

17.

$$\begin{aligned}
 \int_{-1}^1 \int_{-1}^1 |x+y| \, dx \, dy &= 4 \int_0^1 \int_0^1 (x+y) \, dx \, dy \\
 &= 4 \int_0^1 \left( \frac{x^2}{2} + yx \right) \Big|_0^1 dy \\
 &= 4 \left( \frac{1}{2}y + \frac{1}{2}y^2 \right) \Big|_0^1 = 4
 \end{aligned}$$

44.

$$\iiint_V \frac{dx \, dy \, dz}{\sqrt{x^2 + y^2 + (z-2)^2}} = \iiint_V \frac{dx \, dy \, dz}{\sqrt{x^2 + y^2 + z^2}}$$

In cylindrical coordinates, the region is

$$E = \{(r, \theta, z) \mid 0 \leq \theta \leq 2\pi, \, 0 \leq r \leq 1, \, 0 \leq \theta \leq 2\pi, \, -3 \leq z \leq -1\}$$

Therefore we have

$$\begin{aligned}
 \iiint_V \frac{r \, dz \, dr \, d\theta}{\sqrt{r^2 + z^2}} &= \int_0^{2\pi} d\theta \int_0^1 \int_{-3}^{-1} \frac{r}{\sqrt{r^2 + z^2}} \, dz \, dr \\
 &= 2\pi \int_0^1 \int_{-3}^{-1} \frac{r}{\sqrt{r^2 + z^2}} \, dz \, dr
 \end{aligned}$$

34.

a)  $x = 4y - y^2, \, x + y = 6$

The 2 lines intersect at  $y = 2, \, y = 3$ .

$$\begin{aligned}
 \int_2^3 |(4y - y^2) - (y - 6)| \, dy &= \int_2^3 -y^2 + 3y + 6 \, dy \\
 &= \left( -\frac{y^3}{3} + \frac{3y^2}{2} + 6y \right) \Big|_2^3
 \end{aligned}$$

35.

a)  $z = 1 - x^2 - y^2, \, y = x, \, y = \sqrt{3}x, \, z = 0$

$$\begin{aligned}
 \int_0^1 \int_x^{\sqrt{3}x} (1 - x^2 - y^2) \, dy \, dx &= \int_0^1 \left( y - x^2y - \frac{1}{3}y^3 \right) \Big|_x^{\sqrt{3}x} dx \\
 &= (\sqrt{3} - 1) \int_0^1 x - \frac{4}{3}x^3 \, dx \\
 &= (\sqrt{3} - 1) \left( \frac{x^2}{2} - \frac{x^4}{3} \right) \Big|_0^1 \\
 &= \frac{\sqrt{3} - 1}{6}
 \end{aligned}$$

b)  $x^2 + y^2 = a, \, x^2 + z^2 = a$