

# 1 Applicative laws

Identity, composition, homomorphism, interchange.

Definition : Identity

pure id <\*> x

Definition : Composition

pure (.) <\*> u <\*> v <\*> w  
u <\*> (v <\*> w)

Definition : Homomorphism

A *homomorphism* is a structure-preserving map between 2 algebraic structures.

Definition : Interchange

u <\*> pure y = pure (\$ y) <\*> u

```
cowFromString :: String
               → Int
               → Int
               → Maybe Cow
cowFromString name' age' weight' =
  case noEmpty name' of
    Nothing → Nothing
    Just nammy →
      case noNegative age' of
        Nothing → Nothing
        Just agey →
          case noNegative weight' of
            Nothing → Nothing
            Just weighty →
              Just (Cow nammy agey weighty)

cowFromString' :: String
               → Int
               → Int
               → Maybe Cow
cowFromString' name' age' weight' =
  Cow <$> noEmpty name' <*> noNegative age' <*> noNegative weight'
```

Validation, failure and success.

# 2 Definition

Applicative can be thought of characterizing monoidal functors. It's a way to functorially apply a function embedded in structure *f* of the same type as the value we are mapping over.

Note: Idiom means applicative functor and is a useful search term for published work on applicative functor.