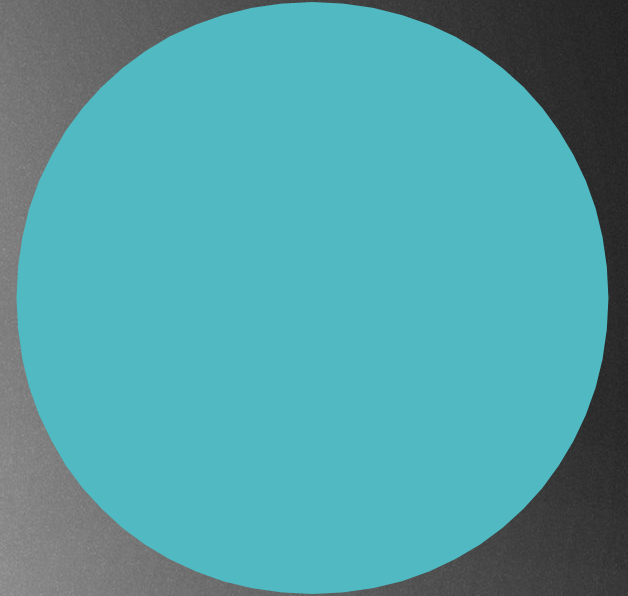
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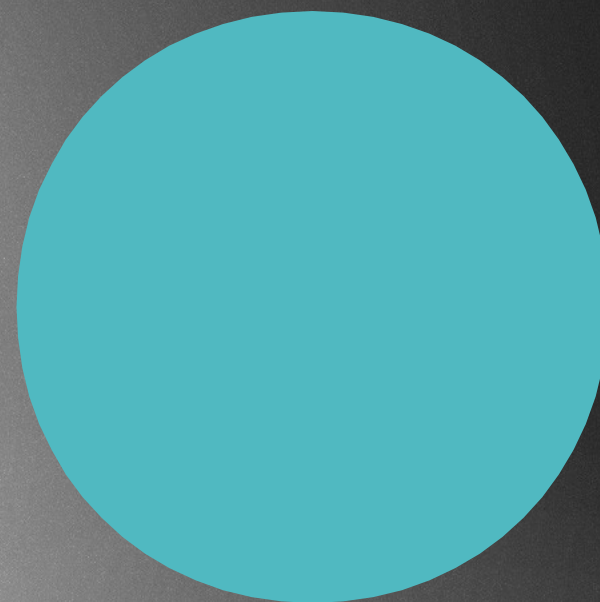


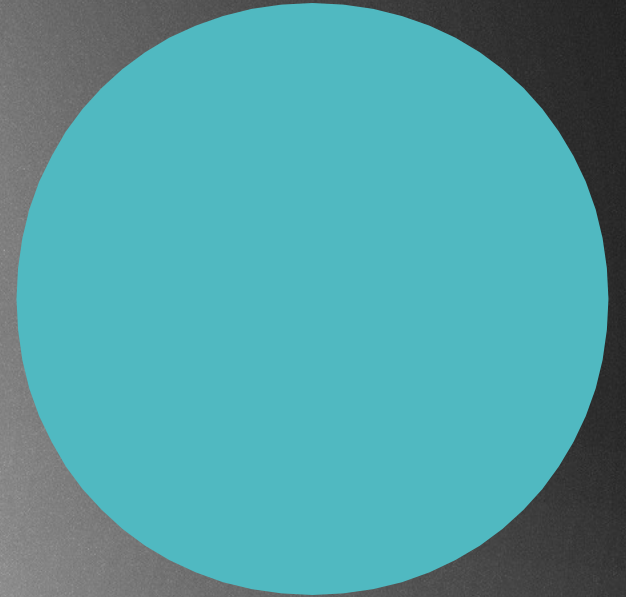
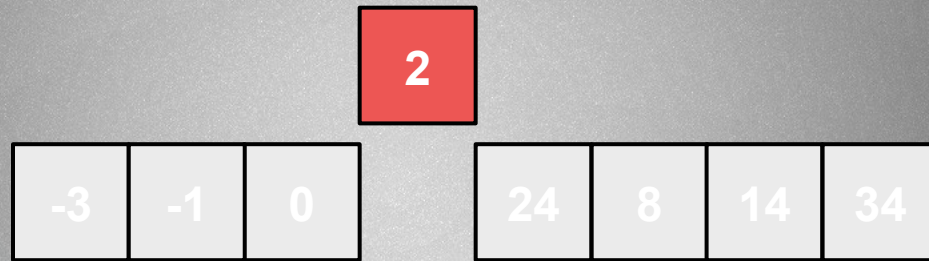


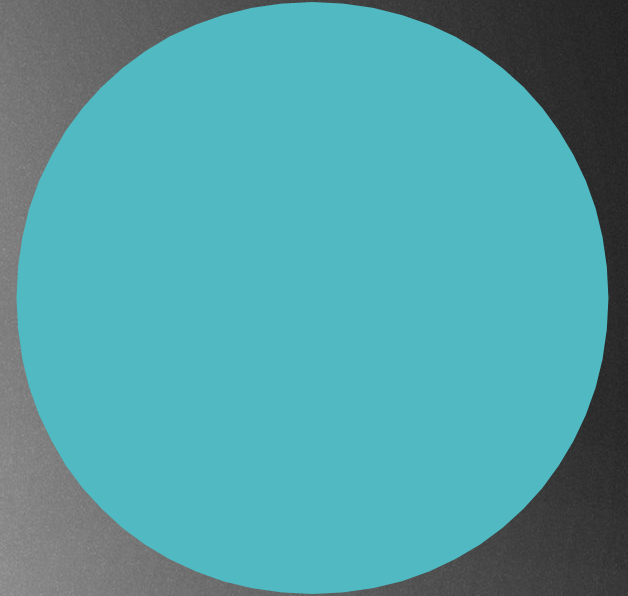
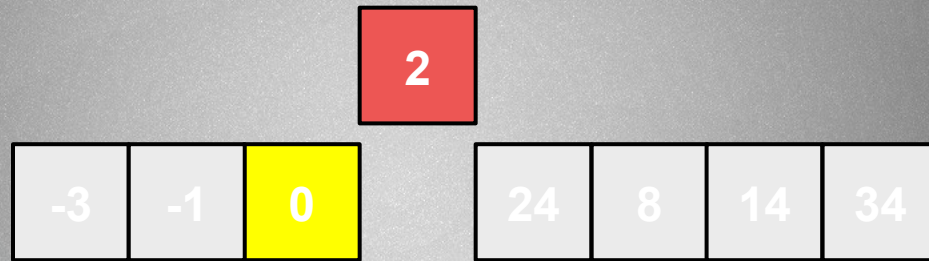
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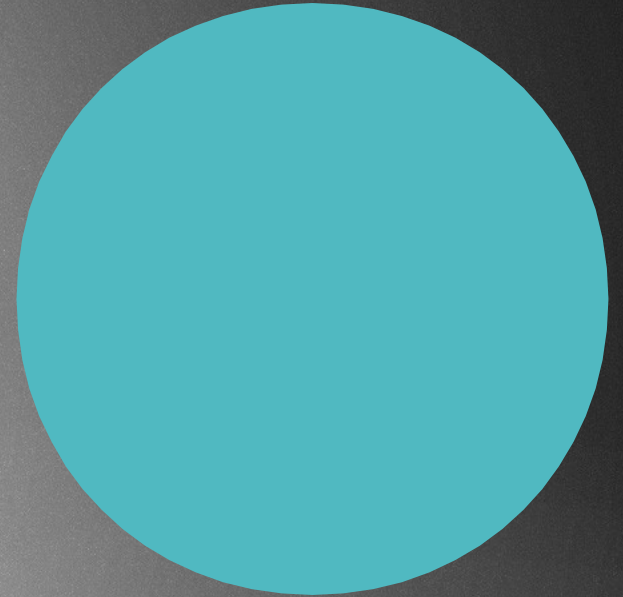
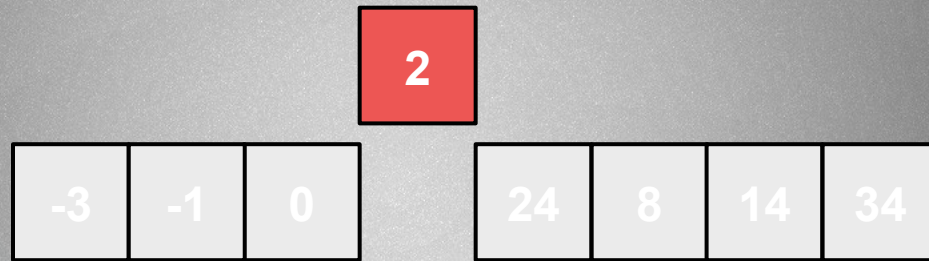


-3	-1	0	2	24	8	14	34
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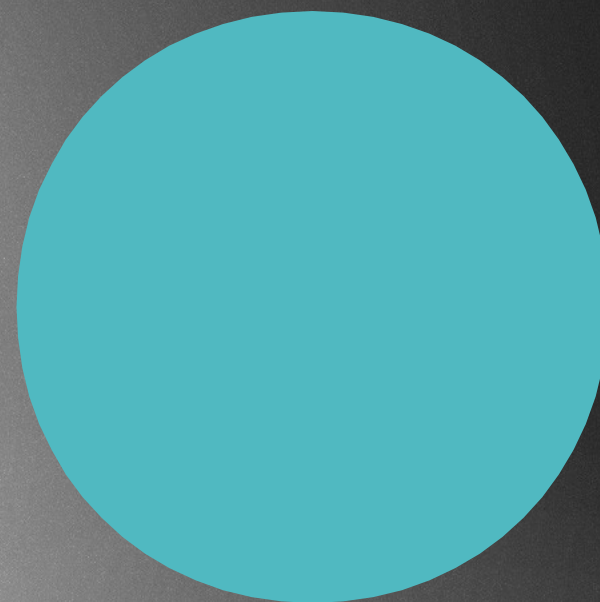
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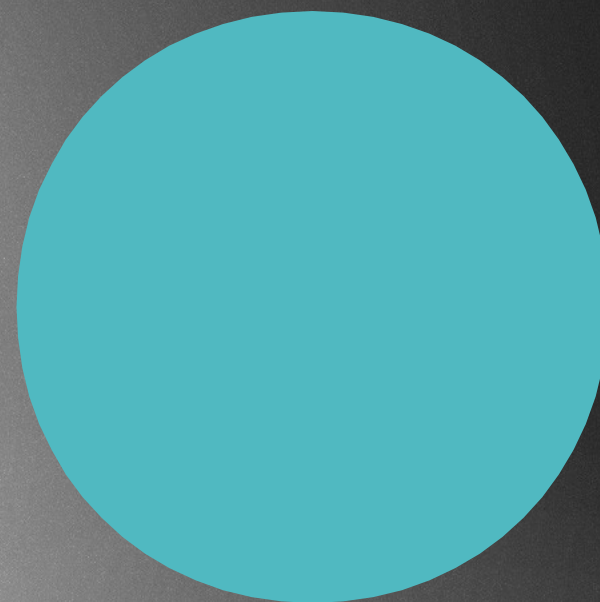
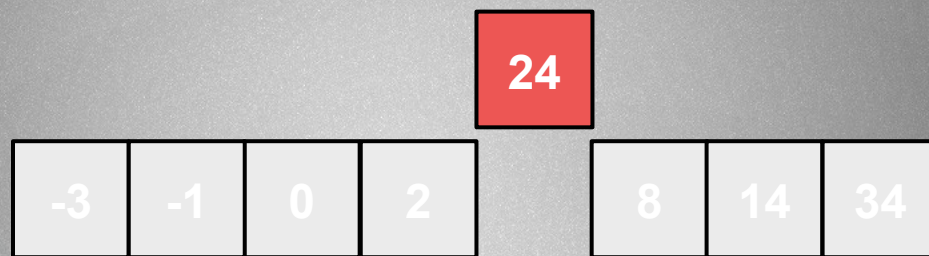


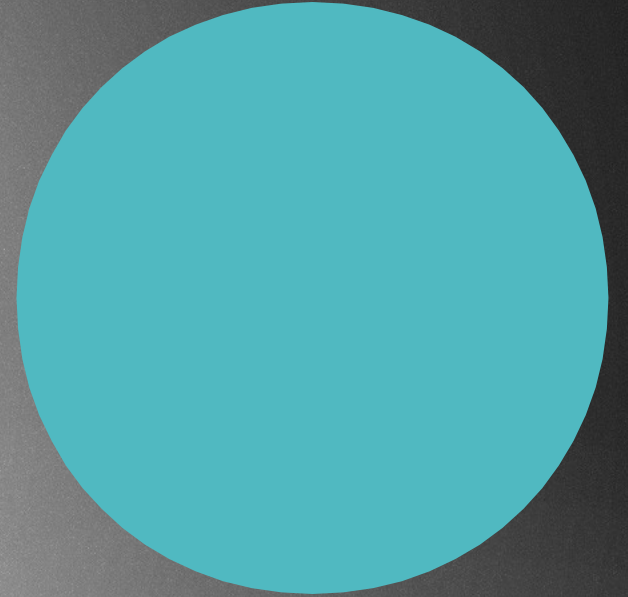
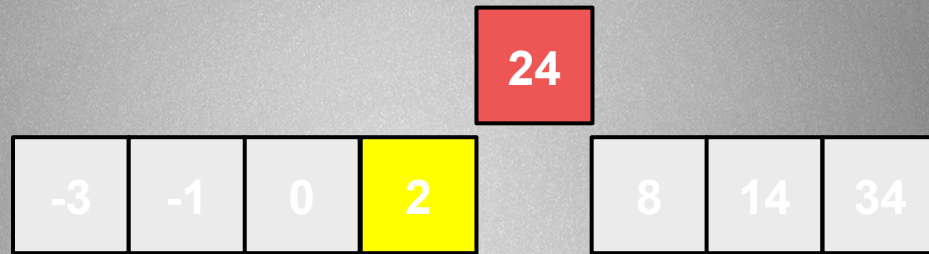
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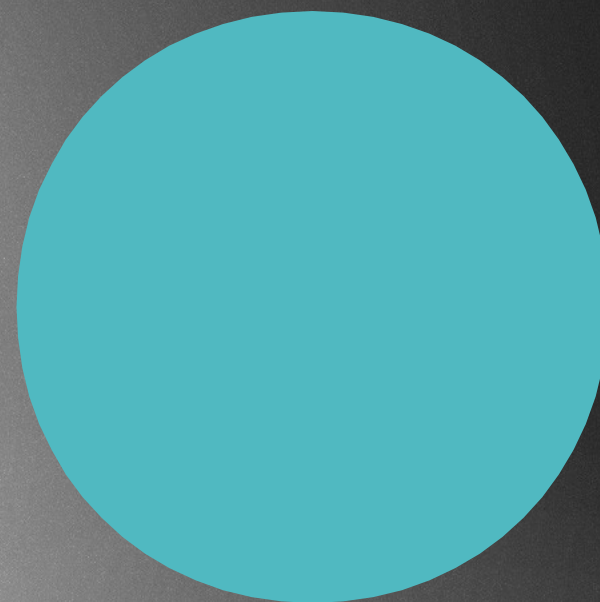
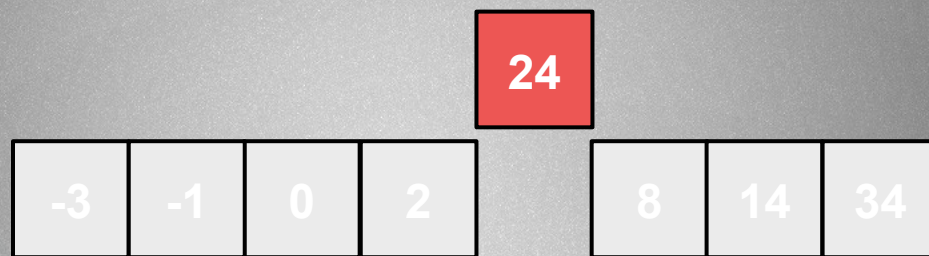


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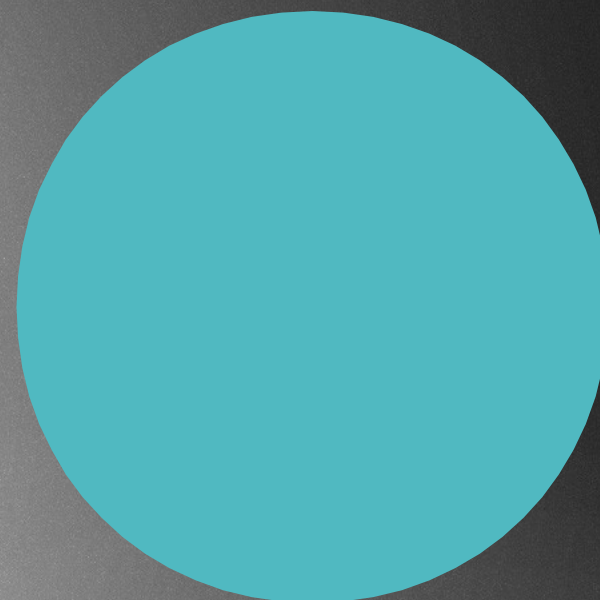








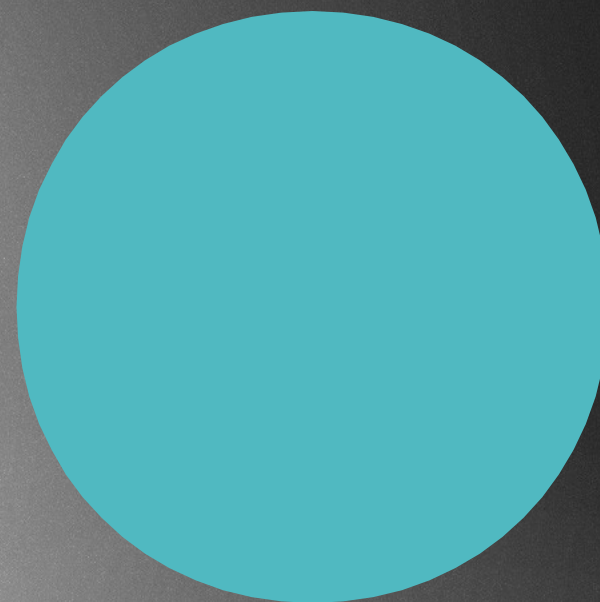
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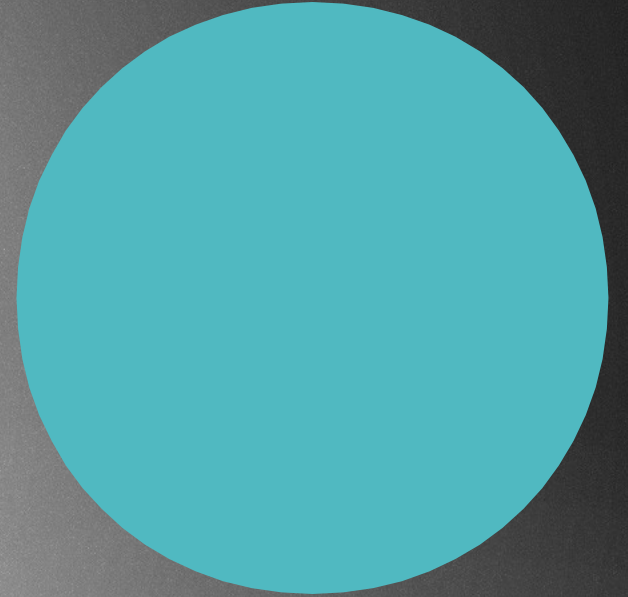
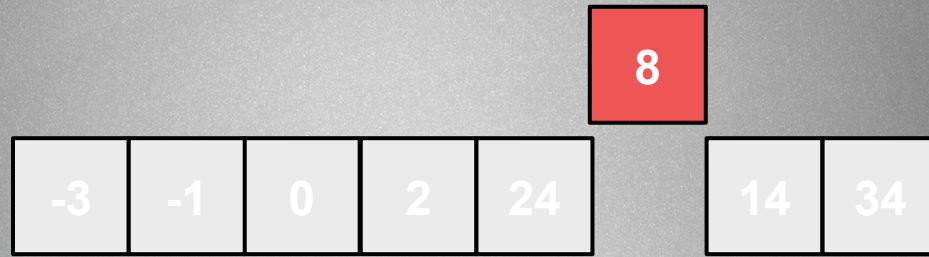


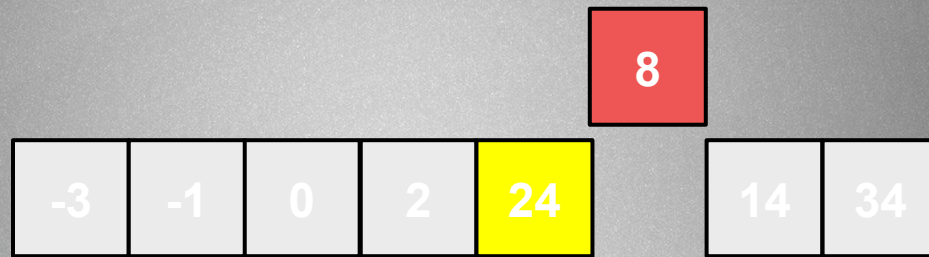
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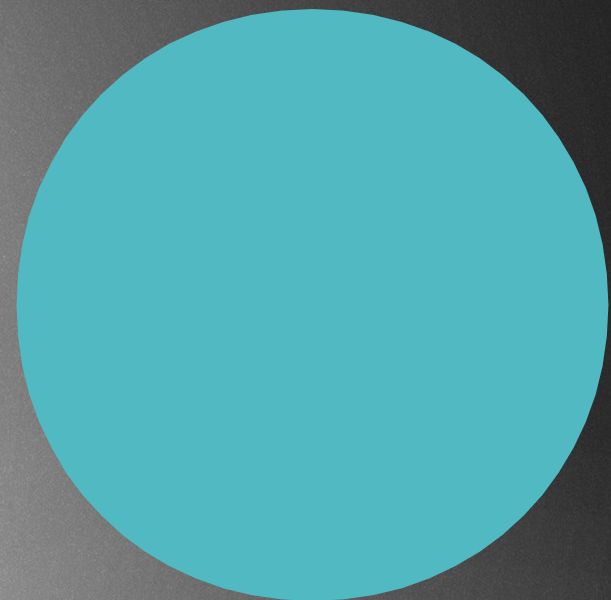


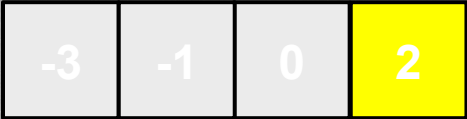


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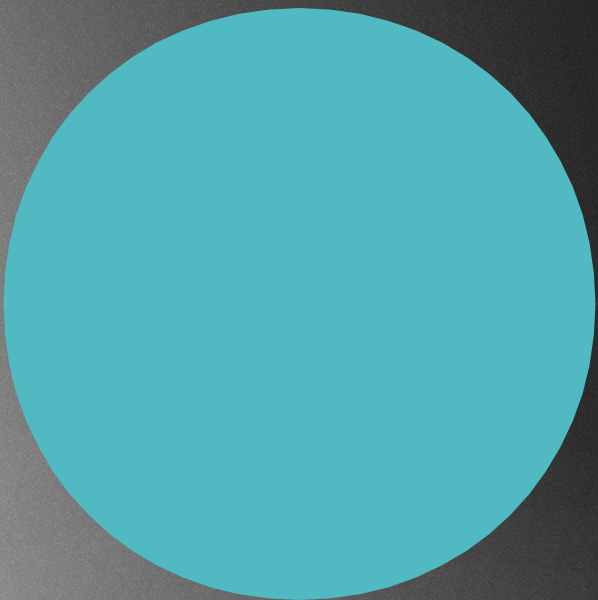
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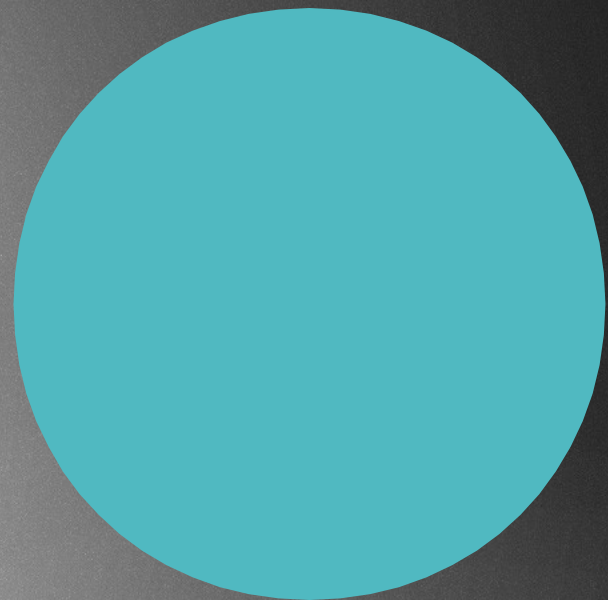




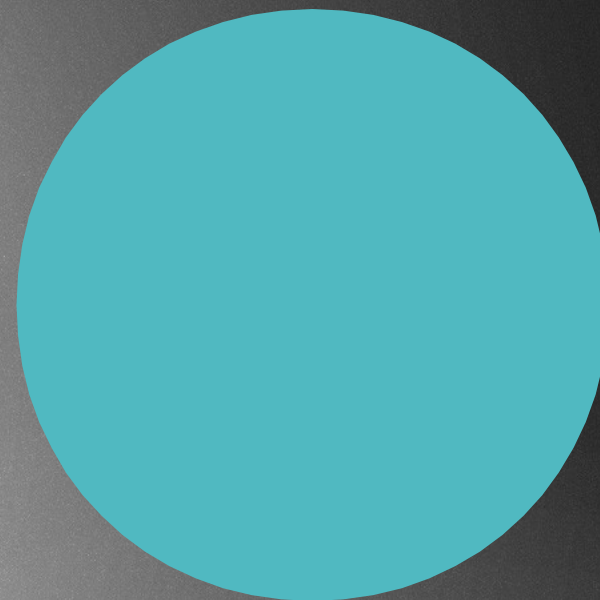
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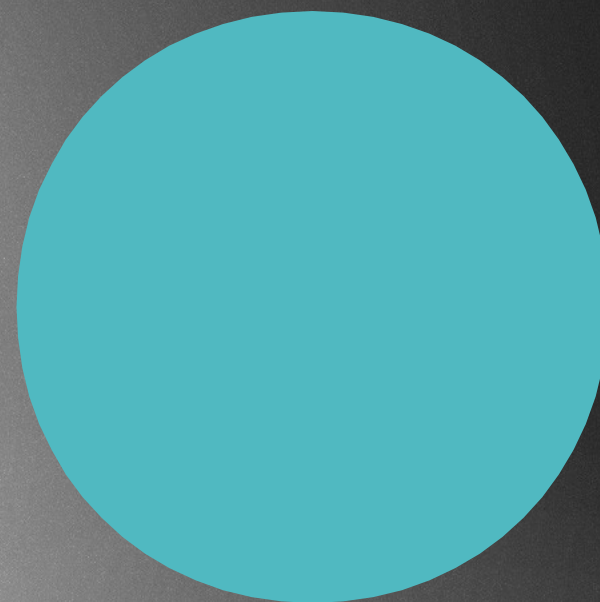
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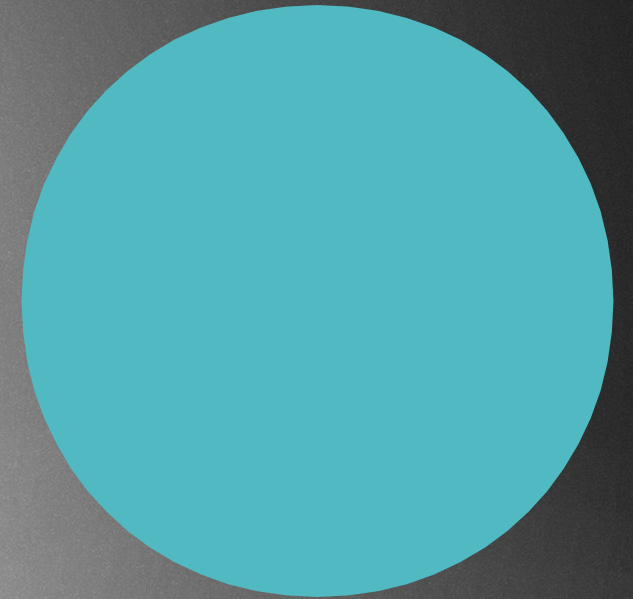
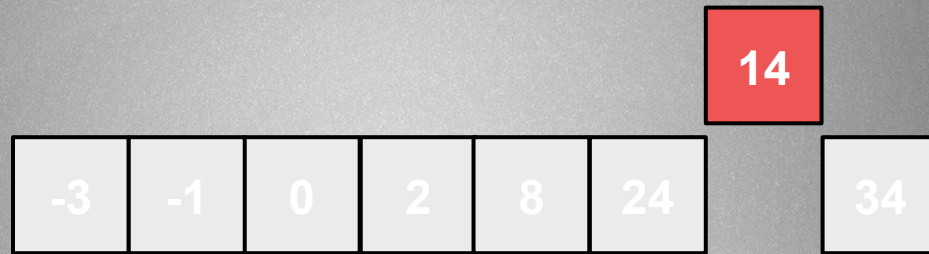


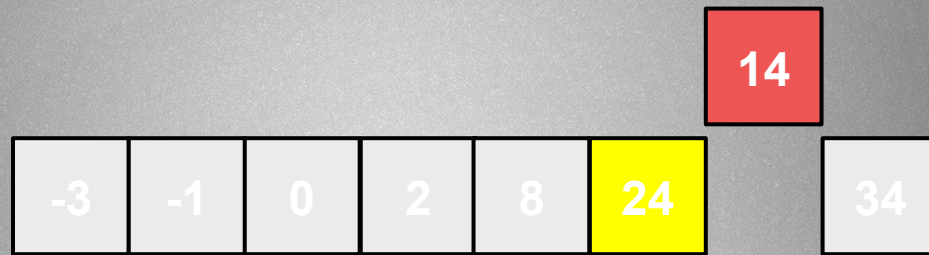
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-3	-1	0	2	8	24	14	34
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-3	-1	0	2	8
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14

24	34
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-3	-1	0	2	8
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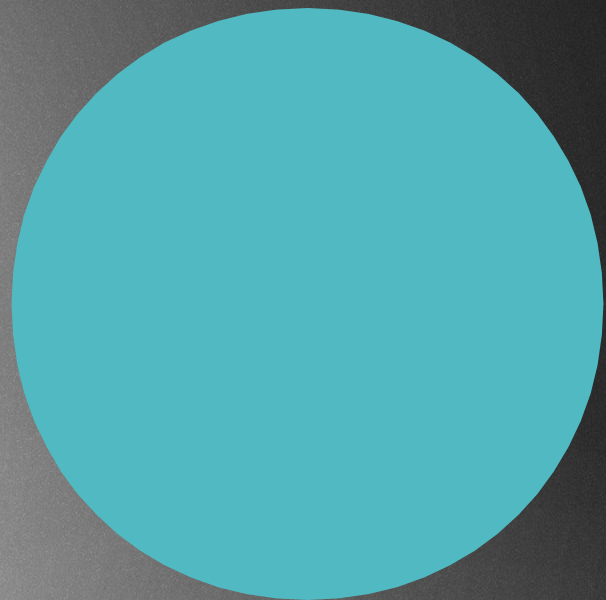
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24	34
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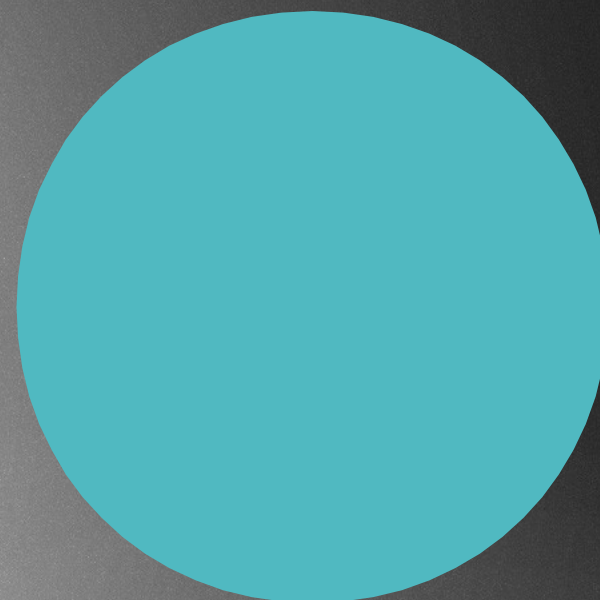
14	
24	34



-3	-1	0	2	8	14	24	34
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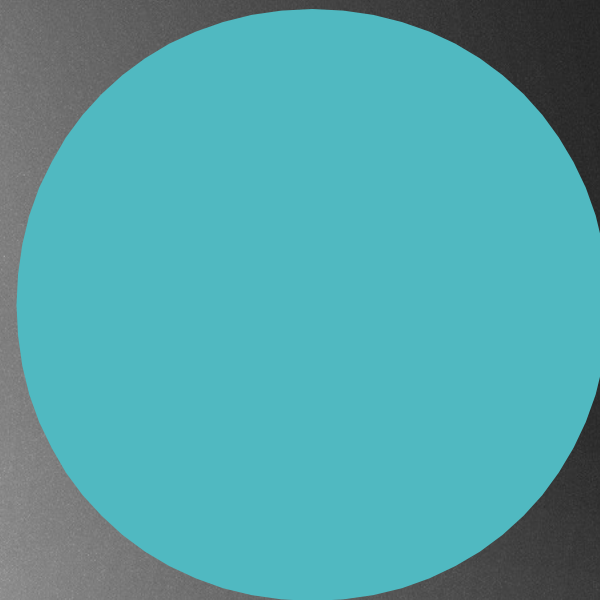
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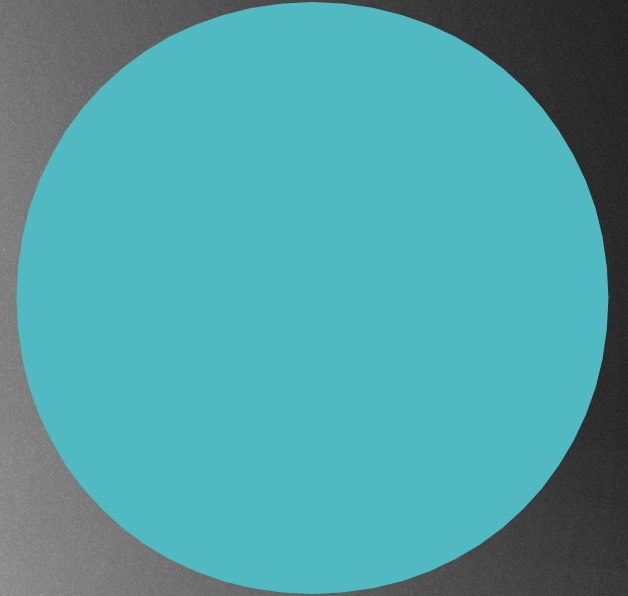
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34



-3	-1	0	2	8	14	24
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34



-3	-1	0	2	8	14	24	34
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-3	-1	0	2	8	14	24	34
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