

Example 2: Prisoner's Dilemma

If they both stay quiet \Rightarrow each will spend 1 yr in prison.

If one and only one of them finks \Rightarrow 4 yrs. jail to the other person.

If both fink \Rightarrow each will spend 3 yrs in prison.

Strategic game:

players \Rightarrow The 2 suspects

Actions \Rightarrow Each player's set of actions is $\{\text{Quiet}, \text{fink}\}$

Preferences \Rightarrow Suspect 1's ordering of the action profiles, from best to worst: $(\text{fink}, \text{Quiet})$, $(\text{Quiet}, \text{Quiet})$, $(\text{fink}, \text{fink})$, $(\text{Quiet}, \text{fink})$.

Suspect 2's $\Rightarrow (\text{Quiet}, \text{fink})$, $(\text{Quiet}, \text{Quiet})$, $(\text{fink}, \text{fink})$, $(\text{fink}, \text{Quiet})$.

Payoff functions:

for suspect 1, we need u_1 for which:

$$u_1(\text{fink}, \text{Quiet}) > u_1(\text{Quiet}, \text{Quiet}) > u_1(\text{fink}, \text{fink}) > u_1(\text{Quiet}, \text{fink})$$

Simple specification $\Rightarrow u_1(f, q) = 3$

$$u_1(q, q) = 2$$

$$u_1(f, f) = 1$$

$$u_1(q, f) = 0$$

Similarly for suspect 2,

$$u_2(q, f) = 3$$

$$u_2(q, q) = 2$$

$$u_2(f, f) = 1$$

$$u_2(f, q) = 0$$

		<u>suspect 2</u>	
		Quiet	fink
<u>suspect 1</u>	Quiet	2, 2	0, 3
	fink	3, 0	1, 1

The Prisoner's Dilemma models a situation in which there are gains from cooperation (each player prefers that both players choose Quiet than they both choose Fink) but each player has an incentive to "free ride" (choose Fink) whatever the other player does.

There are many examples that follow similar structures: