

# Experimental particle. physics

**esipap...**

European School of Instrumentation  
in Particle & Astroparticle Physics

2.

a few things about  
particle accelerators



# Why?

a small hint...

$$E = mc^2$$

Aren't natural radioactive processes enough?  
What about cosmic rays?

# Why accelerating and colliding particles?

Aren't natural radioactive processes enough? What about cosmic rays?

High energy

$$E = mc^2$$

Large number of collisions

$$N = \mathcal{L} \cdot \sigma$$

- Probe smaller scale
- Produce heavier particles
- Detect rare processes
- Precision measurements

# Luminosity

Number of events  
in unit of time

$$N = \mathcal{L} \cdot \sigma$$

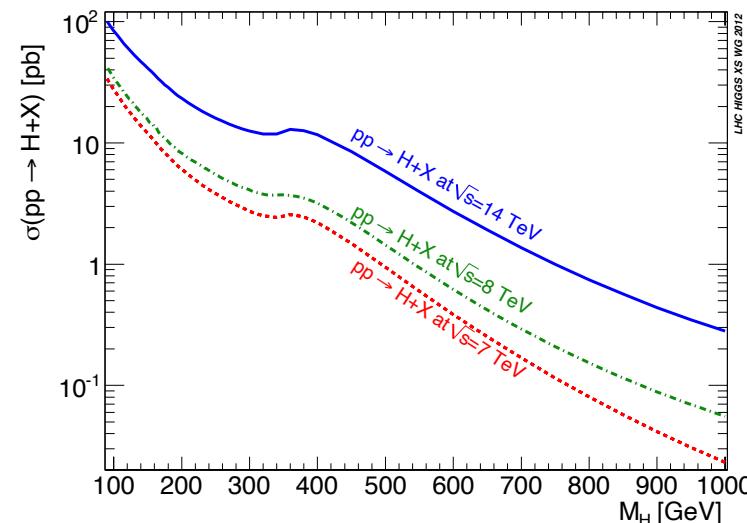
$\mathcal{L}$  [t<sup>-1</sup>]       $\sigma$  [L<sup>-2</sup> t<sup>-1</sup>]       $\sigma$  [L<sup>2</sup>]  
10<sup>34</sup> cm<sup>-2</sup> s<sup>-1</sup>



In a collider ring...

$$\mathcal{L} = \frac{1}{4\pi} \frac{fkN_1N_2}{\sigma_x\sigma_y}$$

Current Beam sizes (RMS)



# What particle to accelerate and collide?

- **Stable (charged) particle**

- ✓ Electron/positron
- ✓ Proton/antiproton



*what particle should we use?*

- **Secondary beams of charged or neutral particles**

- ✓ (Anti)neutrinos
- ✓ Muons
- ✓ Photons
- ✓ Charged pions
- ✓ Kaons
- ✓ ...

# Particle accelerations for dummies

(non-relativistic)  
Lorentz Force

$$\vec{F}_L = q \left( \vec{E} + \vec{v} \times \vec{B} \right)$$

time variation of  
kinetic energy

$$\frac{dE_{\text{kin}}}{dt} = \vec{F}_L \cdot \vec{v} = q\vec{v} \cdot \vec{E}$$

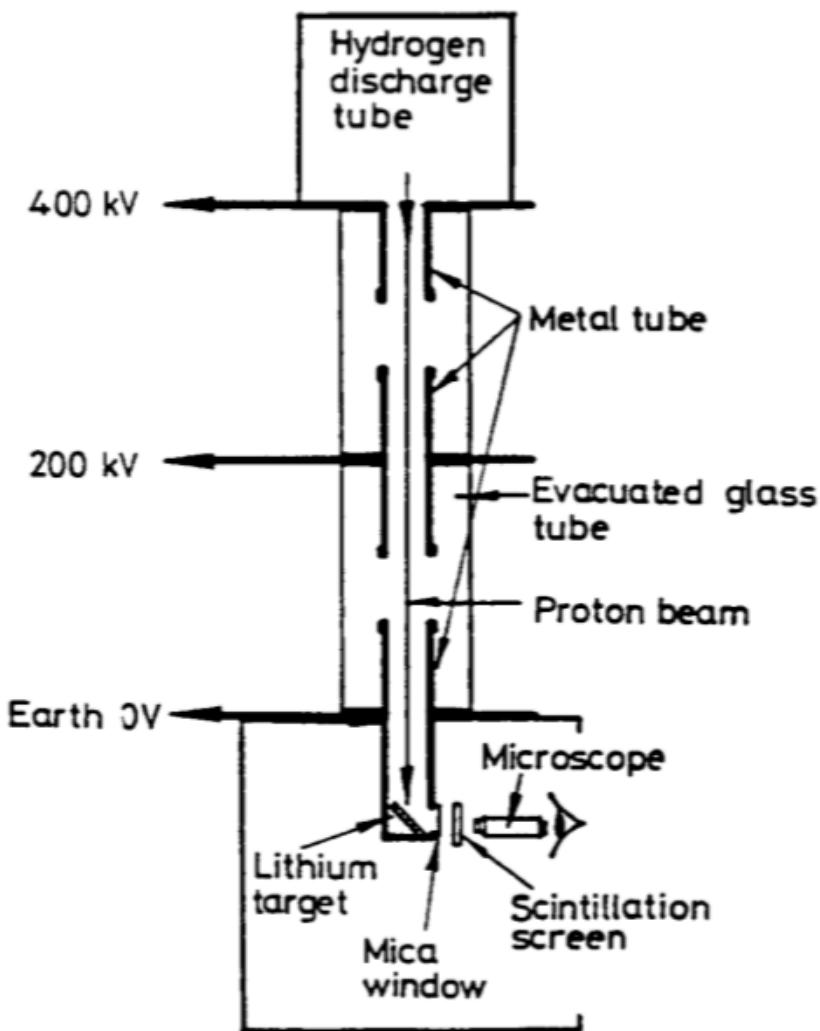
- Only longitudinal component of electrical field matters
- Time-varying electrical field to change energy
- (Static) magnetic field cannot change particle momentum...
- ... but can be used to bend its trajectory!

# A brief history of particle accelerators – part I

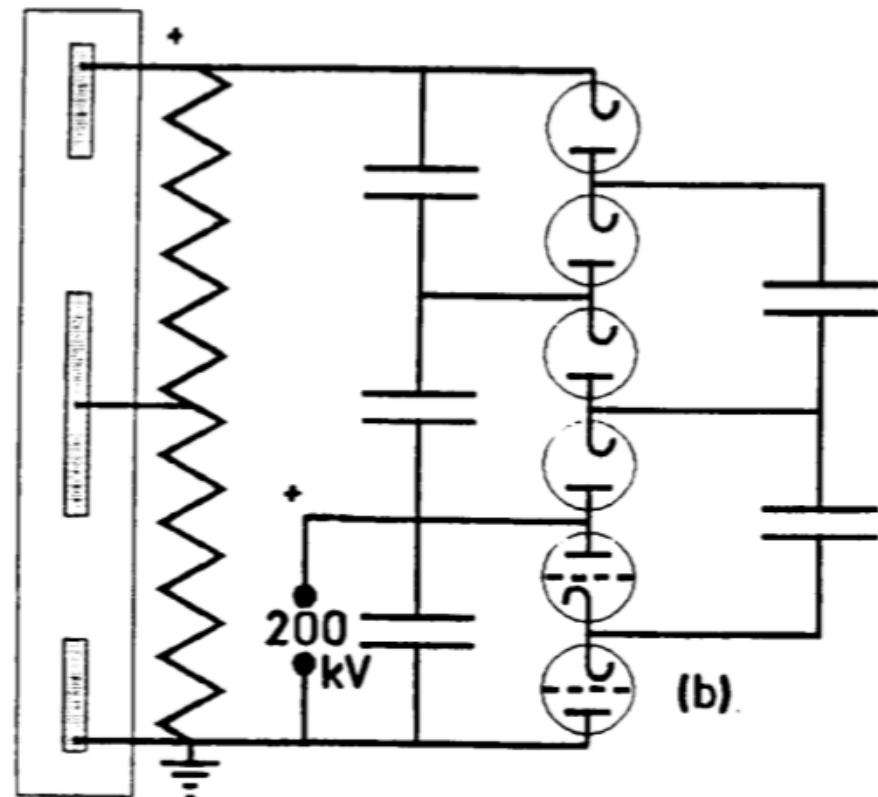
1906	Rutherford bombards mica sheet with natural alphas and develops the theory of atomic scattering.	Natural alpha particles of several MeV
1911	Rutherford publishes theory of atomic structure.	
1919	Rutherford induces a nuclear reaction with natural alphas.	
... Rutherford believes he needs a source of many MeV to continue research on the nucleus. This is far beyond the electrostatic machines then existing, but ...		
1928	<b>Gamov predicts tunnelling and</b> perhaps 500 keV would suffice ...	
1928	Cockcroft & Walton start designing an 800 kV generator encouraged by Rutherford.	
1932	Generator reaches 700 kV and Cockcroft & Walton split lithium atom with only 400 keV protons. They received the Nobel Prize in 1951.	

(inspired by “A brief history and review of accelerators” by P.J Bryant <https://cds.cern.ch/record/2610621>)

# Cockcroft and Walton's apparatus

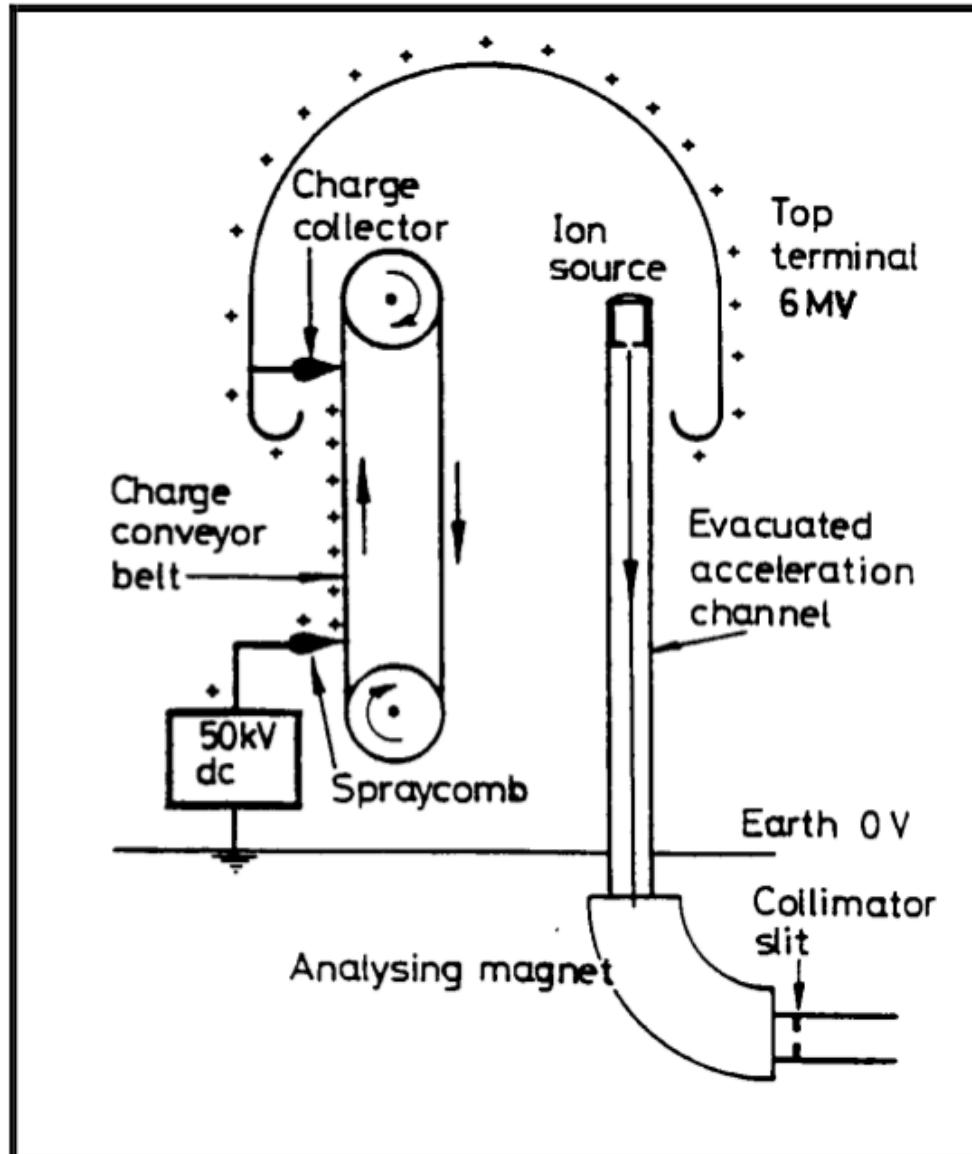


(a) Accelerating column

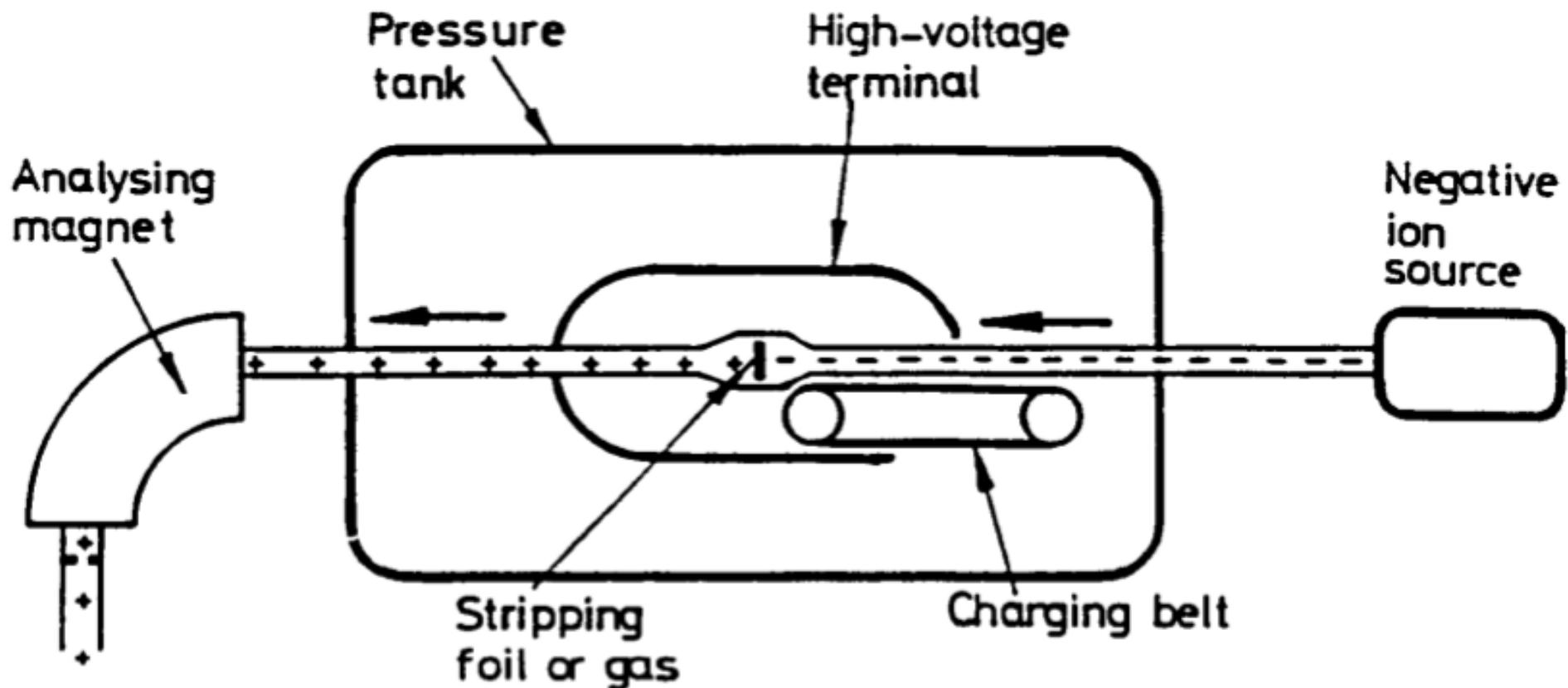


(b) DC generator

# Van de Graaff electrostatic generator



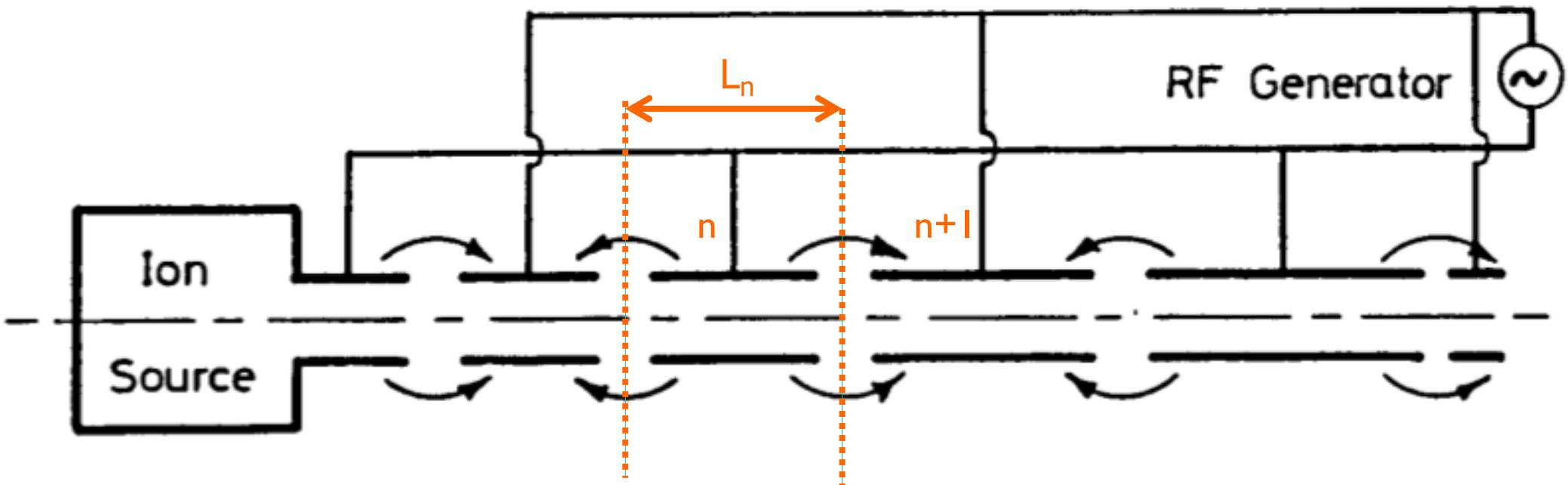
# Two-stage Tandem accelerator



# A brief history of particle accelerators – part 2

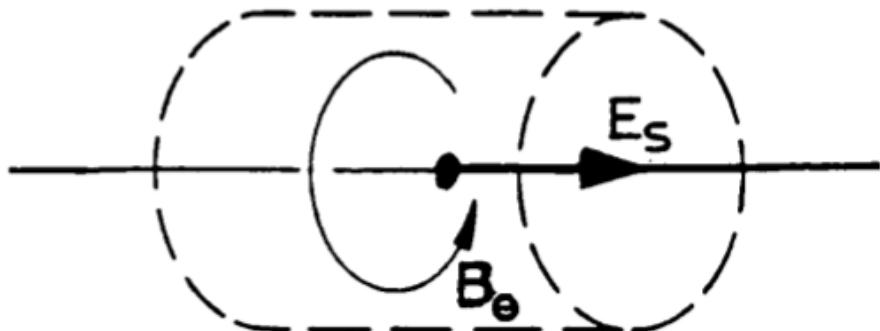
- 1924 Ising proposes time-varying fields across drift tubes. This is "resonant acceleration", which can achieve energies above that given by the highest voltage in the system.
- 1928 Wideröe demonstrates Ising's principle with a 1 MHz, 25 kV oscillator to make 50 keV potassium ions.
- 1929 Lawrence, inspired by Wideröe and Ising, conceives the cyclotron.
- 1931 Livingston demonstrates the cyclotron by accelerating hydrogen ions to 80 keV.
- 1932 Lawrence's cyclotron produces 1.25 MeV protons and he also splits the atom just a few weeks after Cockcroft and Walton (Lawrence received the Nobel Prize in 1939).

# RF linear accelerator (LINAC)



$$L_n = k \frac{v_n \lambda}{c} \frac{2}{2}$$

Wideore:  $k=1$ ,  $L < \lambda$



# LINAC length

Total LINAC length

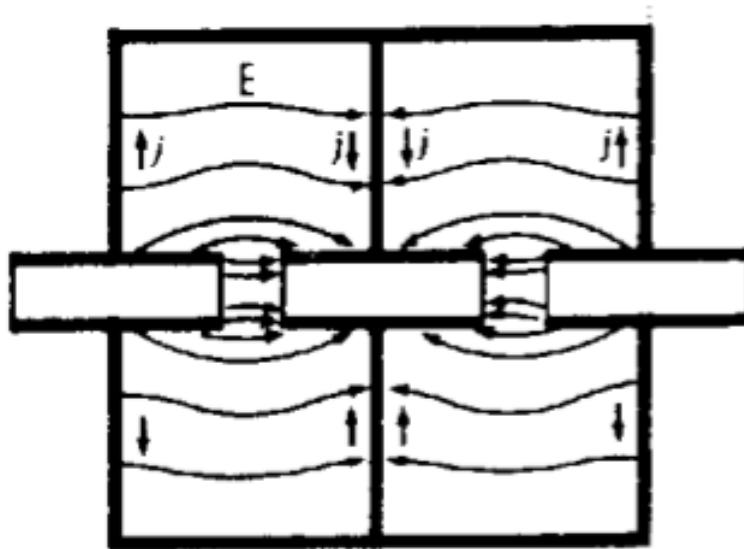
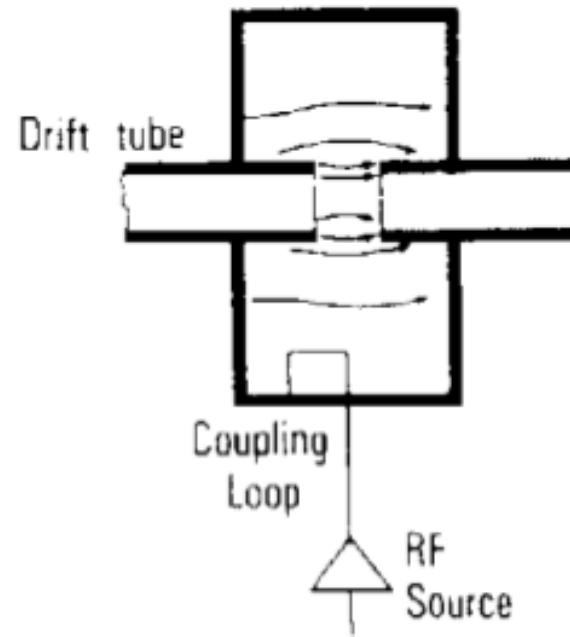
$$L = \frac{k}{\Delta E} \sqrt{\frac{E^3}{Amc^2}} \frac{\lambda}{2}$$

final particle energy  
energy gain per gap  
ion atomic number

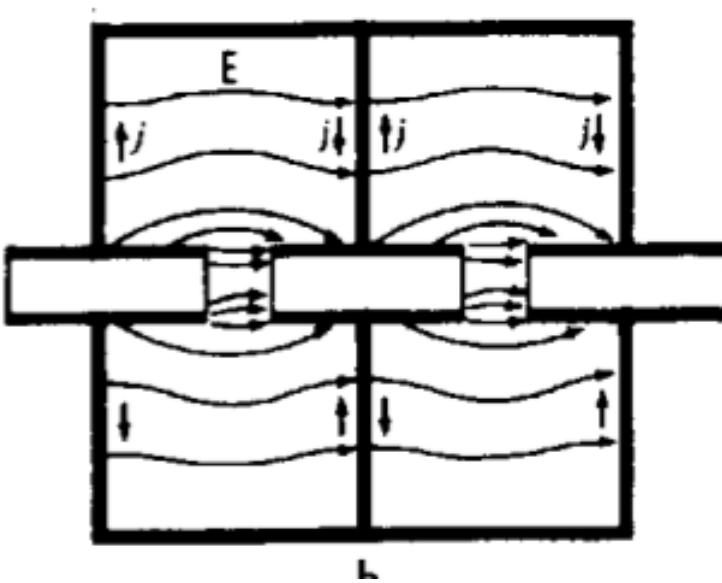
- Example:
  - ✓ proton ( $A=1$ ) with  $E = 1 \text{ MeV}$  ( $\beta = 4.6 \cdot 10^{-2}$ )
  - ✓ if  $v_{RF} = 7 \text{ MHz}$  proton will travel about 1m in half a RF cycle
- **Total LINAC length increases dramatically with speed**
- A possible solution would be to increase  $v_{RF}$
- ... but at very high  $v_{RF}$  open tube structure radiates too much energy!

# RF cavities

- The problem can be solved by closing the structure as a **cavity**...
- Cavities can be joined
- Choosing  $k=2$  currents on walls cancel, and walls can be eliminated

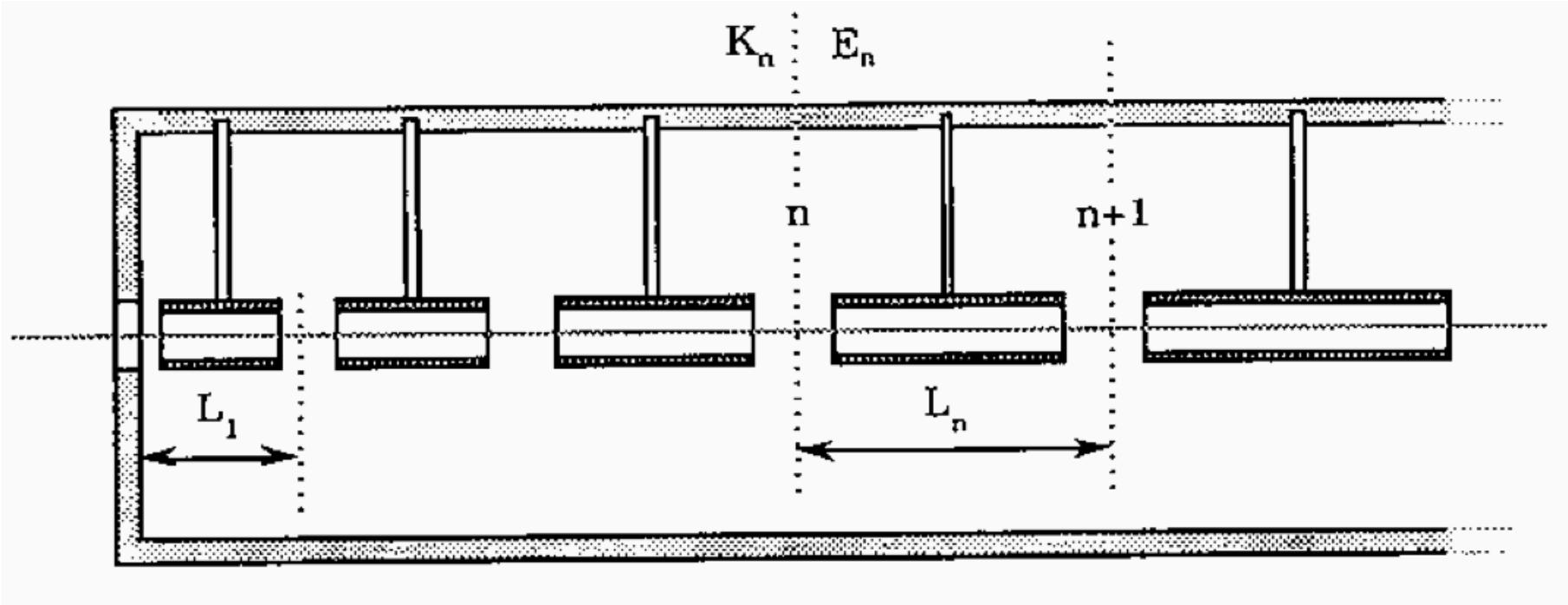


$k=1$



$k=2$

# Alvarez structure



$$k = 2, v_{RF} \sim 100 \text{ MHz}, \lambda < L$$

protons  $\beta \sim 1$  for  $E \sim 10 \text{ GeV}$

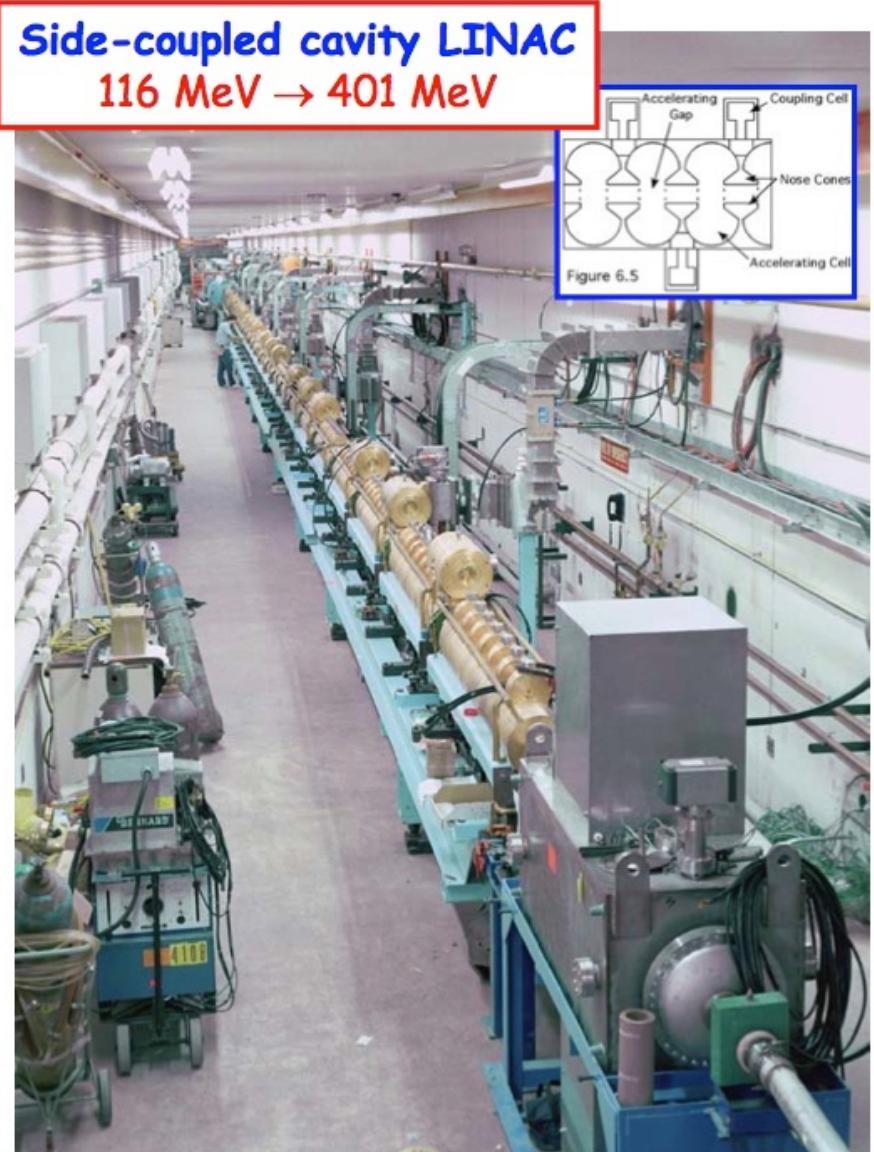
electrons  $\beta \sim 1$  for  $E \sim 10 \text{ MeV}$

already at those energies  $v \sim c \rightarrow$  drift tube length can stay constant!

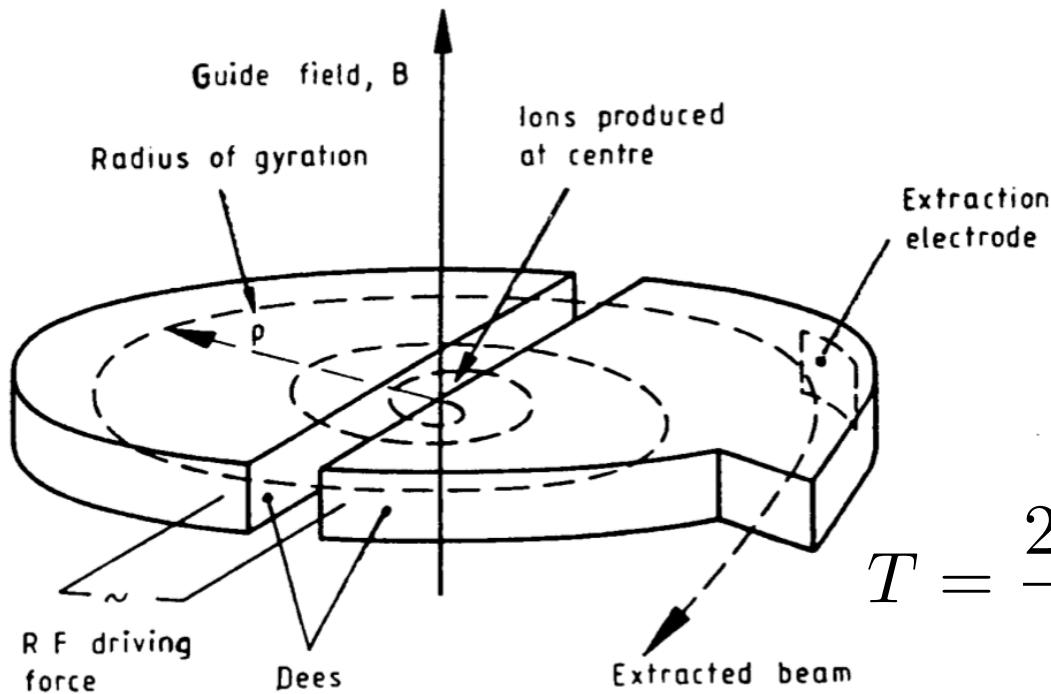
# Example: Fermilab LINAC



Drift tube (Alvarez) LINAC  
 $750 \text{ keV} \rightarrow 116 \text{ MeV}$

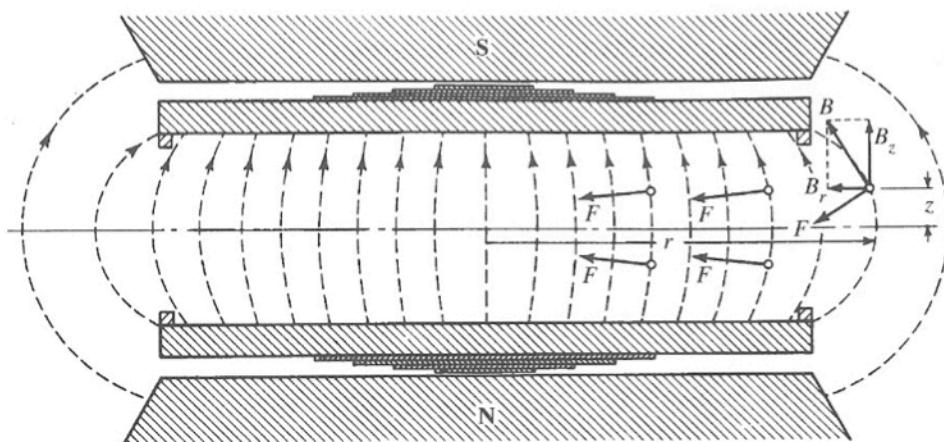


# (Syncro) Cyclotron



$$p = m\gamma\beta$$
$$p = eBR$$

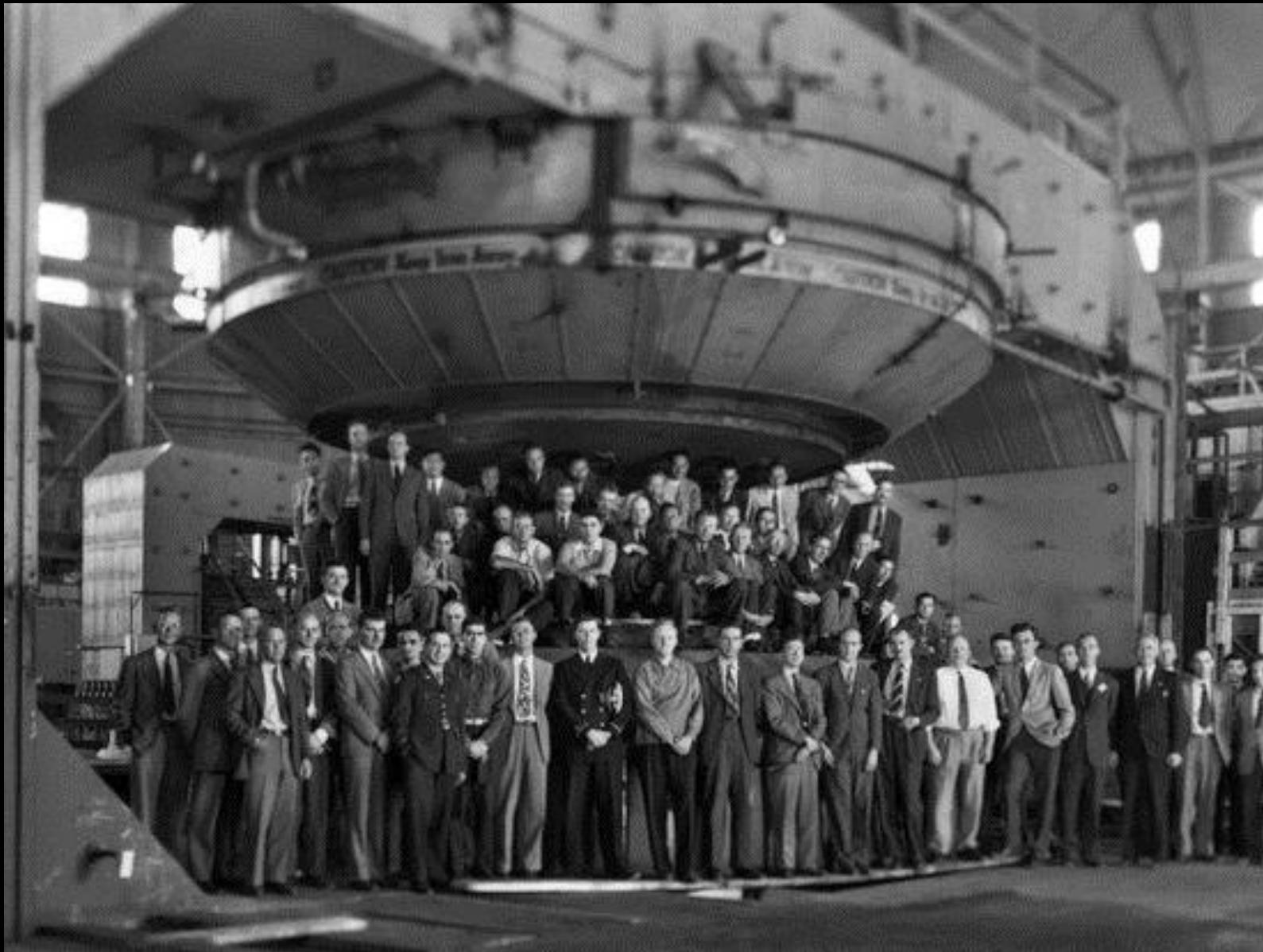
$$T = \frac{2\pi R}{v} = \frac{2\pi R}{\beta} = \frac{\pi p}{eB\beta c} = \gamma \frac{\pi m}{eB}$$



for relativistic particle **cyclotron frequency**  
should be adjusted to speed/energy  
**(syncro-cyclotron)**

weak focusing

# Berkeley syncro-cyclotron ( $p, E = 340$ MeV)



# The road toward synchrotrons

- Problems in RF acceleration in the 1940s...

- ✓ Linacs

- Poor RF sources; electron tube technology was yet in its infancy

- ✓ Cyclotrons

- Relativistic effects → asynchronous RF

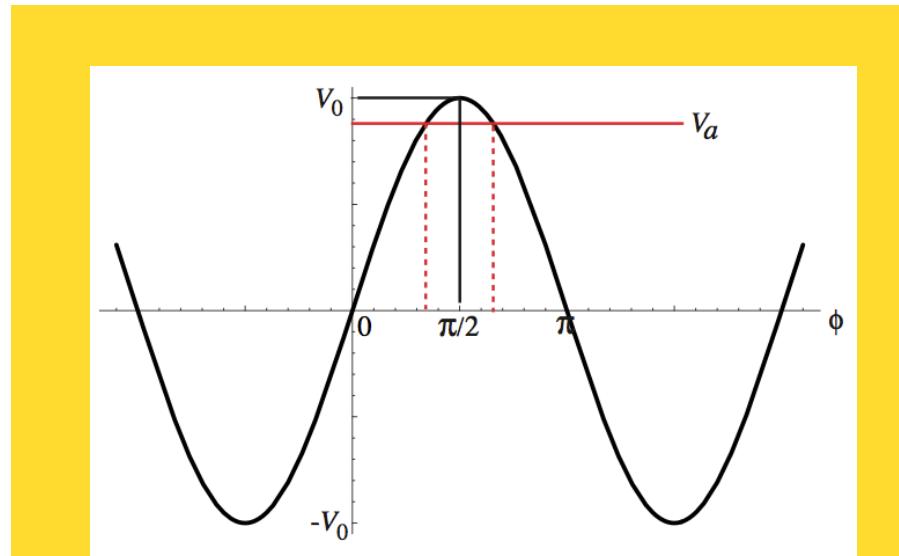
- Advancements during WW2

- ✓ High power microwave tubes for the radars were put to practical use
    - Magnetrons and klystrons

- ✓ Discovery of the **phase stability principle** in RF acceleration

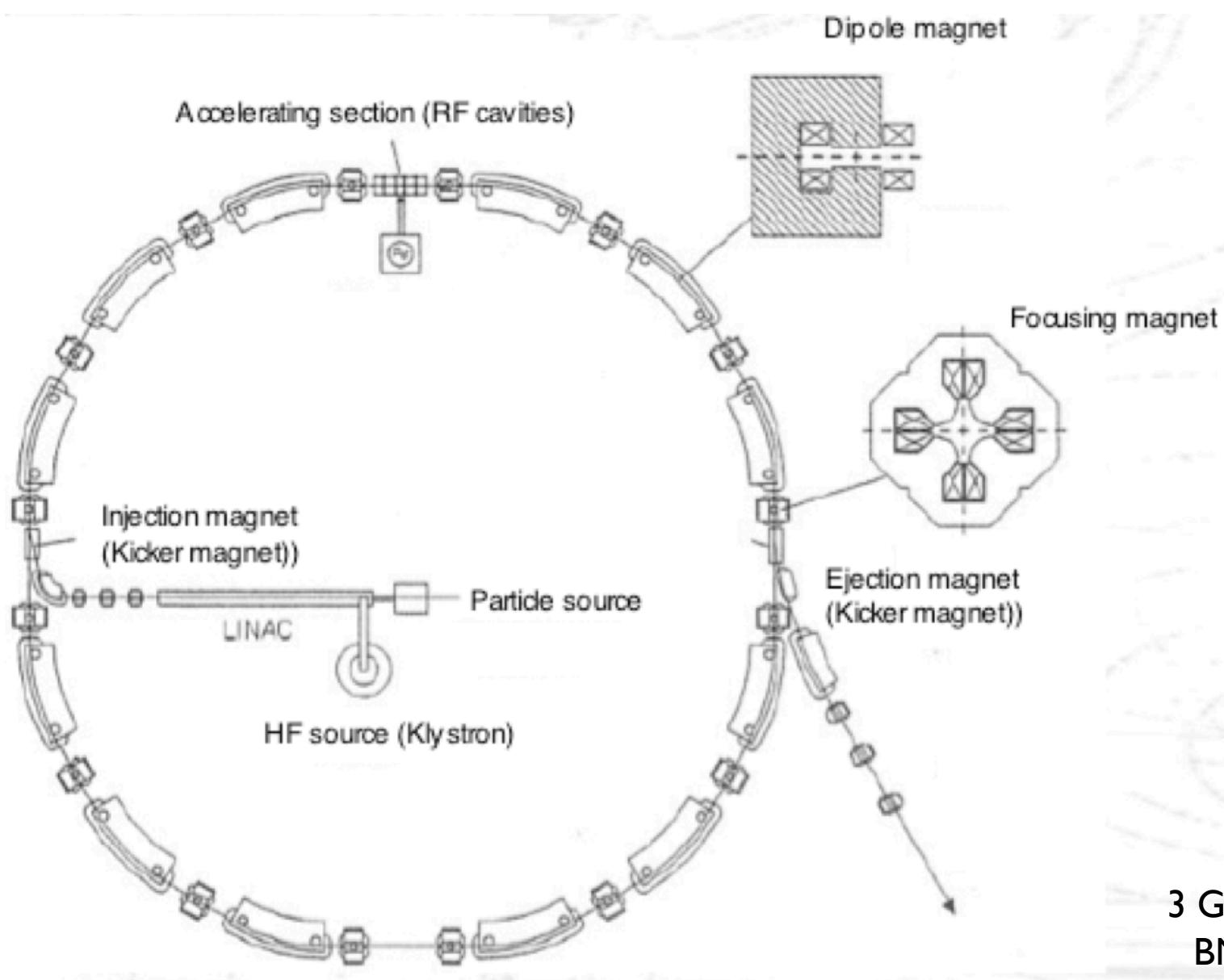
- Veksler (1944) and McMillan (1945)

- ✓ **Cyclotron → synrocyclotron → synchrotron**

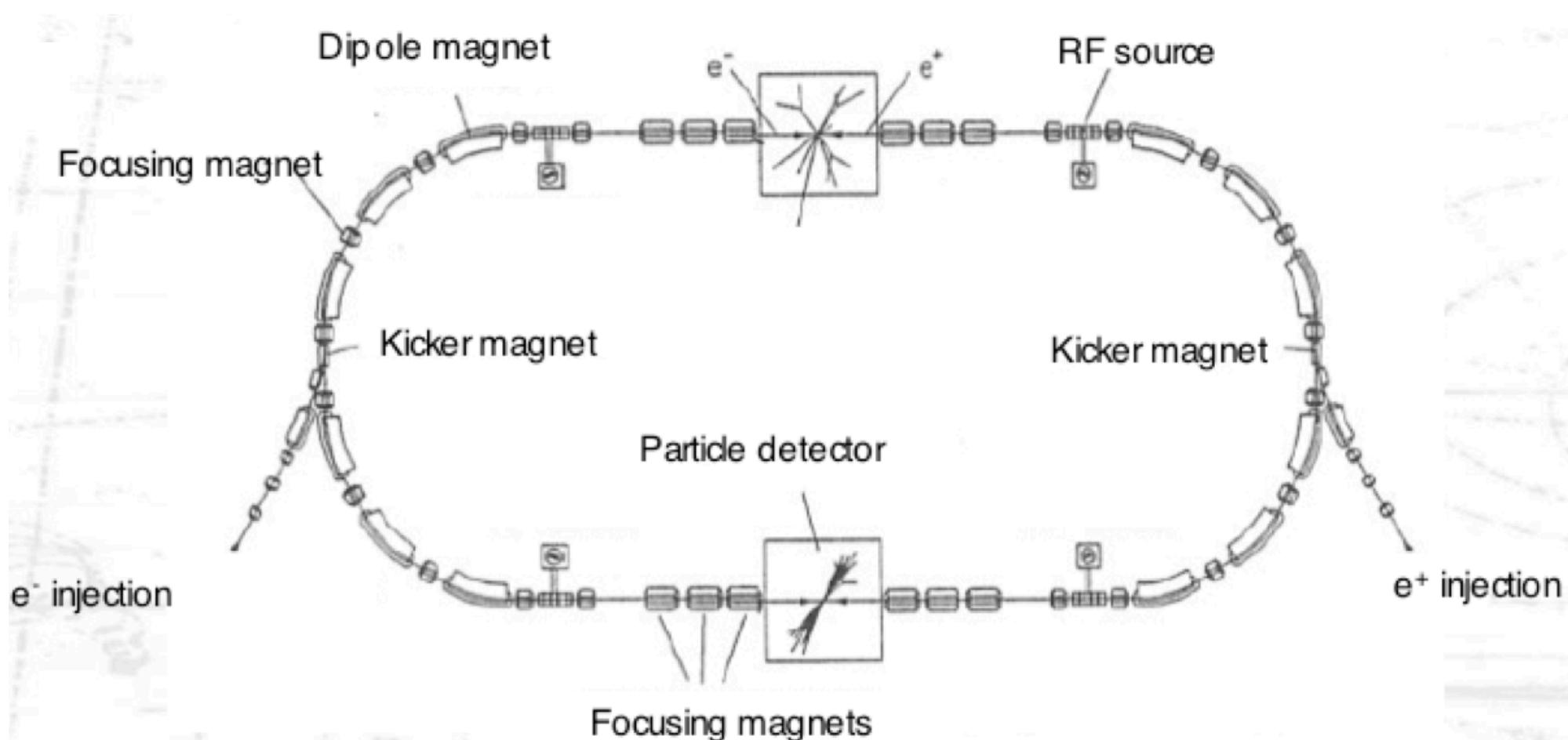


- Particles of different energies have differences in velocity and in orbit length
  - ✓ particles may be asynchronous wrt RF frequency
- RF field have however a restoring force at a certain phase, around which asynchronous particles be captured in **bunches**

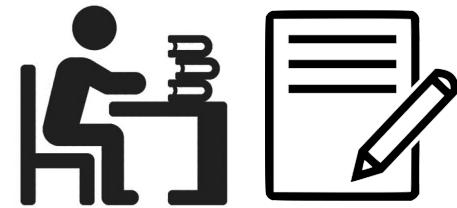
# Syncrotron



# Storage rings



# Fixed target vs. collider



$$m_1 \quad \longrightarrow$$

$$\mathbf{p}_1$$

$$m_2$$



$$\mathbf{p}_2 = 0$$

$$m_1 \quad \longrightarrow$$

$$\mathbf{p}'_1$$

$$\longleftarrow \quad m_2$$

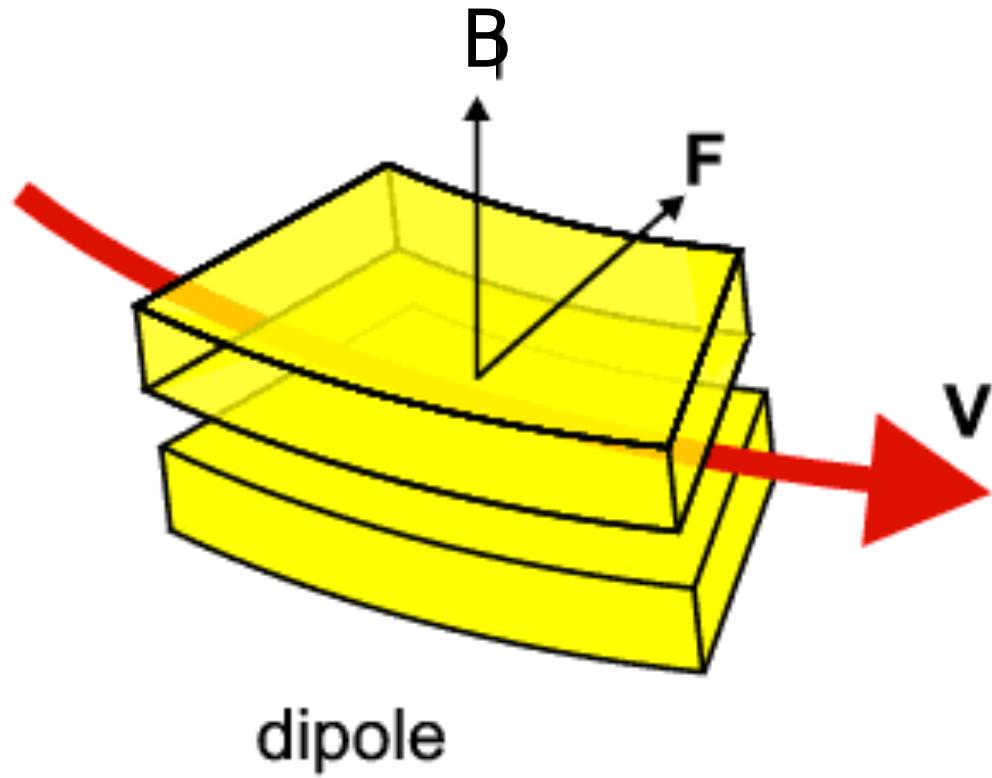
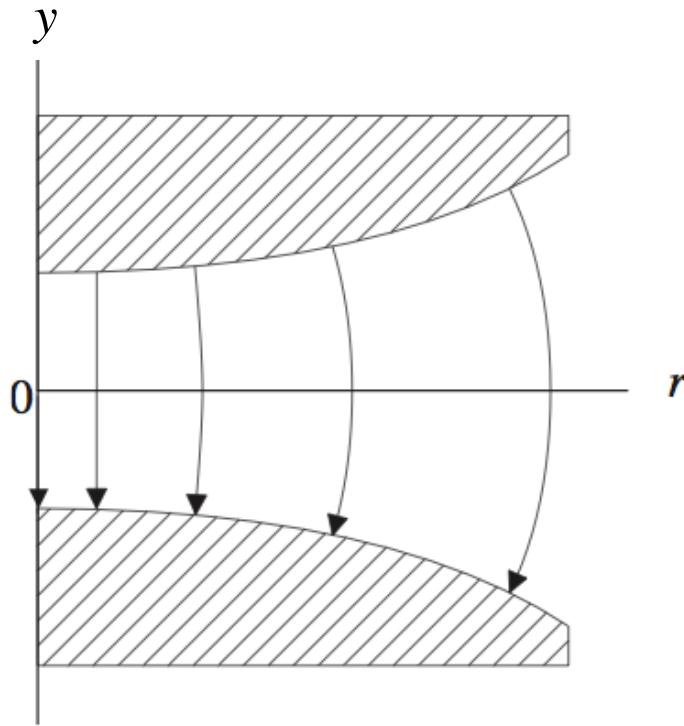
$$\mathbf{p}'_2 = -\mathbf{p}'_1$$

How much energy should a fixed target experiment have to equal the center of mass energy of two colliding beam?

$$E_{\text{fix}} = 2 \frac{E_{\text{col}}^2}{m} - m$$

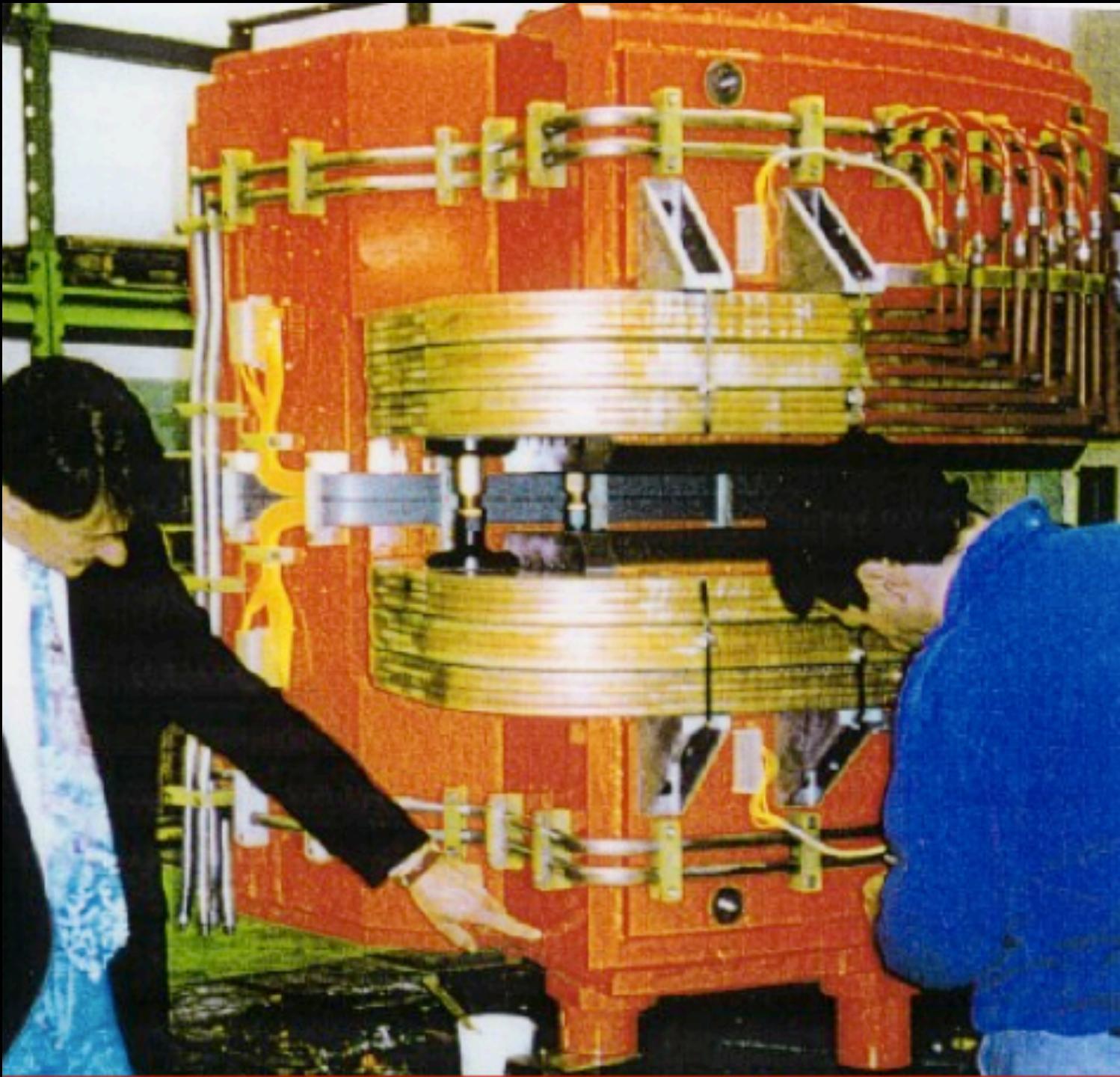
Try to compute it as homework

# Bending: dipoles

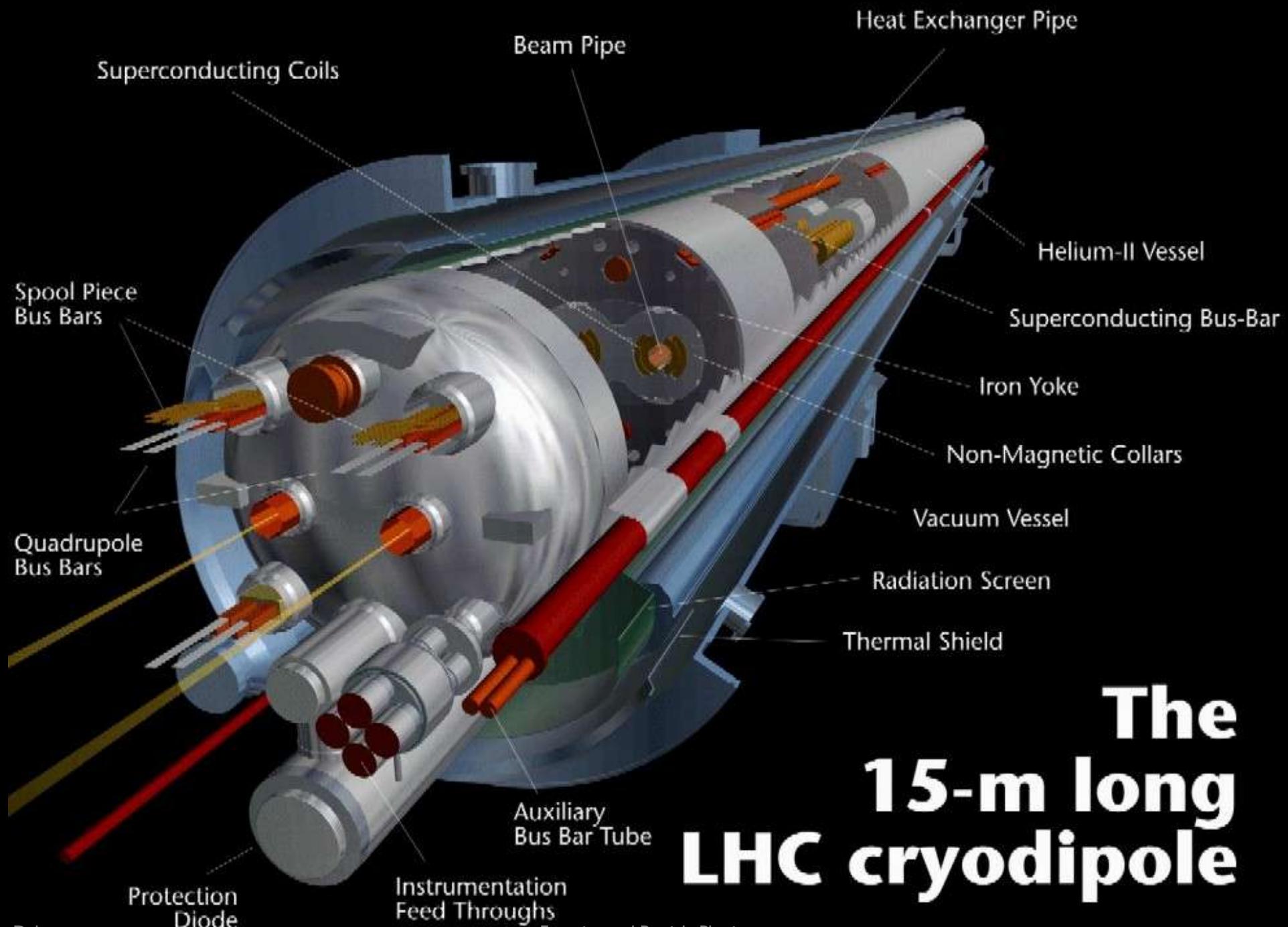


$$\begin{aligned}B_x &= 0 \\B_y &= B \\B_z &= 0\end{aligned}$$

$$\frac{1}{R} [\text{m}^{-1}] = 0.3 \frac{B [\text{T}]}{E [\text{GeV}]}$$





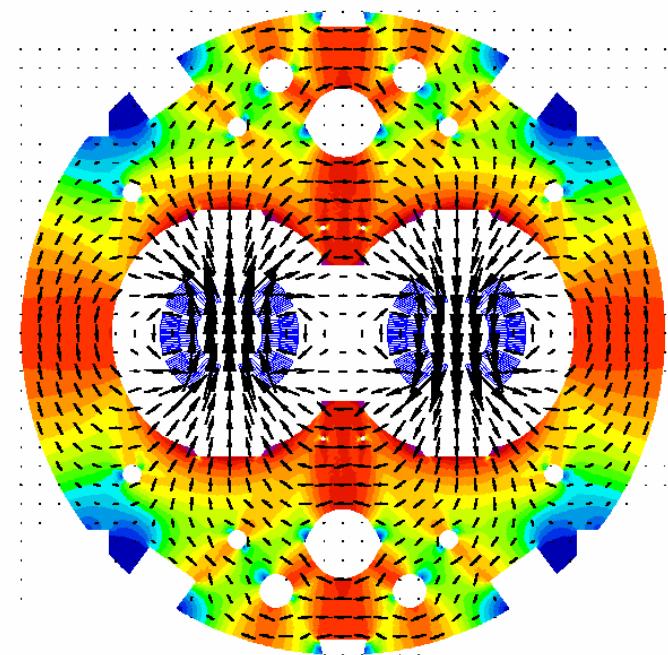
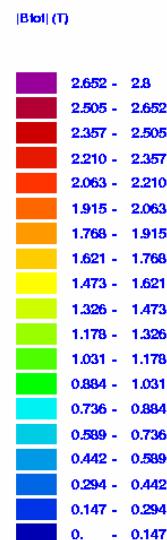
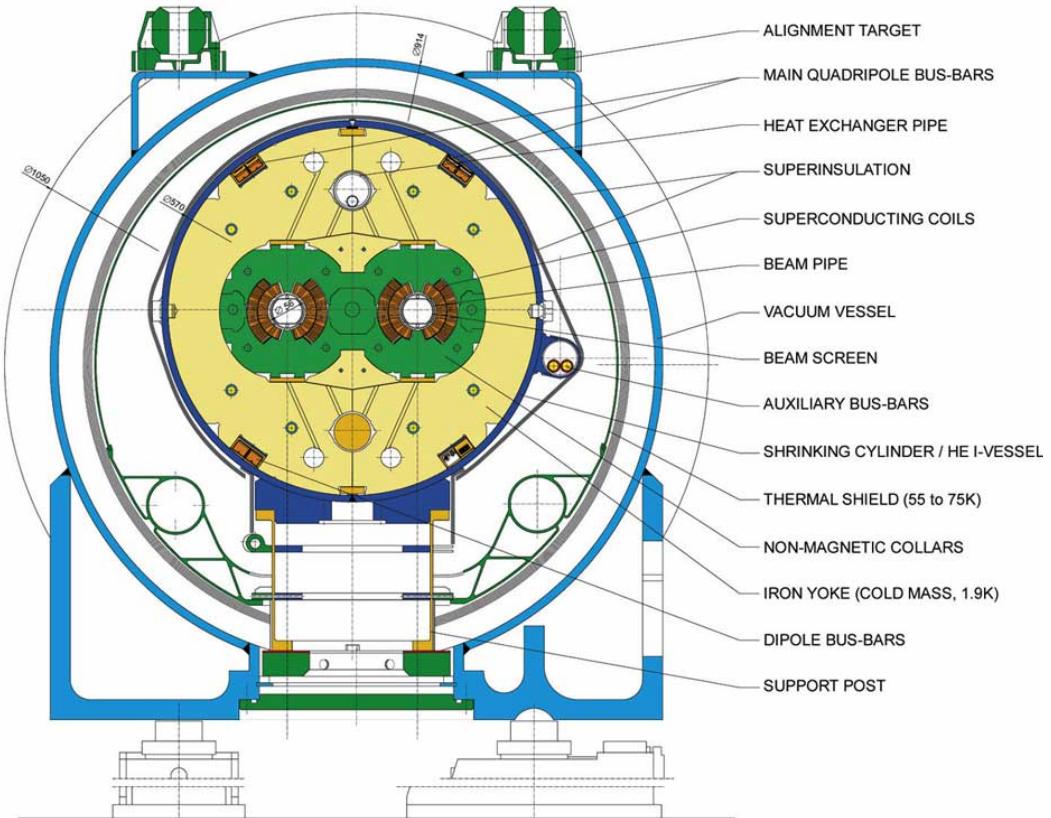


# The 15-m long LHC cryodipole

# LHC dipoles

## LHC DIPOLE : STANDARD CROSS-SECTION

CERN AC/DI/MM - HE107 - 30 04 1999



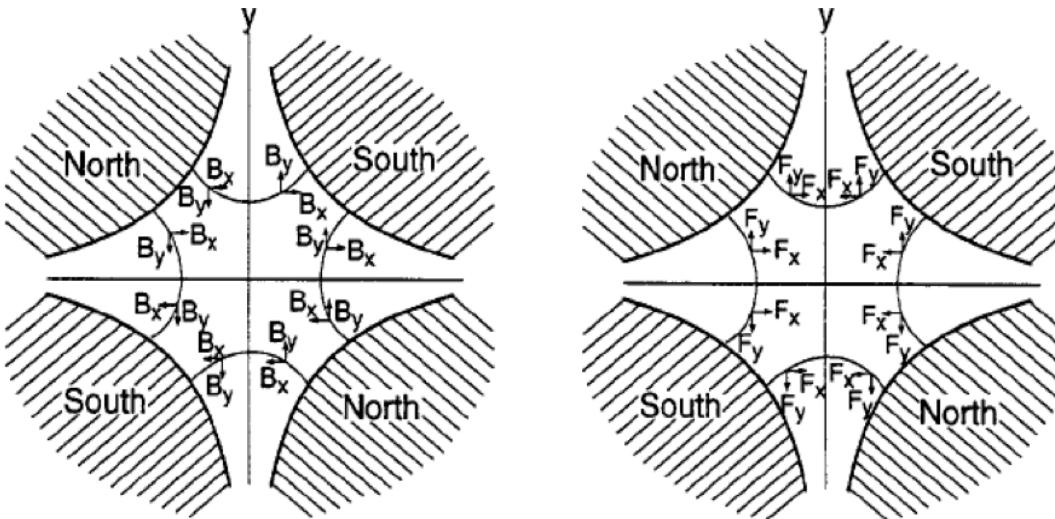
# Focusing (defocusing): quadrupoles

$$\mathbf{B}_x = -g \times \mathbf{x}$$

$$\mathbf{B}_y = -g \times \mathbf{y}$$

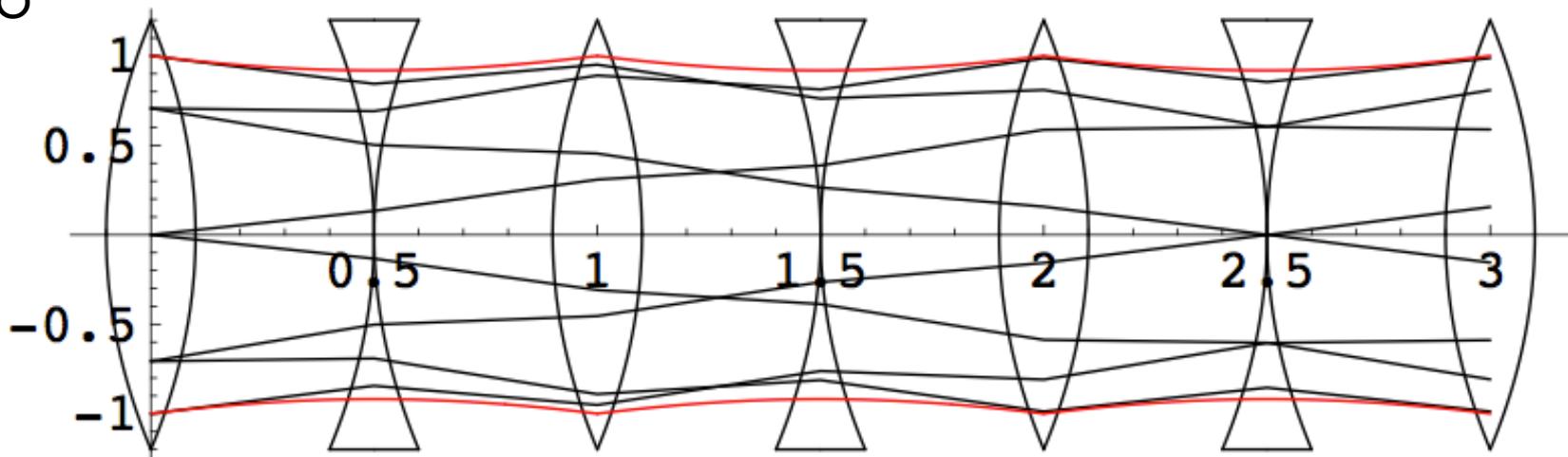
$$\mathbf{B}_z = 0$$

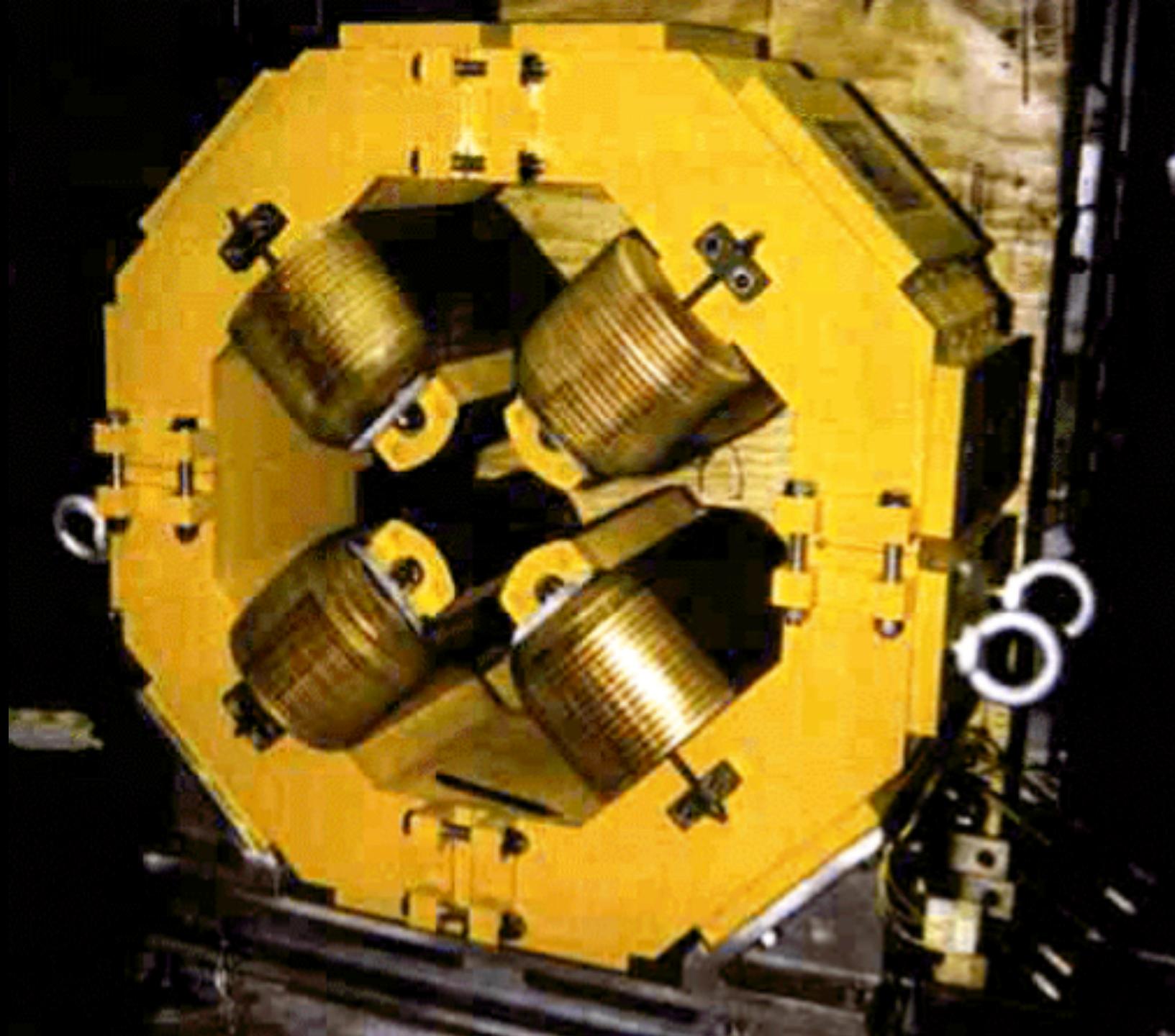
$$g[\text{T/n}] = \text{field gradient}$$



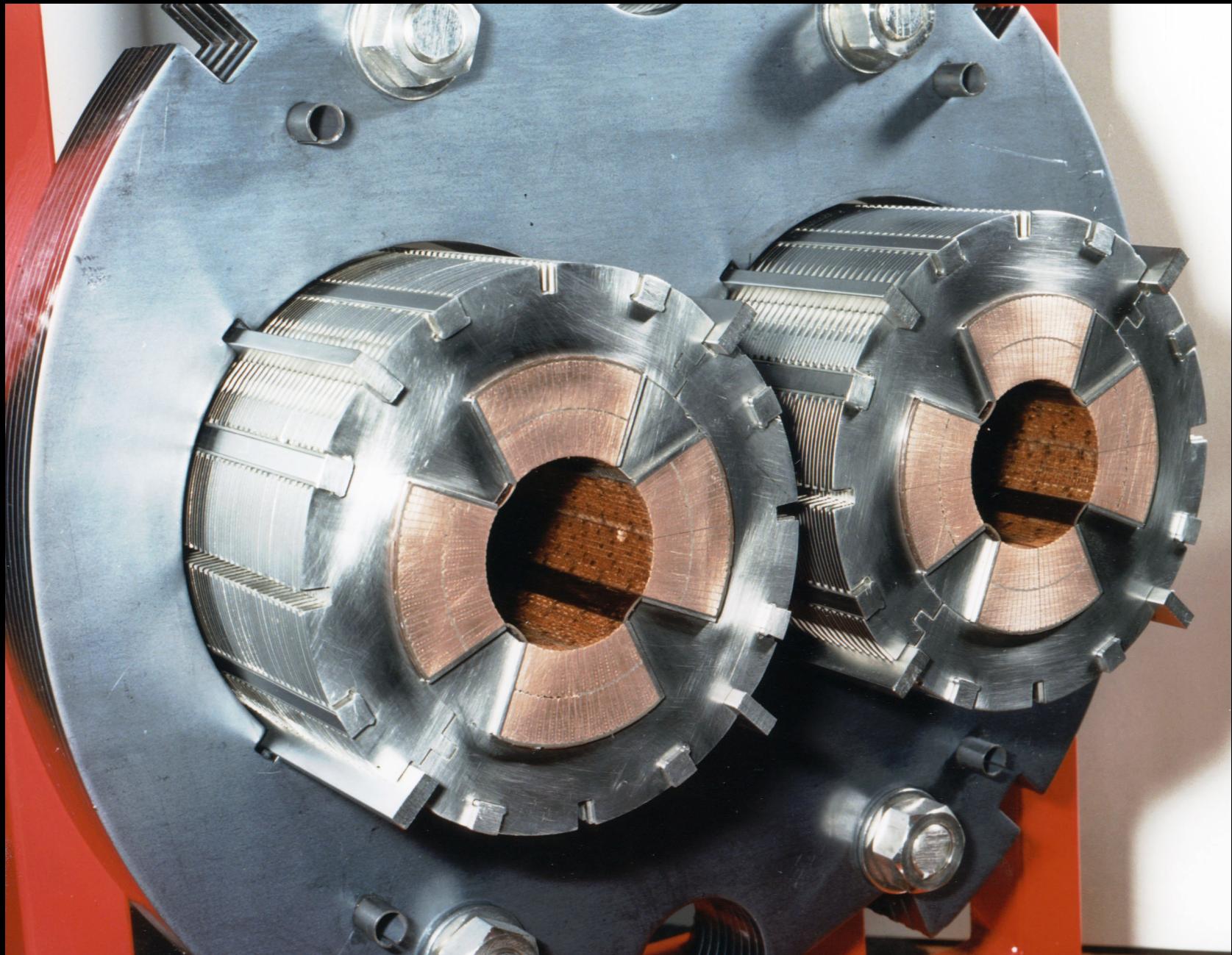
Focusing in one direction, defocusing in the other

FO-DO  
array









# Group exercise! LHC dipole magnetic field

Assuming a proton beam of momentum

$$p = 7 \text{ TeV}$$



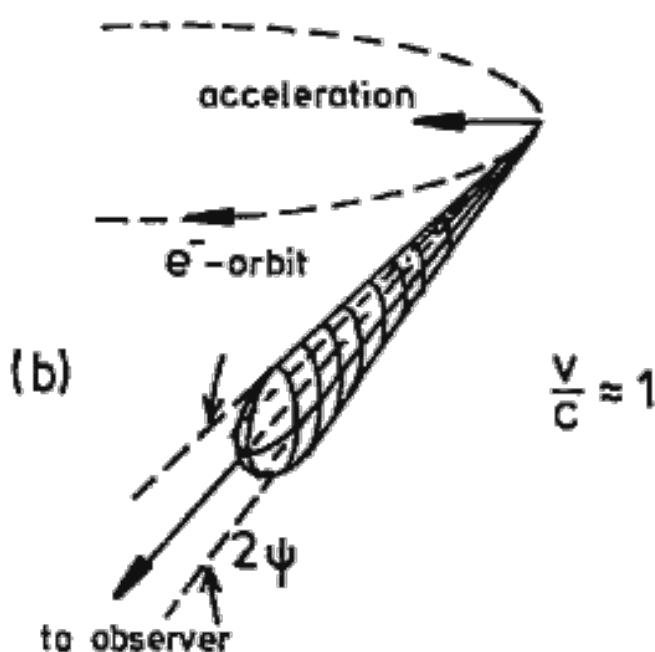
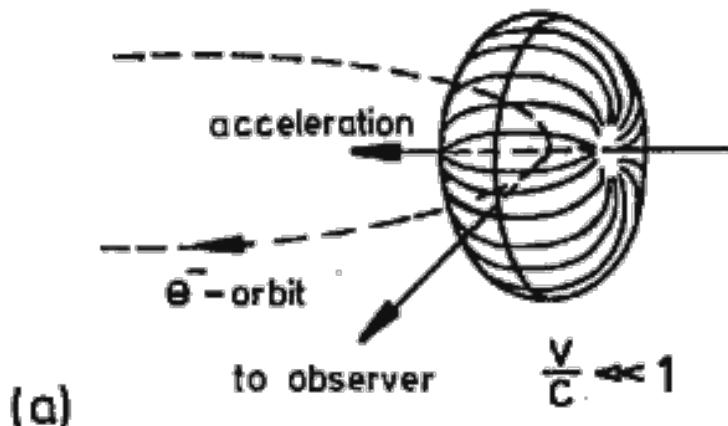
What is the magnetic field of the LHC dipoles?

Reminders:

- The LHC is 27 km long
- There are 1230 dipoles in LHC
- Each dipole is 14.4 m long

$$\frac{1}{R} [\text{m}^{-1}] = 0.3 \frac{B[\text{T}]}{E[\text{GeV}]}$$

# Syncrotron radiation



energy lost per revolution

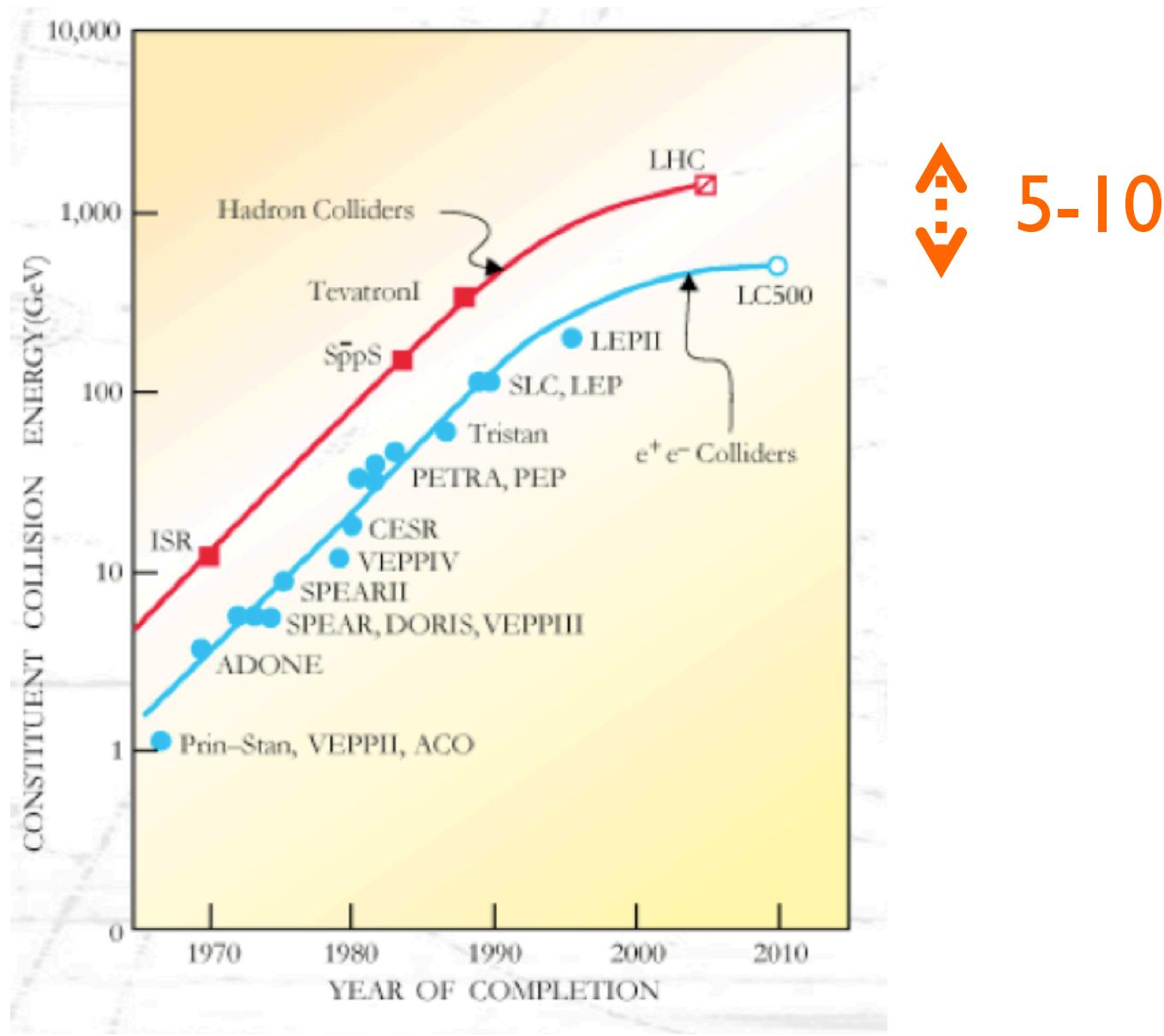
$$\Delta E = \frac{4\pi}{3} \frac{1}{4\pi\epsilon_0} \left( \frac{e^2 \beta^3 \gamma^4}{R} \right)$$

electrons vs. protons

$$\frac{\Delta E_e}{\Delta E_p} \simeq \left( \frac{m_p}{m_e} \right)^4$$

It's easier to accelerate protons to higher energies, but protons are fundamentals...

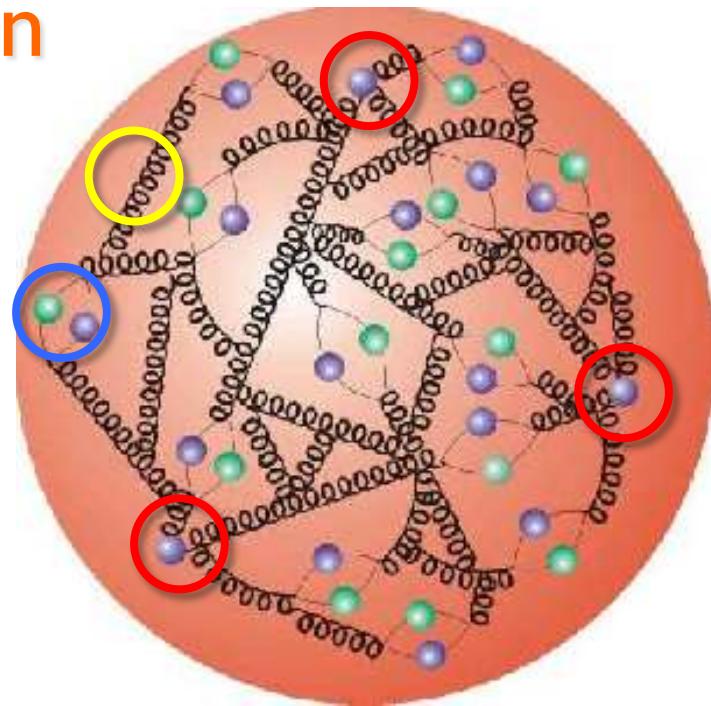
# $e^+e^-$ vs. hadron collider



# About the inner life of a proton

- **protons have substructures**

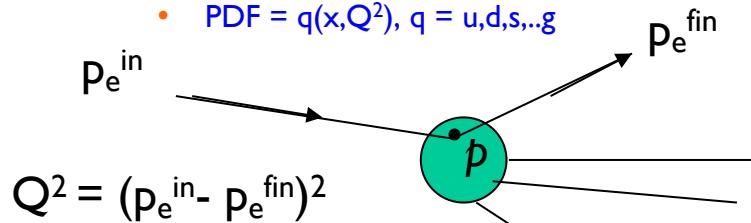
- ✓ partons = quarks & gluons
- ✓ 3 valence (colored) quarks bound by gluons
- ✓ Gluons (colored) have self-interactions
- ✓ Virtual quark pairs can pop-up (sea-quark)
- ✓  $\not{p}$  momentum shared among constituents
  - described by  $\not{p}$  structure functions



- **Parton energy not 'monochromatic'**

- ✓ Parton Distribution Function

- $\text{PDF} = q(x, Q^2)$ ,  $q = u, d, s, g$

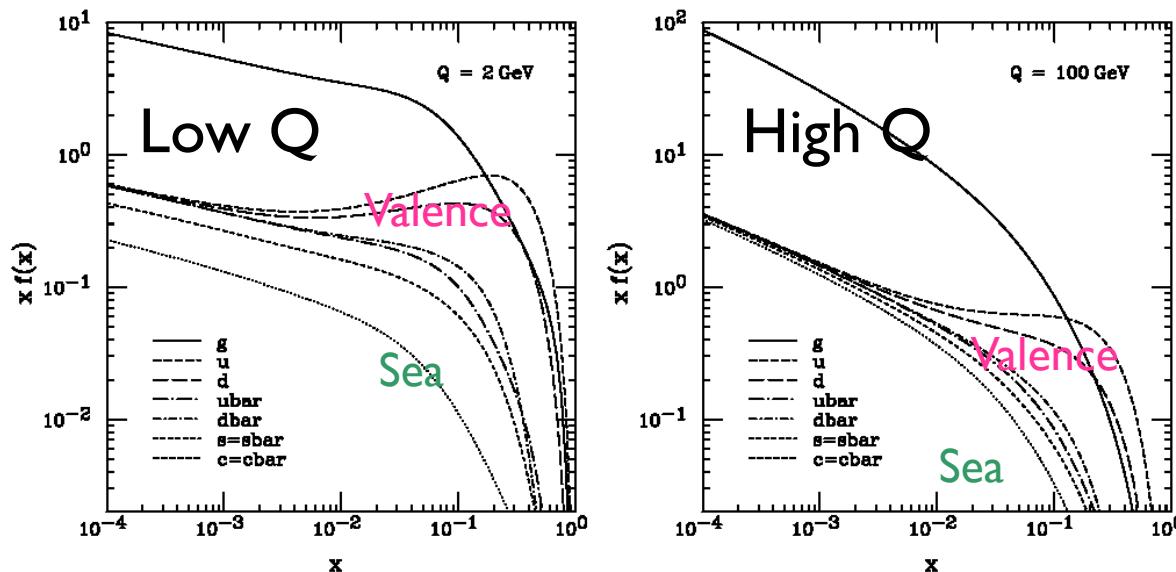


- **Kinematic variables**

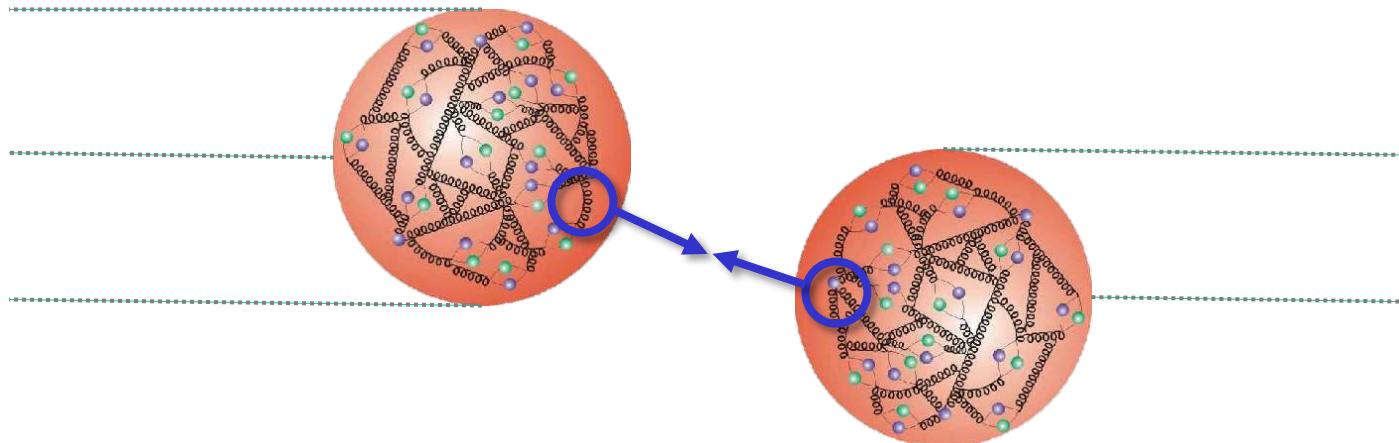
- ✓ Bjorken- $x$ : fraction of the proton momentum carried by struck parton

- $x = p_{\text{parton}}/p_{\text{proton}}$

- ✓  $Q^2$ : 4-momentum<sup>2</sup> transfer

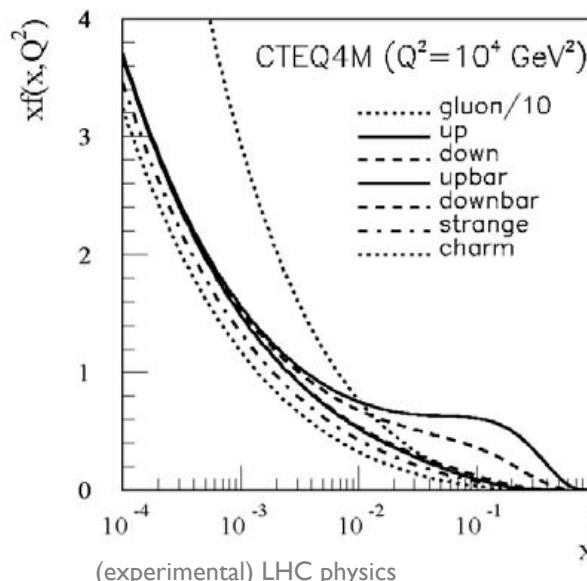
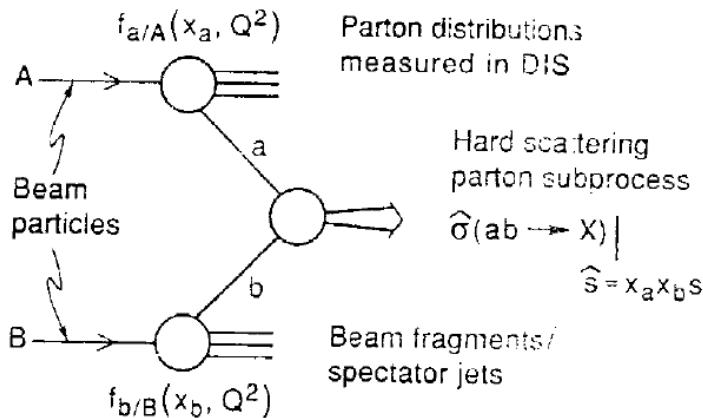


# Cross sections at a proton-proton collider



$$\sqrt{\hat{s}} = \sqrt{x_a x_b s}$$

$$\sigma = \sum_{a,b} \int dx_a dx_b f_a(x, Q^2) f_b(x, Q^2) \hat{\sigma}_{ab}(x_a, x_b)$$

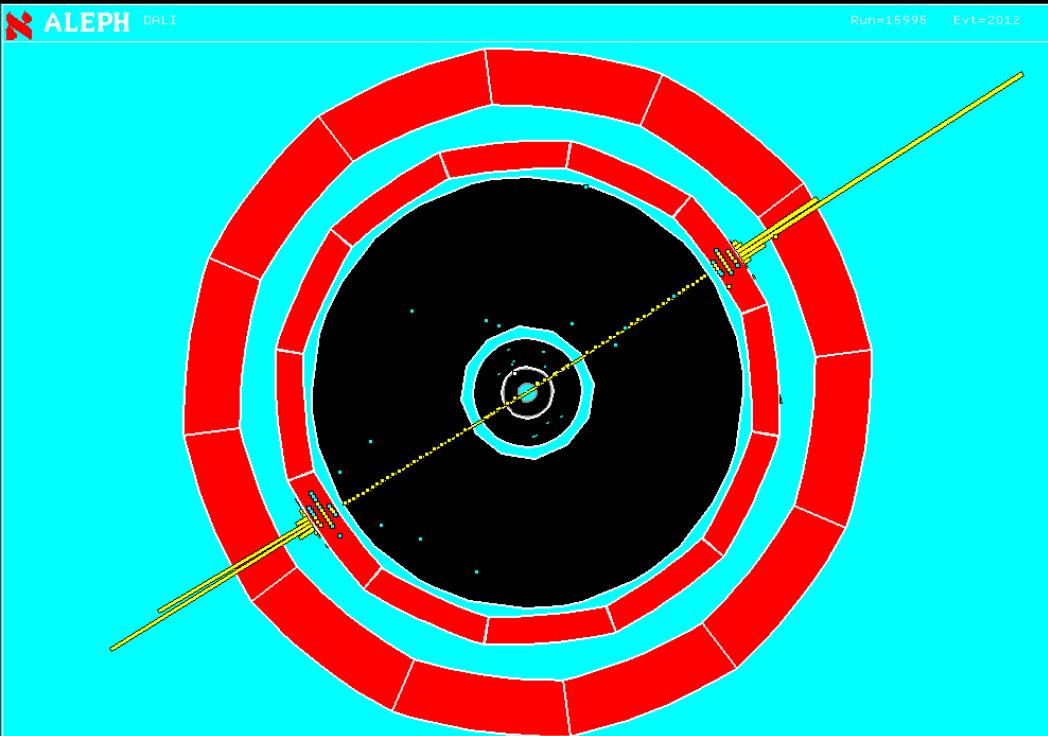


Example: to produce a particle with mass  $m = 100 \text{ GeV}$

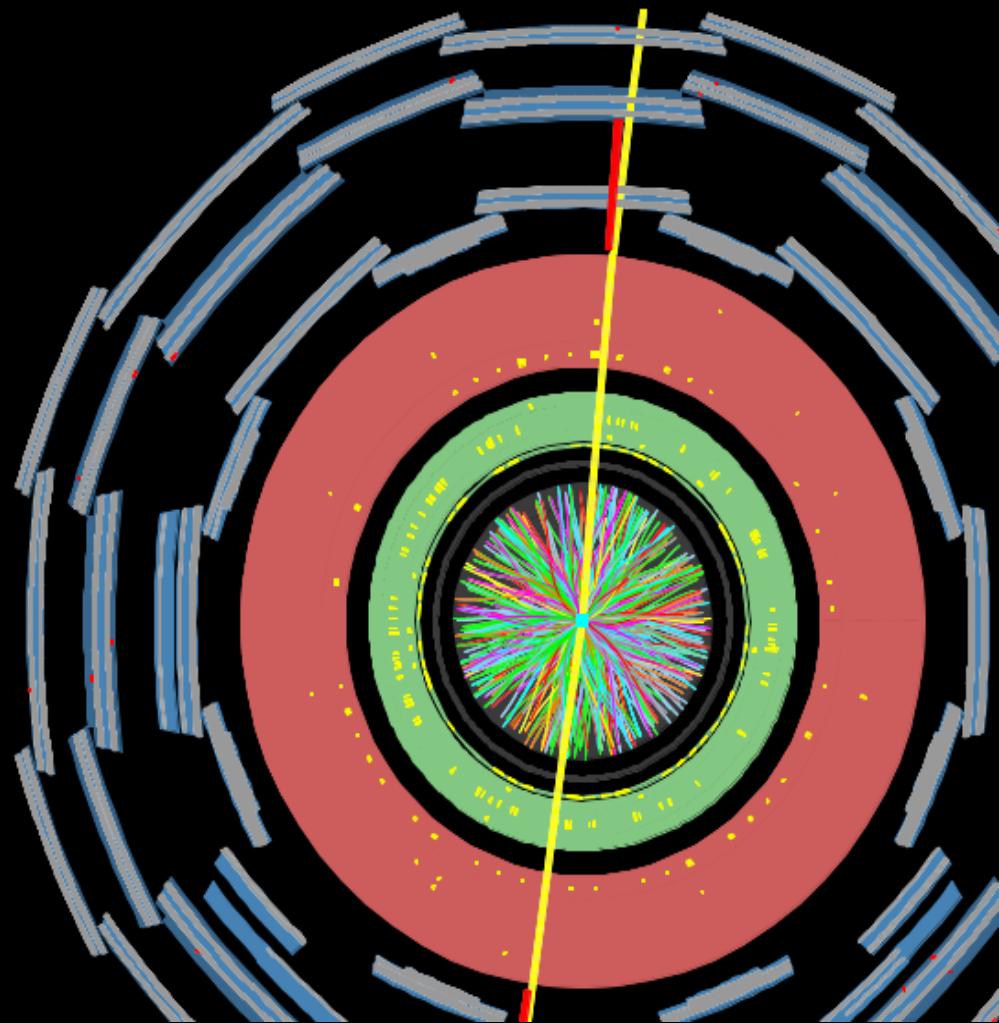
$$\sqrt{\hat{s}} = 100 \text{ GeV}$$

$$\sqrt{s} = 14 \text{ TeV} \rightarrow x_a x_b = 0.007$$

# A $Z \rightarrow e^+e^-$ event at LEP and at LHC



ALEPH @ LEP

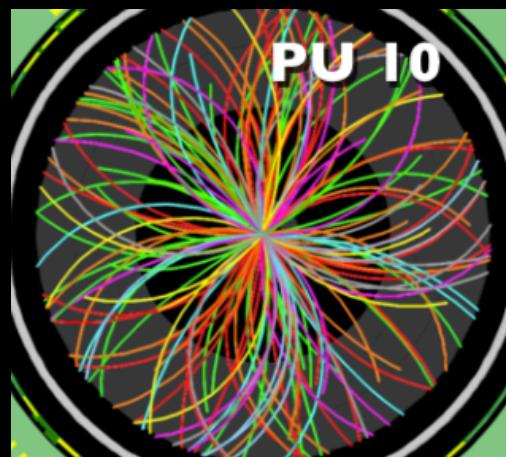
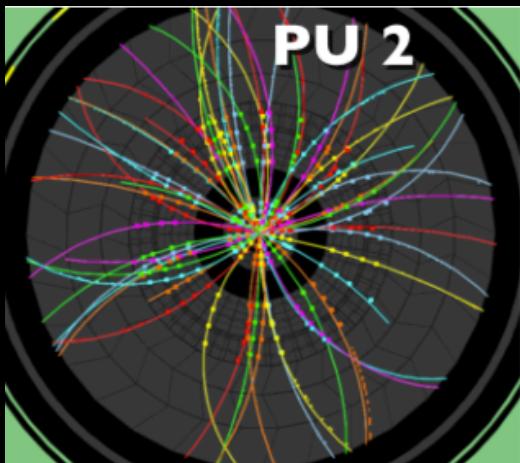
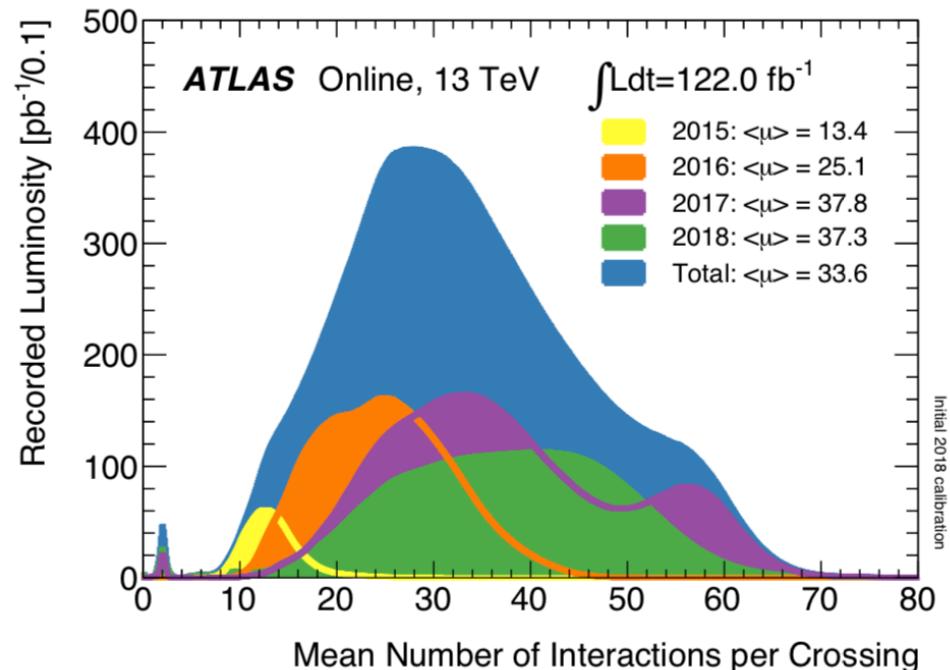


ATLAS @ LHC

# Pile-Up

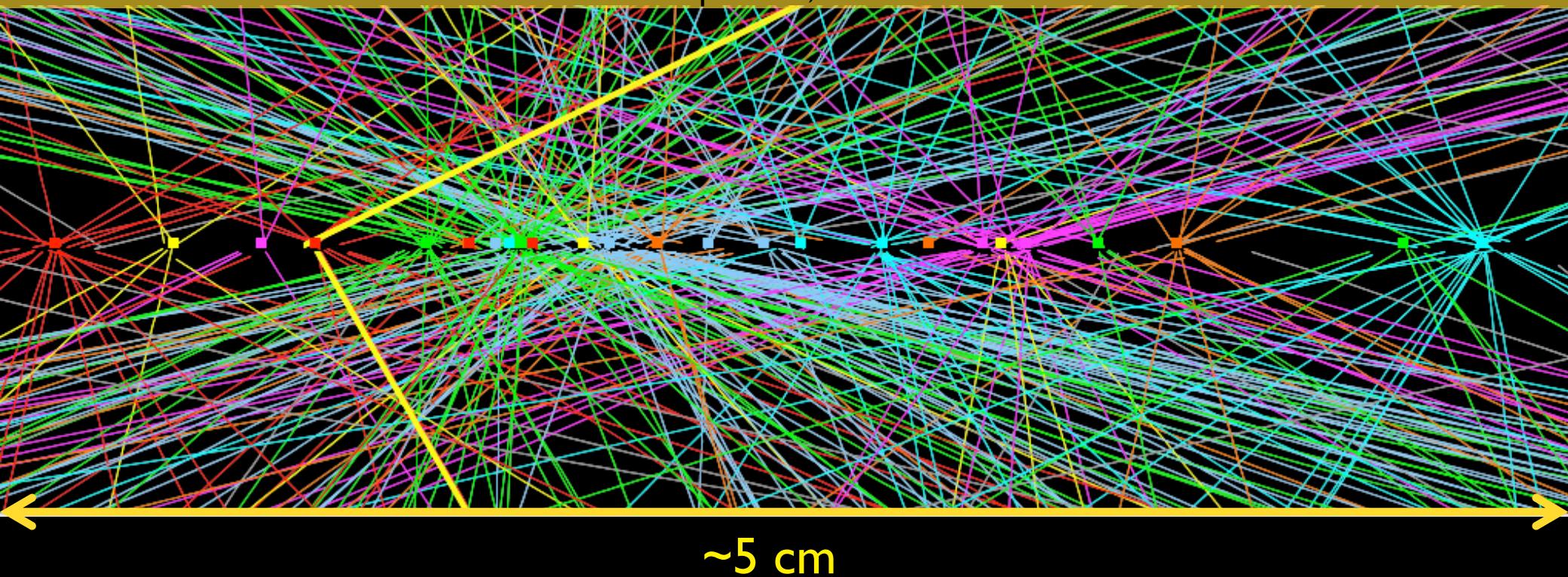
$$\mathcal{L} = \frac{1}{4\pi} \frac{fkN_1N_2}{\sigma_x \sigma_y}$$

PU = number of inelastic interactions per beam bunch crossing

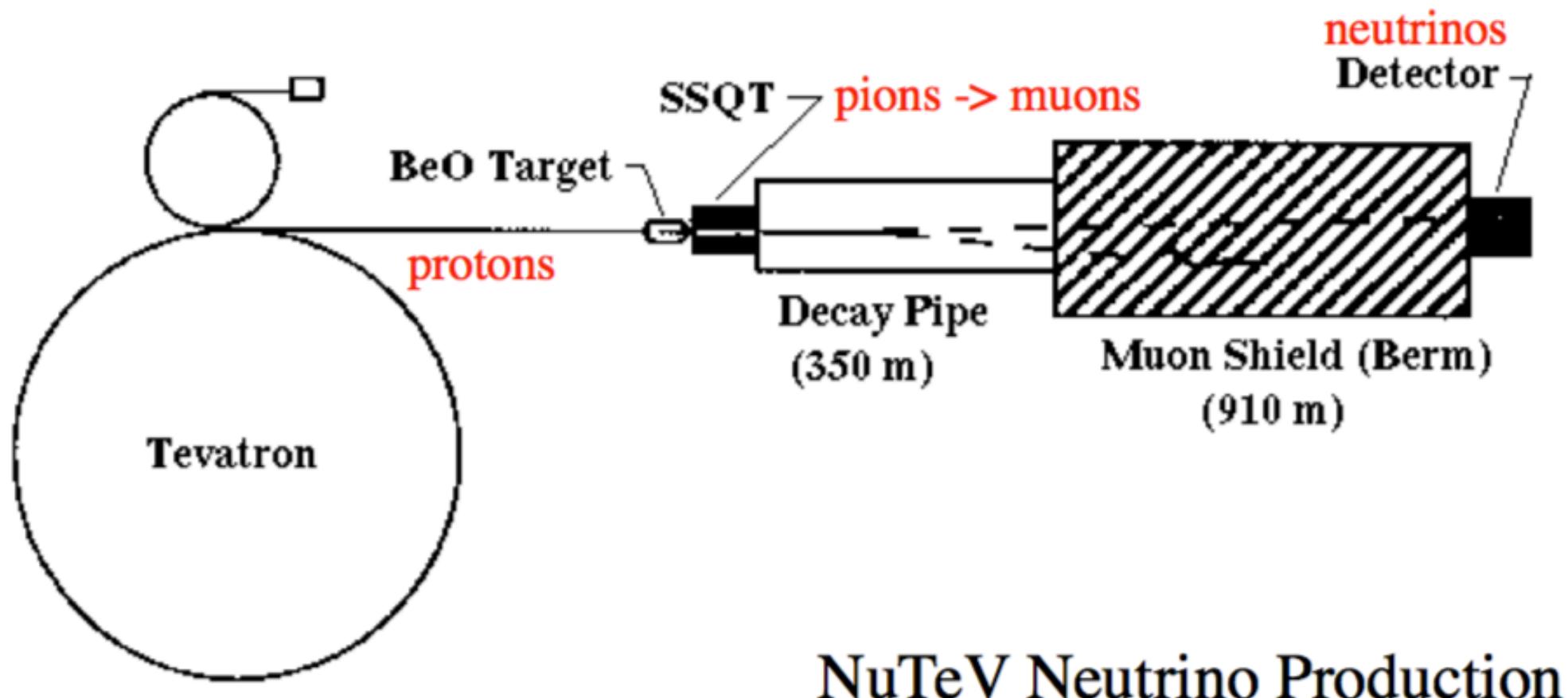


# $Z \rightarrow \mu\mu$ event with 25 reconstructed vertices

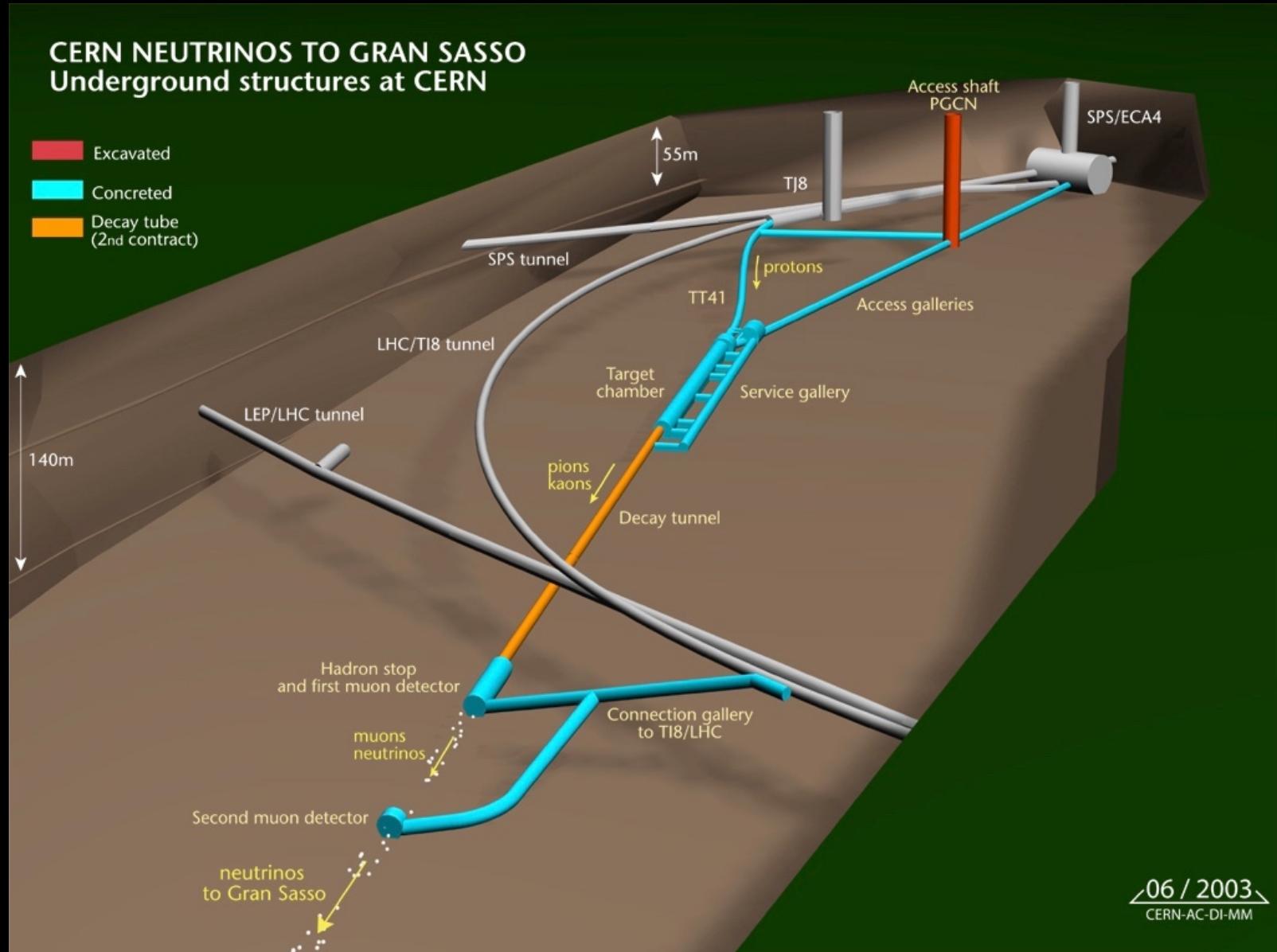
April 15<sup>th</sup>, 2012



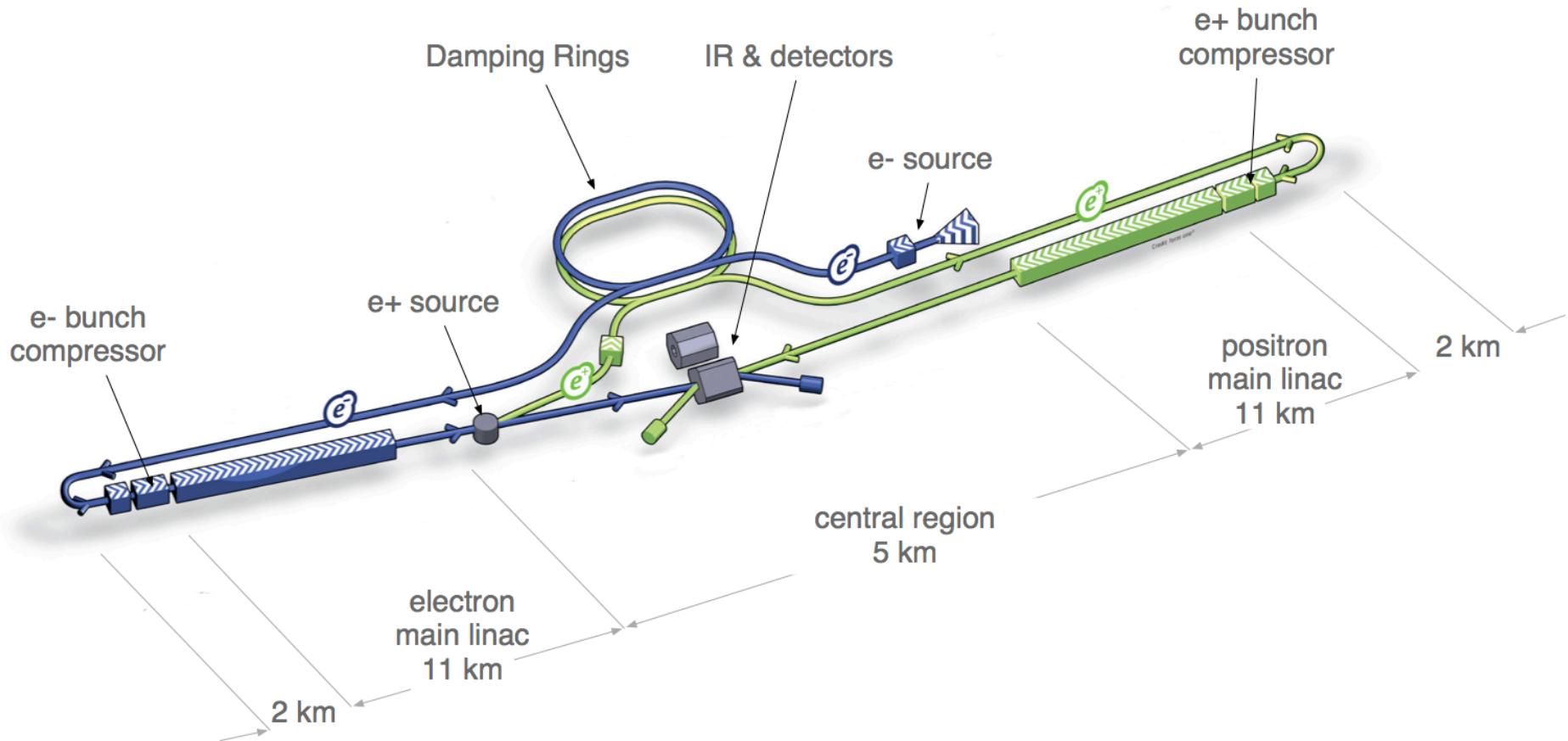
# Production of secondary beams



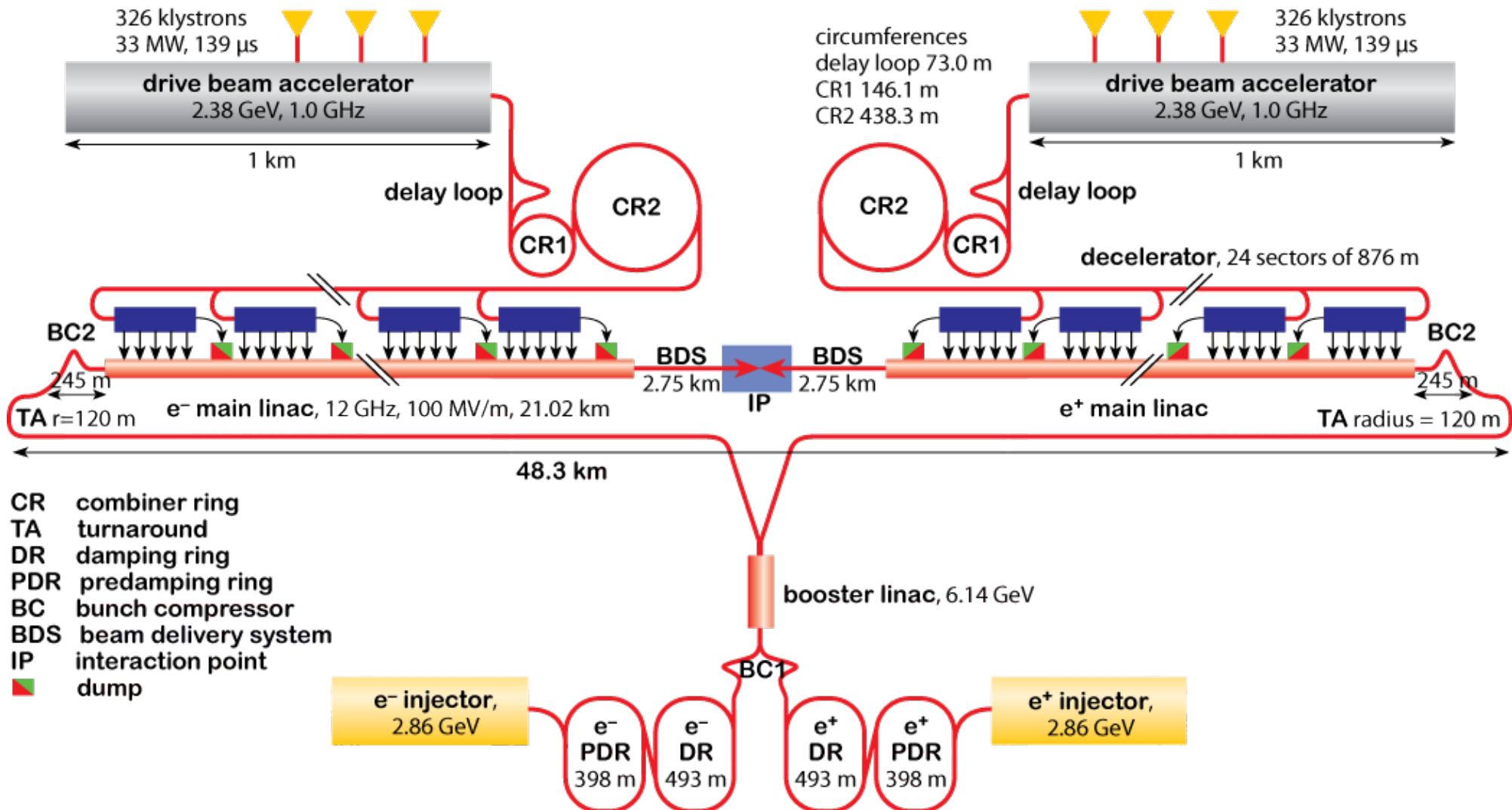
# Production of secondary beams



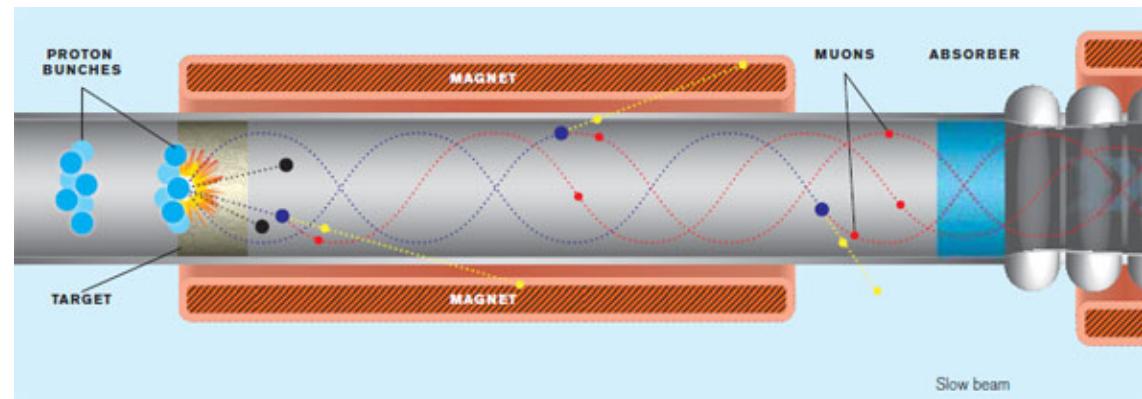
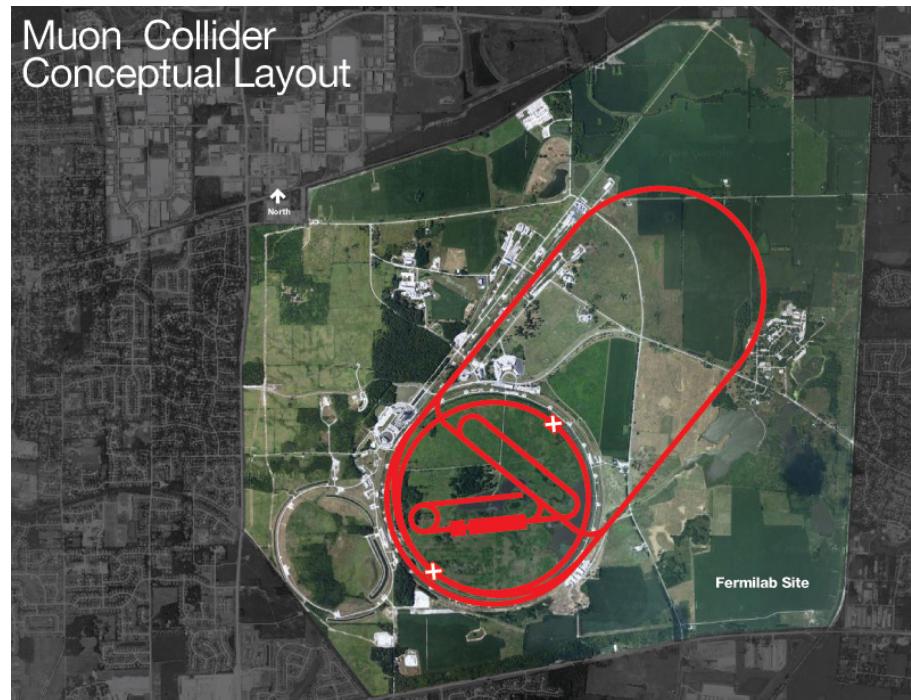
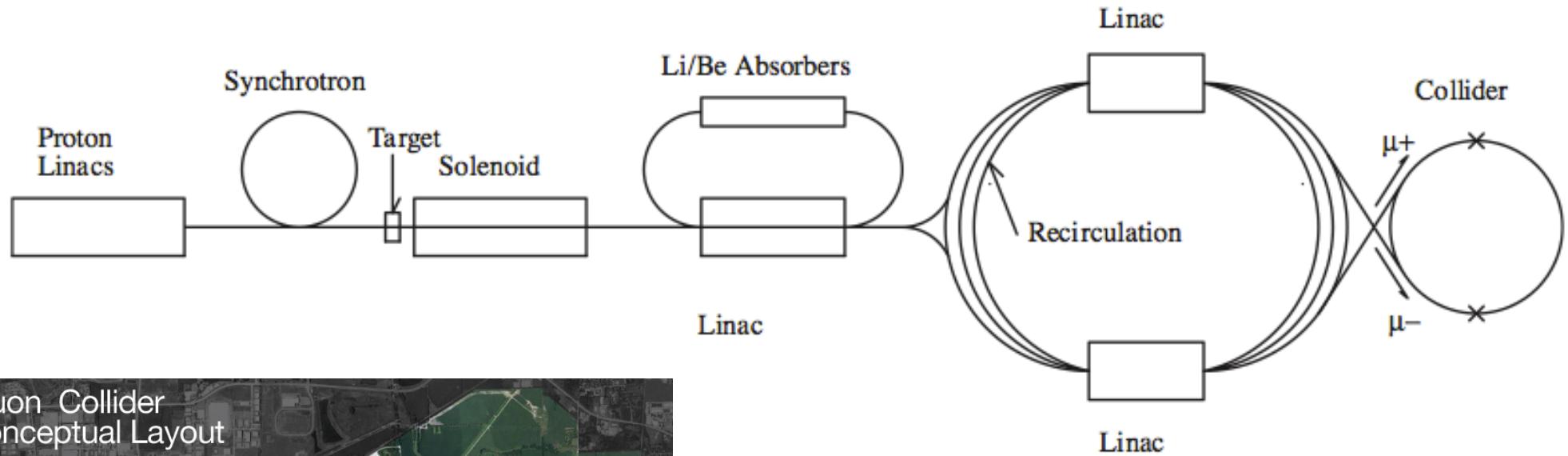
# Future colliders? ILC



# Future colliders? CLIC



# Future colliders? Muon collider





**Muon collider**  
 $d=2\text{km}$



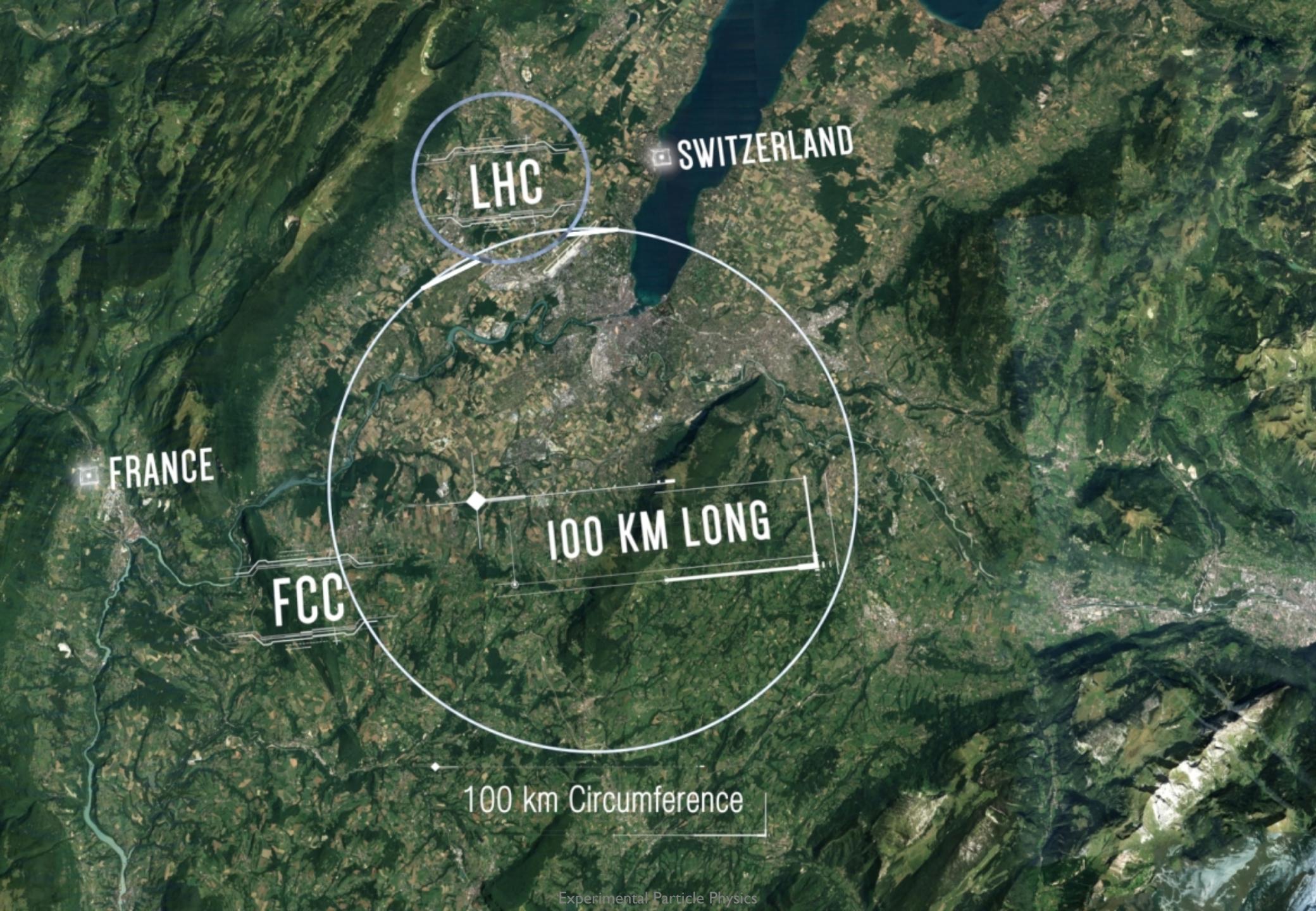
**ILC**  
 $l=30\text{km}$



**CLIC**  
 $l=50\text{km}$



**LHC**  
 $d=8.4\text{km}$



LHC

SWITZERLAND

FRANCE

FCC

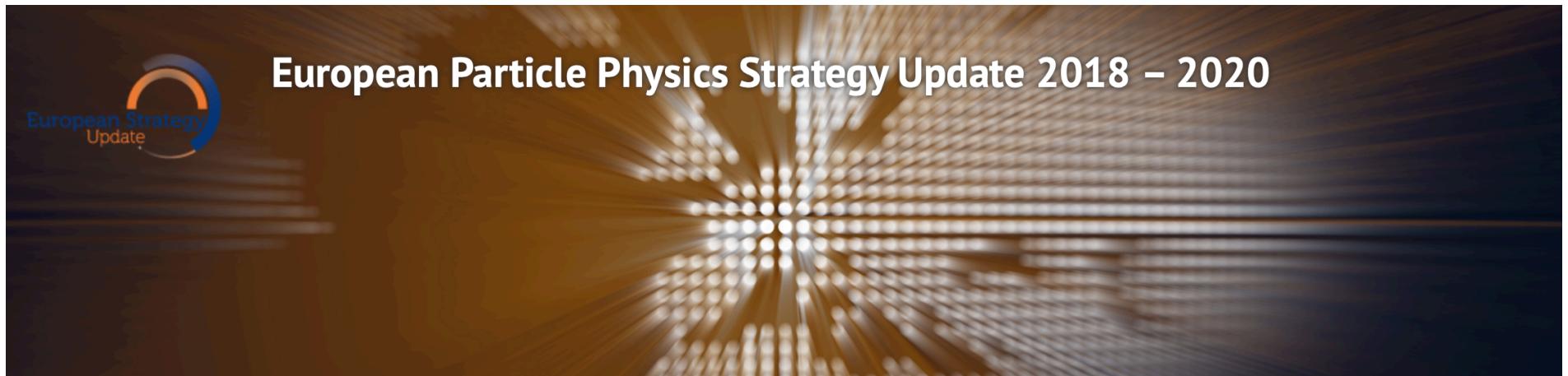
100 KM LONG

100 km Circumference

# Get curious, inform yourself on the future!

- **European Strategy for Particle Physics**

- ✓ <http://europeanstrategyupdate.web.cern.ch>



- **Physics Briefing Book : Input for the European Strategy for Particle Physics Update 2020**

- ✓ <https://arxiv.org/abs/1910.11775>