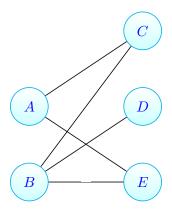
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CSCI 3104, Algorithms Quiz 8 Q1 S17

Instructions: This quiz is open book and open note. You may post clarification questions to Piazza, with the understanding that you may not receive an answer in time and posting does count towards your time limit (30 min for 1x, 37.5 min for 1.5x, 45 min for 2x). Questions posted to Piazza must be posted as **PRIVATE QUESTIONS.** Other use of the internet, including searching for answers or posting to sites like Chegg, is strictly prohibited. Violations of these are grounds to receive a 0 on this quiz. Proofs should be written in **complete sentences. Show and justify all work to receive full credit.** 

**Standard 17.** Let G(V, E) be a graph. A matching of G is a set of edge  $\mathcal{M}$  such that no two edges in  $\mathcal{M}$  share a common vertex. That is, if  $(i, j), (u, v) \in \mathcal{M}$  are distinct edges, then  $i \neq u, i \neq v, j \neq u$ , and  $j \neq v$ .

A graph is bipartite if its vertices can be partitioned into two sets  $V(G) = L \cup R$  such that every edge has one endpoint in L and one endpoint in R. Note that L and R are disjoint. The graph pictured below is an example.



Consider the following problem

## **Bipartite Maximum Matching**

Input: A bipartite graph G = (L, R; E)

Output: A matching  $\mathcal{M} \subseteq E(G)$  whose size  $|\mathcal{M}|$  is as large as possible.

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(a) Describe how to reduce the above problem to the (one-source, one-sink) max-flow problem from class. Your description should be **general**, and not tied to a specific example. (You may illustrate with an example for expository purposes, but an example alone is not sufficient. E.g., "This is how my construction is performed in general. Then for example, this is how we apply the construction to the graph I selected.")

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(b) Using your reduction, find a maximum matching in the graph above. Show your work, as well as your final answer. Note that there may be multiple maximum matchings in the graph above; you need only find one such matching.