

## Question:

Given an array representing profit or loss from a stock over a period of days, write a function that calculates total profit or loss for a given range of days.

## Example:

$SP[i]$  : <sup>0</sup>-5   <sup>1</sup>10   <sup>2</sup>20   <sup>3</sup>40   <sup>4</sup>50   <sup>5</sup>-10   <sup>6</sup>80   <sup>7</sup>-90   <sup>8</sup>-20   <sup>9</sup>-10

## Queries

<u>S</u>	<u>E</u>	<u>Net</u>		
0	9	65	$O(N)$	<u><math>O(Q * N)</math></u>
1	4	120	$O(N)$	
0	0	-5	"	$1 \leq Q \leq 10^5$
7	9	-120	"	$1 \leq N \leq 10^5$
2	7	90	"	

```
int [][] queries = new int [Q][2];
```

queries[i]  $\rightarrow$  ith query.

queries[i][0]  $\rightarrow$  s for ith query.

queries[i][1]  $\rightarrow$  e for ith query.

```

void printQuerySum (int[] A, int[][] Q)
{
    for (i=0; i<Q.length; i++)
    {
        int s = Q[i][0];
        int e = Q[i][1];
        int sum = 0;
        for (j=s; j<=e; j++)
        {
            sum = sum + A[j];
        }
        println(sum);
    }
}

```

$$1 \leq Q \leq 10^5$$

$$1 \leq N \leq 10^5$$

$$TC: O(N*Q)$$

$$SC: O(1)$$

### Question:

Given  $N$  elements and  $Q$  queries.  
For each query, calculate sum of all elements from  $L$  to  $R$ .

Eg:

		0	1	2	3	4	5	6	7	8	9
A :	-3	6	2	4	5	2	8	-9	3	1	
C :	-3	3	5	9	14	16	24	15	18	19	

  

<u>L</u>	<u>R</u>	<u>Sum</u>	
4	8	9	$C[R] - C[L-1]$
3	7	10	
1	3	12	
0	4	14	
7	7	-9	

Given the scores of the 1st 10 overs of a cricket match

RS :	2	6	6	15	2	18	16	14	9	9
	1	2	3	4	5	6	7	8	9	10
	2	8	14	29	31	49	65	79	88	97

a. Runs scored in 7th over =  $R(7) - R(6)$   
 $= \underline{\underline{16}}$

b. Runs scored from 6th to 10th over =  $R(10) - R(5)$   
 $= 97 - 31 = 66$

c. Runs scored in the 10th over :  $R(10) - R(9) = 9$

d. Runs scored from 3<sup>rd</sup> to 6th over :  $R(6) - R(2)$   
 $= \underline{\underline{41}}$

# Prefix Sum Array:

HW

A: <sup>0</sup>2   <sup>1</sup>5   <sup>2</sup>-1   <sup>3</sup>7   <sup>4</sup>1

PF:

A: <sup>0</sup>10   <sup>1</sup>32   <sup>2</sup>6   <sup>3</sup>12   <sup>4</sup>20   <sup>5</sup>1

PF:

A: <sup>0</sup>-3   <sup>1</sup>6   <sup>2</sup>2   <sup>3</sup>4   <sup>4</sup>5   <sup>5</sup>2   <sup>6</sup>8   <sup>7</sup>-9   <sup>8</sup>3   <sup>9</sup>1

L

R

Sum

4

8

3

7

1

3

0

4

7

7

## Create a prefix array:

$SP[]$  :    <sup>0</sup>-5    <sup>1</sup>10    <sup>2</sup>20    <sup>3</sup>40    <sup>4</sup>50    <sup>5</sup>-10    <sup>6</sup>80    <sup>7</sup>-90    <sup>8</sup>-20    <sup>9</sup>-10  
 $psa[]$  : -5    5

$$\begin{aligned} psa[1] &= A[1] + psa[0] \\ psa[2] &= A[2] + psa[1] \\ psa[i] &= A[i] + psa[i-1] \end{aligned}$$

```
long[] getPrefixSum(int[] A)
{
    long[] psa = new int[A.length];
    psa[0] = A[0];
    for (i = 1; i < A.length; i++)
    {
        psa[i] = psa[i-1] + A[i];
    }
    return psa;
}
```

TC:  $O(N)$   
SC:  $O(N)$

## Using prefix array to answer queries:

```
void printQuerySum (int[] A, int[][] Q)
{
    int[] psa = createPSA(A);           → O(N)
    for (i=0; i<Q.length; i++)
    {
        int s = Q[i][0];
        int e = Q[i][1];
        if (s==0)
            print(psa[e]);
        else { psa[e] - psa[s-1] };
    }
}
```

O(Q)

TC: O(N+Q)

SC: O(N)

$$1 \leq Q \leq 10^5$$

$$1 \leq N \leq 10^5$$

## Question:

Given an array of size  $N$  and  $Q$  queries with start and end index. For each query return the sum of all even indexed elements from  $s$  to  $e$ .

	<sup>*</sup> 0	<sup>1</sup>	<sup>*</sup> 2	<sup>3</sup>	<sup>*</sup> 4	<sup>5</sup>
A:	2	3	1	6	4	5
pse:	2	2	3	3	7	7
<u>s</u>	<u>e</u>		<u>sum</u>		<u>pse</u>	
1	3		1			
2	5		5			
0	4		7			
3	3		0			

$pse[e] - pse[s-1]$					
<sup>*</sup> 0	<sup>1</sup>	<sup>*</sup> 2	<sup>3</sup>	<sup>*</sup> 4	
2	4	3	1	5	
pse:	2	2	5	5	10

```
long[] getPrefixSumEv (int[] A)
{
```

HW

Break 8:38 AM

Question: Given a string  $S$  of lower case letters, return the count of pairs  $(i, j)$  such that  $i < j$  and  $S[i] = 'a'$  and  $S[j] = 'g'$ .

Eg:

$S = "a b e g a g"$   
 (0, 3) (4, 5)  
 (0, 5) (4, 3) 3

$S = "a c g d g a g"$   
 (0, 2) (0, 6)  
 (0, 4) (5, 6)

$S = "b c a g g a a g"$   
 (2, 3) (5, 7)  
 (2, 4) (6, 7)  
 (2, 7)

Brute Force:

$S = "b c a g g a a g"$   
 i  
 ↓

res :

```
function countAG(String S)
{
    result = 0;
    for (i = 0; i < S.length; i++)
    {
        if (S[i] == 'a')
        {
            for (j = i + 1 → S.length - 1)
            {
                if (S[j] == 'g')
                {
                    res++;
                }
            }
        }
    }
    return res;
}
```

i	j	res.
0		0
1		0
2	[3, 7]	3
3		3
4		3
5	[6, 7]	4
6	[7, 7]	5

TC:  $O(N^2)$

SC:  $O(1)$



## Optimised Solution:

Carry Fwd

S = <sup>0</sup>b <sup>1</sup>c <sup>2</sup>a <sup>3</sup>g <sup>4</sup>g <sup>5</sup>a <sup>6</sup>a <sup>7</sup><sup>i</sup>g

countA: ~~str~~ 3

res: ~~str~~ 5

if (g)  
{ res = res + countA }

if (A)  
{ countA++; }

TC:  $O(N)$

SC:  $O(1)$

## Subarrays:

Continuous part

of an array.

A: <sup>0</sup>4 <sup>1</sup>1 <sup>2</sup>2 <sup>3</sup>3 <sup>4</sup>-1 <sup>5</sup>6 <sup>6</sup>9 <sup>7</sup>8 <sup>8</sup>12

2, 3, -1, 6 → ✓

9 → ✓

$s = 0$

$e \rightarrow n$

2 4 1 6 -3 7 8 4

4, 12

1, 6, 8

1, 2, 6

3 2 1 4

(s, e)

7 8 4

<u>s</u>	<u>ne</u>	<u>N</u>
0	N	N
1	N-1	N-1
5	N-5	N-5

(4, 6) → -1, 6, 9

(0, 4) → 4, 1, 2, 3, -1

## Representation Of A SubArray:

A: <sup>0</sup>4 <sup>1</sup>1 <sup>2</sup>2 <sup>3</sup>3 <sup>4</sup>-1 <sup>5</sup>6 <sup>6</sup>9 <sup>7</sup>8 <sup>8</sup>12

(start, end)

$i \rightarrow N-i$

$7-1 \Rightarrow \underline{6}$

Problem: Print all sub-arrays of a given array A.

A: <sup>0</sup>3 <sup>1</sup>8 <sup>2</sup>10

i	j	
0	[0-2]	→ 3
1	[1-2]	→ 2
2	[2-2]	→ 1

```
{  
  for (i → 0 to N-1) // fix s  
  {
```

```
    for (j → i to N-1) // fix e
```

$N^2$   
↳ N

```
    {  
      for (k → i to j)
```

```
      {
```

$O(N^3)$

```
      }
```

```
    }
```

```
  }
```

Prefix sum

Carry Forward

Subarrays.

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