

Name:

ID:

**CSCI 3104, Algorithms**  
**Quiz 8 Q1 S16**

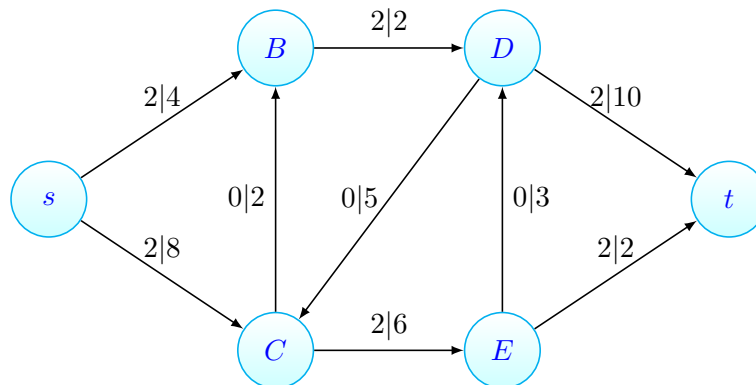
**Profs. Chen & Grochow**  
**Spring 2020, CU-Boulder**

**Instructions:** This quiz is open book and open note. You **may** post clarification questions to Piazza, with the understanding that you may not receive an answer in time and posting does count towards your time limit (30 min for 1x, 37.5 min for 1.5x, 45 min for 2x). Questions posted to Piazza **must be posted as PRIVATE QUESTIONS**. Other use of the internet, including searching for answers or posting to sites like Chegg, is strictly prohibited. Violations of these are grounds to receive a 0 on this quiz. Proofs should be written in **complete sentences**. **Show and justify all work to receive full credit.**

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**Standard 16.** Consider the following for the flow network where  $a|b$  on an edge denotes a flow of  $a$  and a total capacity of  $b$  (meaning, starting from this, you cannot add more than  $b - a$  flow to that edge without exceeding its capacity). The node  $s$  is the source and  $t$  is the sink.

Several iterations of the Ford–Fulkerson algorithm have already been completed. In this problem you will complete the Ford–Fulkerson algorithm in parts (a) and (b) below.



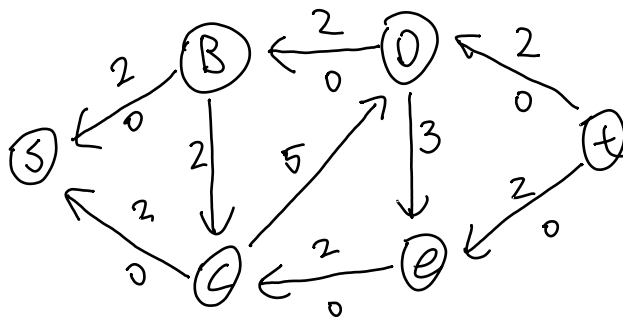
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- a. Draw the residual graph of the graph above. (Because there are no 2-cycles in this graph, you do not have to worry about the gadget from class that deals with 2-cycles.)



- b. Complete the Ford–Fulkerson algorithm. Show your work. End your answer with your final flow, its value, and the corresponding min cut.