

1 Applicative laws

Identity, composition, homomorphism, interchange.

Definition : Identity

pure id <*> x

Definition : Composition

pure (.) <*> u <*> v <*> w
u <*> (v <*> w)

Definition : Homomorphism

A *homomorphism* is a structure-preserving map between 2 algebraic structures.

Definition : Interchange

u <*> pure y = pure (\$ y) <*> u

```
cowFromString :: String
               → Int
               → Int
               → Maybe Cow
cowFromString name' age' weight' =
  case noEmpty name' of
    Nothing → Nothing
    Just nammy →
      case noNegative age' of
        Nothing → Nothing
        Just agey →
          case noNegative weight' of
            Nothing → Nothing
            Just weighty →
              Just (Cow nammy agey weighty)

cowFromString' :: String
               → Int
               → Int
               → Maybe Cow
cowFromString' name' age' weight' =
  Cow <$> noEmpty name' <*> noNegative age' <*> noNegative weight'
```